

00:24

Digital Image Processing

Lecture No – 51

Detection of Discontinuities

Dr. Sapna Katiyar

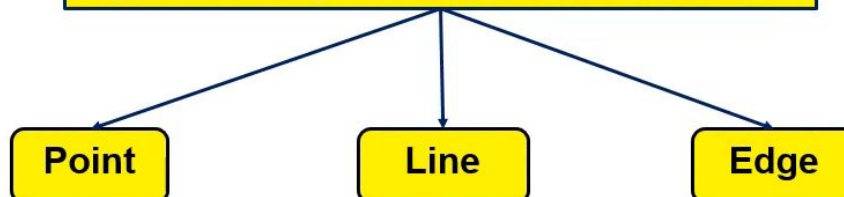
Professor, ECE Department



00:56

Detection of Discontinuities

Types of Grey Level discontinuities are:





02:20

02:24

Detection of Discontinuities

Types of Grey Level discontinuities are:

Point

* Isolated point

Line

* Horizontal
* Vertical
* Slanted



Edge

* Object outline



02:47

02:58

Detection of Discontinuities

Point Detection

An isolated point is a point whose grey level is significantly different from its background in a homogeneous area



03:55

Detection of Discontinuities

Point Detection

An isolated point is a point whose grey level is significantly different from its background in a homogeneous area

3x3				3x3		
	w_1	w_2	w_3	z_1	z_2	z_3
	w_4	w_5	w_6	z_4	z_5	z_6
	w_7	w_8	w_9	z_7	z_8	z_9
	Mask			Image		

Response of the mask:

$$R = \sum_{i=1}^9 w_i z_i$$



04:22

Detection of Discontinuities

Point Detection

An isolated point is a point whose grey level is significantly different from its background in a homogeneous area

3×3

w_1	w_2	w_3
w_4	w_5	w_6
w_7	w_8	w_9

Mask

3×3

z_1	z_2	z_3
z_4	z_5	z_6
z_7	z_8	z_9

Image

Response of the mask:

$$R = \sum_{i=1}^9 w_i z_i$$

If,
 $|R| \geq T$, a point is detected
 where,
 T is a non negative integer

-1	-1	-1
-1	8	-1
-1	-1	-1

Sample Mask for Point Detection



05:42

Detection of Discontinuities

Line Detection

In line detection, **four types of masks** are used to get the responses i.e, R_1 , R_2 , R_3 and R_4 for the directions vertical, horizontal, $+45^\circ$ and -45° respectively

→

-1	-1	-1
2	2	2
-1	-1	-1

Horizontal

-1	2	-1
-1	2	-1
-1	2	-1

Vertical

-1	-1	2
-1	2	-1
2	-1	-1

$+45^\circ$

2	-1	-1
-1	2	-1
-1	-1	2

-45°



06:24

Detection of Discontinuities

Line Detection

In line detection, **four types of masks** are used to get the responses i.e, R_1 , R_2 , R_3 and R_4 for the directions vertical, horizontal, $+45^\circ$ and -45° respectively

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-1	②	-1																																						
-1	-1	②																																						
	Horizontal	Vertical	+45°	-45°																																				

Response of the mask:

$$✓ R_k = \sum_{k=1}^4 \omega_k z_k$$

If, at a certain point in the image, $|R_i| > |R_j|$ for all $j \neq i$, that **point** is said to be more likely associated with a **line** in the direction of mask i



07:42

Detection of Discontinuities

Line Detection

In line detection, **four types of masks** are used to get the responses i.e, R_1 , R_2 , R_3 and R_4 for the directions vertical, horizontal, $+45^\circ$ and -45° respectively

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-1	②	-1																																						
-1	-1	②																																						
	Horizontal	Vertical	+45°	-45°																																				

$R_1 \rightarrow LR$
 $R_2 \rightarrow TB$
 R_3
 $✓ R_4$

Response of the mask:

$$✓ R_k = \sum_{k=1}^4 \omega_k z_k$$

If, at a certain point in the image, $|R_i| > |R_j|$ for all $j \neq i$, that **point** is said to be more likely associated with a **line** in the direction of mask i



08:30

Detection of Discontinuities

Edge Detection

- ❑ An edge is a set of connected pixels that lies on the boundary between two regions which differ in grey value. Pixels on edge is known as **edge points**
- ❑ **Edges provide an outline of the object**



12:00

Detection of Discontinuities

Edge Detection

Some of the commonly encountered edges in image processing are:

Step Edge

Ramp Edge

Spike Edge

Roof Edge



Detection of Discontinuities

Edge Detection

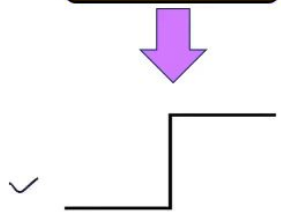
Some of the commonly encountered edges in image processing are:

Step Edge

Ramp Edge

Spike Edge

Roof Edge



An abrupt change in intensity



Detection of Discontinuities

Edge Detection

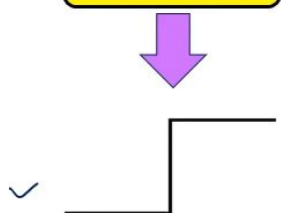
Some of the commonly encountered edges in image processing are:

Step Edge

Ramp Edge

Spike Edge

Roof Edge



An abrupt change in intensity



A slow and gradual change in intensity

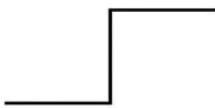


Detection of Discontinuities

Edge Detection

Some of the commonly encountered edges in image processing are:

Step Edge



An abrupt change in intensity

Ramp Edge



A slow and gradual change in intensity

Spike Edge



Quick change or immediately returns to original intensity level

Roof Edge



Detection of Discontinuities

Edge Detection

Some of the commonly encountered edges in image processing are:

Step Edge



An abrupt change in intensity

Ramp Edge



A slow and gradual change in intensity

Spike Edge



Quick change or immediately returns to original intensity level

Roof Edge



It is not instantaneous over short distance



13:54

Detection of Discontinuities

Stages in Edge Detection



14:36

Detection of Discontinuities

Stages in Edge Detection



It involves smoothing.
This stage may be
performed explicitly
or implicitly

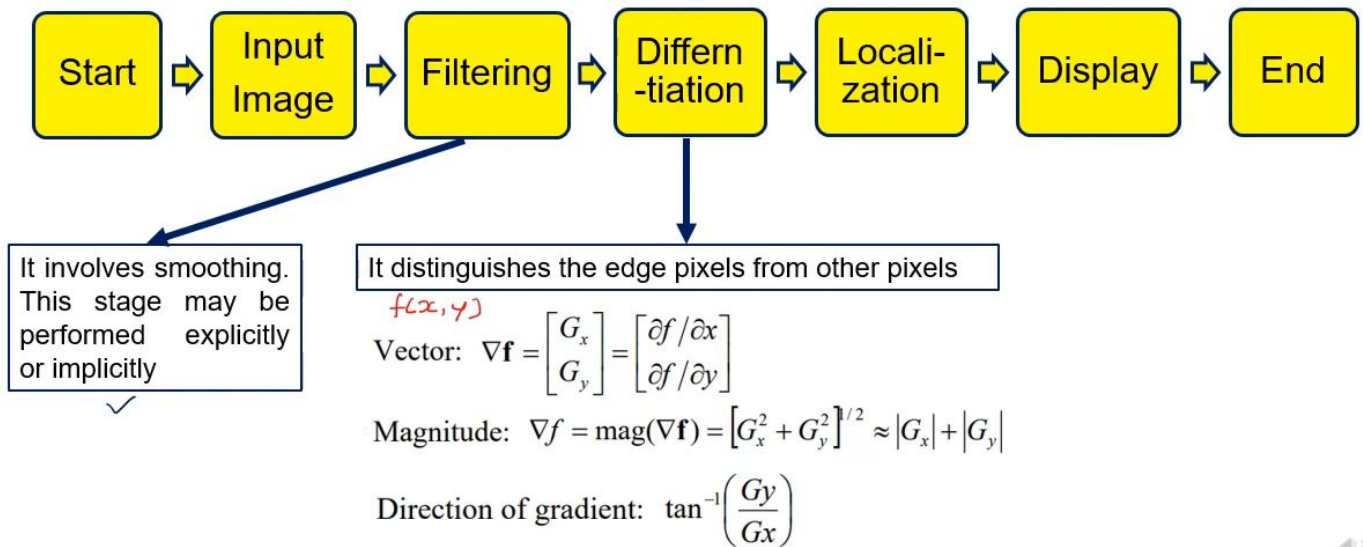


17:02

Detection of Discontinuities

Stages in Edge Detection

A B ✓

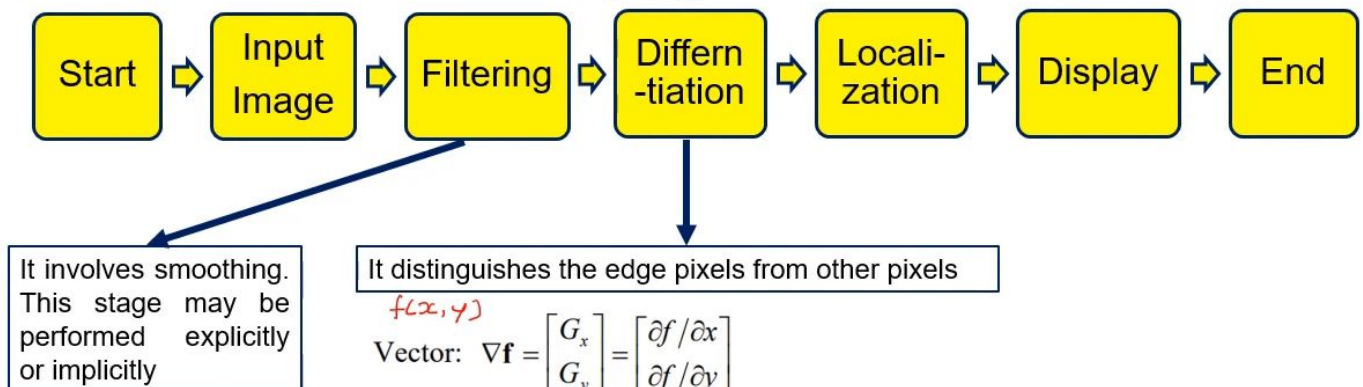


18:04

Detection of Discontinuities

Stages in Edge Detection

A B ✓



✓ Magnitude: $\nabla f = \text{mag}(\nabla \mathbf{f}) = [G_x^2 + G_y^2]^{1/2} \approx |G_x| + |G_y|$

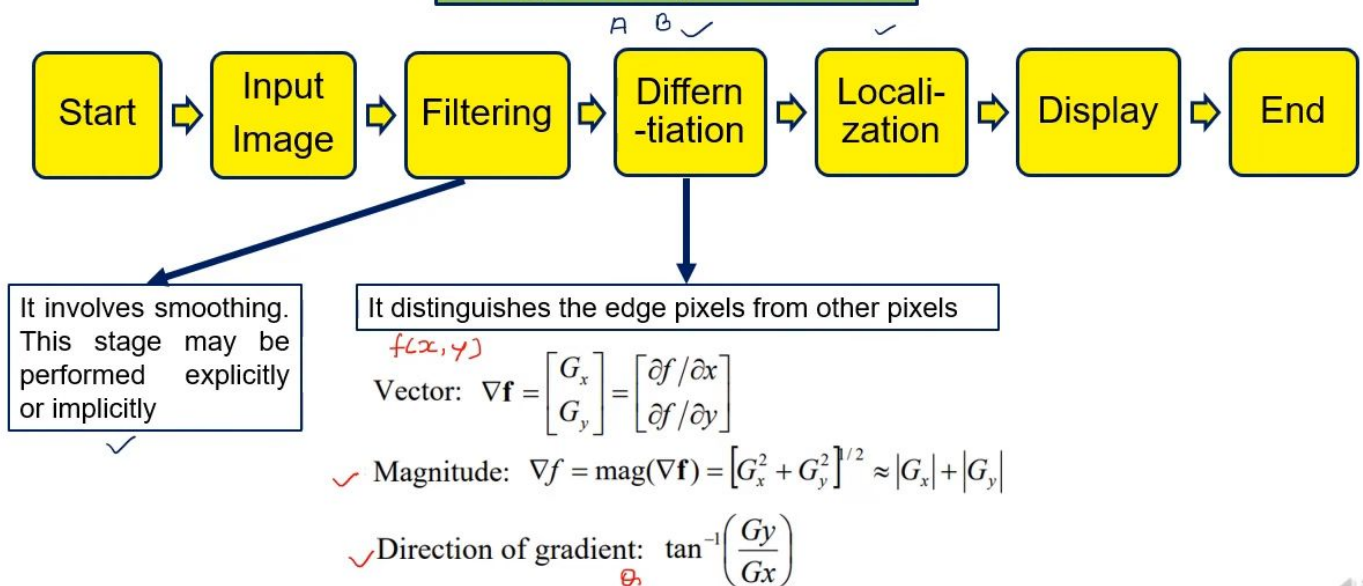
✓ Direction of gradient: $\tan^{-1}\left(\frac{G_y}{G_x}\right)$



18:31

Detection of Discontinuities

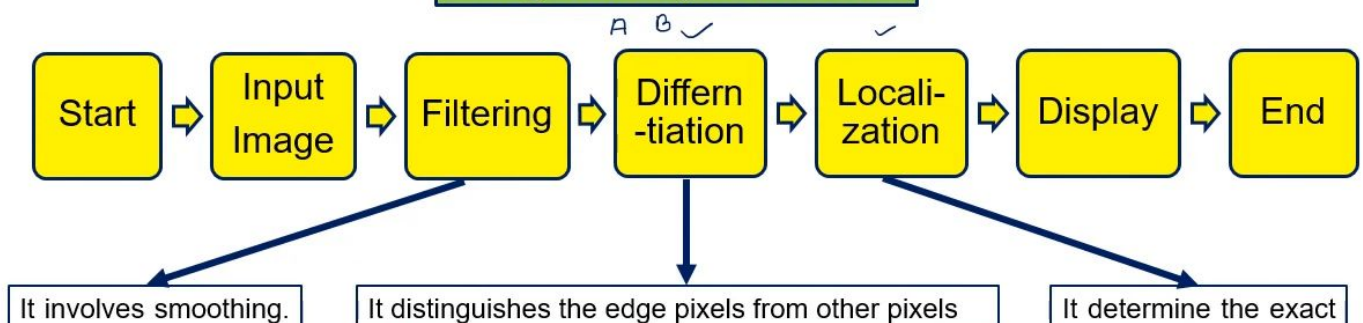
Stages in Edge Detection



19:10

Detection of Discontinuities

Stages in Edge Detection



This stage may be performed explicitly or implicitly



$f(x, y)$
Vector: $\nabla f = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \partial f / \partial x \\ \partial f / \partial y \end{bmatrix}$

location of edge



✓ Magnitude: $\nabla f = \text{mag}(\nabla f) = [G_x^2 + G_y^2]^{1/2} \approx |G_x| + |G_y|$

✓ Direction of gradient: $\theta = \tan^{-1}\left(\frac{G_y}{G_x}\right)$



19:31

Detection of Discontinuities

Edge Detection



20:00

Detection of Discontinuities

Edge Detection

Edge Detection Algorithms



Derivative
Types

Template
Matching

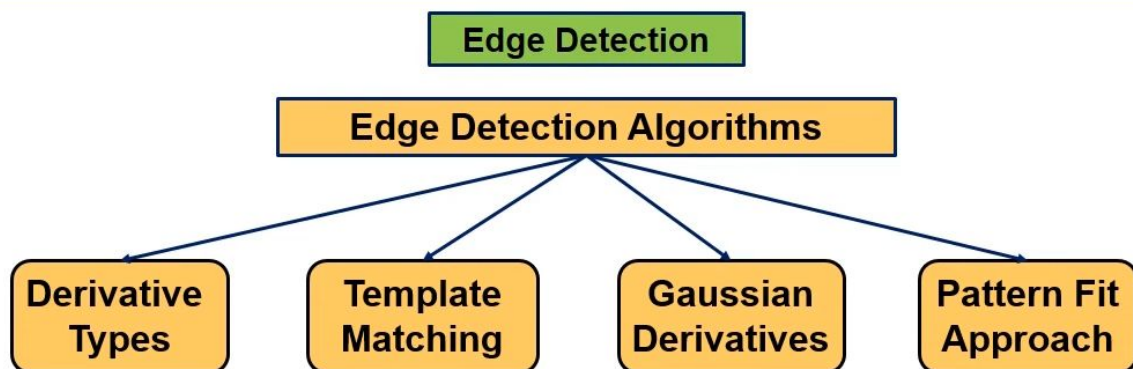
Gaussian
Derivatives

Pattern Fit
Approach



20:01

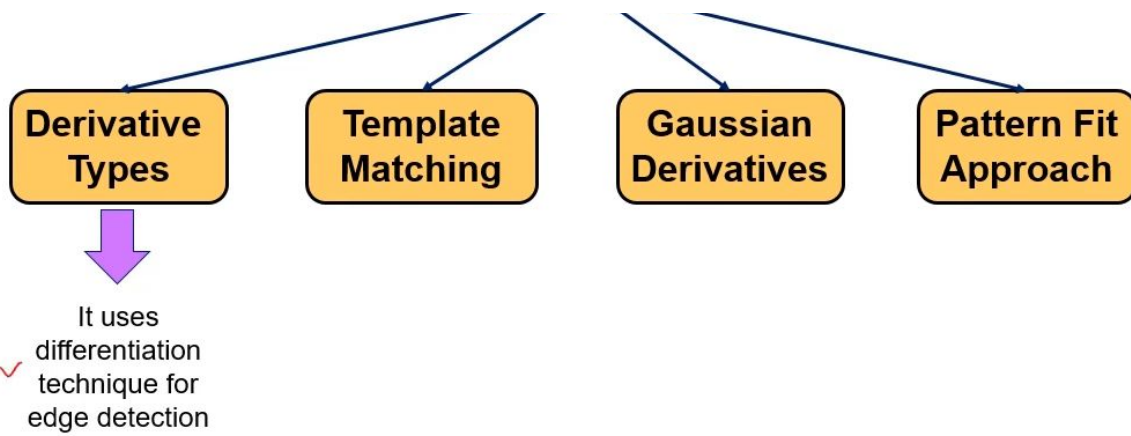
Detection of Discontinuities



20:15

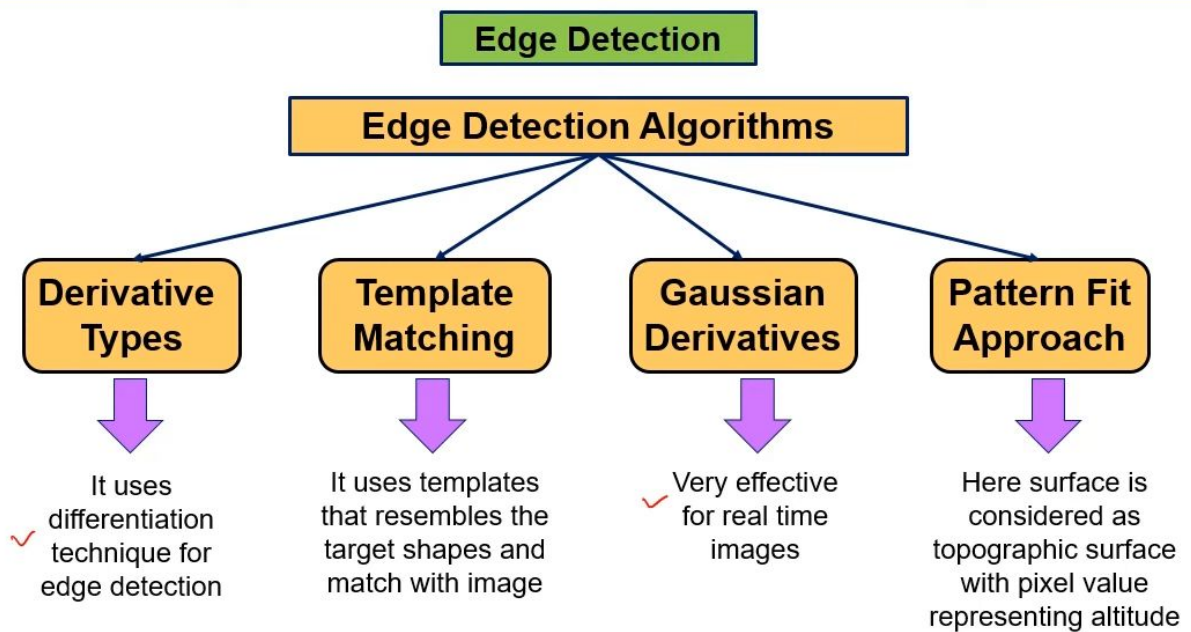
Detection of Discontinuities





21:27

Detection of Discontinuities



Detection of Discontinuities

Edge Detection

- ❑ An edge is a set of connected pixels that lies on the boundary between two regions which differ in grey value. Pixels on edge is known as **edge points**
- ❑ **Edges provide an outline of the object**



In physical plane, **edge corresponds** to the **discontinuities in** depth, Surface orientation, change in material properties, light variations etc.

- ❖ It locates sharp changes in the intensity function
- ❖ Edges are pixels where brightness changes abruptly
- ❖ An edge can be extracted by computing the derivative of the image function
 - ✓ **Magnitude of the derivative**, indicates the strength or contrast of edge
 - ✓ **Direction of the derivative vector**, indicates the edge orientation



