# Multimedia Security and Privacy

# **TP4:** Watermark Detection

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## Submission

Please archive your report and codes in "Name\_Surname.zip" (replace "Name" and "Surname" with your real name), and upload to "Assignments/TP4: Watermark Detection" on https://chamilo.unige.ch before Wednesday, May 1st 2019, 23:59 PM. Note, the assessment is mainly based on your report, which should include your answers to all questions and the experimental results.

# 1 Watermark Embedding and Channel modeling

#### 1.1 Exercise

- Read in a gray scale image x, for example liftingbody.png. It will serve as the host image
- Generate a matrix  $\mathbf{w}$ ' of size  $\mathbf{x}$  with uniform distributed values  $\{-1,1\}$ . The magnitude of these two values governs the watermark strength.
- Randomly sample from matrix  $\mathbf{w}$ ' with a given density  $\theta_N = 0.5$ . The result is watermark  $\mathbf{w}$ . The watermark length N is defined as:

$$N = (N_1 \cdot N_2) \cdot \theta_N \tag{1}$$

where  $N_1$  and  $N_2$  are the dimensions of host image  $\mathbf{x}$ .

 $\bullet$  Embed the watermark **w** in to the host image **x** forming watermarked image **y**:

$$\mathbf{y} = \mathbf{x} + \mathbf{w} \tag{2}$$

• Generate a matrix **z** with Additive White Gaussian Noise (AWGN):

$$\mathbf{z} \sim \mathcal{N}(\boldsymbol{\mu}, \sigma_{noise}^2 \mathbf{I})$$
 (3)

where  $\mu = 0$  and  $\sigma_{noise}^2 = 1$ .

• Add the AWGN matrix **z** to the watermarked image **y**, resulting in attacked image **v**:

$$\mathbf{v} = \mathbf{y} + \mathbf{z} = \mathbf{x} + \mathbf{w} + \mathbf{z} \tag{4}$$

 $\bullet$  Show the original image  $\mathbf{x}$ , the watermarked image  $\mathbf{y}$  and the attacked watermarked image  $\mathbf{v}$  on the screen. What do you see?

### 2 Non-blind watermark detection

In this set exercises you will attack a watermarked image leveraging knowledge of the original image. See Figure 1.

#### 2.1 Exercise

• Extract the estimated watermark  $\hat{\mathbf{w}}$  from the marked image  $\mathbf{v}$  using the original image  $\mathbf{x}$ :

$$\hat{\mathbf{w}}_{non-blind} = \mathbf{v} - \mathbf{x} \tag{5}$$

• Determine the linear correlation  $\rho_{non-blind}$  between the original watermark  $\mathbf{w}$  and the estimated watermark  $\hat{\mathbf{w}}_{non-blind}$ :

$$\rho_{non-blind} = \frac{1}{N} \sum_{k=1}^{N} \hat{w}_{non-blind}[k] \cdot w[k]$$
(6)

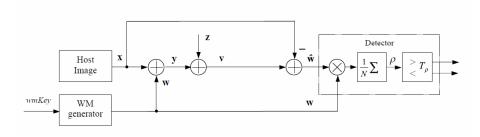


Figure 1 – Non-blind watermark detection

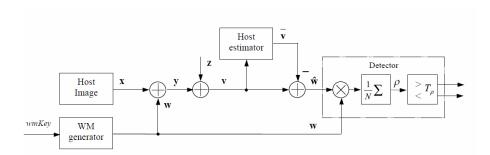


Figure 2 - Blind watermark detection

# 3 Blind watermark detection using the Maximum Likelihood estimate

This exercise will introduce a simple method to blindly estimated a watermark when one only has access to the marked image. See Figure 2.

#### 3.1 Exercise

• Given only the marked image  $\mathbf{v}$ , blindly estimate the watermark  $\hat{\mathbf{w}}_{blind}$  using the following formula:

$$\hat{\mathbf{w}}_{blind} = \mathbf{v} - \bar{\mathbf{v}} \tag{7}$$

where  $\bar{\mathbf{v}}$  is the local mean of marked image  $\mathbf{v}$ .

• Why can you assume that  $\bar{\mathbf{v}} = \mathbf{x}$ ?

**Remark 1.** Matlab offers a number of functions to facilitate region based processing, amongst them are blockproc, blkproc and colfilt.

#### 3.2 Exercise

• Determine the linear correlation  $\rho_{blind}$  between the original watermark  $\mathbf{w}$  and the blindly estimated watermark  $\hat{\mathbf{w}}_{blind}$ :

$$\rho_{blind} = \frac{1}{N} \sum_{k=1}^{N} \hat{w}_{blind}[k] \cdot w[k]$$
(8)

• What can you say about the difference between blind and non-blind watermark detection in terms of the linear correlations  $\rho_{blind}$  and  $\rho_{non-blind}$ ?