

## RELATIONAL ALGEBRA SOLUTIONS

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1. Consider the following relational database, where primary keys are underlined.

**employee**(person\_name,street,city)

**works**(person\_name,company\_name,salary)

**company**(company\_name,city)

**manages**(person\_name,manager\_name)

Given an expression in the relational algebra to express each of the following queries.

- i) Find the name of all employees who work for first bank corporation.

$\Pi_{\text{person\_name}} (\sigma_{\text{company\_name}=\text{"first bank corporation"}}(\text{works}))$

- ii) Find the name and cities of residence of all employees who work for first bank corporation.

$\Pi_{\text{person\_name,city}} (\sigma_{\text{company\_name}=\text{"first bank corporation"}}(\text{employee} \bowtie \text{works}))$

- iii) Find the name, street address and city of residence of all employees who work for first bank corporation and earn more than \$10000 per annum.

$\Pi_{\text{person\_name,street,city}} (\sigma_{\text{company\_name}=\text{"first bank corporation"} \wedge \text{salary} > 10000}(\text{employee} \bowtie \text{works}))$

- iv) Find the name of all employees in this database who lives in same city as the company for which they work.

$\Pi_{\text{person\_name}}(\text{employee} \bowtie \text{works} \bowtie \text{company})$

- v) Find the name of all employees who live in the same city and on the same street as do their managers.

$\Pi_{\text{person\_name}} ((\text{employee} \bowtie \text{manages}) \bowtie (\text{manages.manager\_name} = \text{employee2.person\_name} \wedge \text{employee.street} = \text{employee2.street} \wedge \text{employee.city} = \text{employee2.city})) (\rho_{\text{employee2}} (\text{employee}))$

- vi) Find the name of all employees in this database who do not work for first bank corporation

$\cdot \Pi_{\text{person\_name}} (\sigma_{\text{company\_name} \neq \text{"first bank corporation"}}(\text{works}))$

- vii) Assume that companies may be located in several cities. Find all companies located in every city in which small bank corporation is located.

$\Pi_{\text{company\_name,city}}(\text{company}) \div \Pi_{\text{city}} (\sigma_{\text{company\_name} = \text{"small bank corporation"}}(\text{company}))$

**2. Consider the following relational database.**

**Students(RollNo, StudentName, Address, Semester)**

**Teachers(TeacherID, TeacherName, CourseID, Salary, Department)**

**Courses(CourseID, RollNo, CourseTitle, Semester)**

**Write relational Algebra Expressions for the following requests.**

- i) Find the name of students of 4<sup>th</sup> semester and studying “Operating System”**

$\Pi_{\text{StudentName}} (\sigma_{\text{semester} = \text{"4th"} \wedge \text{CourseTitle} = \text{"Operating System"}} (\text{Students} \bowtie \text{Courses}))$

- ii) Find the name of teacher who teaches subject “DBMS” to “Arten Khadka”**

$\Pi_{\text{TeacherName}} (\sigma_{\text{CourseTitle} = \text{"DBMS"} \wedge \text{Student\_name} = \text{"Arten Khadka"}} ((\text{Students} \bowtie \text{Courses}) \bowtie \text{Teachers}))$

- iii) Delete Record of 2<sup>nd</sup> semester students of Account Department**

$\text{Students} \leftarrow \Pi_{\text{RollNo, StudentName, Address, Semester}} (\text{students})$

$-\Pi_{\text{RollNo, StudentName, Address, Semester}} (\sigma_{\text{department} = \text{"account"} \wedge \text{semester} = \text{2nd}} ((\text{Students} \bowtie \text{Courses}) \bowtie \text{Teachers}))$

- iv) Increase salary of “Bhaskar Bhatta” by 6%**

$\text{Teachers} \leftarrow \Pi_{\text{TeacherID, TeacherName, CourseID, Salary} * 1.06, \text{Department}} (\sigma_{\text{TeacherName} = \text{"Bhaskar Bhatta"}} (\text{Teachers})) \cup (\text{Teachers} - \sigma_{\text{TeacherName} = \text{"Bhaskar Bhatta"}} (\text{Teachers}))$

**3. Consider the following schema**

**SUPPLIER(Sid, S\_name, S\_addr)**

**PARTS(Pid, p\_name, color)**

**CATALOG(sid, pid, cost)**

**[PU:2014 fall]**

**Now answer the following queries in Relational Algebra.**

- i) Find the name of all supplier who supply yellow parts**

$\Pi_{\text{S\_name}} (\sigma_{\text{color} = \text{'yellow'}} (\text{SUPPLIER} \bowtie \text{CATALOG} \bowtie \text{PARTS}))$

- ii) Find the name of suppliers who supply Both blue and black parts.**

$\Pi_{\text{S\_name, color}} (\text{SUPPLIER} \bowtie (\text{CATALOG} \bowtie \text{PARTS})) \div \Pi_{\text{color}} (\sigma_{\text{color} = \text{'blue'} \wedge \text{color} = \text{'black'}} (\text{PARTS}))$

- iii) Find the name of suppliers who supply all parts.**

$\Pi_{\text{S\_name, pid}} (\text{SUPPLIER} \bowtie \text{CATALOG}) \div \Pi_{\text{pid}} (\text{PARTS})$

4. consider the following schema

customer(cust\_id,cus\_name,cus\_phno)  
employee(cus\_id,emp\_id,emp\_name,emp\_add)  
works(branch\_id,salary,cus\_id)  
branch(branch\_id,branch\_name)

Write relational algebra notations for the following queries for the given schema.  
[PU:2011 spring]

- i) select name of all employees.

$\Pi_{\text{emp\_name}}(\text{employee})$

- ii) Give salary rise to 5% to all the employee

$\text{works} \leftarrow \Pi_{\text{branch\_id}, \text{salary} * 1.05, \text{cust\_id}}(\text{works})$

- iii) List all branch names

$\Pi_{\text{branch\_name}}(\text{branch})$

- iv) select name of all employees working for “manang” branch

$\Pi_{\text{emp\_name}}(\sigma_{\text{branch\_name} = \text{“manang”}}((\text{branch} \bowtie (\text{works} \bowtie \text{employee})))$

- v) Delete any record from work table

$\text{works} \leftarrow \text{works} - \sigma_{\text{branch\_id} = 101}(\text{works})$

This operation can be customized according to requirement.

- vi) List the name and phno of all customers

$\Pi_{\text{cust\_name}, \text{cust\_phno}}(\text{customer})$

- vii) select name of all employees deal with customer having id “201”

$\Pi_{\text{emp\_name}}(\sigma_{\text{cust\_id} = 201}(\text{employee}))$

- viii) Delete all records from works table whose salary is less than 10000

$\text{works} \leftarrow \text{works} - \sigma_{\text{salary} < 10000}(\text{works})$

ix) Delete all records from works table  

$$\text{works} \leftarrow \text{works} - \Pi_{\text{branch\_id}, \text{salary}, \text{cust\_id}}(\text{works})$$

5. By using the following schemas write relational algebraic expression and SQL statements.  
 (underlined attributes represent primary key attributes)

EMPLOYEE(EMPNO, NAME, ADDRESS)  
 PROJECT(PNO, PNAME)  
 WORKON(EMPNO, PNO)  
 PART(PARTNO, PARTNAME, QTY\_ON\_HAND)  
 USE(EMP\_NO, PNO, PARTNO, NUMBER)

i) Listing all employees details who are not working yet

$$\Pi_{\text{EMPNO}, \text{NAME}, \text{ADDRESS}} (\text{Employee}) - \Pi_{\text{EMPNO}, \text{NAME}, \text{ADDRESS}} (\text{Employee} \bowtie \text{WORKON})$$

ii) Listing Part Name and Quantity on hand those were used in DBMS project

$$\Pi_{\text{PARTNAME}, \text{QTY\_ON\_HAND}} (\text{PART} \bowtie (\text{USE} \bowtie \sigma_{\text{PNAME} = \text{"DBMS"}}(\text{PROJECT})))$$

OR

$$\Pi_{\text{PARTNAME}, \text{QTY\_ON\_HAND}} (\sigma_{\text{PNAME} = \text{"DBMS"}} (\text{PART} \bowtie (\text{USE} \bowtie \text{PROJECT})))$$

iii) List the name of projects that are used by employee from Kathmandu

$$\Pi_{\text{PNAME}} (\sigma_{\text{ADDRESS} = \text{"Kathmandu"}} ((\text{EMPLOYEE} \bowtie \text{WORKON}) \bowtie \text{PROJECT}))$$

6. Consider the following relations for order processing database application in a company.

CUSTOMER(Cust#, Cname, City)  
 ORDER(Order#, Odate, Cust#, ord\_Amt)  
 ORDER\_ITEM(Order#, Item#, Qty)  
 ITEM(Item#, Unit\_price)  
 SHIPMENT(Order#, Warehouse#, Ship\_date)  
 WAREHOUSE(Warehouse#, City)

Answer the following queries in relational algebra.

- i) List the order# and ship\_date for all orders shipped from Warehouse number “W2”.

$$\Pi_{\text{Order\#,Ship\_date}} (\sigma_{\text{warehouse\#}=\text{"w2"}} (\text{SHIPMENT}))$$

- ii) List the warehouse information for which the customer named ‘JOSE Copez’ was supplied his orders.

$$\Pi_{\text{warehouse\#,city}} (\sigma_{\text{cname}=\text{"JOSE Copez"}} (\text{CUSTOMER} \bowtie (\text{ORDER} \bowtie (\text{SHIPMENT} \bowtie \text{WAREHOUSE}))))$$

- iii) List the orders that were not shipped within 30 days of ordering.

$$\text{TIMELY\_SHIPPED} \leftarrow \sigma_{\text{Ship\_date} \leq \text{Odate}+30} (\text{ORDER} \bowtie \text{SHIPMENT})$$

$$\text{RESULT} \leftarrow \Pi_{\text{Order\#}} (\text{ORDER}) - \Pi_{\text{Order\#}} (\text{TIMELY\_SHIPPED})$$

- iv) List the order # for orders that were shipped from all warehouses in the network.

$$\Pi_{\text{Order\#, Warehouse\#}} (\text{Shipment}) \div \Pi_{\text{Warehouse\#}} (\sigma_{\text{City} = \text{"New York"}} (\text{Warehouse}))$$

7. consider the following database: [PU:2012 fall]

Student(sid,name,age)

Has(sid,cid)

College(cid,cname)

Write relational algebra expression to perform the following.

- i) find the average age of student.

$$\mathcal{G}_{\text{avg(age)}} (\text{student})$$

- ii) Display the name of student who studies in “QWERT” college.

$$\Pi_{\text{name}} (\sigma_{\text{cname}=\text{"QWERT"}} (\text{Student} \bowtie (\text{Has} \bowtie \text{College})))$$

- iii) Insert a new student.

$$\text{Student} \leftarrow \text{Student} \cup \{104, \text{"Roshan"}, 29\}$$

- iv) Delete record of "ASDFG" college from college relation

$$\text{College} \leftarrow \text{College} - (\sigma_{\text{cname} = \text{"ASDFG"}}(\text{College}))$$

- v) Display name of students whose name begin from 'S.'

$$\Pi_{\text{name}}(\sigma_{\text{name LIKE 'S\%'}}(\text{Student}))$$

8. Consider the following schema:

[PU:2017 fall]

employee(person\_name, street, city)

works(person\_name, company\_name, salary)

company(company\_name, city)

manages(person\_name, manager\_name)

Given an expression in relational algebra to express each of the following queries.

- i) Find the name of all employees who earn more than their managers.

$$\Pi_{\text{person\_name}}((\text{works} \bowtie \text{manages}) \bowtie_{\text{manages.manager\_name} = \text{e2.person\_name} \wedge \text{works.salary} > \text{e2.salary}}(\rho_{\text{e2}}(\text{works})))$$

***In SQL this will work***

```
SELECT works.person_name
FROM works NATURAL JOIN manages
JOIN works AS e2 ON manages.manager_name = e2.person_name
AND works.salary > e2.salary;
```

- ii) Find the name of all employees who live in the same city and on the same street as their managers.

$$\Pi_{\text{person\_name}}((\text{employee} \bowtie \text{manages}) \bowtie_{(\text{manages.manager\_name} = \text{employee2.person\_name} \wedge \text{employee.street} = \text{employee2.street} \wedge \text{employee.city} = \text{employee2.city})}(\rho_{\text{employee2}}(\text{employee})))$$

- iii) Find the name of all employees with database that do not work for "NBL company".

$$\Pi_{\text{person\_name}}(\sigma_{\text{company\_name} \neq \text{"NBL company"}}(\text{works}))$$

- iv) Find the name of all employees in the database who earn more than top earner at "NBL company in the database".

$$\begin{aligned} \text{topearner} &\leftarrow \mathcal{G}_{\max(\text{salary})}(\sigma_{\text{company\_name} = \text{"NBL company"}}(\text{works})) \\ \text{result} &\leftarrow \Pi_{\text{personname}}(\sigma_{\text{salary} > \text{topearner}}(\text{works})) \end{aligned}$$

9. Consider the relational database of figure below, where primary keys are underlined. Given an expression in the relational algebra to express each of the following queries. [PU:2014 spring]

Employee(person\_name,street,city)

Works(person\_name,bank\_name,salary)

Bank(bank\_name,city)

Manages(person\_name,manager\_name)

- i) Find the total salary sum of all the banks.

$$\mathcal{G}_{\text{sum(salary)}}(\text{works})$$

- ii) Modify the database so that Ram now lives in Kathmandu.

$$\text{Employee} \leftarrow \Pi_{\text{personname,street,"Kathmandu"}} (\sigma_{\text{person\_name}=\text{"Ram"}}(\text{Employee})) \\ \cup (\text{Employee} - \sigma_{\text{person\_name}=\text{"Ram"}}(\text{Employee}))$$

- iii) Find the name, street address and cities of residence of all employees who work for Nepal world Bank corporation and earn more than \$10,000 per annum.

$$\Pi_{\text{personname,street,city}} (\sigma_{\text{bank\_name}=\text{"Nepal World Bank Corporation"} \wedge \text{salary} > 10000} (\text{Employee} \bowtie \text{Works}))$$

*Here, we assume salary attribute represent annual salary.*

- iv) Delete all tuples in work relation for employee of small bank corporation.

$$\text{Works} \leftarrow \text{Works} - \sigma_{\text{bank\_name}=\text{"Small Bank Corporation"}}(\text{Works})$$

10. Consider the following relational database of figure below, Where primary keys are underlined. Given an expression in the relational algebra to express each of the following queries.

employee(person\_name,street,city)  
 works(person\_name,bank\_name,salary)  
 bank(bank\_name,city)  
 manages(person\_name,manager\_name)

- i) Find the name of all employees who work for Nepal Rastra Bank and Salary greater than \$10000.

$$\Pi_{\text{personname}} (\sigma_{\text{bank\_name}=\text{"Nepal Rastra Bank"} \wedge \text{salary} > 10000} (\text{employee} \bowtie \text{works}))$$

- ii) Find the name and cities of residence of all employees who work for Nepal Rastra Bank

$$\Pi_{\text{personname}, \text{city}} (\sigma_{\text{bank\_name}=\text{"Nepal Rastra Bank"}} (\text{employee} \bowtie \text{works}))$$

- iii) Find name,street address,and cities of residence of all employees who work for Nepal Rastra Bank Corporation and earn more than \$10000 per annum.

$$\Pi_{\text{personname}, \text{street}, \text{city}} (\sigma_{\text{bank\_name}=\text{"Nepal Rastra Bank corporation"} \wedge \text{salary} > 10000 * 12} (\text{employee} \bowtie \text{works}))$$

- iv) Delete all tuples in work relation for employee of Nepal Rastra Bank

$$\text{works} \leftarrow \text{works} - \sigma_{\text{bank\_name}=\text{"Nepal Rastra Bank"}} (\text{works})$$