

$$I = \int_1^{10} (3x^3 + 2x^2 + 24x + 1) dx \quad \text{where}$$
$$a = 3$$
$$b = 2$$
$$c = 24$$
$$d = 1$$

$$= \int_1^{10} 3x^3 dx + \int_1^{10} 2x^2 dx + \int_1^{10} 24x dx + \int_1^{10} 1 dx$$

$$= 3 \left[\frac{x^4}{4} \right]_1^{10} + 2 \left[\frac{x^3}{3} \right]_1^{10} + 24 \left[\frac{x^2}{2} \right]_1^{10} + \left[x \right]_1^{10}$$

$$= 3 \left(\frac{10^4 - 1}{4} \right) + 2 \left(\frac{10^3 - 1}{3} \right) + 24 \left(\frac{10^2 - 1}{2} \right) + (10 - 1)$$

$$= 7500 - 0.75 + 666.67 - 0.67 + 1200 - 12 + 9$$

$$= 9376.67 - 14.2 = ~~9362.47~~ 9362.25$$

$$\therefore I_{\text{analytical}} = 9362.25$$