

## RELATIONAL ALGEBRA SOLUTIONS

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1. Consider the following relational database, where primary keys are underlined.

**employee**(person\_name,street,city)

**works**(person\_name,company\_name,salary)

**company**(company\_name,city)

**manages**(person\_name,manager\_name)

Given an expression in the relational algebra to express each of the following queries.

- i) Find the name of all employees who work for first bank corporation.

$\Pi_{\text{person\_name}} (\sigma_{\text{company\_name}="first bank corporation"}(\text{works}))$

- ii) Find the name and cities of residence of all employees who work for first bank corporation.

$\Pi_{\text{person\_name},\text{city}} (\sigma_{\text{company\_name}="first bank corporation"}(\text{employee} \bowtie \text{works}))$

- iii) Find the name, street address and city of residence of all employees who work for first bank corporation and earn more than \$10000 per annum.

$\Pi_{\text{person\_name},\text{street},\text{city}} (\sigma_{\text{company\_name}="first bank corporation" \wedge \text{salary}>10000}(\text{employee} \bowtie \text{works}))$

(Here we assume attribute named salary represent Annual Salary)

- iv) Find the name of all employees in this database who lives in same city as the company for which they work.

$\Pi_{\text{person\_name}}(\text{employee} \bowtie \text{works} \bowtie \text{company})$

- v) Find the name of all employees who live in the same city and on the same street as do their managers.

$\Pi_{\text{person\_name}} ((\text{employee} \bowtie \text{manages}) \bowtie_{(\text{manages.manager\_name}=\text{employee2.person\_name} \wedge \text{employee.street}=\text{employee2.street} \wedge \text{employee.city}=\text{employee2.city})} (\rho_{\text{employee2}} (\text{employee})))$

- vi) Find the name of all employees in this database who do not work for first bank corporation

$\Pi_{\text{person\_name}} (\sigma_{\text{company\_name} \neq "first bank corporation"}(\text{works}))$

- vii) Assume that companies may located in several cities. Find all companies located in every city in which small bank corporation is located.

$\Pi_{\text{company\_name},\text{city}}(\text{company}) \div \Pi_{\text{city}} (\sigma_{\text{company\_name}="small bank corporation"}(\text{company}))$

**2. Consider the following relational database.**

**Students(RollNo, StudentName, Address, Semester)**

**Teachers(TeacherID, TeacherName, CourseID, Salary, Department)**

**Courses(CourseID, RollNo, CourseTitle, Semester)**

**Write relational Algebra Expressions for the following requests.**

- i) Find the name of students of 4<sup>th</sup> semester and studying “Operating System”**

$\Pi_{\text{StudentName}} (\sigma_{\text{Semester} = \text{"4th"} \wedge \text{CourseTitle} = \text{"Operating System"}} (\text{Students} \bowtie \text{Courses}))$

- ii) Find the name of teacher who teaches subject “DBMS” to “Arten Khadka”**

$\Pi_{\text{TeacherName}} (\sigma_{\text{CourseTitle} = \text{"DBMS"} \wedge \text{StudentName} = \text{"Arten Khadka"}} ((\text{Students} \bowtie \text{Courses}) \bowtie \text{Teachers}))$

- iii) Delete Record of 2<sup>nd</sup> semester students of Account Department**

$\text{Students} \leftarrow \Pi_{\text{RollNo, StudentName, Address, Semester}} (\text{Students})$

$-\Pi_{\text{RollNo, StudentName, Address, Semester}} (\sigma_{\text{Department} = \text{"account"} \wedge \text{Semester} = 2\text{nd}} ((\text{Students} \bowtie \text{Courses}) \bowtie \text{Teachers}))$

- iv) Increase salary of “Bhaskar Bhatta” by 6%**

$\text{Teachers} \leftarrow \Pi_{\text{TeacherID, TeacherName, CourseID, Salary} * 1.06, \text{Department}} (\sigma_{\text{TeacherName} = \text{"Bhaskar Bhatta"}} (\text{Teachers})) \cup (\text{Teachers} - \sigma_{\text{TeacherName} = \text{"Bhaskar Bhatta"}} (\text{Teachers}))$

**3. Consider the following schema**

**SUPPLIER(Sid, S\_name, S\_addr)**

**PARTS(Pid, p\_name, color)**

**CATALOG(sid, pid, cost)**

**[PU:2014 fall]**

Now answer the following queries in Relational Algebra.

- i) Find the name of all supplier who supply yellow parts**

$\Pi_{\text{S\_name}} (\sigma_{\text{color} = \text{'yellow'}} (\text{SUPPLIER} \bowtie \text{CATALOG} \bowtie \text{PARTS}))$

- ii) Find the name of suppliers who supply Both blue and black parts.**

$\Pi_{\text{S\_name, color}} (\text{SUPPLIER} \bowtie (\text{CATALOG} \bowtie \text{PARTS})) \div \Pi_{\text{color}} (\sigma_{\text{color} = \text{'blue'} \wedge \text{color} = \text{'black'}} (\text{PARTS}))$

- iii) Find the name of suppliers who supply all parts.**

$\Pi_{\text{S\_name, Pid}} (\text{SUPPLIER} \bowtie \text{CATALOG}) \div \Pi_{\text{Pid}} (\text{PARTS})$

4. Consider the following schema

customer(cus\_id,cus\_name,cus\_phno)  
employee(cus\_id,emp\_id,emp\_name,emp\_add)  
works(branch\_id,salary,cus\_id)  
branch(branch\_id,branch\_name)

Write relational algebra notations for the following queries for the given schema.  
[PU:2011 spring]

- i) select name of all employees.

$\Pi_{\text{emp\_name}}(\text{employee})$

- ii) Give salary rise to 5% to all the employee

$\text{works} \leftarrow \Pi_{\text{branch\_id}, \text{salary} * 1.05, \text{cust\_id}}(\text{works})$

- iii) List all branch names

$\Pi_{\text{branch\_name}}(\text{branch})$

- iv) select name of all employees working for “manang” branch

$\Pi_{\text{emp\_name}}(\sigma_{\text{branch\_name} = \text{“manang”}}(\text{branch} \bowtie (\text{works} \bowtie \text{employee})))$

- v) Delete any record from work table

$\text{works} \leftarrow \text{works} - \sigma_{\text{branch\_id} = 101}(\text{works})$

*This operation can be customized according to requirement.*

- vi) List the name and phno of all customers

$\Pi_{\text{cust\_name}, \text{cus\_phno}}(\text{customer})$

- vii) select name of all employees deal with customer having id “201”

$\Pi_{\text{emp\_name}}(\sigma_{\text{cus\_id} = 201}(\text{employee}))$

- viii) Delete all records from works table whose salary is less than 10000

$\text{works} \leftarrow \text{works} - \sigma_{\text{salary} < 10000}(\text{works})$

- ix) Delete all records from works table

$\text{works} \leftarrow \text{works} - \Pi_{\text{branch\_id}, \text{salary}, \text{cus\_id}}(\text{works})$

5. By using the following schemas write relational algebraic expression and SQL statements. (underlined attributes represent primary key attributes)

EMPLOYEE(EMPNO,NAME,ADDRESS)  
 PROJECT(PNO,PNAME)  
 WORKON(EMPNO,PNO)  
 PART(PARTNO,PARTNAME,QTY\_ON\_HAND)  
 USE(EMP\_NO,PNO,PARTNO,NUMBER)

- i) Listing all employees details who are not working yet

$$\Pi_{EMPNO,NAME,ADDRESS} (Employee) - \Pi_{EMPNO,NAME,ADDRESS} (Employee \bowtie WORKON)$$

- ii) Listing Part Name and Quantity on hand those were used in DBMS project

$$\Pi_{PARTNAME,QTY\_ON\_HAND} (PART \bowtie (USE \bowtie \sigma_{PNAME='DBMS'}(PROJECT)))$$

OR

$$\Pi_{PARTNAME,QTY\_ON\_HAND} ( \sigma_{PNAME='DBMS'} (PART \bowtie (USE \bowtie PROJECT)))$$

- iii) List the name of projects that are used by employee from Kathmandu

$$\Pi_{PNAME} ( \sigma_{ADDRESS='Kathmandu'} ((EMPLOYEE \bowtie WORKON) \bowtie PROJECT))$$

6. Consider the following relations for order processing database application in a company.

CUSTOMER(Cust#,Cname,City)  
 ORDER(Order#,Odate,Cust#,ord\_Amt)  
 ORDER\_ITEM(Order#,Item#,Qty)  
 ITEM(Item#,Unit\_price)  
 SHIPMENT(Order#,Warehouse#,Ship\_date)  
 WAREHOUSE(Warehouse#,City)

Answer the following queries in relational algebra.

- i) List the order# and ship\_date for all orders shipped from Warehouse number "W2".

$$\Pi_{Order\#,Ship\_date} (\sigma_{warehouse\#='w2'} (SHIPMENT))$$

- ii) List the warehouse information for which the customer named 'JOSE Copez' was supplied his orders.

$$\Pi_{\text{warehouse\#,city}} (\sigma_{\text{Cname}=\text{"JOSE Copez"}} (\text{CUSTOMER} \bowtie (\text{ORDER} \bowtie (\text{SHIPMENT} \bowtie \text{WAREHOUSE})))$$

- iii) List the orders that were not shipped within 30 days of ordering.

$$\text{TIMELY\_SHIPPED} \leftarrow \sigma_{\text{Ship\_date} \leq \text{Odate}+30} (\text{ORDER} \bowtie \text{SHIPMENT})$$

$$\text{RESULT} \leftarrow \Pi_{\text{Order\#}} (\text{ORDER}) - \Pi_{\text{Order\#}} (\text{TIMELY\_SHIPPED})$$

- iv) List the order# for orders that were shipped from all warehouses in the network.

$$\Pi_{\text{Order\#, Warehouse\#}} (\text{Shipment}) \div \Pi_{\text{Warehouse\#}} (\sigma_{\text{City} = \text{"New York"}} (\text{Warehouse}))$$

7. consider the following database: [PU:2012 fall]

Student(sid,name,age)

Has(sid,cid)

College(cid,cname)

Write relational algebra expression to perform the following.

- i) find the average age of student.

$$\mathcal{G}_{\text{avg(age)}} (\text{Student})$$

- ii) Display the name of student who studies in "QWERT" college.

$$\Pi_{\text{name}} (\sigma_{\text{cname}=\text{"QWERT"}} (\text{Student} \bowtie (\text{Has} \bowtie \text{College})))$$

- iii) Insert a new student.

$$\text{Student} \leftarrow \text{Student} \cup \{104, \text{"Roshan"}, 29\}$$

- iv) Delete record of "ASDFG" college from college relation

$$\text{College} \leftarrow \text{College} - (\sigma_{\text{cname}=\text{"ASDFG"}} (\text{College}))$$

- v) Display name of students whose name begin from 'S.'

$$\Pi_{\text{name}} (\sigma_{\text{name LIKE 'S\%'}} (\text{Student}))$$

8. Consider the following schema: [PU:2017 fall]

employee(person\_name,street,city)

works(person\_name,company\_name,salary)

company(company\_name,city)

manages(person\_name,manager\_name)

Given an expression in relational algebra to express each of the following queries.

i) Find the name of all employees who earn more than their managers.

$\Pi_{\text{person\_name}} ((\text{works} \bowtie \text{manages}) \bowtie_{\text{manages.manager\_name}=\text{e2.person\_name} \wedge \text{works.salary} > \text{e2.salary}} (\rho_{\text{e2}} (\text{works})))$

*In SQL this will work*

*SELECT works.person\_name*

*FROM works NATURAL JOIN manages*

*JOIN works AS e2 ON manages.manager\_name = e2.person\_name*

*AND works.salary > e2.salary;*

ii) Find the name of all employees who live in the same city and on the same street as their managers.

$\Pi_{\text{person\_name}} ((\text{employee} \bowtie \text{manages}) \bowtie_{(\text{manages.manager\_name}=\text{employee2.person\_name} \wedge \text{employee.street}=\text{employee2.street} \wedge \text{employee.city}=\text{employee2.city})} (\rho_{\text{employee2}} (\text{employee})))$

iii) Find the name of all employees with database that do not work for "NBL company".

$\Pi_{\text{person\_name}} (\sigma_{\text{company\_name} \neq \text{"NBL company"}} (\text{works}))$

iv) Find the name of all employees in the database who earn more than top earner at "NBL company in the database".

$\text{topearner} \leftarrow \mathcal{G}_{\max(\text{salary})} (\sigma_{\text{company\_name} = \text{"NBL company"}} (\text{works}))$   
 $\text{result} \leftarrow \Pi_{\text{person\_name}} (\sigma_{\text{salary} > \text{topearner}} (\text{works}))$

9. Consider the relational database of figure below, where primary keys are underlined. Given an expression in the relational algebra to express each of the following queries. [PU:2014 spring]

Employee(person\_name,street,city)

Works(person\_name,bank\_name,salary)

Bank(bank\_name,city)

Manages(person\_name,manager\_name)

- i) Find the total salary sum of all the banks.

$$\mathcal{G}_{\text{sum(salary)}}(\text{works})$$

- ii) Modify the database so that Ram now lives in Kathmandu.

$$\text{Employee} \leftarrow \Pi_{\text{person\_name,street,"Kathmandu"}} (\sigma_{\text{person\_name}=\text{"Ram"}}(\text{Employee})) \\ \cup (\text{Employee} - \sigma_{\text{person\_name}=\text{"Ram"}}(\text{Employee}))$$

- iii) Find the name, street address and cities of residence of all employees who work for Nepal world Bank corporation and earn more than \$10,000 per annum.

$$\Pi_{\text{person\_name,street,city}} (\sigma_{\text{bank\_name}=\text{"Nepal World Bank Corporation"} \wedge \text{salary} > 10000} (\text{Employee} \bowtie \text{Works}))$$

*Here, we assume attribute named salary represent annual salary.*

- iv) Delete all tuples in work relation for employee of small bank corporation.

$$\text{Works} \leftarrow \text{Works} - \sigma_{\text{bank\_name}=\text{"Small Bank Corporation"}}(\text{Works})$$

10. Consider the following relational database of figure below, Where primary keys are underlined.  
Given an expression in the relational algebra to express each of the following queries.

employee(person\_name,street,city)  
works(person\_name,bank\_name,salary)  
bank(bank\_name,city)  
manages(person\_name,manager\_name)

- i) Find the name of all employees who work for Nepal Rastra Bank and Salary greater than \$10000.

$$\Pi_{\text{person\_name}} (\sigma_{\text{bank\_name} = \text{"Nepal Rastra Bank"} \wedge \text{salary} > 10000} (\text{employee} \bowtie \text{works}))$$

- ii) Find the name and cities of residence of all employees who work for Nepal Rastra Bank

$$\Pi_{\text{person\_name}, \text{city}} (\sigma_{\text{bank\_name} = \text{"Nepal Rastra Bank"}} (\text{employee} \bowtie \text{works}))$$

- iii) Find name, street address, and cities of residence of all employees who work for Nepal Rastra Bank Corporation and earn more than \$10000 per annum.

$$\Pi_{\text{person\_name}, \text{street}, \text{city}} (\sigma_{\text{bank\_name} = \text{"Nepal Rastra Bank corporation"} \wedge \text{salary} > 10000 * 12} (\text{employee} \bowtie \text{works}))$$

(Here we assume that attributed named salary represents monthly salary)

- iv) Delete all tuples in work relation for employee of Nepal Rastra Bank

$$\text{works} \leftarrow \text{works} - \sigma_{\text{bank\_name} = \text{"Nepal Rastra Bank"}} (\text{works})$$

11. Consider the student registration database comprising of below schema.

Student(CRN,Name,Gender,Address,Telephone)  
Course(CourseID,CourseName,Hour,TeacherID)  
Teacher(TeacherID,TeacherName,Office)  
Registration(CRN,CourseID,Date)

- i) Count the number of student registered subject in year 2015 gender wise.

$$\text{Gender} \quad \text{count}(\text{CRN}) (\sigma_{\text{EXTRACT}(\text{YEAR FROM Date})=2015} (\text{Student}))$$

- ii) Show student details taught by teacher Ronit Shreshta.

$$\Pi_{\text{CRN}, \text{Name}, \text{Gender}, \text{Address}, \text{Telephone}} (\sigma_{\text{TeacherName} = \text{"Ronit Shreshta"}} ((\text{Student} \bowtie \text{Registration}) \bowtie \text{course}) \bowtie \text{Teacher}))$$

- iii) Delete student information taught by teacher N.Mathema

$$\text{Student} \leftarrow \text{Student} - \Pi_{\text{CRN}, \text{Name}, \text{Gender}, \text{Address}, \text{Telephone}} (\sigma_{\text{TeacherName} = \text{"N.Mathema"}} ((\text{Student} \bowtie \text{Registration}) \bowtie \text{course}) \bowtie \text{Teacher}))$$



12. Consider the following relational schema [PU:2018 Fall]

Department(**DepartmentID**,DepartmentName)  
Designation(**DesignationID**,DesignationName,Salary)  
Employee(**EmpID**,EmpName,Gender,DesignationID,DepartmentID)  
Allowance(**AllowanceID**,AllowanceName)  
Allowance\_Details(DetailID,EmpID,AllowanceID,Amount)

Write the relational algebraic expression for the following task:

i) Find the number of employees department-wise.

$$\text{DepartmentName} \overset{G}{\text{count(eid)}} (\text{Employee} \bowtie \text{Department})$$

ii) List the employee details whose salary is above 50000.

$$\Pi_{\text{EmpID,EmpName,Gender,DesignationID,DepartmentID}} (\sigma_{(\text{Salary}+\text{amount})>50000} ((\text{Employee} \bowtie \text{Designation}) \bowtie \text{Allowance}))$$

iii) List the employee those who are getting house allowance.

$$\Pi_{\text{EmpName}} (\sigma_{\text{AllowanceName}=\text{"houseallowance"}} ((\text{Employee} \bowtie \text{Allowance\_Details}) \bowtie \text{Allowance}))$$

13. Consider the relational database model

Users(uid,cname,city)  
Items(itemid,itemname,city,quantity,price)  
Manager(mid,aname,city)  
Query(queryno,uid,mid,itemid,query\_details,hitratio)  
[PU:2018 spring]

Write the relational algebraic expressions for the following tasks.

i) Find all (queryno,uid) pairs for query with a hit ratio value greater than 500.

$$\Pi_{\text{queryno,uid}} (\sigma_{\text{hitratio}>500} (\text{Query}))$$

ii) Find all item names of items in Pokhara ordered with query details as Pokhara details.

$$\Pi_{\text{itemname}} (\sigma_{\text{querydetails}=\text{"Pokhara details"} \wedge \text{city}=\text{"Pokhara"}} (\text{Items} \bowtie \text{Query}))$$

iii) Find item ids of items ordered through manager 35 but not through manager 27.

$$\Pi_{\text{itemid}} (\sigma_{\text{mid}=35} (\text{Query})) - \Pi_{\text{itemid}} (\sigma_{\text{mid}=27} (\text{Query}))$$

14. Using the following schema represent the following queries using Relational algebra.

PROJECT(Projectnum,ProjectName,ProjectType,ProjectManager)

EMPLOYEE(Empnum,Empname)

ASSIGNED\_TO(Projectnum,Empnum)

[PU:2019 spring]

i) Find employee details working on project name starts with 'L'.

$$\Pi_{\text{Empnum,Empname}}(\sigma_{\text{ProjectName Like 'L\%'}}((\text{EMPLOYEE} \bowtie \text{ASSIGNED\_TO}) \bowtie \text{PROJECT}))$$

ii) List all the employee details who are working under project manager "Rohan".

$$\Pi_{\text{Empnum,Empname}}(\sigma_{\text{ProjectManager="Rohan"}}((\text{EMPLOYEE} \bowtie \text{ASSIGNED\_TO}) \bowtie \text{PROJECT}))$$

iii) List the employees who are still not assigned with any project.

$$\Pi_{\text{Empnum,Empname}}(\text{EMPLOYEE}) - \Pi_{\text{Empnum,Empname}}(\text{EMPLOYEE} \bowtie \text{ASSIGNED\_TO})$$

iv) List the employees who are working in more than one project.

$$\text{temp} \leftarrow \Pi_{\text{Empname}} \left( \mathcal{G}_{\text{count (Projectnum)}} (\text{Employee} \bowtie \text{ASSIGNED\_TO}) \right)$$
$$\text{result} \leftarrow \Pi_{\text{Empname}}((\sigma_{\text{Projectnum} > 1}(\text{temp})))$$

**15. Write relational algebra for the following schemas. (Underlined indicates Primary key )**[PU:2020 spring]

Employee(Emp\_No,Name,Address)  
 Project(PNO,Pname)  
 Workon(Emp\_No,PNo)  
 Part(Partno,Part\_name,Qty\_on\_hand)  
 Use(Emp\_No,PNO,Partno,Number)

**i) Listing all employees details who are not working yet.**

$$\Pi_{\text{Emp\_No,Name,Address}} (\text{Employee}) - \Pi_{\text{Emp\_No,Name,Address}} (\text{Employee} \bowtie \text{Workon})$$

**ii) Listing Part Name and Quantity on hand those were used in DBMS project**

$$\Pi_{\text{Part\_name,Qty\_On\_hand}} (\text{Part} \bowtie (\text{Use} \bowtie \sigma_{\text{Pname}=\text{"DBMS"}}(\text{Project})))$$

**iii) List the name of projects that are used by employee from London**

$$\Pi_{\text{Pname}} (\sigma_{\text{Address}=\text{"London"}} ((\text{Employee} \bowtie \text{Workon}) \bowtie \text{Project}))$$

**iv) Modify the database so that Jones now live in USA.**

$$\text{Employee} \leftarrow \Pi_{\text{Emp\_No,Name,"USA"}} (\sigma_{\text{Name}=\text{"Jones"}} (\text{Employee})) \cup (\text{Employee} - \sigma_{\text{Name}=\text{"Jones"}} (\text{Employee}))$$

**v) Update address of an employee 'Japan' to 'USA'**

$$\text{Employee} \leftarrow \Pi_{\text{Emp\_No,Name,"USA"}} (\sigma_{\text{Address}=\text{"Japan"}} (\text{Employee})) \cup (\text{Employee} - \sigma_{\text{Address}=\text{"Japan"}} (\text{Employee}))$$