

import statements

```
In [2]: import numpy as np
```

function definition

```
In [3]: def sigmoid (x):  
        return 1/(1 + np.exp(-x))  
  
        def sigmoid_derivative(x):  
            return x * (1 - x)
```

Input datasets

```
In [4]: inputs = np.array([[0,0],[0,1],[1,0],[1,1]])  
        expected_output = np.array([[0],[1],[1],[0]])  
  
        epochs = 10000  
        lr = 0.1  
        inputLayerNeurons, hiddenLayerNeurons, outputLayerNeurons = 2,2,1
```

Random weights and bias initialization

```
In [5]: hidden_weights = np.random.uniform(size=(inputLayerNeurons,hiddenLayerNeurons))  
        hidden_bias =np.random.uniform(size=(1,hiddenLayerNeurons))  
        output_weights = np.random.uniform(size=(hiddenLayerNeurons,outputLayerNeurons))  
        output_bias = np.random.uniform(size=(1,outputLayerNeurons))  
  
        print("Initial hidden weights: ",end='')  
        print(*hidden_weights)  
        print("Initial hidden biases: ",end='')  
        print(*hidden_bias)  
        print("Initial output weights: ",end='')  
        print(*output_weights)  
        print("Initial output biases: ",end='')  
        print(*output_bias)
```

```
Initial hidden weights: [0.82052933 0.39428938] [0.47936364 0.97718061]  
Initial hidden biases: [0.93732222 0.66840377]  
Initial output weights: [0.85877789] [0.81728556]  
Initial output biases: [0.89547486]
```

Training algorithm

```
In [6]: for _ in range(epochs):
        hidden_layer_activation = np.dot(inputs,hidden_weights)
        hidden_layer_activation += hidden_bias
        hidden_layer_output = sigmoid(hidden_layer_activation)

        output_layer_activation = np.dot(hidden_layer_output,output_weights)
        output_layer_activation += output_bias
        predicted_output = sigmoid(output_layer_activation)

        #Backpropagation
        error = expected_output - predicted_output
        d_predicted_output = error * sigmoid_derivative(predicted_output)

        error_hidden_layer = d_predicted_output.dot(output_weights.T)
        d_hidden_layer = error_hidden_layer * sigmoid_derivative(hidden_layer_output)

        #Updating Weights and Biases
        output_weights += hidden_layer_output.T.dot(d_predicted_output) * lr
        output_bias += np.sum(d_predicted_output,axis=0,keepdims=True) * lr
        hidden_weights += inputs.T.dot(d_hidden_layer) * lr
        hidden_bias += np.sum(d_hidden_layer,axis=0,keepdims=True) * lr
```

```
In [7]: print("Final hidden weights: ",end='')
        print(*hidden_weights)
        print("Final hidden bias: ",end='')
        print(*hidden_bias)
        print("Final output weights: ",end='')
        print(*output_weights)
        print("Final output bias: ",end='')
        print(*output_bias)

        print("\nOutput from neural network after 10,000 epochs: ",end='')
        print(*predicted_output)
```

```
Final hidden weights: [2.98033689 6.02213327] [2.97996777 6.01739985]
Final hidden bias: [-4.41556636 -1.87560029]
Final output weights: [-6.28166562] [6.45155088]
Final output bias: [-3.09350009]
```

```
Output from neural network after 10,000 epochs: [0.09022419] [0.885862
8] [0.88587383] [0.13958549]
```

References

<https://towardsdatascience.com/implementing-the-xor-gate-using-backpropagation-in-neural-networks-c1f255b4f20d> (<https://towardsdatascience.com/implementing-the-xor-gate-using-backpropagation-in-neural-networks-c1f255b4f20d>), An Introduction to Neural Networks by Kevin Gurney,
<https://www.analyticsvidhya.com/blog/2017/05/neural-network-from-scratch-in-python-and-r/>
(<https://www.analyticsvidhya.com/blog/2017/05/neural-network-from-scratch-in-python-and-r/>).

In []: