

Unfolding the Atmospheric Muon Flux with IceCube

Pascal Gutjahr

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CR Call

October 28, 2025

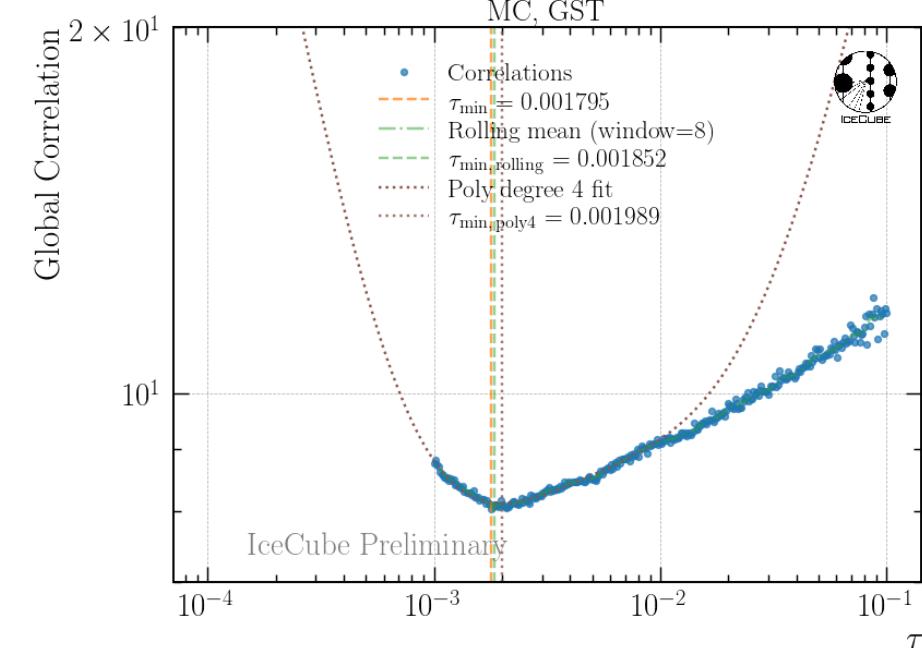
Determine Regularization

Regularization

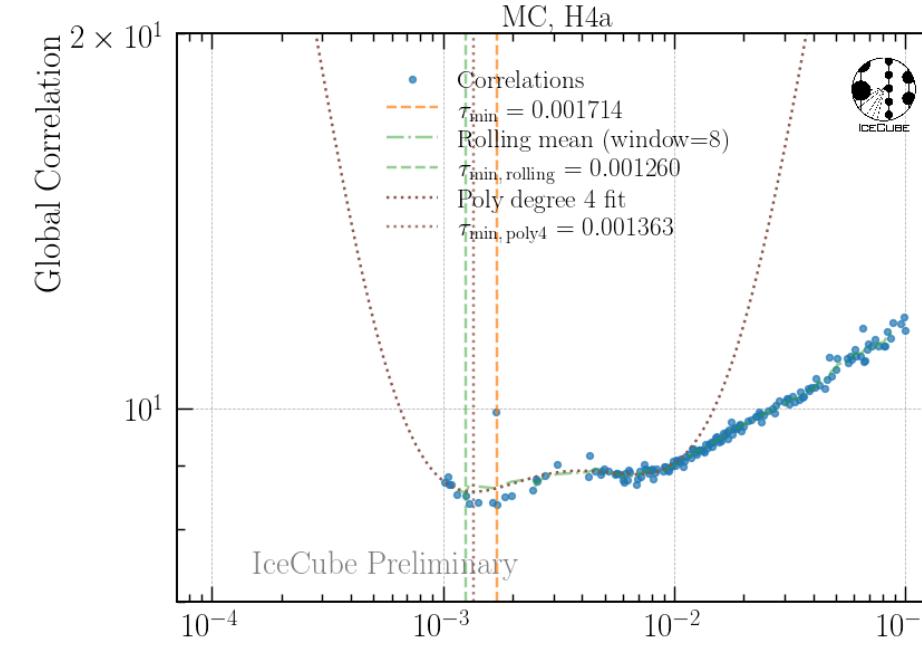
- Find regularization τ with minimal bin-to-bin correlation
- LLH minimization (unfolding) provides full covariance matrix V

➤ Minimize global correlation $\rho = \sum_{i > j} V_{ij}$

- Fits are only accepted, when minuit minimization is valid
 - Sometimes fits fail around the minimum
- Fit polynom from $10^{-3} - 10^{-2}$ to determine minimum



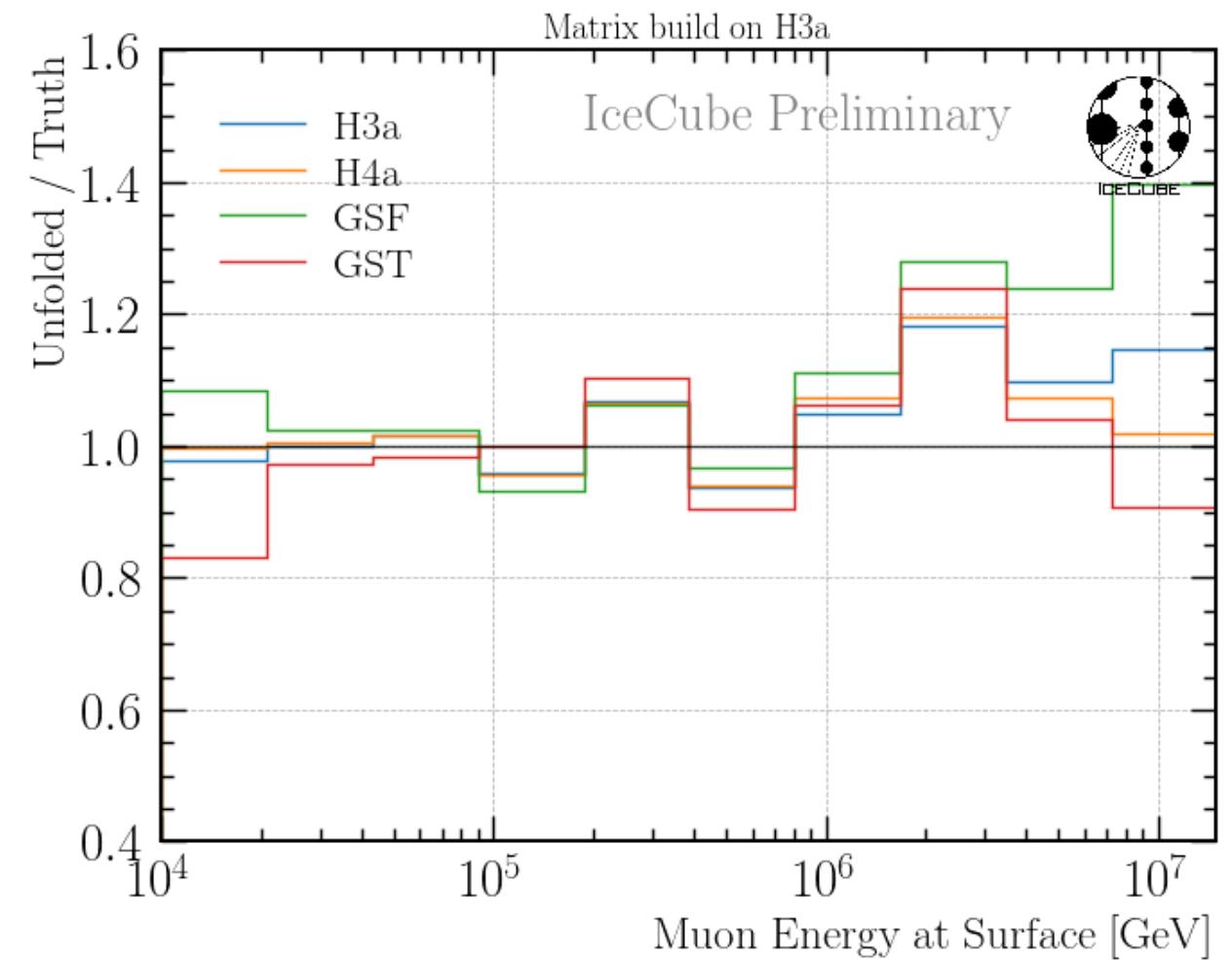
2 examples



“Method Bias”

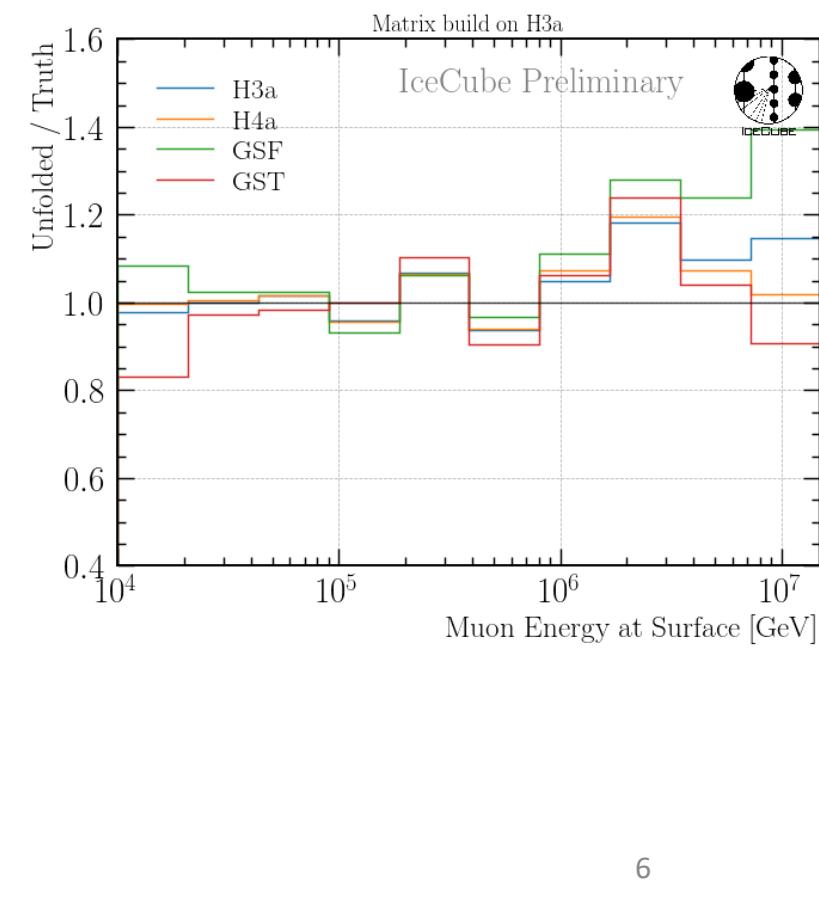
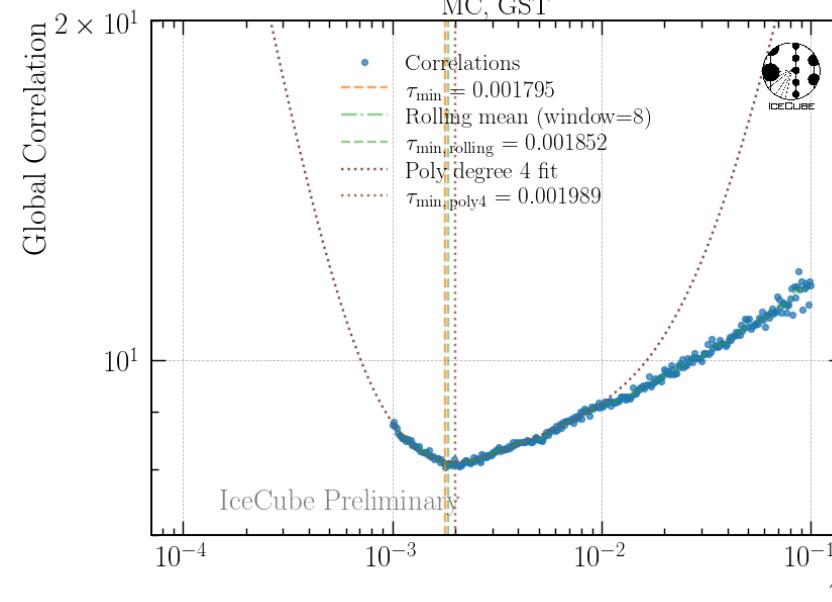
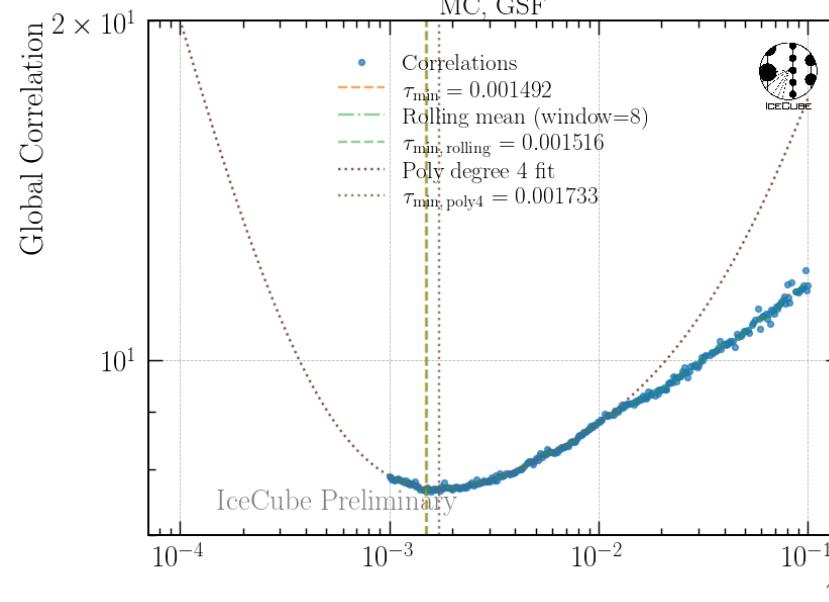
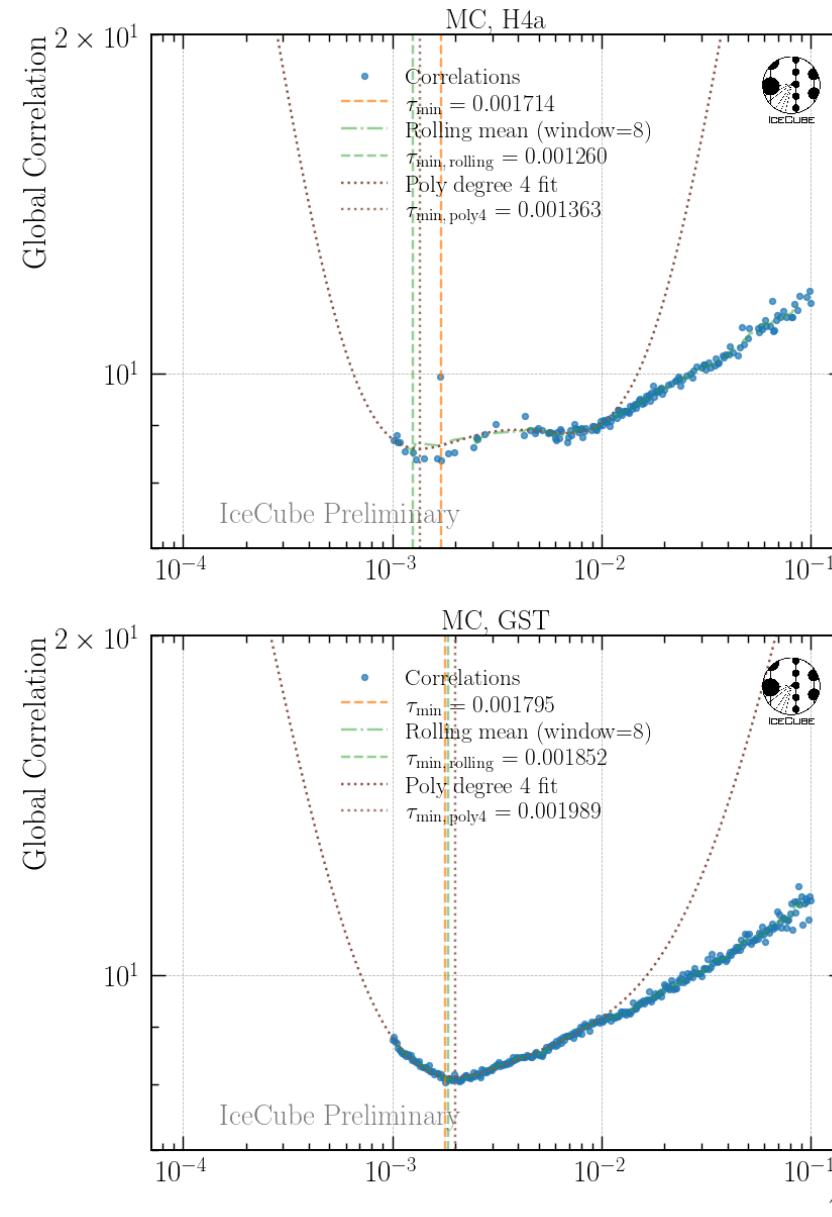
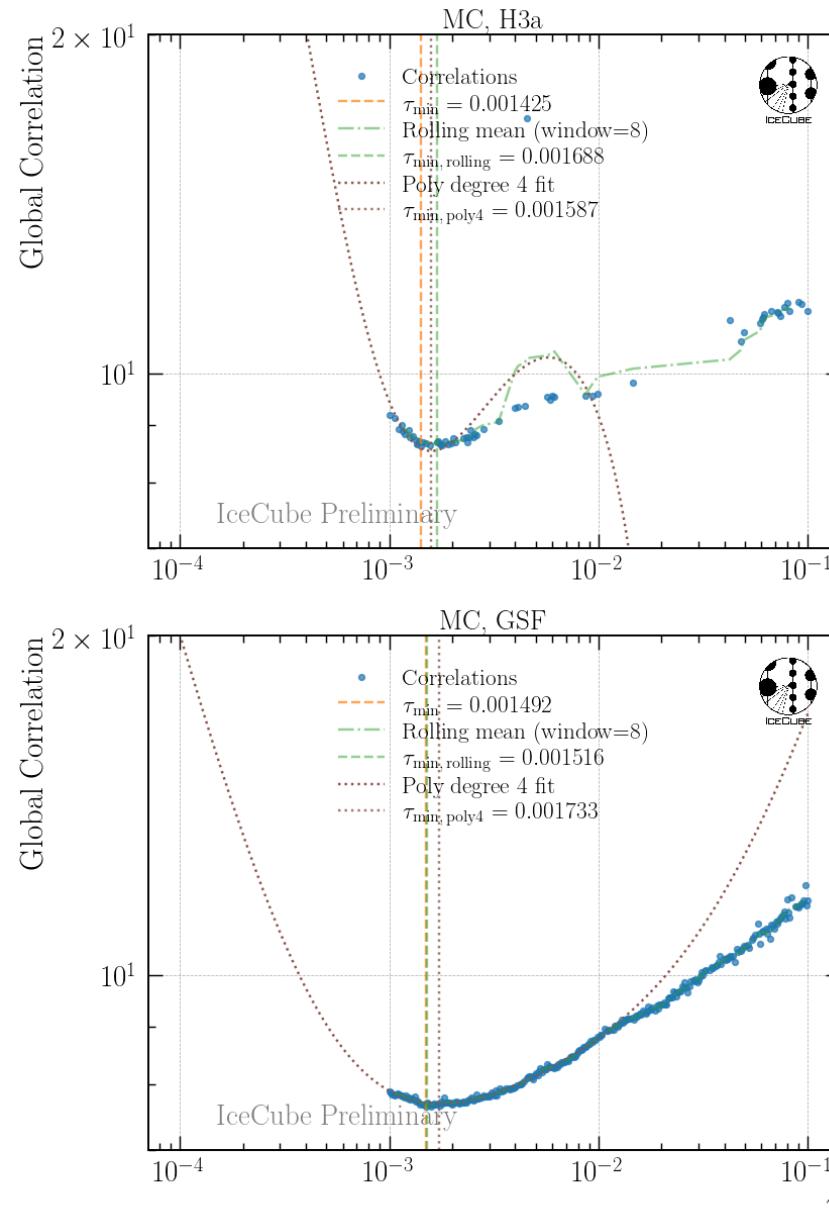
Uncertainties: “Unfolding Bias” (for H3a Matrix)

- Build unfolding matrix on H3a
- Unfold 4 MC weighted datasets for the 4 primary models
- Divide each unfolding by its true MC distribution
 - Ratio of 1 expected
 - Offset to 1 → bias



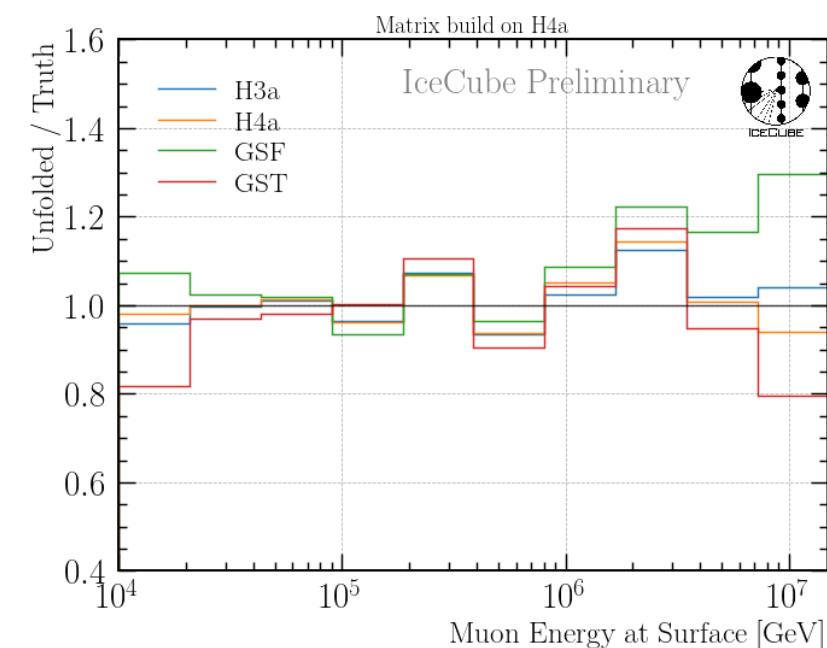
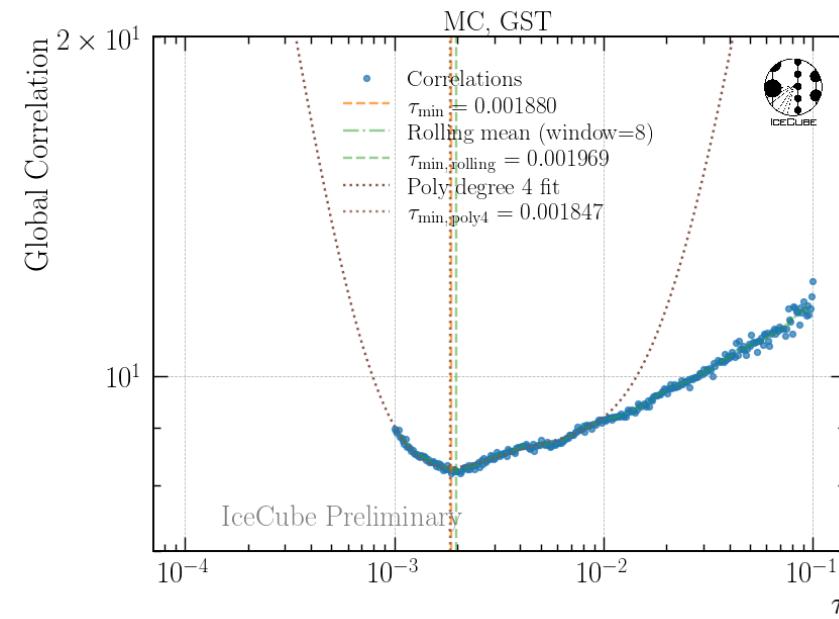
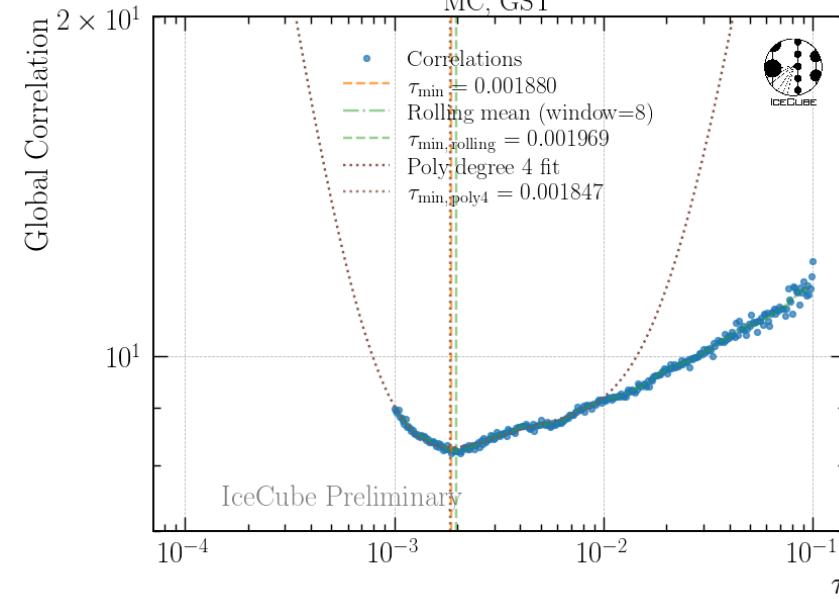
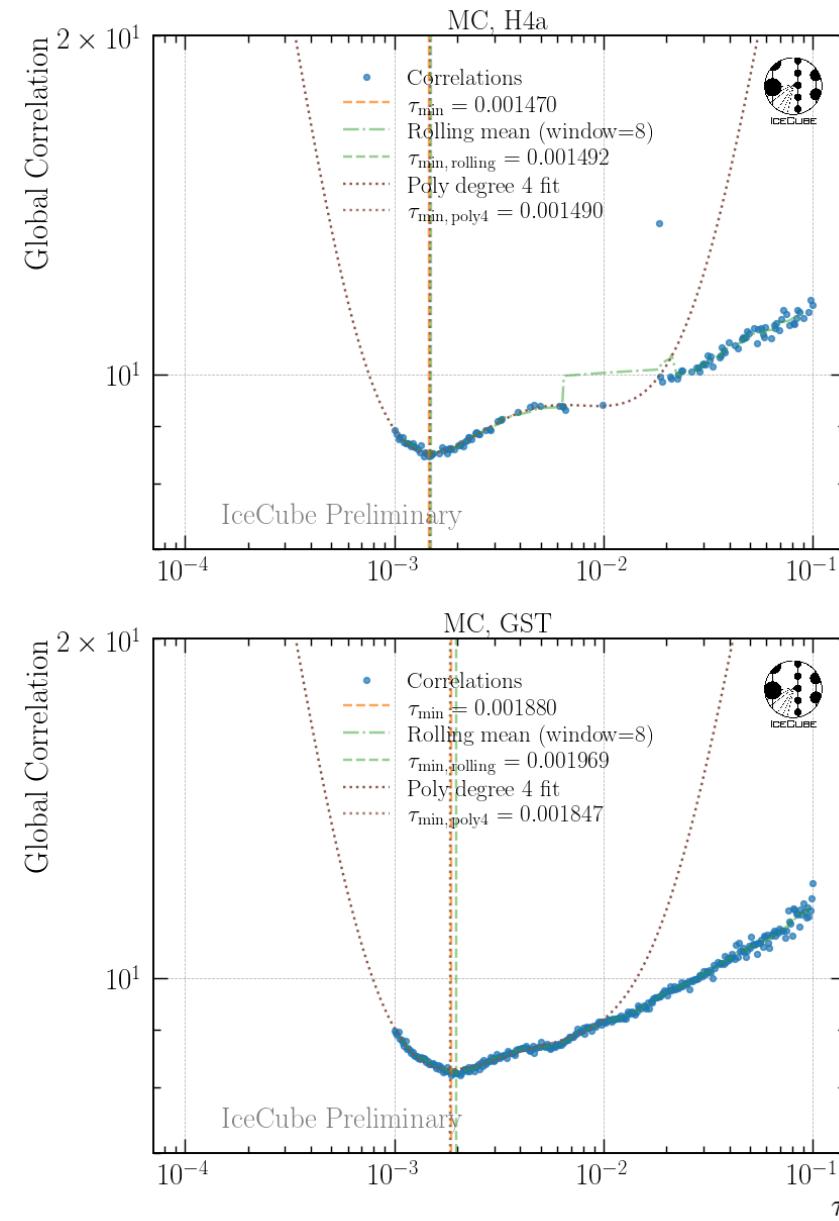
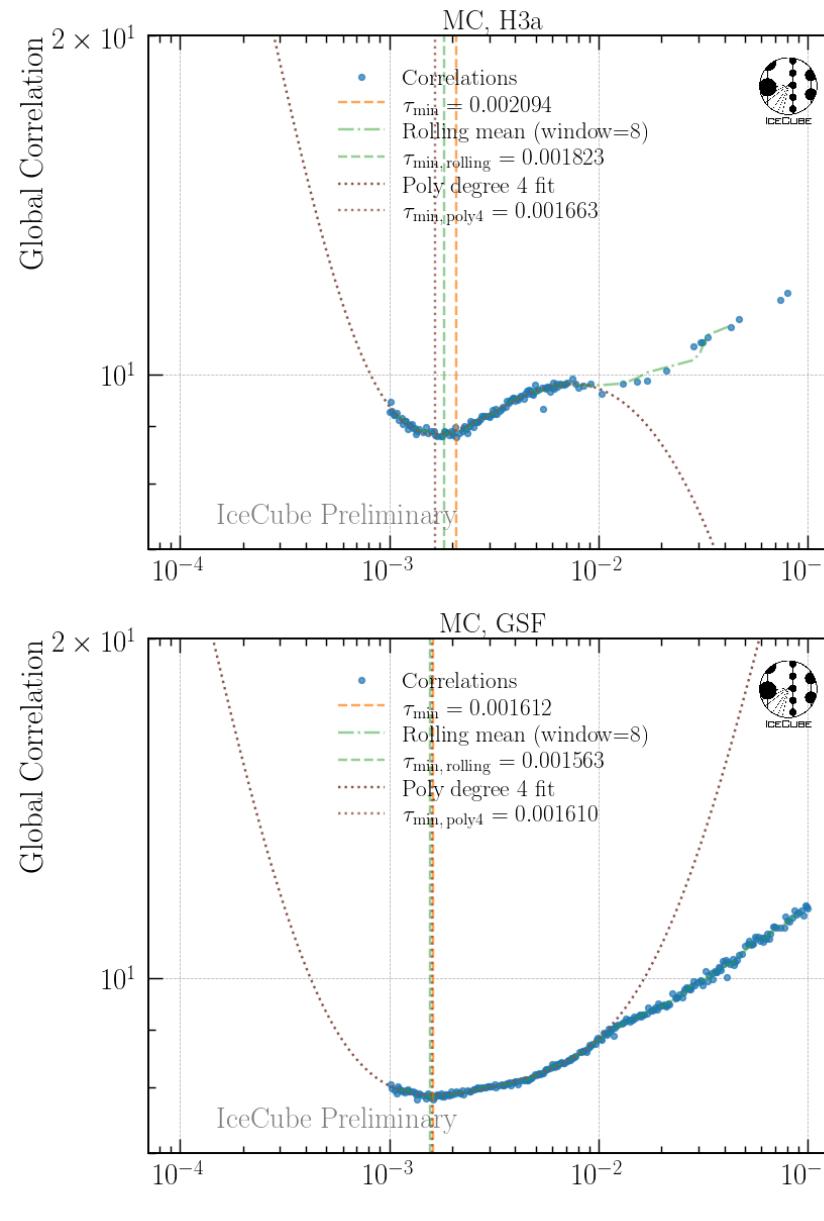
- Fit $\tau \in 10^{-3} - 10^{-2}$

H3a Unfolding Bias



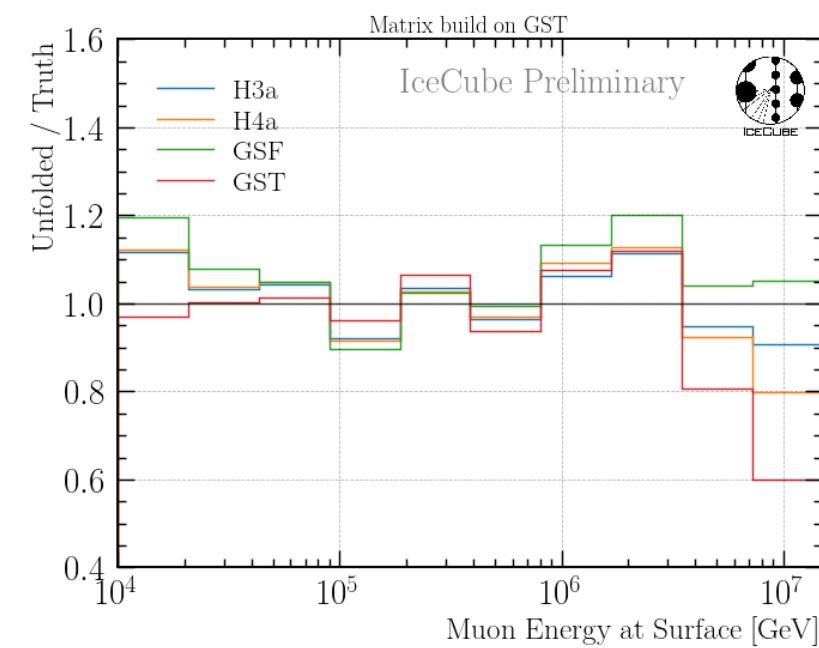
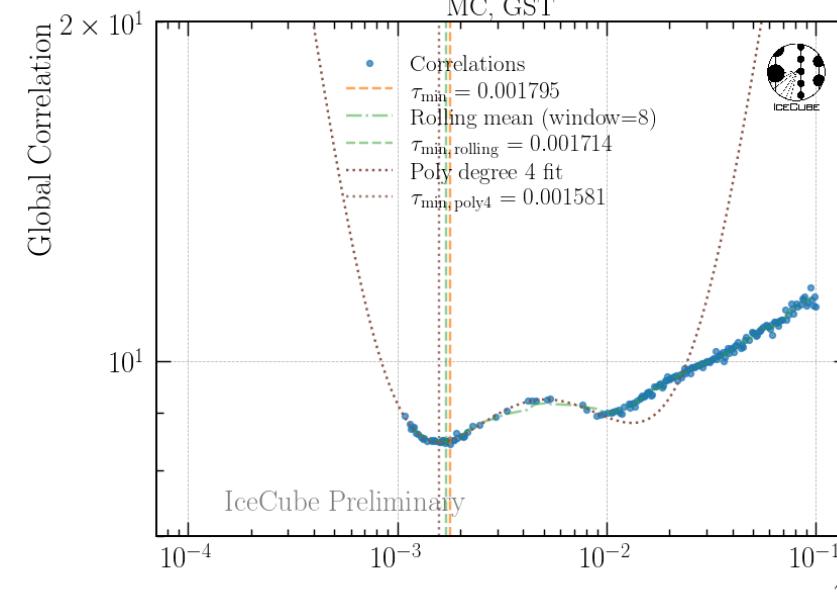
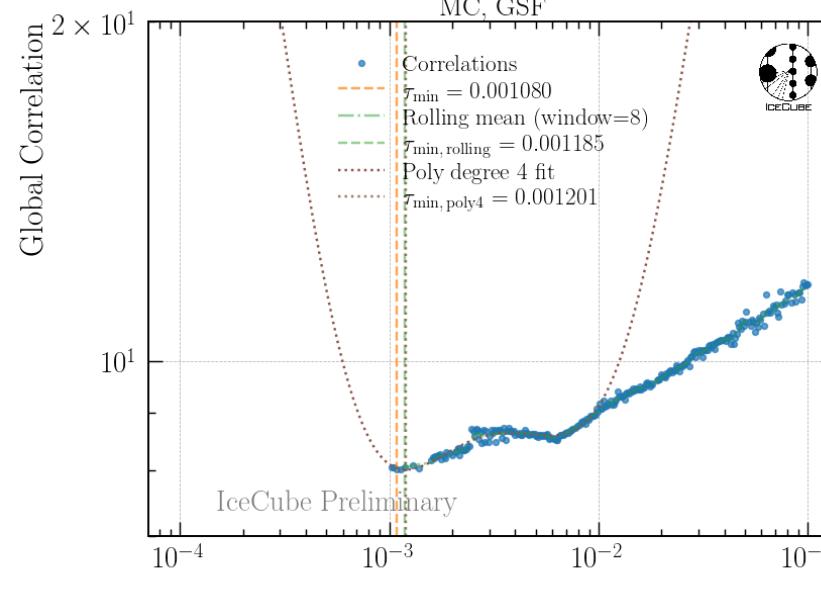
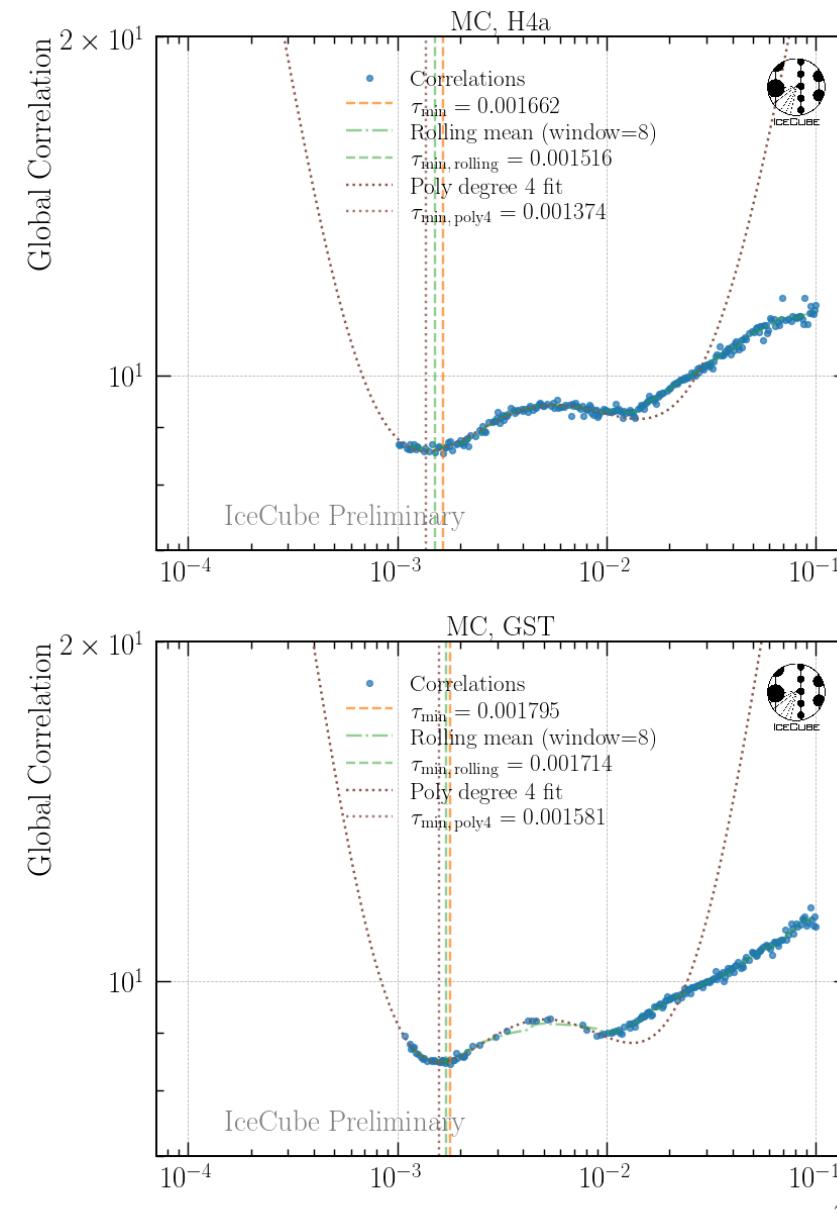
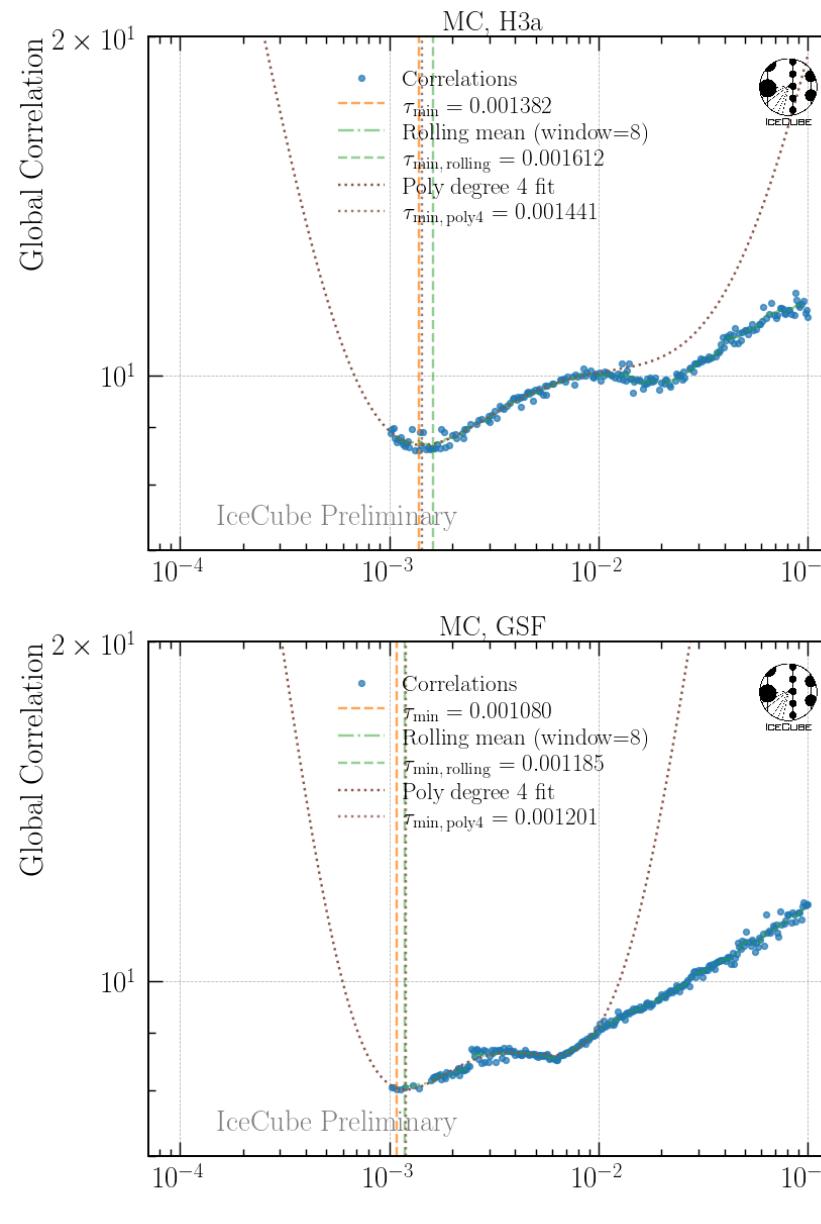
- Fit $\tau \in 10^{-3} - 10^{-2}$

H4a Unfolding Bias



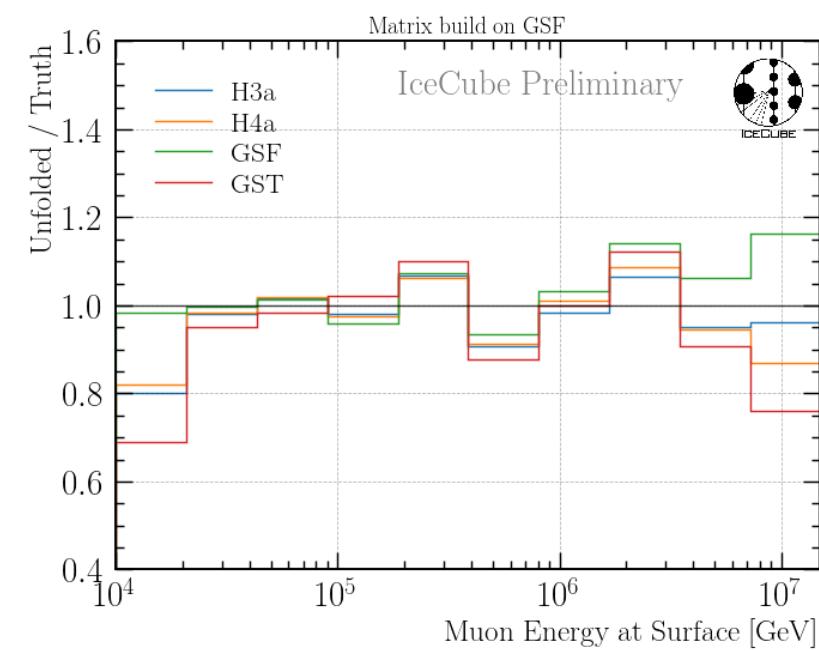
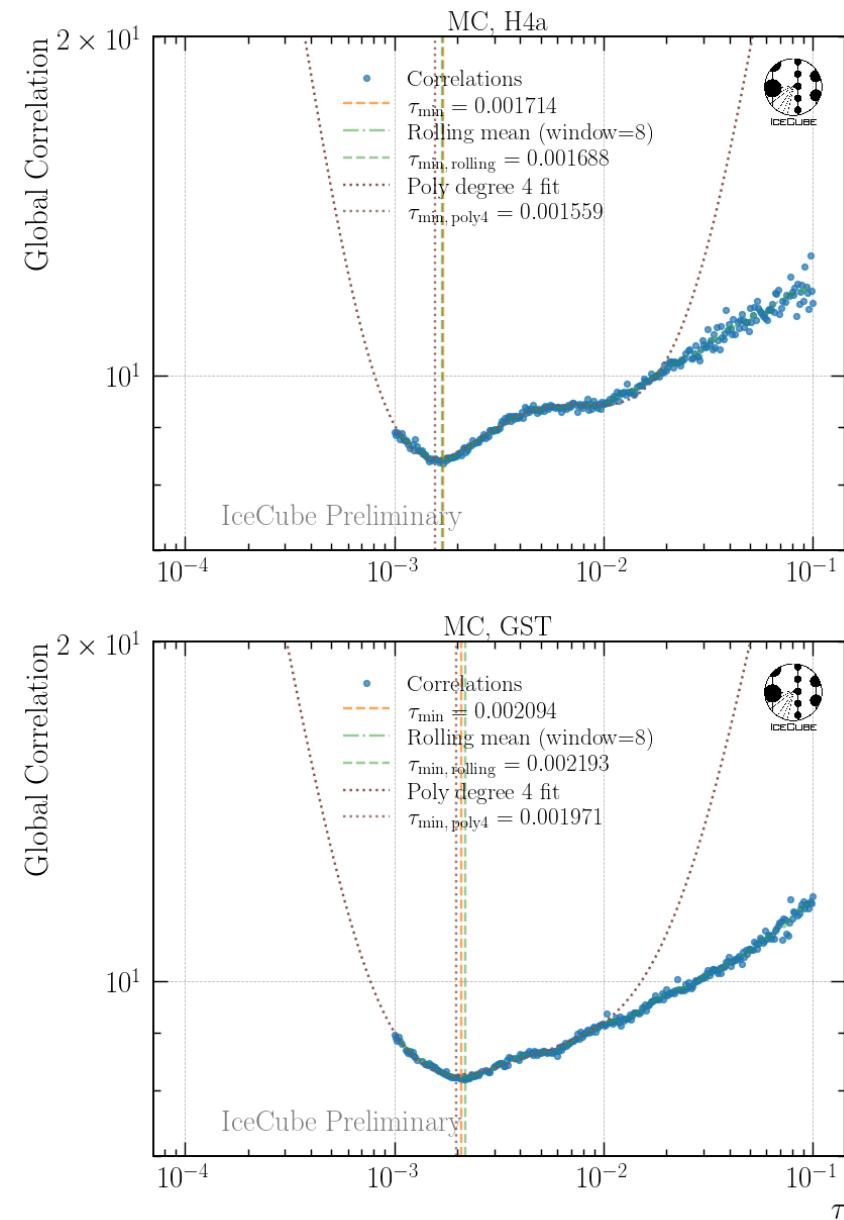
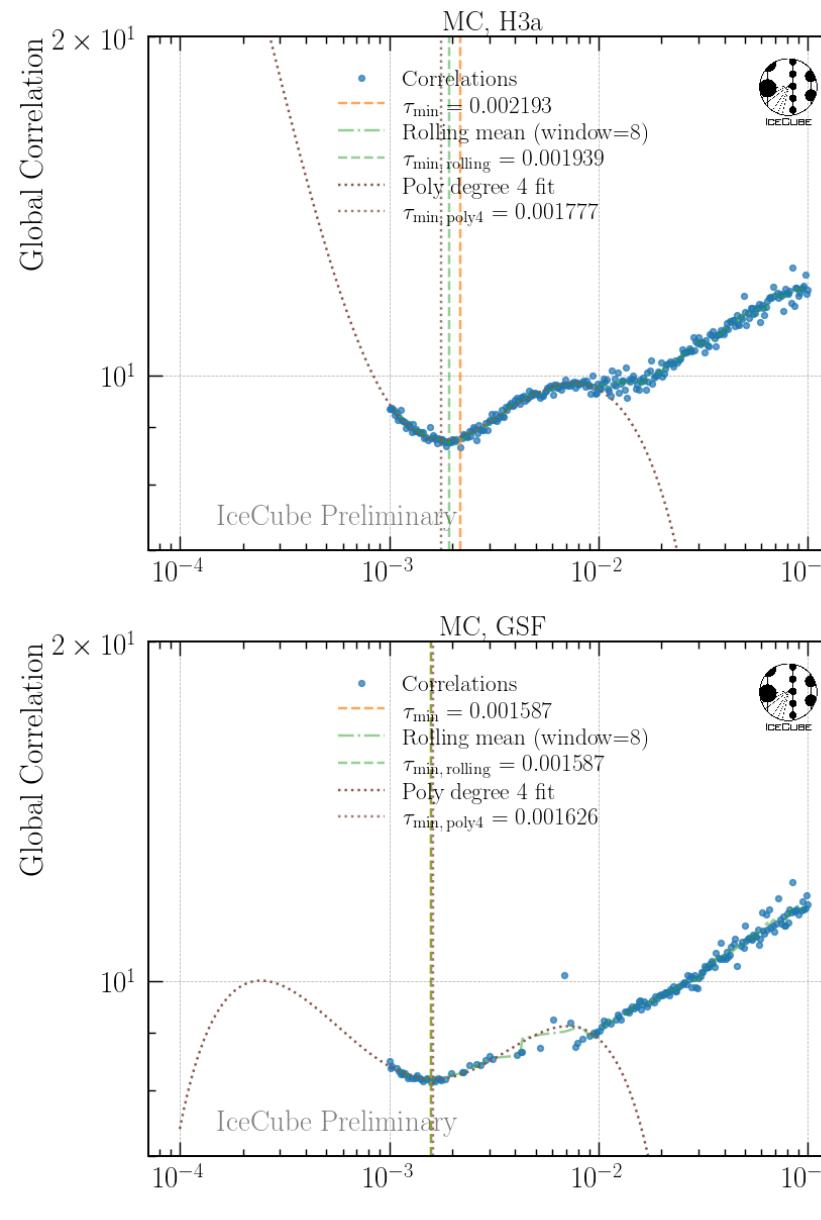
- Fit $\tau \in 10^{-3} - 10^{-2}$

GST Unfolding Bias

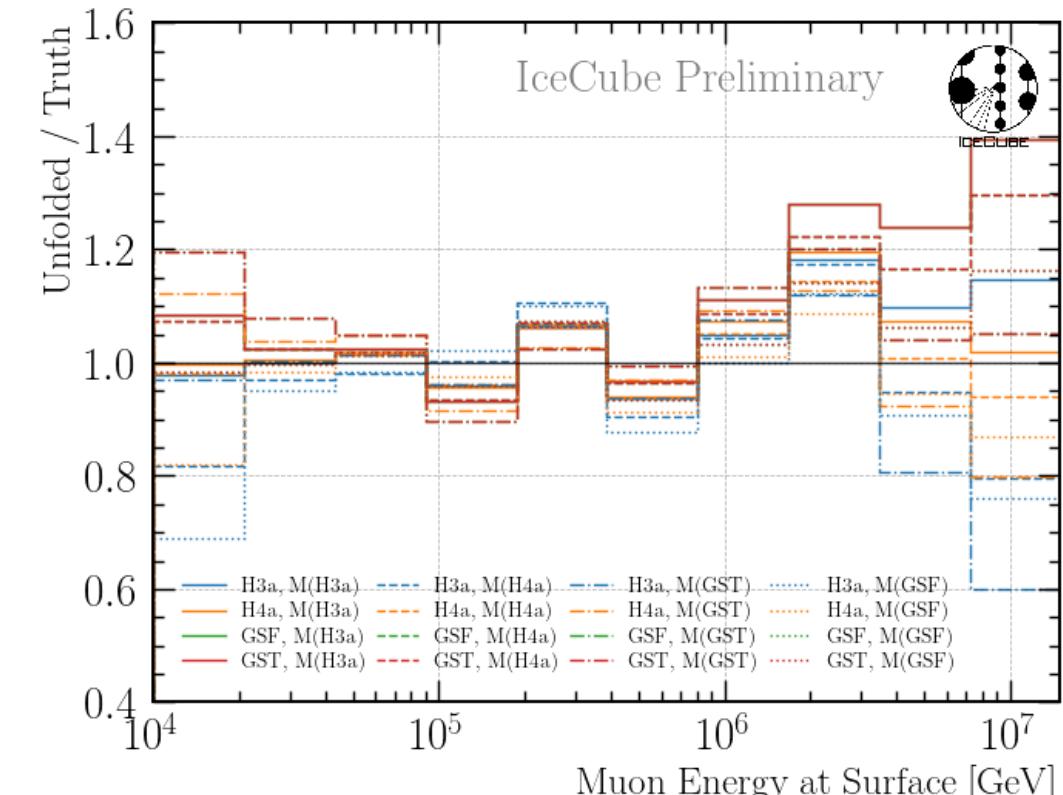
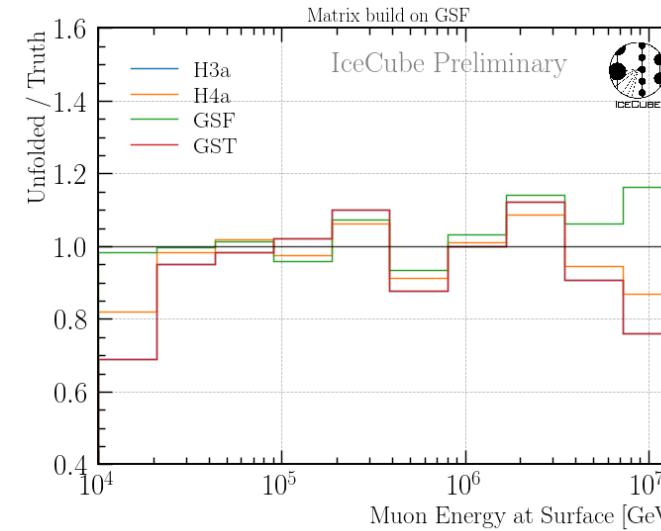
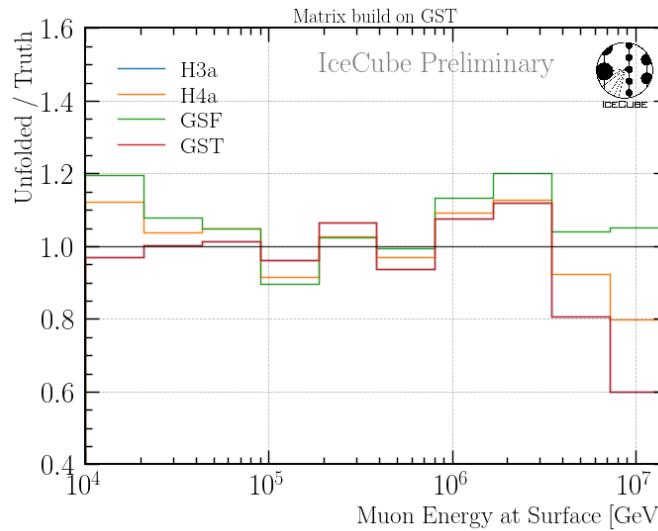
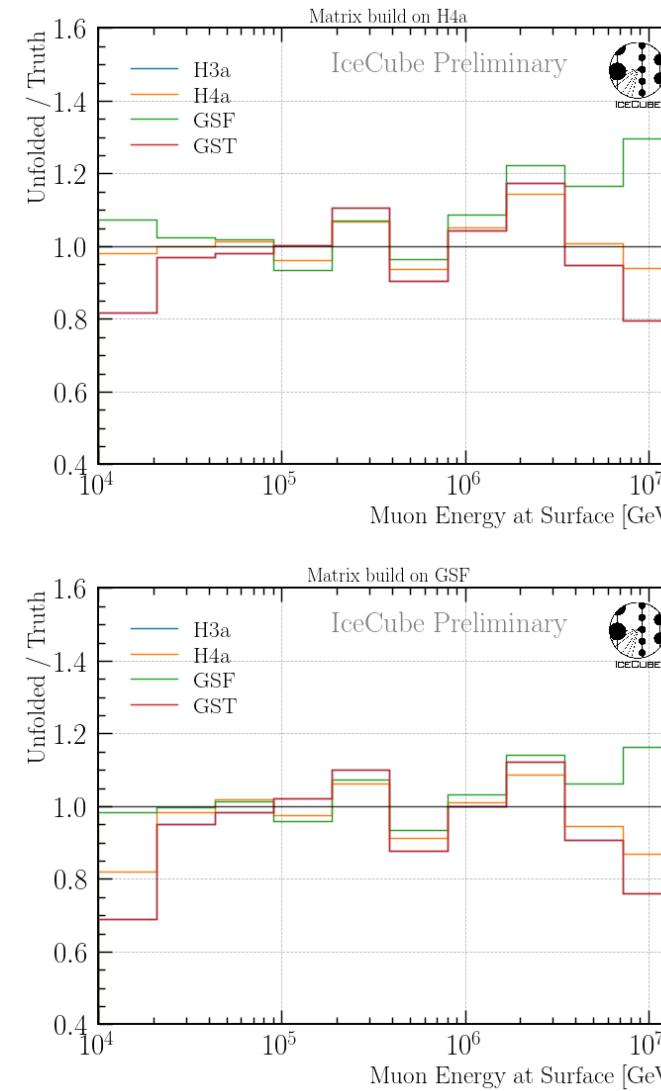
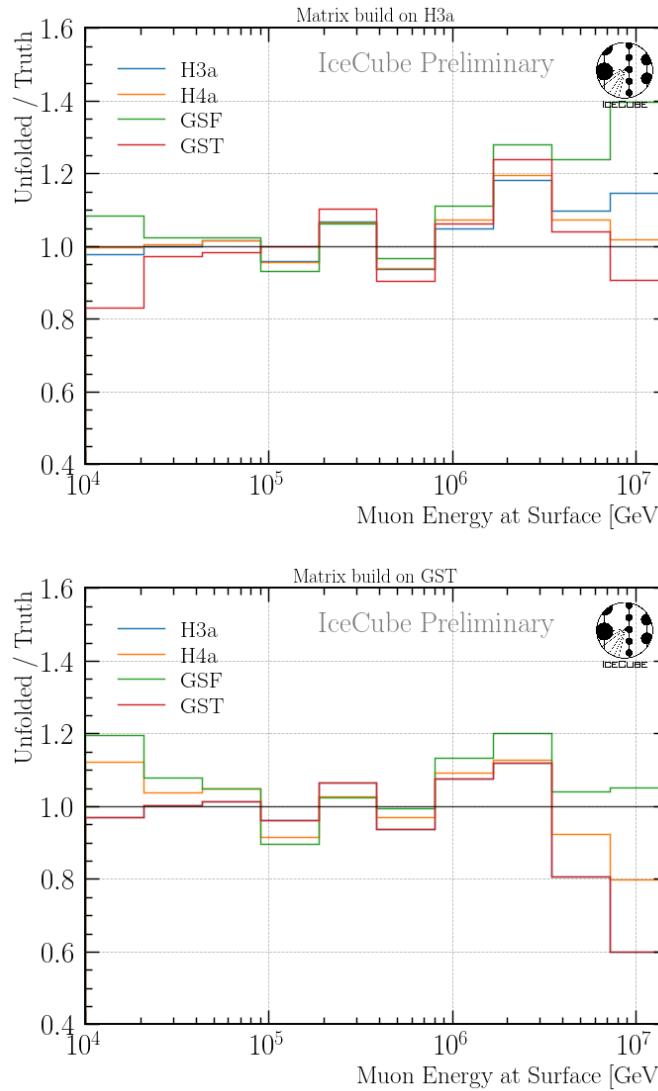


- Fit $\tau \in 10^{-3} - 10^{-2}$

GSF Unfolding Bias

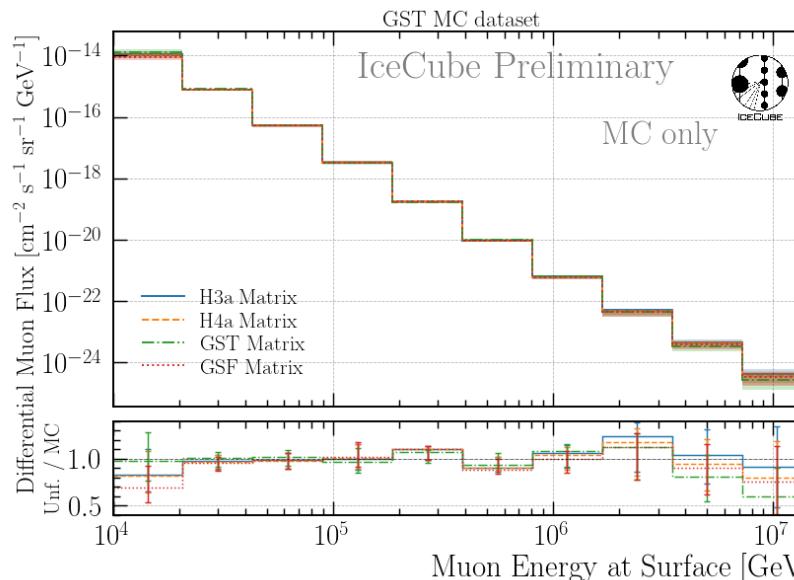
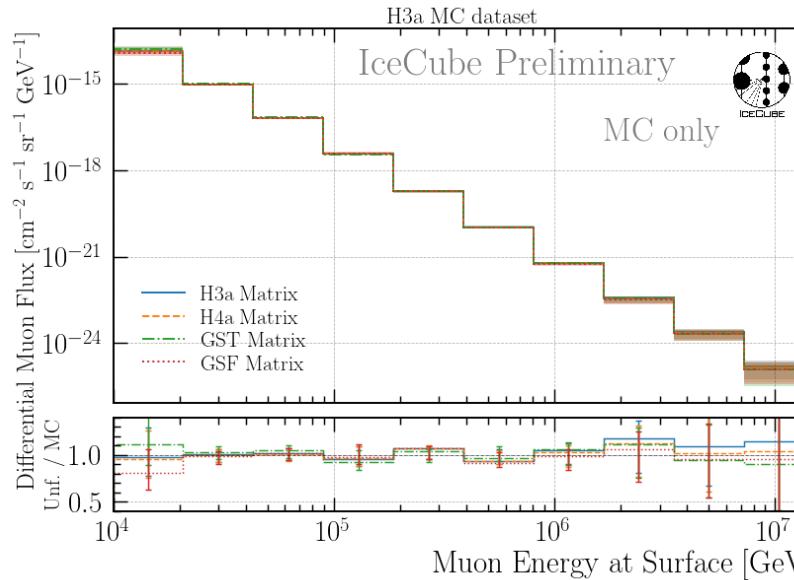


Unfolding Bias for All Models

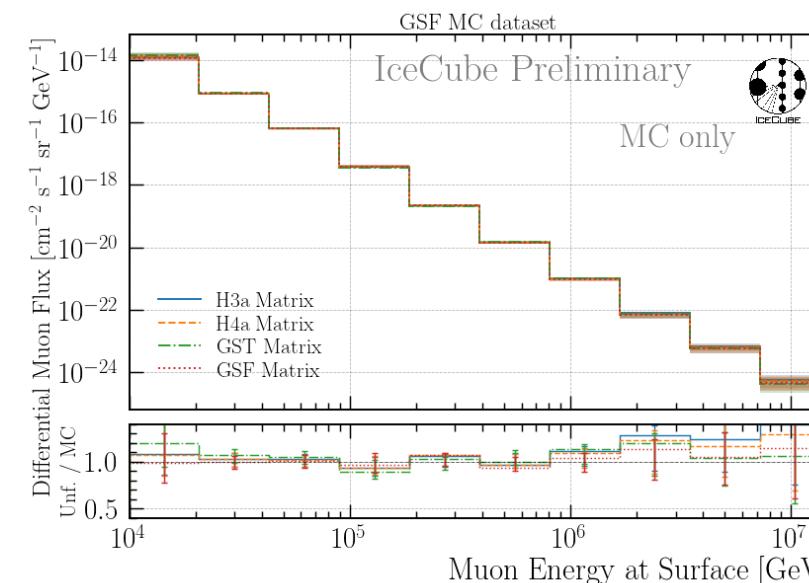
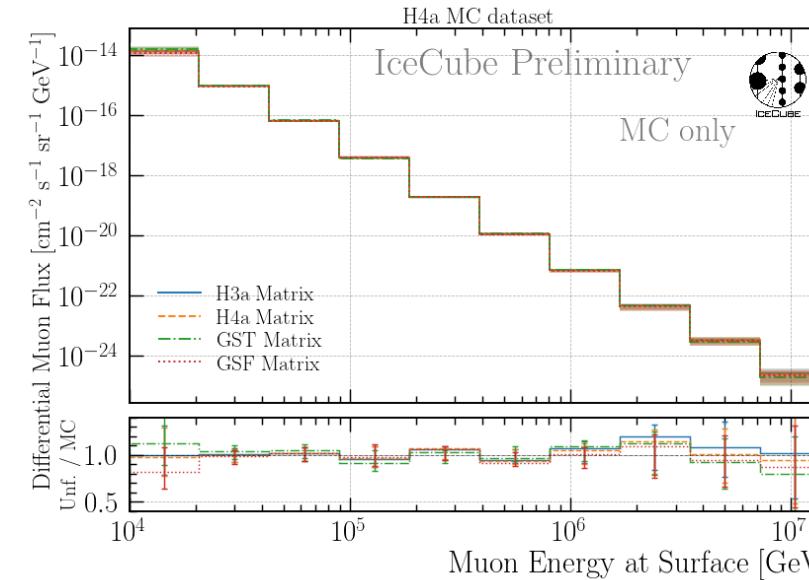


➤ Add these biases as an uncertainty to the unfolding result

Include Uncertainties



$$\sigma_{\text{tot}} = \sqrt{\sigma_{\text{minuit}}^2 + \sigma_{\text{unf-bias}}^2 + \sigma_{A_{\text{eff}},\text{stat}}^2}$$



➤ All 4 test dataset unfoldings agree within the uncertainties with the truth

Nominal / Best Fit → Average of 4 Unfoldings

- Unfold H3a test dataset with all 4 primary models

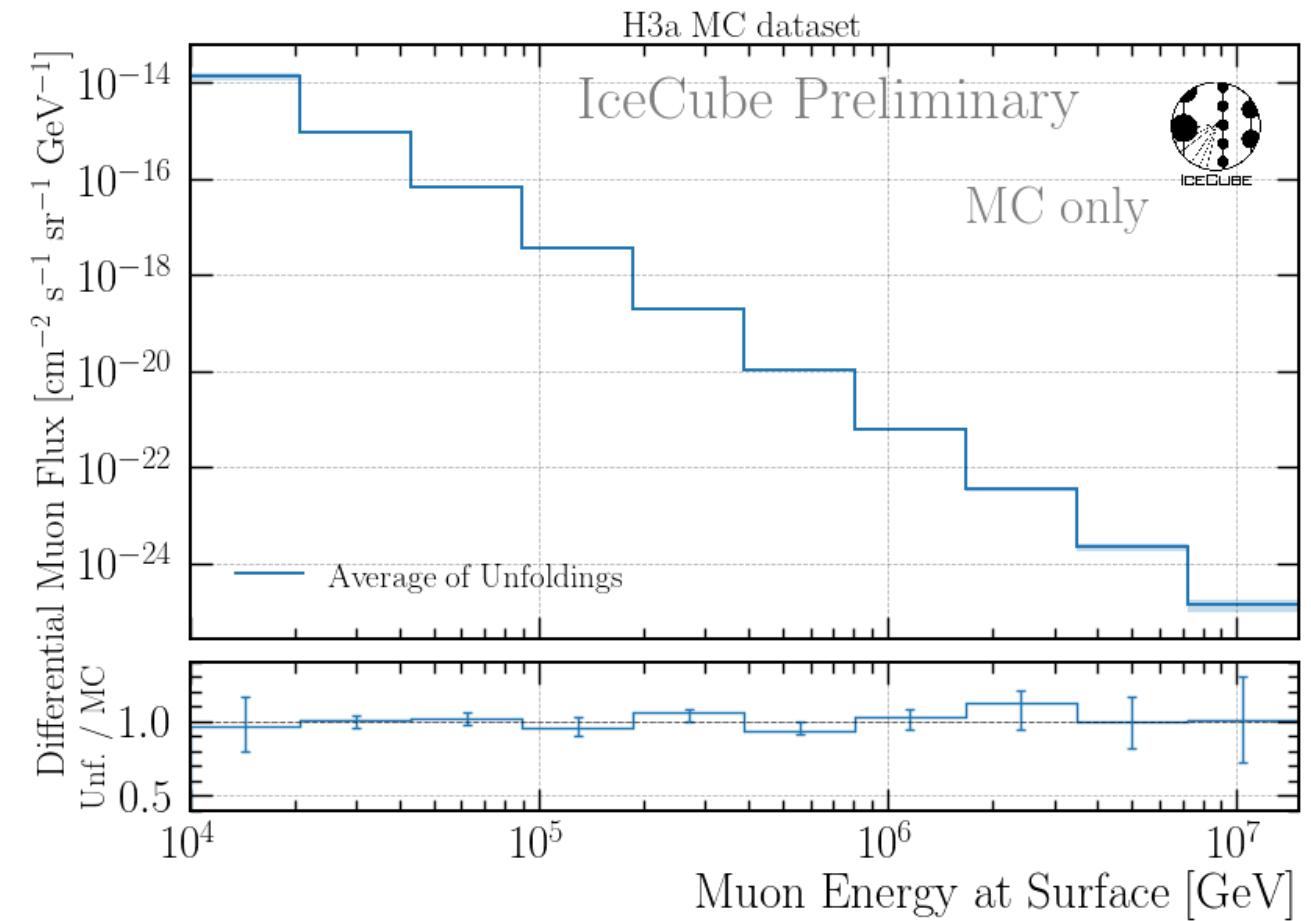
- Build average

$$\sigma_{\text{tot}} = \sqrt{\sigma_{\text{unf}}^2 + \sigma_{\text{spread}}^2}$$

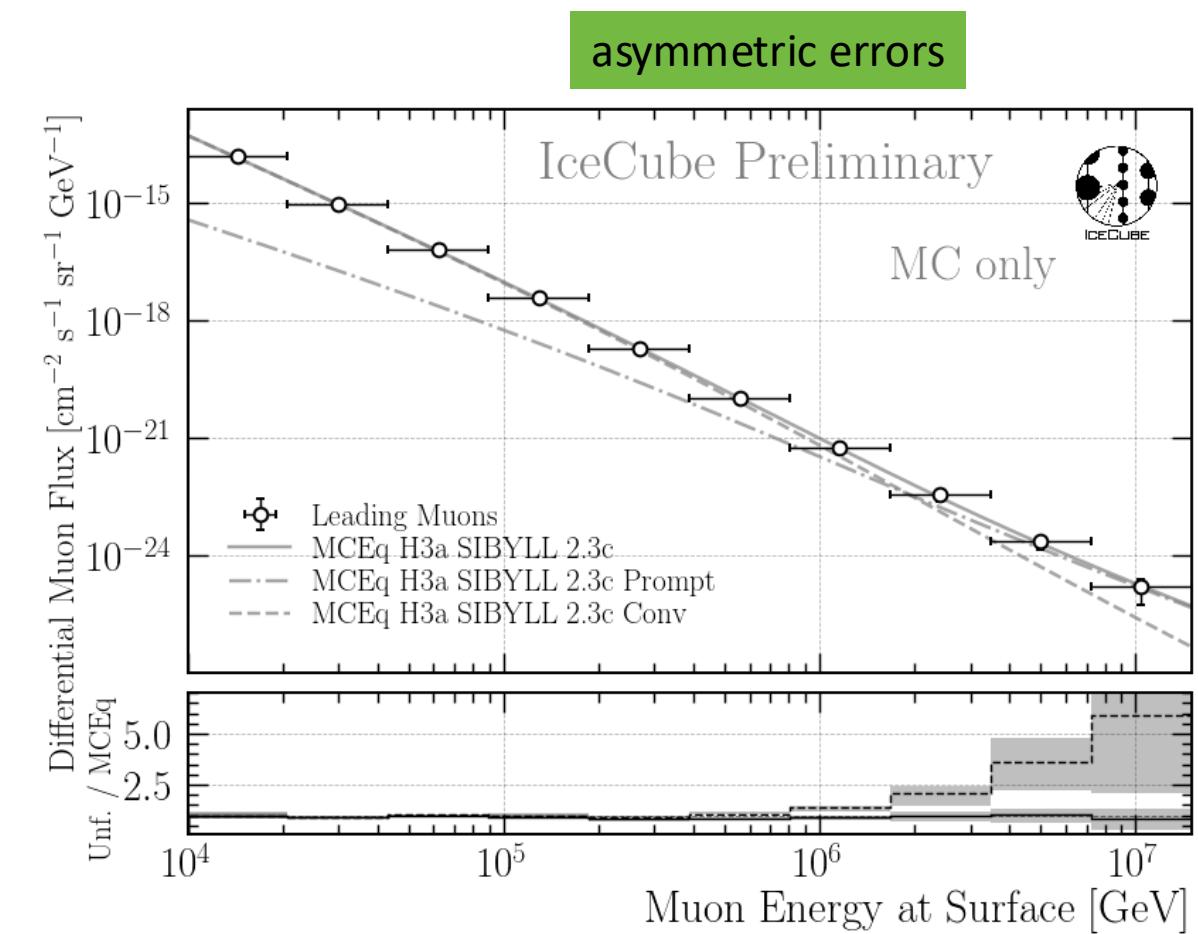
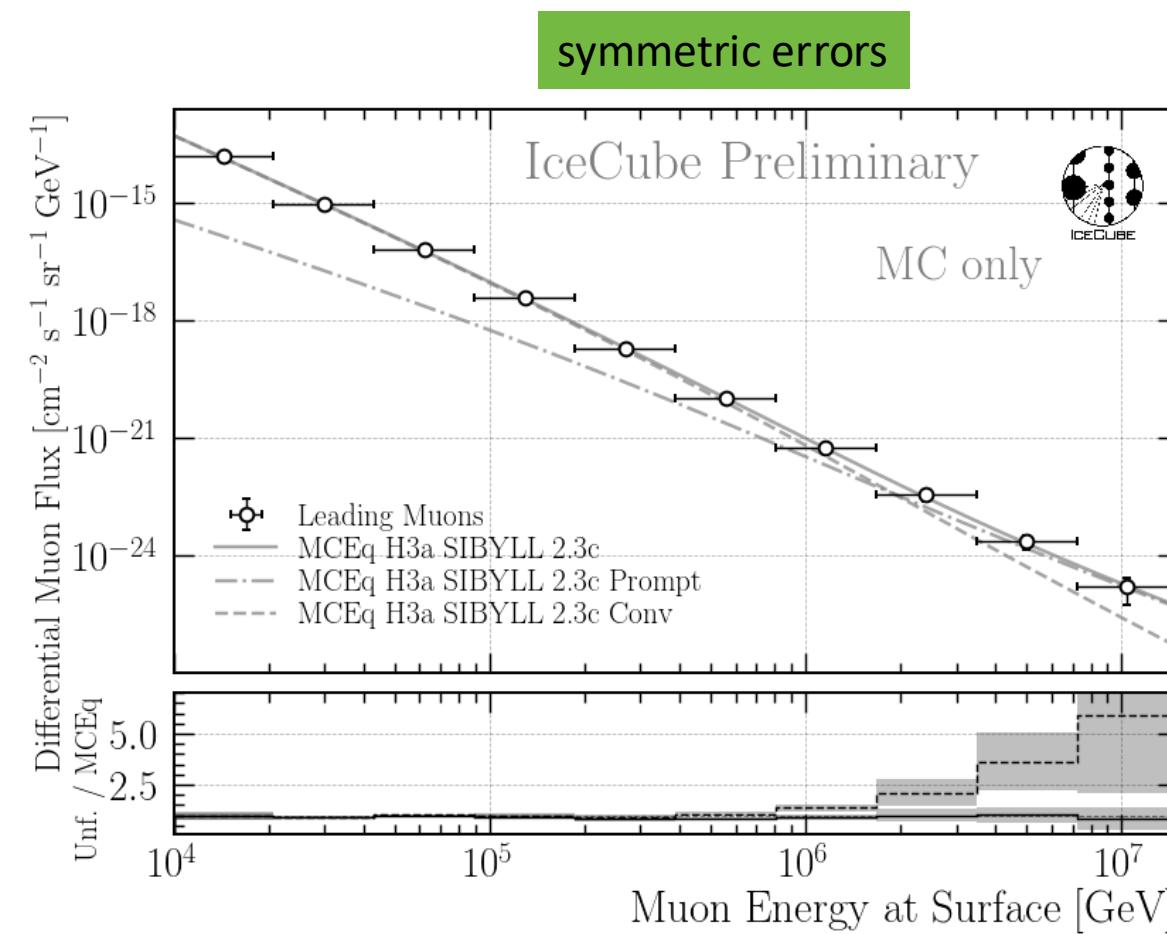
- with

$$\sigma_{\text{unf}} = \frac{\sqrt{\sum \sigma^2}}{N}$$

$$\sigma_{\text{spread}} = \text{std}(f_i)$$

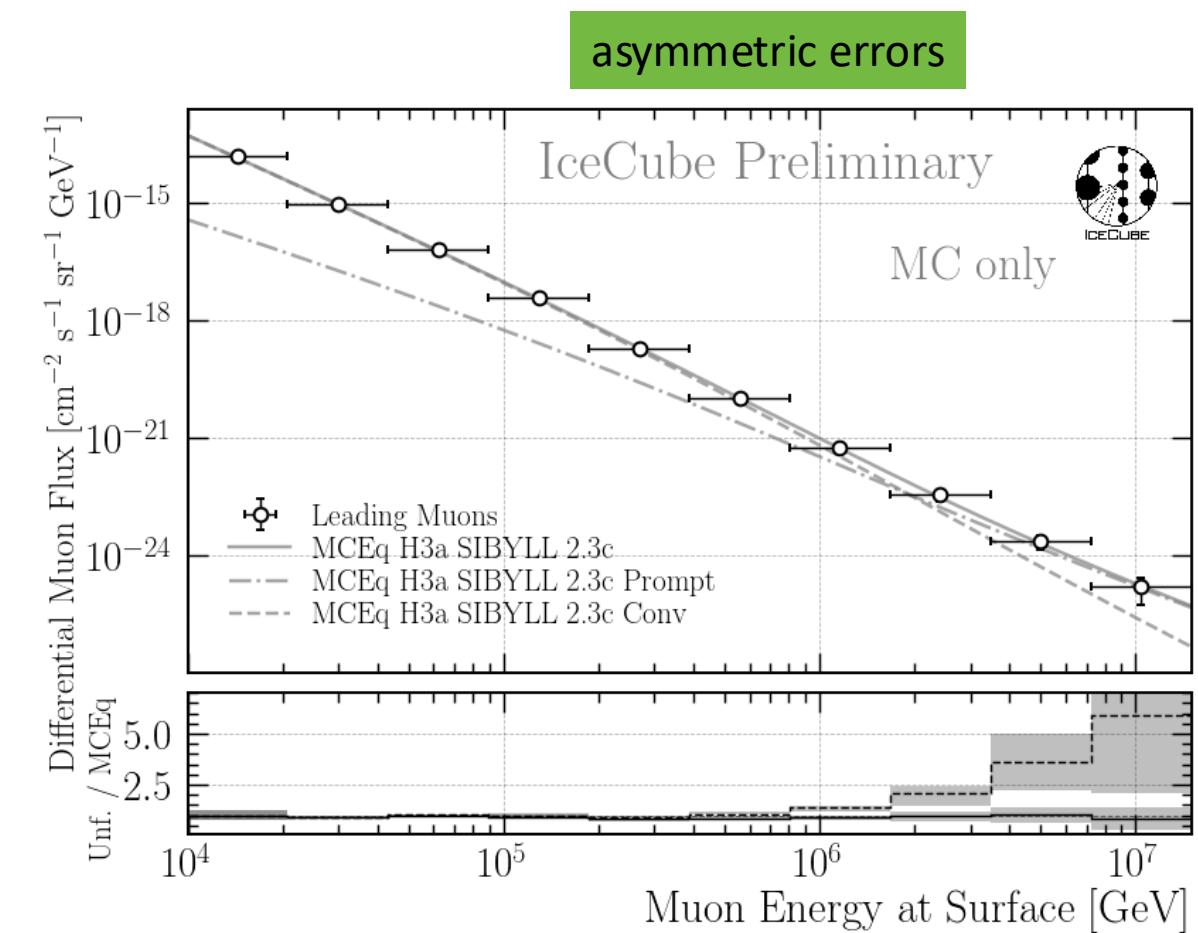
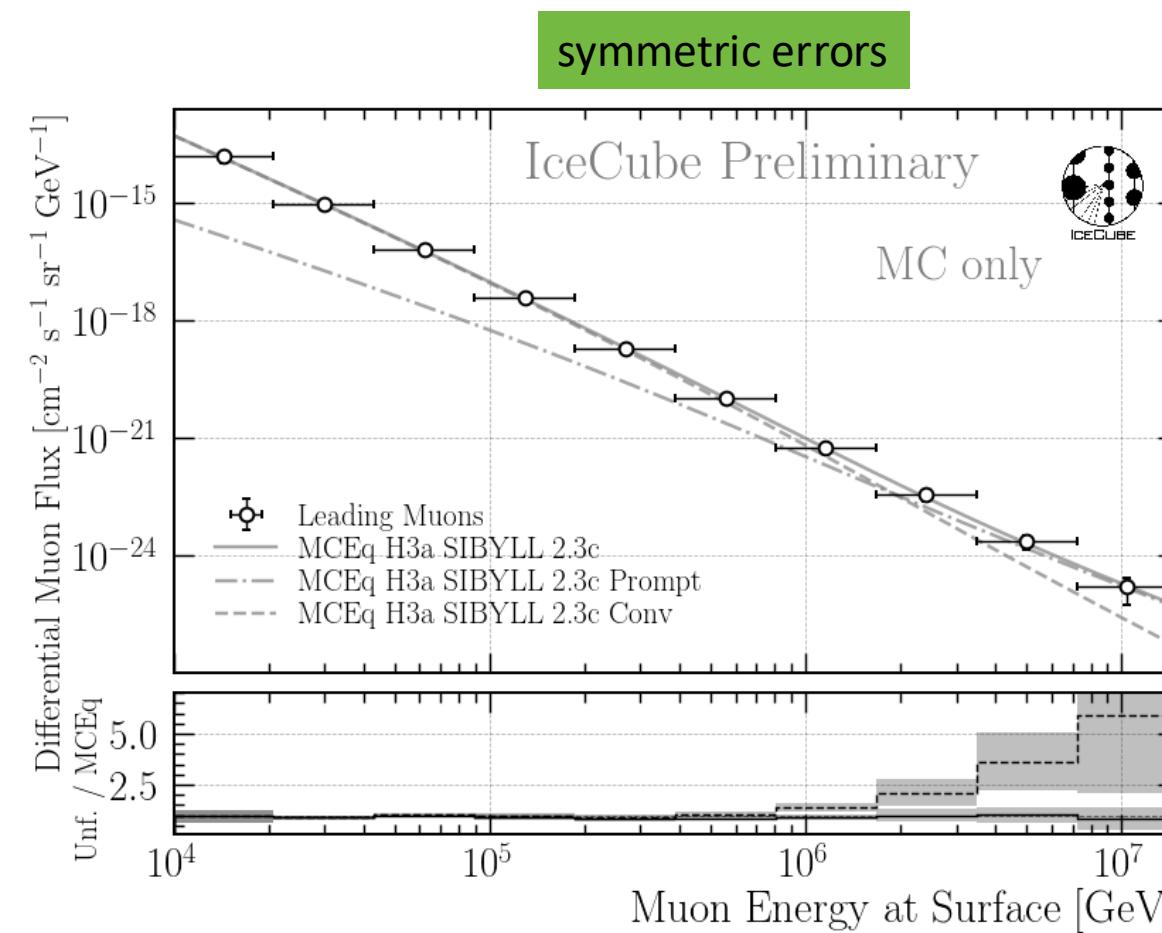


12 Years Prediction



$$\sigma_{\text{tot}} = \sqrt{\sigma_{\text{minuit}}^2 + \sigma_{\text{unf-bias}}^2 + \sigma_{A_{\text{eff}},\text{stat}}^2}$$

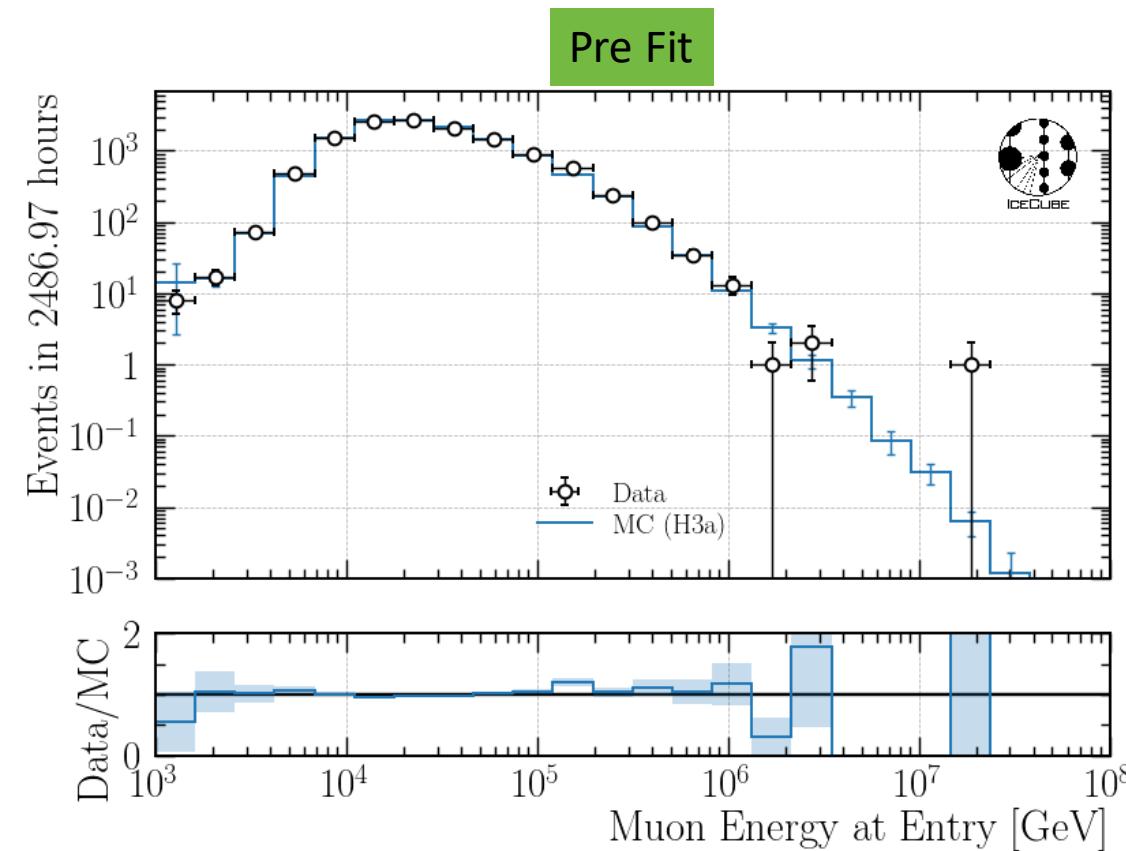
12 Years Prediction



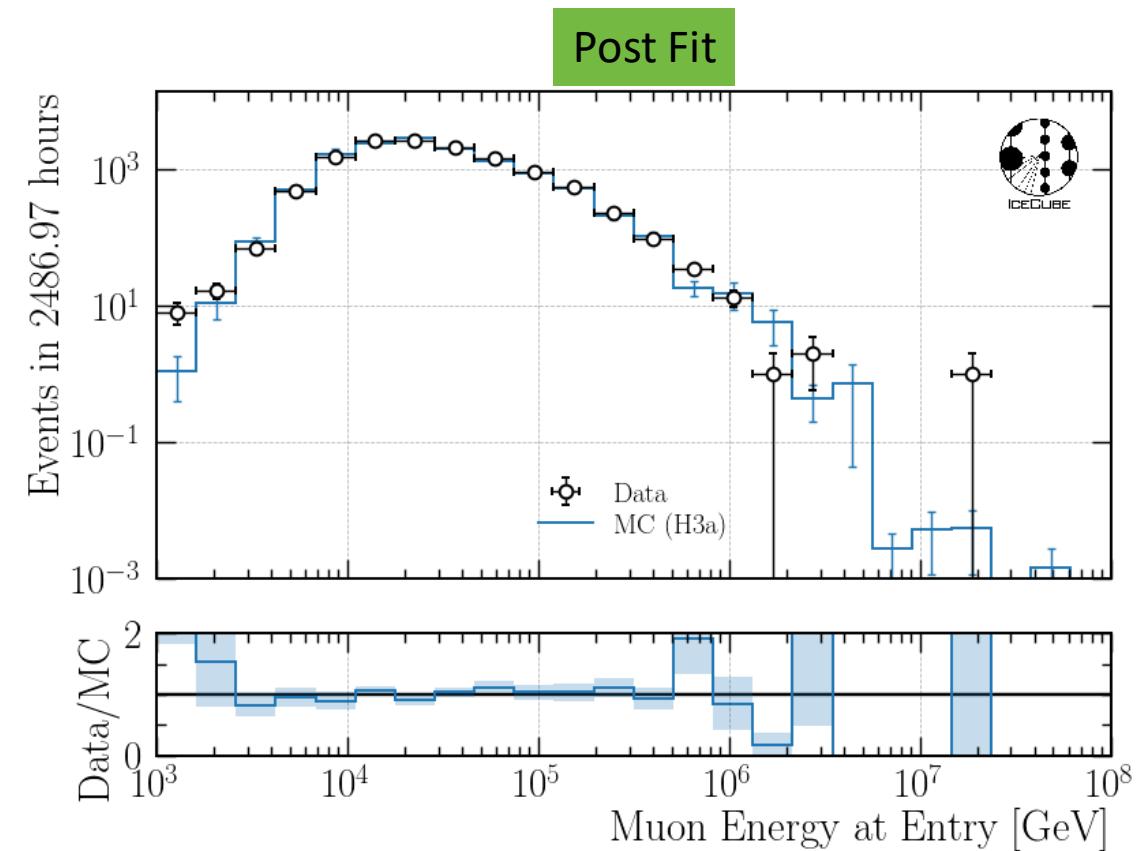
$$\sigma_{\text{tot}} = \sqrt{\sigma_{\text{minuit}}^2 + \sigma_{\text{unf-bias}}^2 + \sigma_{A_{\text{eff}},\text{stat}}^2}$$

Data-MC Post Fit

Data-MC: Burnsample



- include entire Snowstorm dataset



- re-weight to best fit systematics

Flux Characterization

[LikelihoodFitter] Using asymmetric uncertainties (2xN).

LIKELIHOOD FIT SUMMARY

Best-Fit Parameters:

Prompt normalization: 1.051024 ± 0.301881

Conventional normalization: 0.997005 ± 0.042235

$\chi^2 = 0.87$ ndof = 8 $\chi^2/\text{ndof} = 0.108$

Parameter correlation: -0.6246

HYPOTHESIS TEST: H_0 : prompt normalization = 0

$\Delta\chi^2 = 6.061$

p (one-sided, boundary-corrected) = 6.911184e-03

significance $\approx 2.46\sigma$

→ Reject H_0 at 95 % CL → evidence for prompt component.

Unblinding Plan

Unblinding Proposal

Unblinding plans

- Unfold 12 years of data for IC86 from 2011 to 2022
- Determine regularization strength on data
- Perform unfolding on data
 - Build matrix on all 4 primary models
 - Fit prompt/conv normalization (significance) on all 4 unfoldings each
 - Build average of all 4 unfoldings → nominal values

Post-unblinding checks

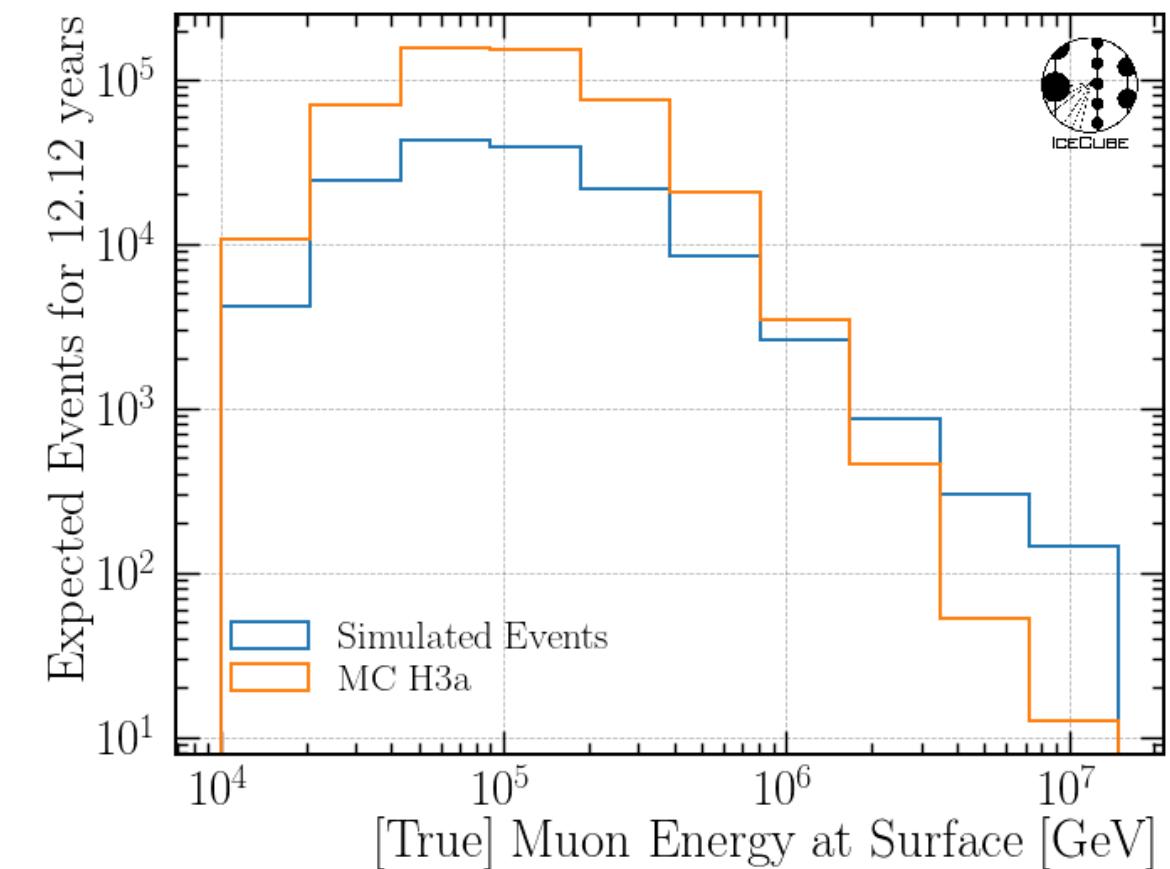
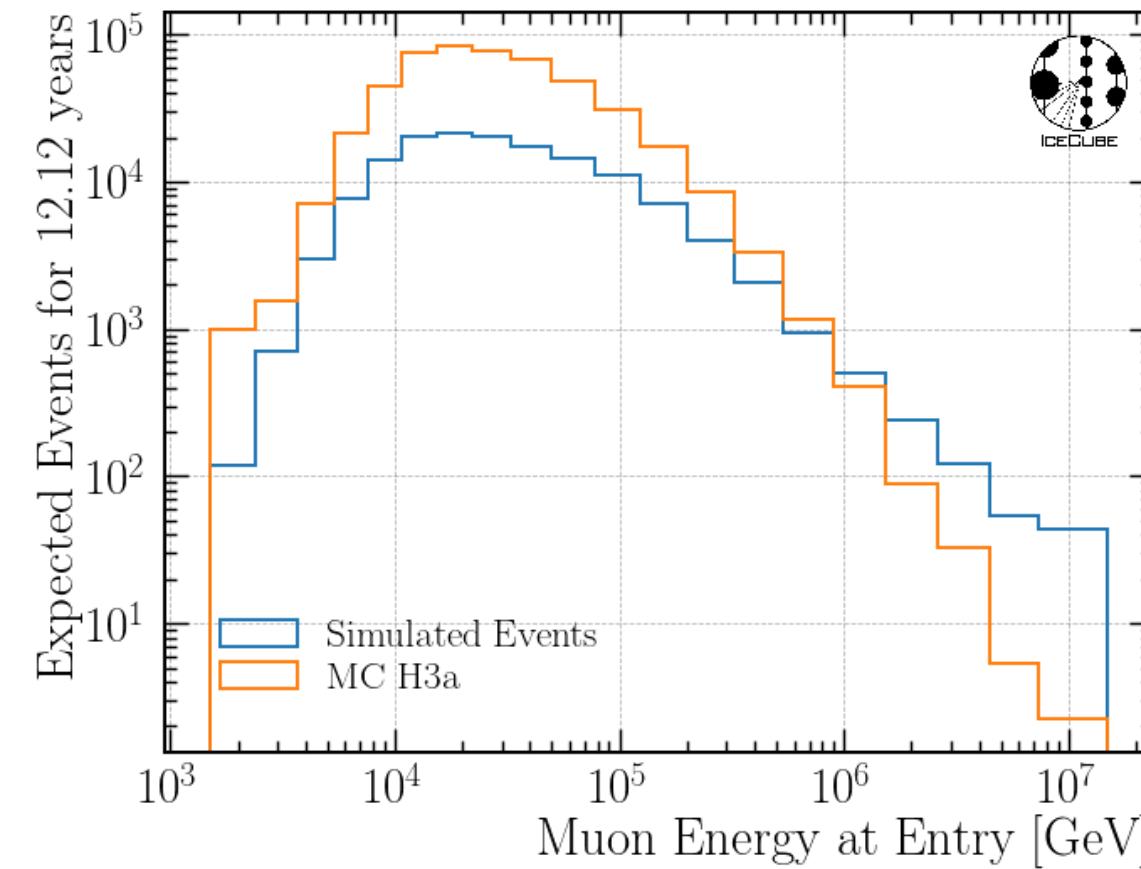
- Check the data-MC agreement for proxy variable (leading energy)
 - pre-fit (on the entire Snowstorm dataset)
 - post-fit (re-weight to fitted systematics)
- Divide total dataset in 3 subsets á 4 years to analyze systematic impacts over the years
- Divide dataset into 4 seasons

Paper Proposal

- Present status of forward folding in November
 - If results look promising → cross—checks can be done until end of January next year
 - Combined forward and unfolding paper: Discovery of prompt?
 - Elif, forward folding needs much more work
 - Unfolding paper: Measurement of muon flux

Backup

MC Statistics



Name	Value	Hesse Error	Minos Error-	Minos Error+	Limit-	Limit+	Fixed
0	x0	0.2e3	0.4e3		2.77	2.77E+04	
1	x1	11.1e3	0.7e3		107	1.07E+06	
2	x2	68.3e3	1.8e3		696	6.96E+06	
3	x3	161.4e3	3.1e3		1.58E+03	1.58E+07	
4	x4	147.9e3	2.9e3		1.55E+03	1.55E+07	
5	x5	79.8e3	1.7e3		749	7.49E+06	
6	x6	19.7e3	0.7e3		208	2.08E+06	
7	x7	3.44e3	0.19e3		34.2	3.42E+05	
8	x8	490	60		4.47	4.47E+04	
9	x9	56	15		0.55	5.5E+03	
10	x10	15	7		0.13	1.3E+03	
11	x11	0	70		0.01	100	
12	x12	1.006	0.020		0.913	1.09	
13	x13	0.9994	0.0029		0.913	1.09	
14	x14	0.998	0.005		0.9	1.1	
15	x15	0.2	0.4		-0.1	0.5	
16	x16	-0.05	0.07		-0.1	0	

Minuit output

	x0	x1	x2	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	
x0	1.74e+05	-0.21e6 (-0.725)	0.24e6 (0.321)	0.16e6 (0.126)	-0.35e6 (-0.287)	-0.08e6 (-0.116)	0.05e6 (0.158)	0.02e6 (0.196)	3.3e3 (0.136)	0.52e3 (0.084)	180 (0.061)	-130 (-0.033)	1.6651 (0.201)	-737.090e-3 (-0.615)	1.199859 (0.630)	-0.00 (-0.000)	0.0006	
x1	-0.21e6 (-0.725)	4.71e+05	-0.3e6 (-0.252)	-0.4e6 (-0.168)	0.4e6 (0.214)	0 (0.034)	-0 (-0.083)	-0.01e6 (-0.099)	-2.7e3 (-0.068)	-0.42e3 (-0.040)	-140 (-0.029)	100 (0.016)	-3.7011 (-0.271)	416.026e-3 (0.211)	-1.320718 (-0.421)	0.00 (0.000)	-0.0008	
x2	0.24e6 (0.321)	-0.3e6 (-0.252)	3.27e+06	-3.8e6 (-0.685)	0.9e6 (0.175)	-0.4e6 (-0.118)	0.1e6 (0.047)	0.04e6 (0.121)	10.9e3 (0.104)	1.88e3 (0.070)	670 (0.053)	-580 (-0.034)	-13.6553 (-0.379)	-2.720238 (-0.524)	1.698607 (0.206)	-0.01 (-0.000)	0.0011 (0.000)	
x3	0.16e6 (0.126)	-0.4e6 (-0.168)	-3.8e6 (-0.685)	9.49e+06	-7e6 (-0.747)	1.4e6 (0.267)	0.1e6 (0.058)	-0.04e6 (-0.065)	-7.1e3 (-0.039)	-0.70e3 (-0.015)	-140 (-0.007)	510 (0.017)	30.4744 (0.497)	309.518e-3 (0.035)	2.800072 (0.199)	-0.00 (-0.000)	0.0003	
x4	-0.35e6 (-0.287)	0.4e6 (0.214)	0.9e6 (0.175)	-7e6 (-0.747)	8.7e+06	-3.0e6 (-0.594)	0.1e6 (0.068)	0.05e6 (0.094)	-8.2e3 (-0.048)	-3.49e3 (-0.080)	-1.65e3 (-0.037)	1.02e3 (-0.244)	-14.3596 (-0.303)	2.565423 (-0.311)	-4.189896 (-0.000)	0.01 (-0.000)	-0.0013	
x5	-0.08e6 (-0.116)	0 (0.034)	-0.4e6 (-0.118)	1.4e6 (0.267)	-3.0e6 (-0.594)	2.85e+06	-0.8e6 (-0.637)	-0.07e6 (-0.206)	15.7e3 (0.159)	5.10e3 (0.202)	2.26e3 (0.192)	-2.29e3 (-0.144)	-1.5699 (-0.047)	679.608e-3 (0.140)	-1.052575 (-0.136)	0.00 (0.000)	-0.0002	
x6	0.05e6 (0.158)	-0 (-0.083)	0.1e6 (0.047)	0.1e6 (0.058)	0.1e6 (0.068)	-0.8e6 (-0.637)	4.91e+05	-0.03e6 (-0.209)	-18.3e3 (-0.447)	-3.61e3 (-0.345)	-1.36e3 (-0.278)	1.74e3 (0.265)	802.9e-3 (0.058)	-376.997e-3 (-0.187)	592.997e-3 (0.185)	-0.00 (0.000)	0.0001	
x7	0.02e6 (0.196)	-0.01e6 (-0.099)	0.04e6 (0.121)	-0.04e6 (-0.065)	0.05e6 (0.094)	-0.07e6 (-0.206)	-0.03e6 (-0.209)	3.64e+04	2.8e3 (0.253)	-0.14e3 (-0.049)	-170 (-0.126)	20 (0.010)	285.8e-3 (0.075)	-108.224e-3 (-0.197)	217.212e-3 (0.249)	-0.00 (0.000)	0.0001	
x8	3.3e3 (0.136)	-2.7e3 (-0.068)	10.9e3 (0.104)	-7.1e3 (-0.039)	-8.2e3 (-0.048)	15.7e3 (0.159)	-18.3e3 (-0.447)	2.8e3 (0.253)	-0.14e3 (-0.049)	-1.36e3 (-0.126)	-170 (-0.126)	20 (0.010)	285.8e-3 (0.075)	-108.224e-3 (-0.197)	217.212e-3 (0.249)	-0.00 (0.000)	0.0001	
x9	0.52e3 (0.084)	-0.42e3 (-0.040)	1.88e3 (0.070)	-0.70e3 (-0.015)	-3.49e3 (-0.079)	5.10e3 (0.202)	-3.61e3 (-0.345)	-0.14e3 (-0.049)	0.69e3 (0.788)	223 (0.788)	100 (0.638)	-100 (-0.727)	6.8e-3 (0.023)	-3.941e-3 (-0.092)	7.366e-3 (0.108)	-0.00 (0.000)	0.0000	
x10	180 (0.061)	-140 (-0.029)	670 (0.053)	-140 (-0.007)	-1.65e3 (-0.080)	2.26e3 (0.192)	-1.36e3 (-0.278)	-170 (-0.126)	260 (0.638)	100 (0.936)	48.7 (-0.711)	-50 (0.015)	2.1e-3 (0.015)	-1.390e-3 (-0.069)	2.506e-3 (0.079)	-0.00 (0.000)	0.0000	
x11	-130 (-0.033)	100 (0.016)	-580 (-0.034)	510 (0.017)	1.02e3 (0.037)	-2.29e3 (-0.144)	1.74e3 (0.265)	20 (0.010)	-320 (-0.580)	-100 (-0.727)	-50 (-0.711)	88.1 (-0.010)	-2.0e-3 (0.034)	920e-6 (-0.049)	-2.090e-3 (-0.049)	0.00 (0.000)	-0.0000	
x12	1.6651 (0.201)	-3.7011 (-0.271)	-13.6553 (-0.379)	30.4744 (0.497)	-14.3596 (-0.244)	-1.5699 (-0.047)	802.9e-3 (0.058)	285.8e-3 (0.075)	50.8e-3 (0.044)	6.8e-3 (0.023)	2.1e-3 (0.015)	-2.0e-3 (-0.010)	0.000397 (-0.091)	5e-6 (0.091)	0.040e-3 (0.443)	-0 (0.000)	0 (0.000)	
x13	-737.090e-3 (-0.615)	416.026e-3 (0.211)	-2.720238 (-0.524)	309.518e-3 (0.035)	2.565423 (0.303)	679.608e-3 (0.140)	-376.997e-3 (-0.187)	-108.224e-3 (-0.197)	-23.767e-3 (-0.142)	-3.941e-3 (-0.092)	-1.390e-3 (-0.069)	920e-6 (0.034)	5e-6 (0.091)	8.26e-06 (-0.437)	-6e-6 (-0.437)	0e-6 (0.000)	-0e-6 (0.000)	
x14	1.199859 (0.630)	-1.320718 (-0.421)	1.698607 (0.206)	2.800072 (0.199)	-4.189896 (-0.311)	-1.052575 (-0.136)	592.997e-3 (0.185)	217.212e-3 (0.249)	46.781e-3 (0.175)	7.366e-3 (0.108)	2.506e-3 (0.079)	-2.090e-3 (-0.049)	0.040e-3 (0.443)	-6e-6 (-0.437)	2.09e-05 (-0.437)	-0 (0.000)	-0 (0.000)	
x15	-0.00 (-0.000)	0.00 (0.000)	-0.01 (-0.000)	-0.00 (-0.000)	0.01 (0.000)	0.00 (0.000)	-0.00 (0.000)	-0.00 (0.000)	-0.00 (0.000)	-0.00 (0.000)	0.00 (0.000)	-0 (0.000)	0e-6 (0.000)	-0 (0.000)	0.0912 (0.000)	-0.0000		
x16	0.0006	-0.0008 (0.000)	0.0011 (0.000)	0.0003 (-0.000)	-0.0013 (-0.000)	-0.0002 (-0.000)	0.0001 (0.000)	0.0001 (0.000)	0.0000 (0.000)	0.0000 (0.000)	0.0000 (0.000)	-0.0000 (0.000)	0 (0.000)	-0e-6 (0.000)	0 (0.000)	-0.0000 (0.000)	0.00253	

Introduction

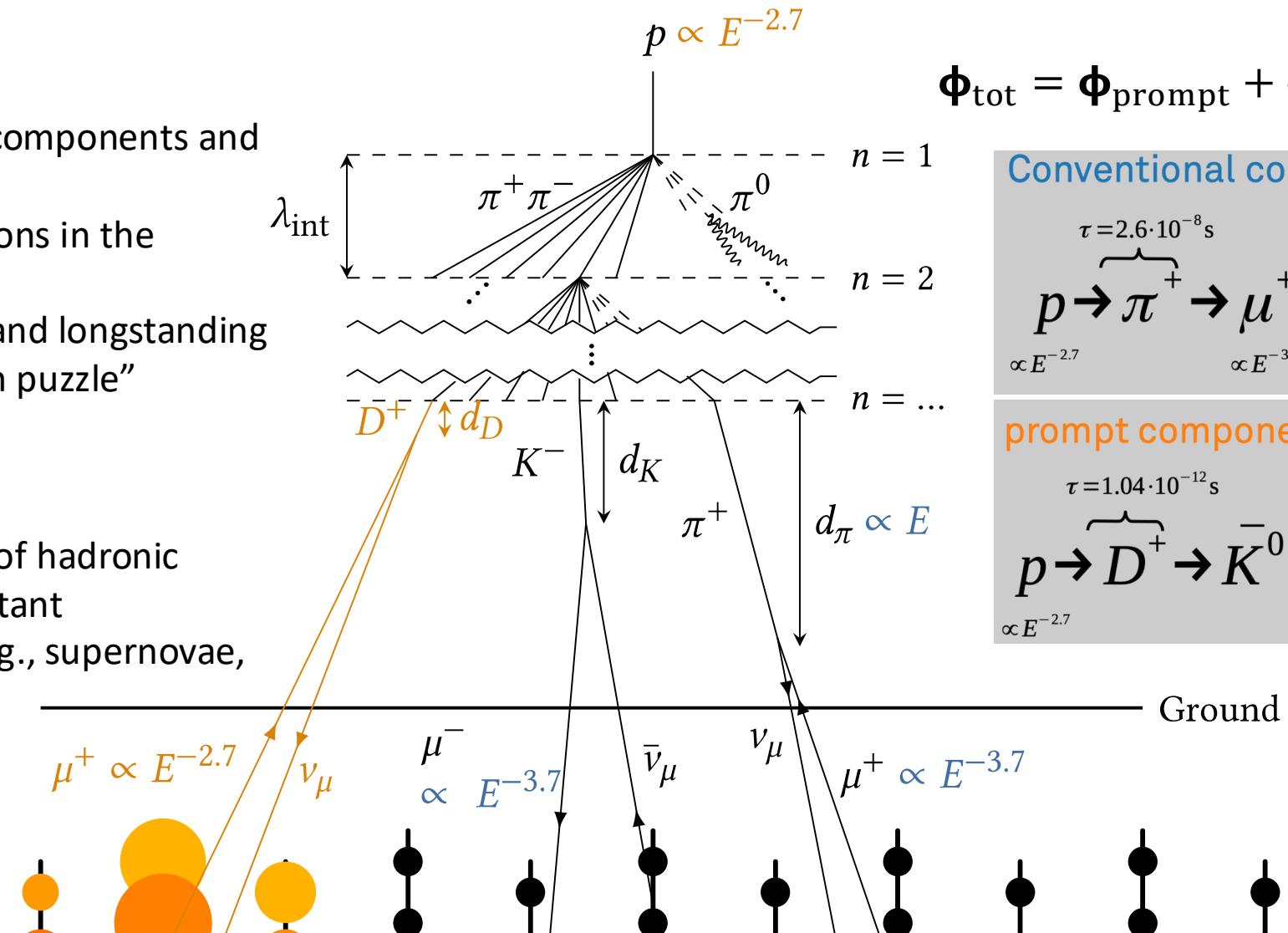
Motivation

- Characterize muon flux components and depth intensity
- Probe hadronic interactions in the atmosphere
- Constrain uncertainties and longstanding questions like the “muon puzzle”

Long term

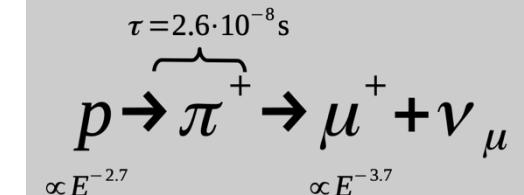
- Enhance understanding of hadronic processes relevant in distant astrophysical sources (e.g., supernovae, AGNs, ...)

Conventional Muon:
Parent is pion or kaon

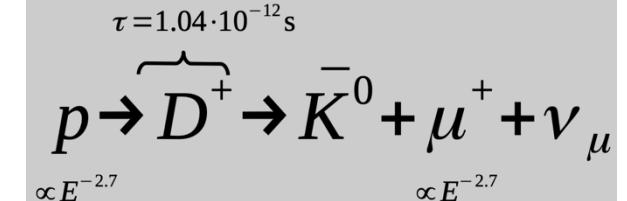


$$\Phi_{\text{tot}} = \Phi_{\text{prompt}} + \Phi_{\text{conventional}}$$

Conventional component:

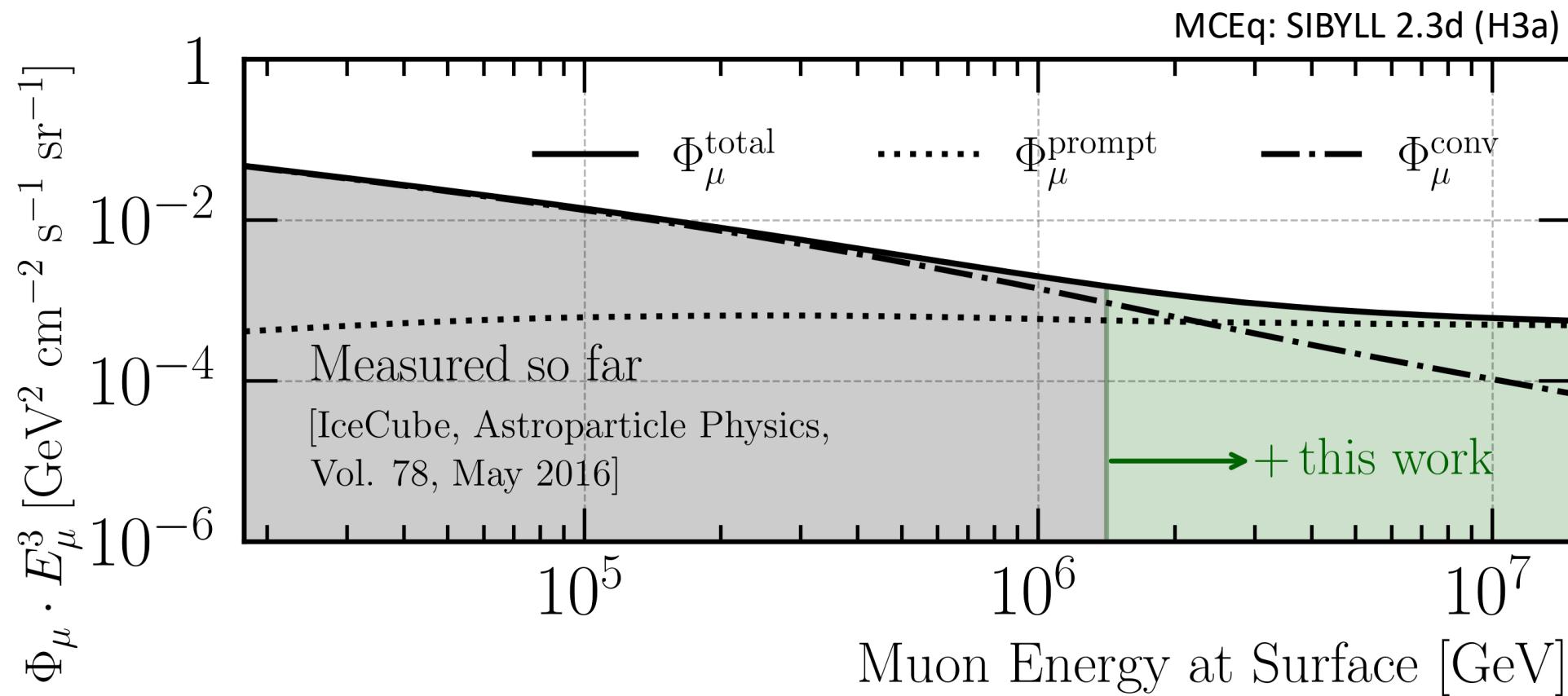


prompt component:

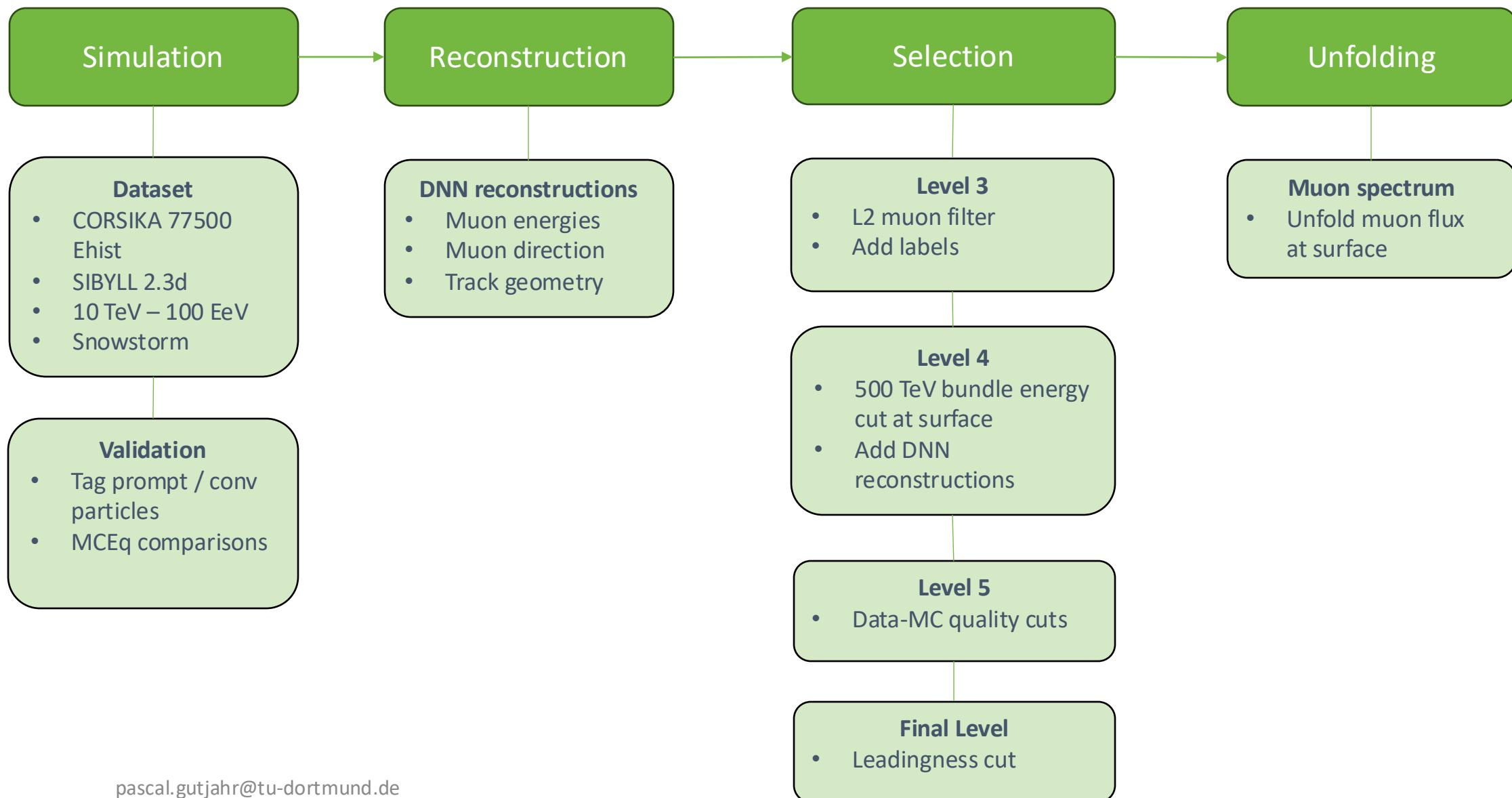


Credit: Ludwig Neste

Goal: Measure Muon Flux at Surface



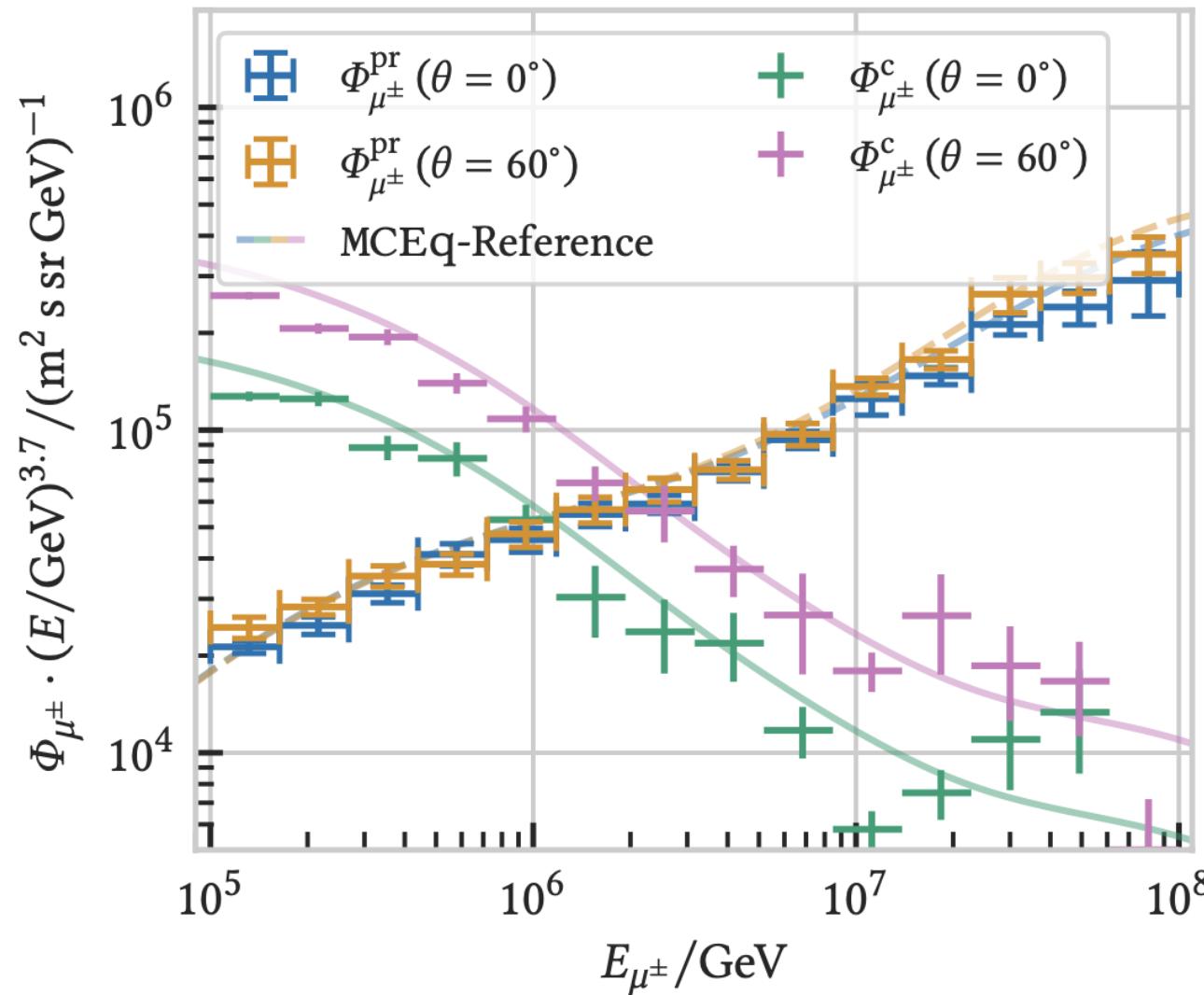
Overview



New CORSIKA simulation

with extended history option for information about the parent particles

CORSIKA 7 vs. MCEq

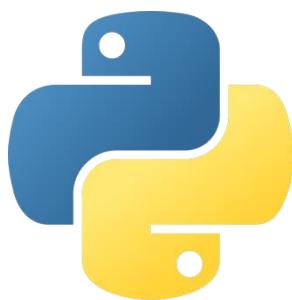


MCEq: tool to numerically solve the cascade equations that describes the evolution of particle densities as they propagate through a gaseous, dense medium
<https://github.com/mceq-project/MCEq>

➤ Good agreement for inclusive flux

Python package developed – PANAMA

- Execute CORSIKA 7 (multi core)
- Read DAT files → pandas DataFrames
- Parse EHIST option
- Calculate primary weightings



Reconstruction

Machine Learning (CNN)

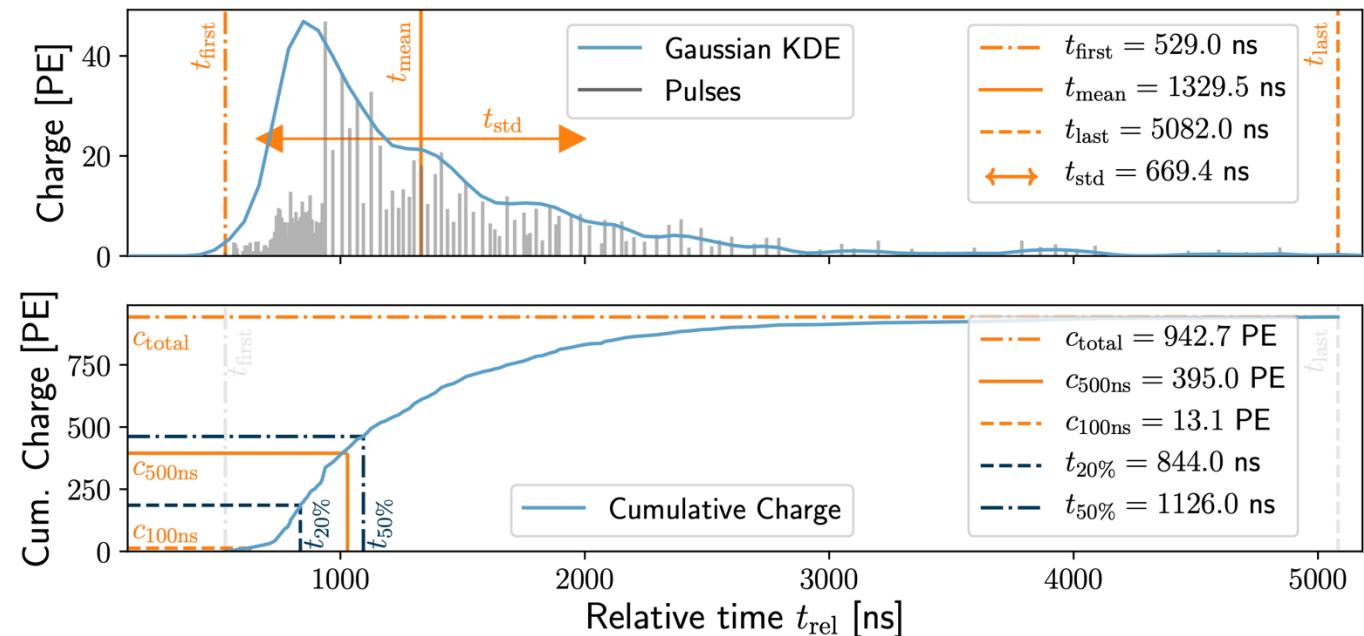
Input data per DOM

3 inputs

- c_{total} : Total charge
 - Sum of charge
- t_{first} : Relative time of first pulse
 - Relative to total time offset, calculated as the charge weighted mean time of all pulses
- t_{std} : Standard deviation of first pulse
 - Charge weighted standard deviation of pulse times relative to total time offset

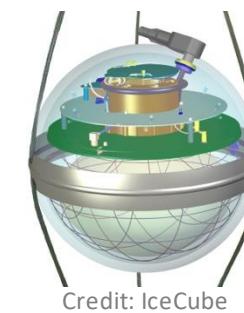
9 inputs

- t_{last} : Relative time of last pulse
 - Relative to total time offset, calculated as the charge weighted mean time of all pulses
- $t_{20\%}$: Relative time of 20% charge
 - Relative to total time offset, calculated as the charge weighted mean time of all pulses
- $t_{50\%}$: Relative time of 50% charge
 - Relative to total time offset, calculated as the charge weighted mean time of all pulses
- t_{mean} : Mean time
 - Charge weighted mean time of all pulses relative to total time offset
- $c_{500\text{ns}}$: Charge at 500ns
 - Sum of charge after 500ns
- $c_{100\text{ns}}$: Charge at 100ns
 - Sum of charge after 100ns



Input pulse cleaning

- 6000 ns



Training data

- Different simulations for robustness

Reconstructed properties

Energy

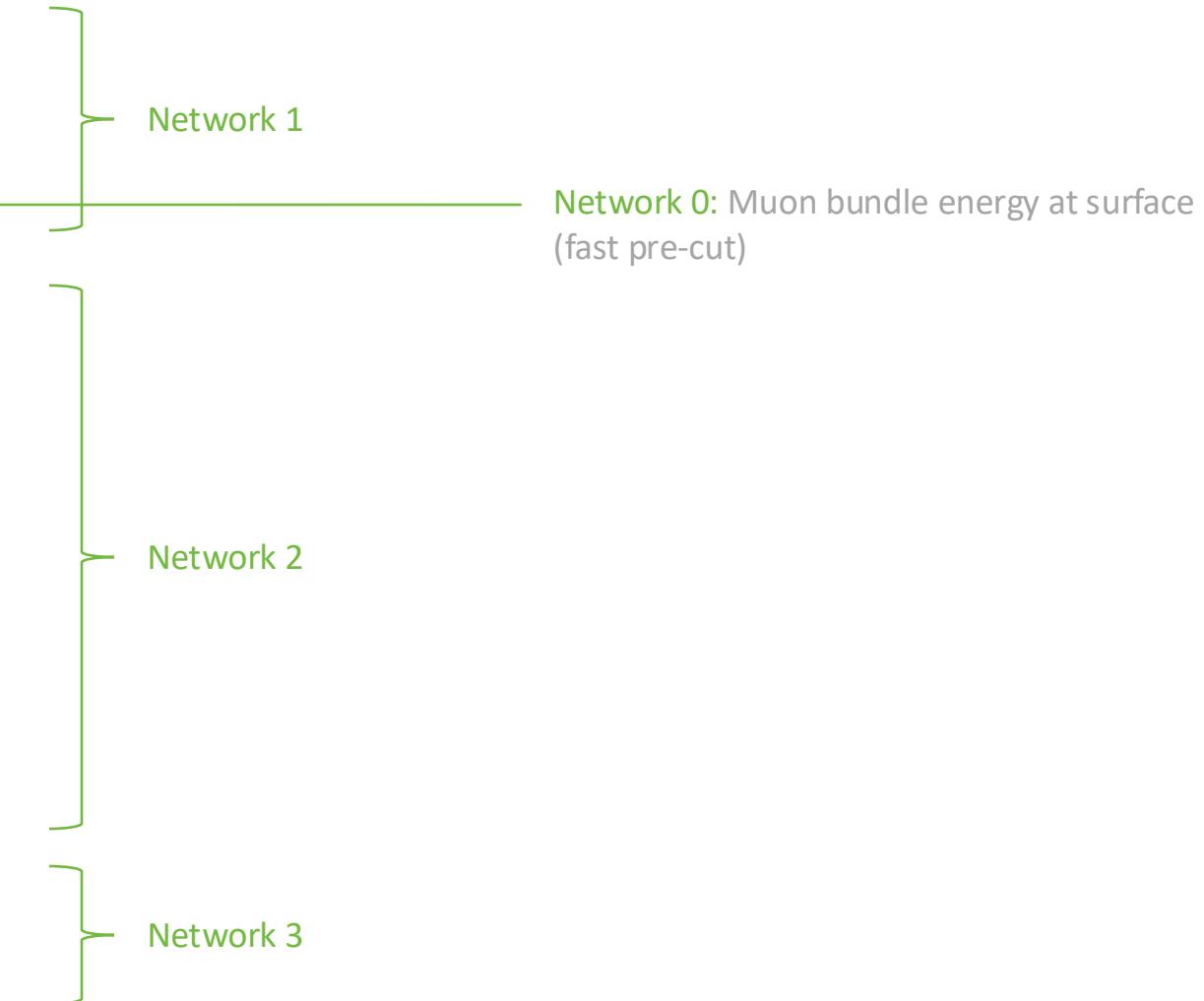
- `entry_energy`: Leading muon energy at the detector entry
- `bundle_energy_at_entry`: Muon bundle energy at the detector entry
- `muon_energy_first_mctree`: Leading muon energy at surface
- `bundle_energy_in_mctree`: Muon bundle energy at surface

Track geometry

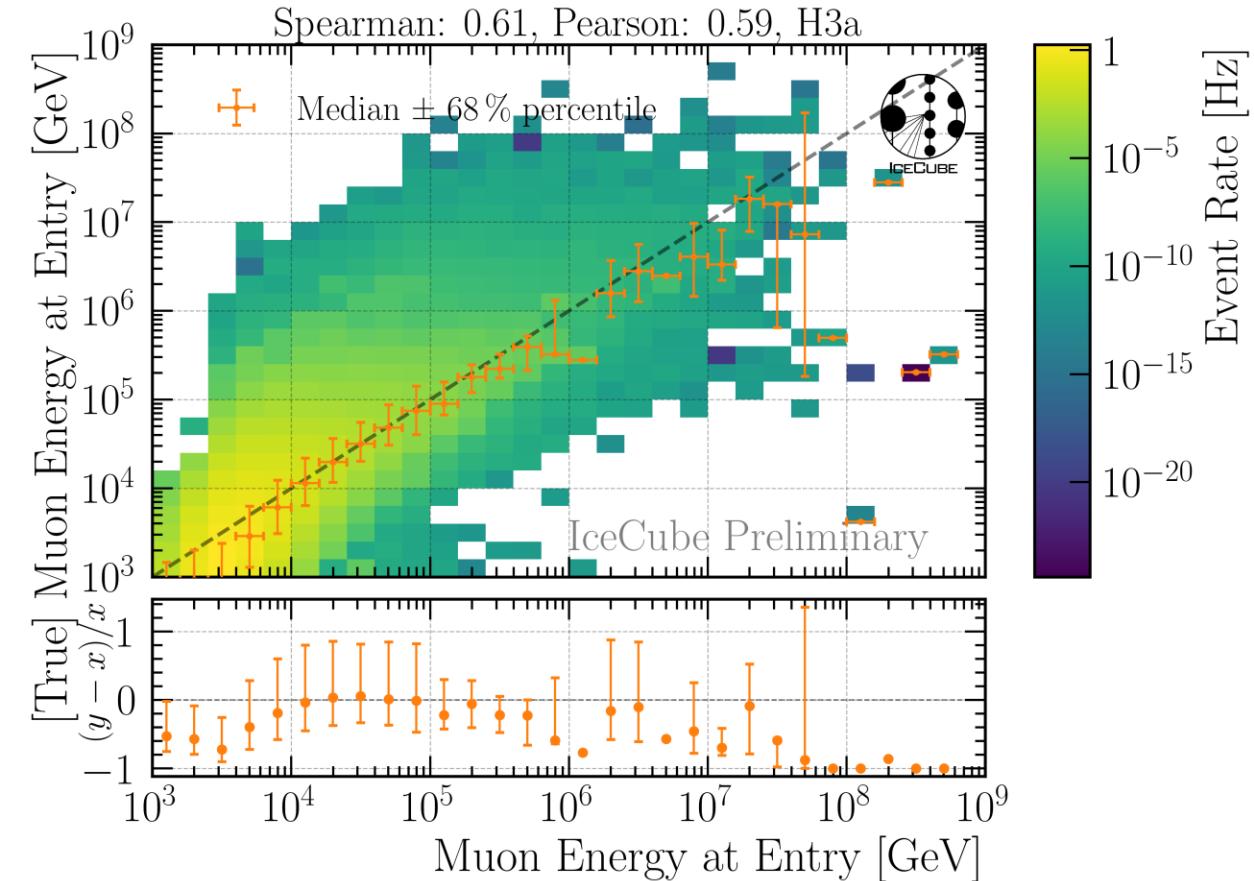
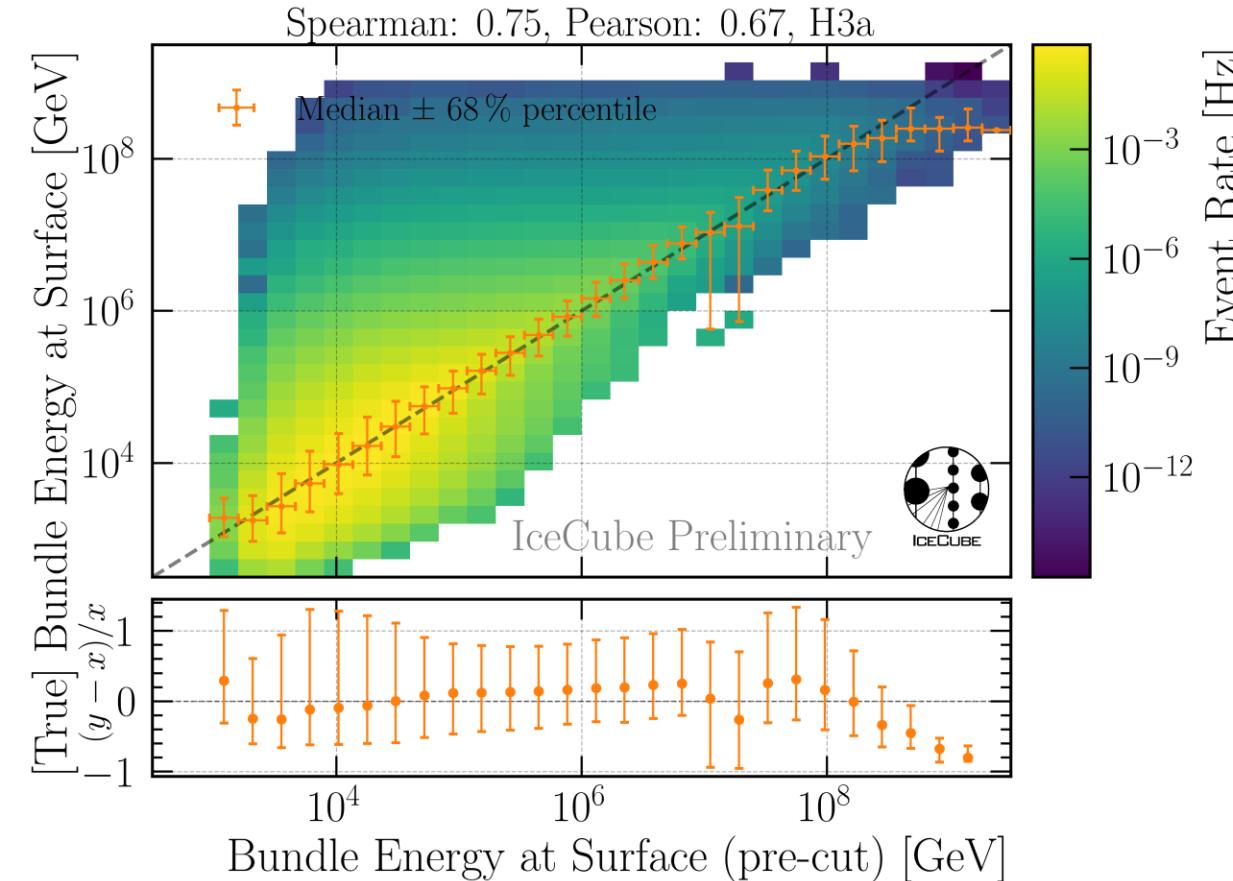
- `Length`: Propagation length of muon in the ice
- `LengthInDetector`: Propagation length of muon in the detector
- `center_pos_x`: Closest x position of muon to center of the detector
- `center_pos_y`: Closest y position of muon to center of the detector
- `center_pos_z`: Closest z position of muon to center of the detector
- `center_pos_t`: Time of closest approach to the center of the detector
- `entry_pos_x`: x position of muon at the detector entry
- `entry_pos_y`: y position of muon at the detector entry
- `entry_pos_z`: z position of muon at the detector entry
- `entry_pos_t`: Time of muon at the detector entry

Direction

- `zenith`: Zenith angle of muon
- `azimuth`: Azimuth angle of muon



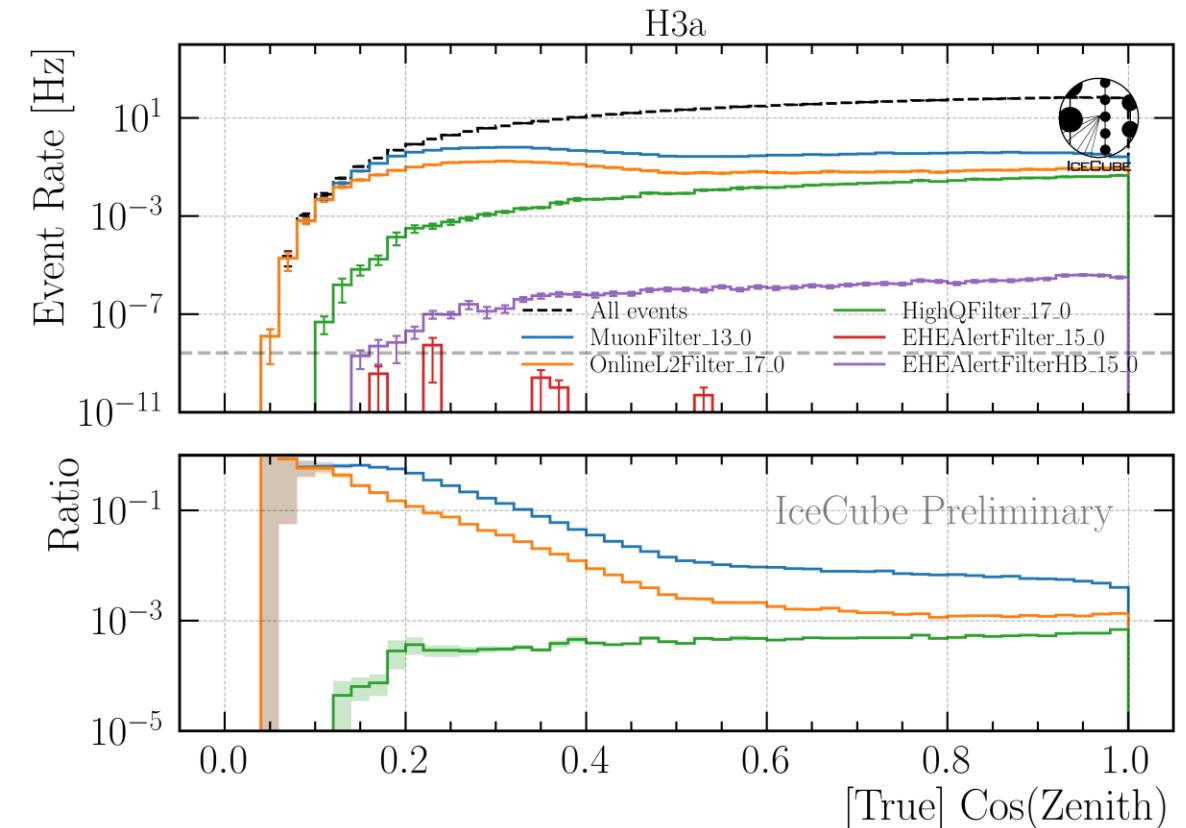
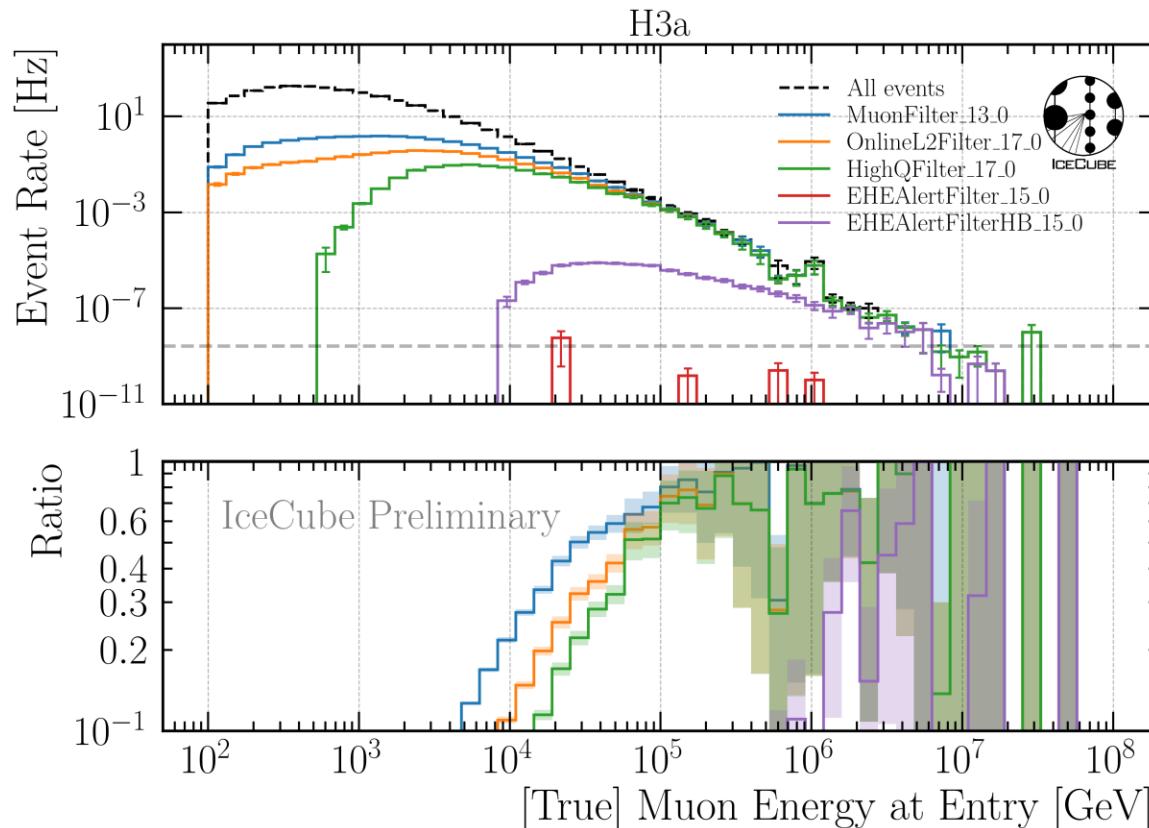
Energy Reconstructions



- Sufficient energy reconstructions
- Tight 68 % intervals, with outliers

Selection

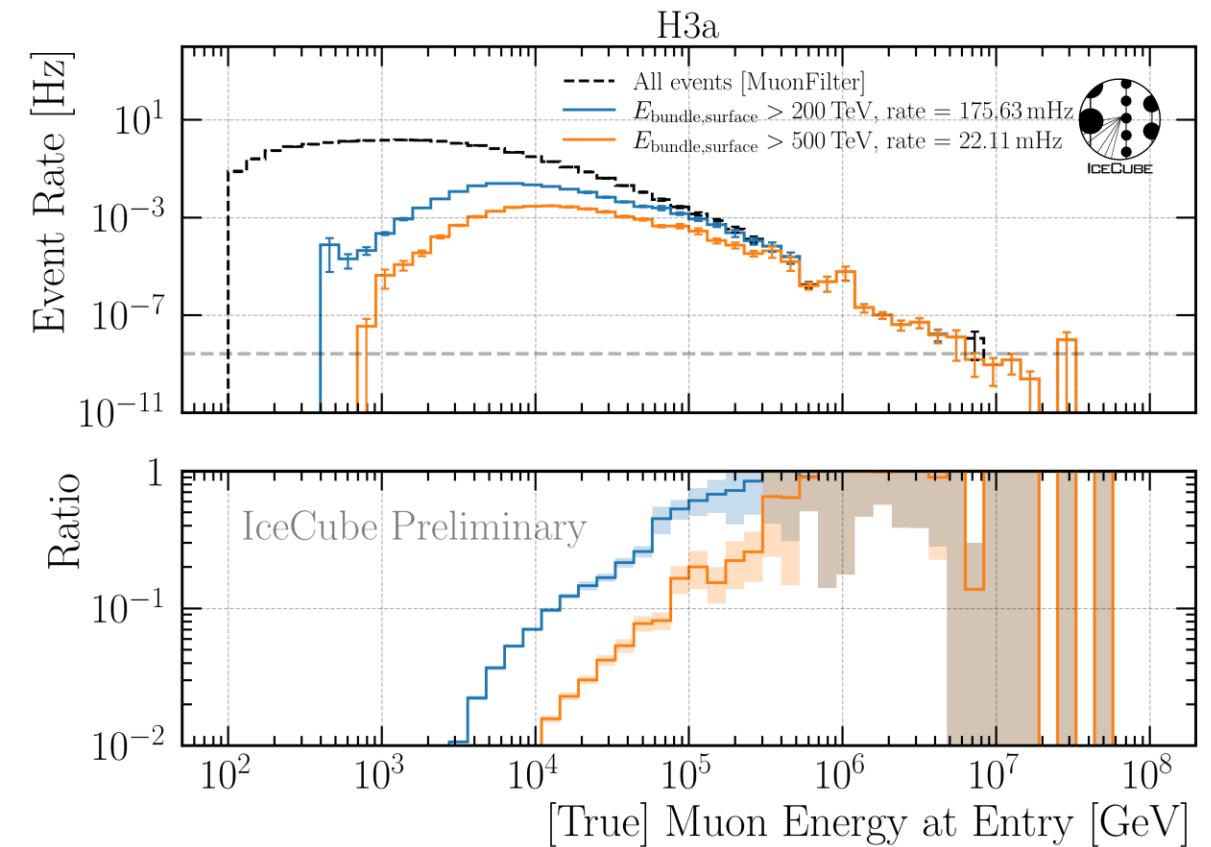
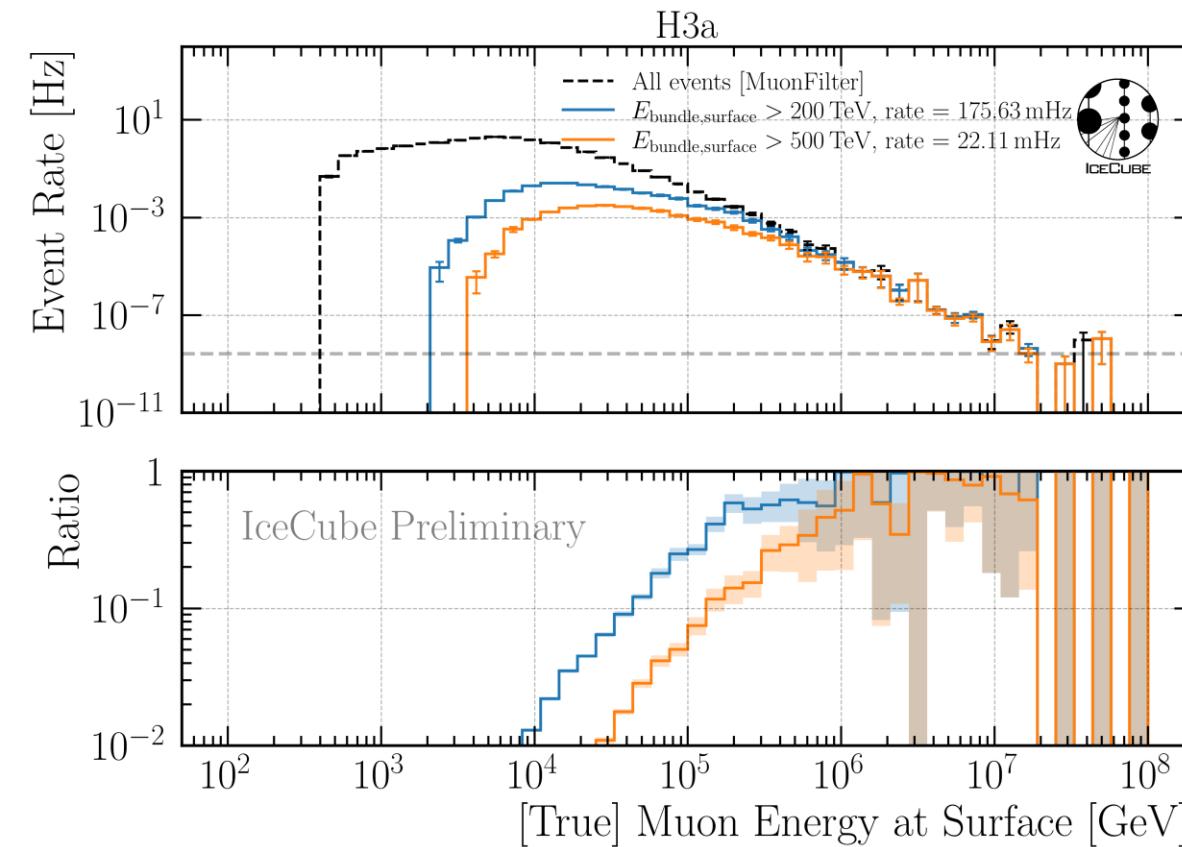
Level 3: Muon Filter



Muon filter: zenith-dependent charge and quality cut

➤ Choose muon filter to select as many high-energy muons as possible

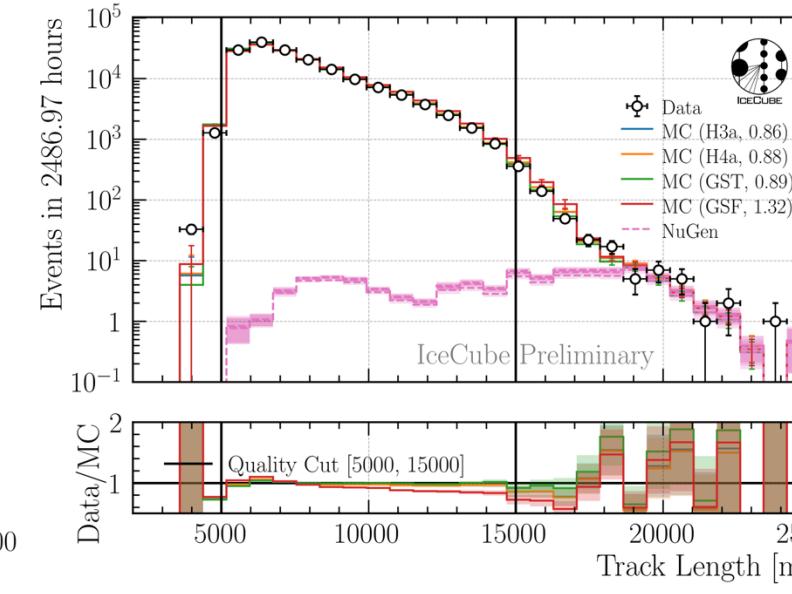
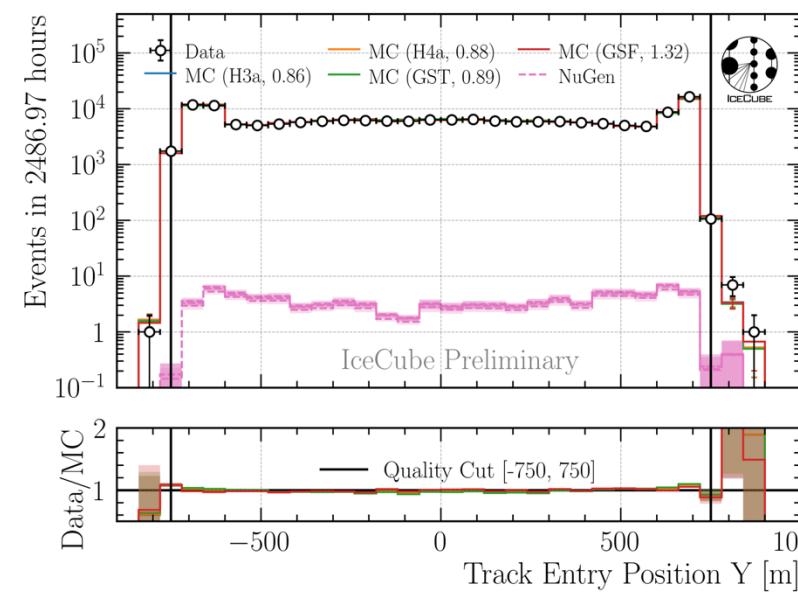
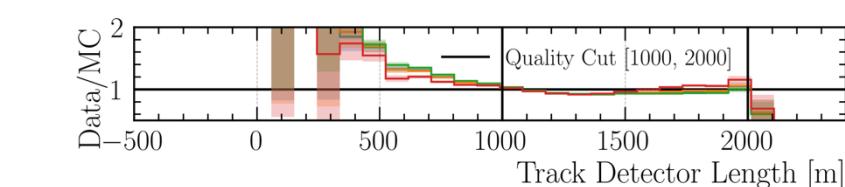
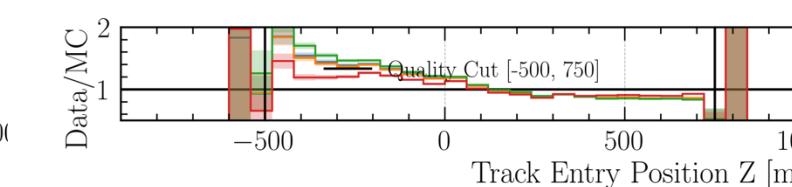
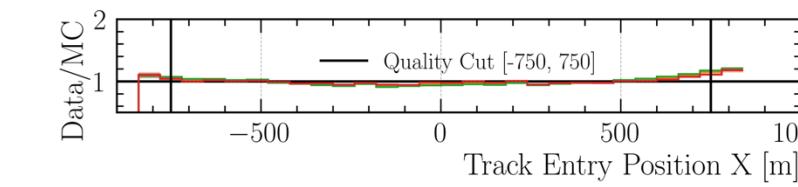
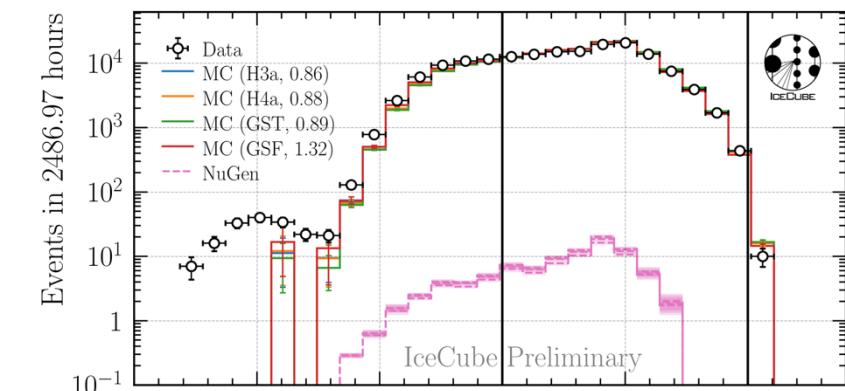
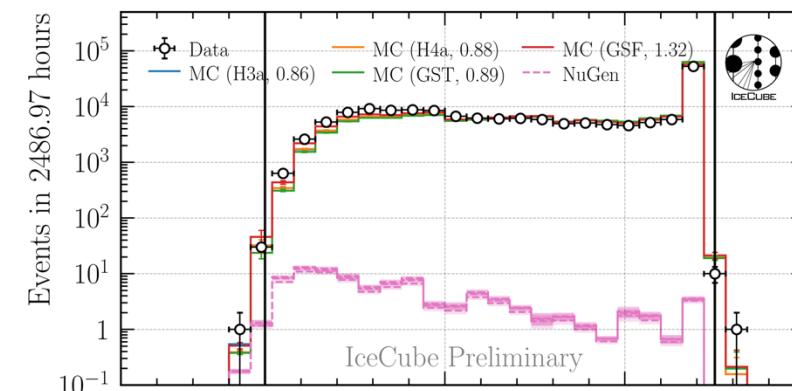
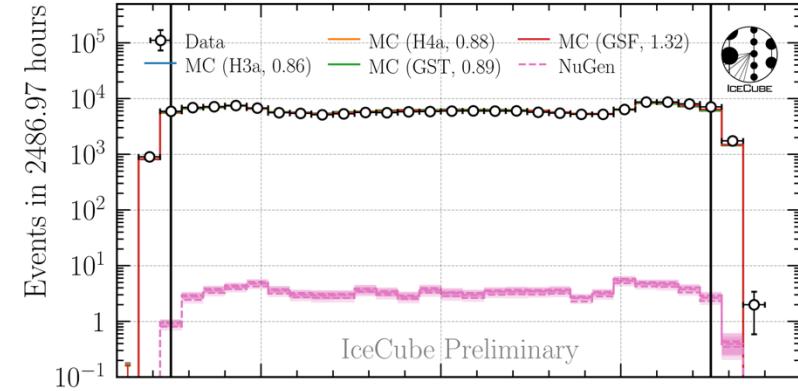
Level 4: Energy Cut



- 6 billion events expected in 10 years → computationally not feasible
- focus on high-energetic events
- Remove low-energy muons: bundle energy at surface > 500 TeV

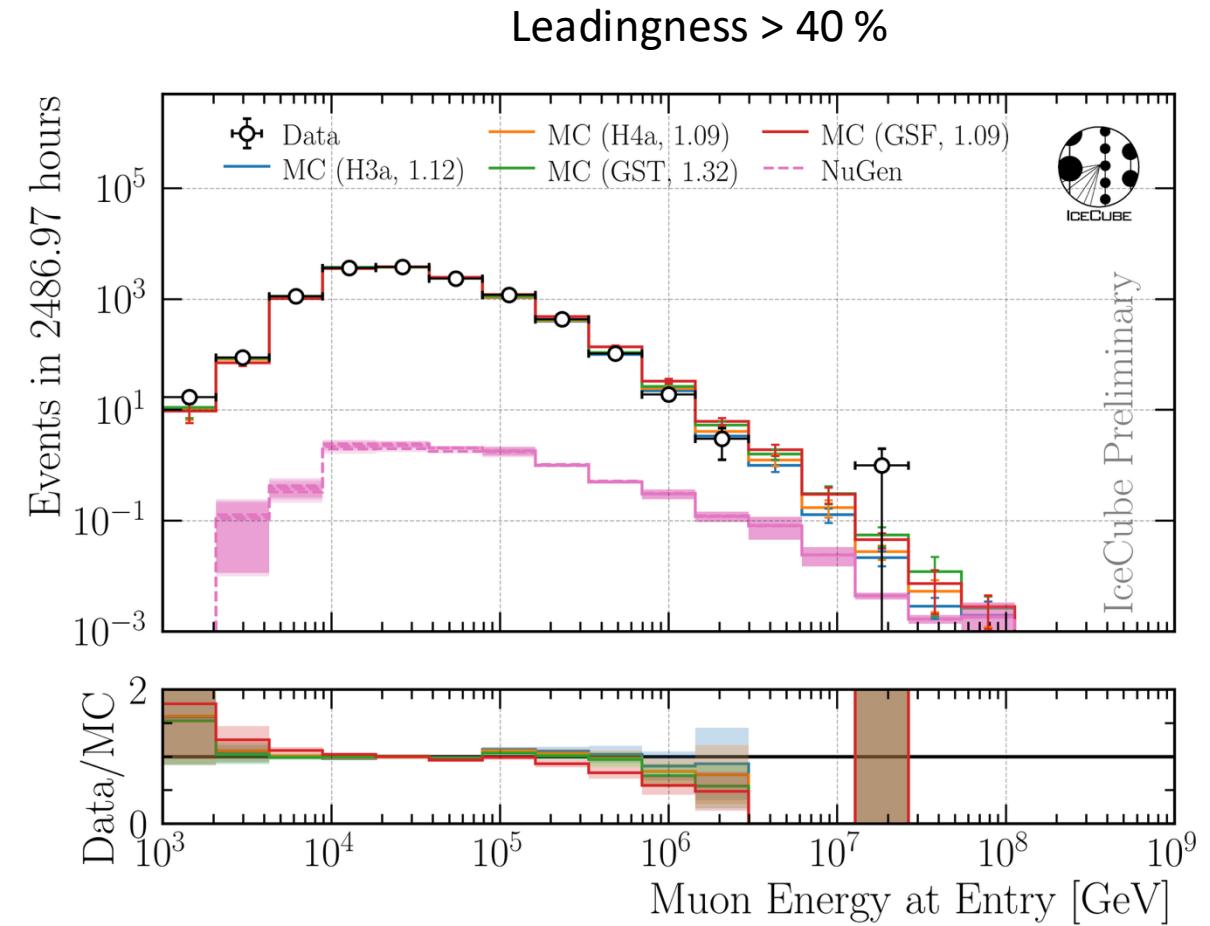
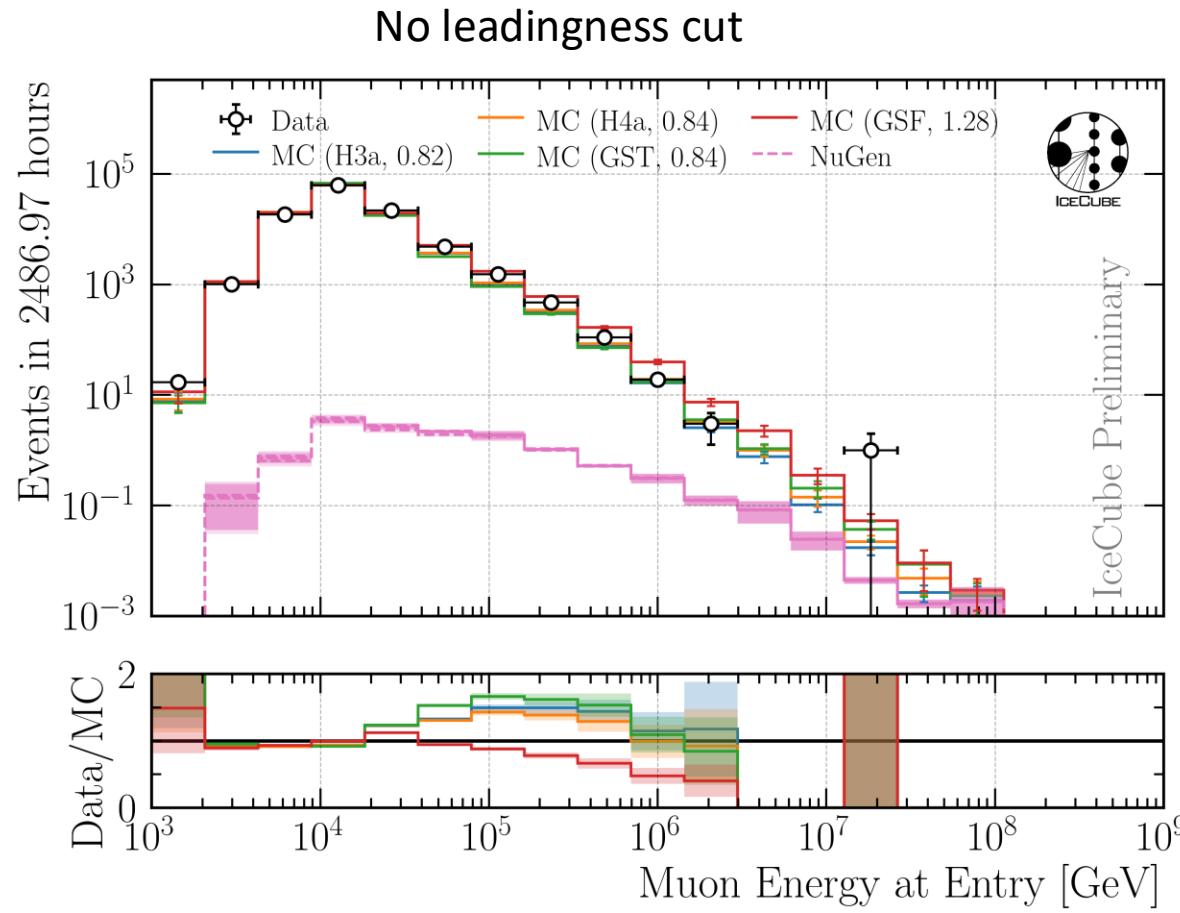
- Remove outliers
- Depth—dependent slope (no analysis relevance)
- CR—model impact on energy reconstruction
- 23 quality cuts in total

Level 5: Data/MC Quality Cuts



Final Level: Leadingness > 40 %

$$L = \frac{\text{Leading Energy at Entry}}{\text{Bundle Energy at Entry}}$$



➤ Improve Data/MC by leadingness cut

Unfolding

Unfolding in a nutshell

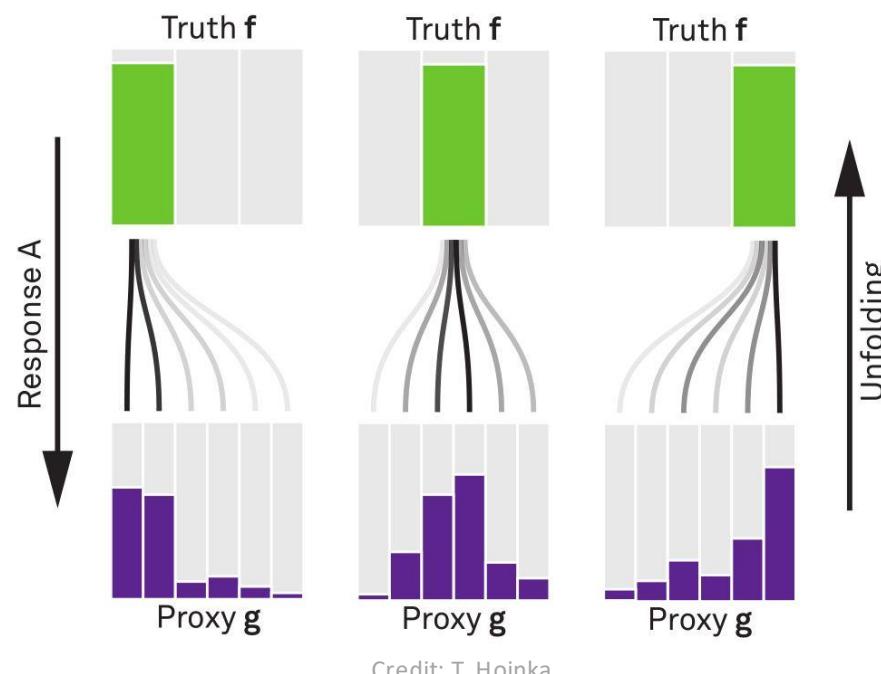
measured proxy

$$g(y) = \int_{E_0}^{E_1} A(E_\mu, y) f(E_\mu) dE_\mu + b(y)$$

detector response

background

true energy distribution



pascal.gutjahr@tu-dortmund.de

1. Discretized form: $\vec{g} = A\vec{f} \leftrightarrow \vec{f} = A^{-1}\vec{g}$

2. Maximum likelihood method:

$$\mathcal{L}(\vec{g}|\vec{f}) = \prod_{j=1}^M \frac{\lambda_j^{g_j}}{g_j!} \exp(-\lambda_j)$$

$$= \prod_{j=1}^M \frac{(A\vec{f})_j^{g_j}}{g_j!} \exp(-(A\vec{f})_j)$$

3. Tikhonov regularization:

$$t(\vec{f}) = -\frac{1}{2} (\vec{C}\vec{f})^T (\tau_1)^{-1} (\vec{C}\vec{f})$$

4. Maximize $\log(\mathcal{L}(\vec{g}|\vec{f})) + t(\vec{f})$
with respect to \vec{f} using
Markov Chain Monte Carlo (MCMC)
or Minuit

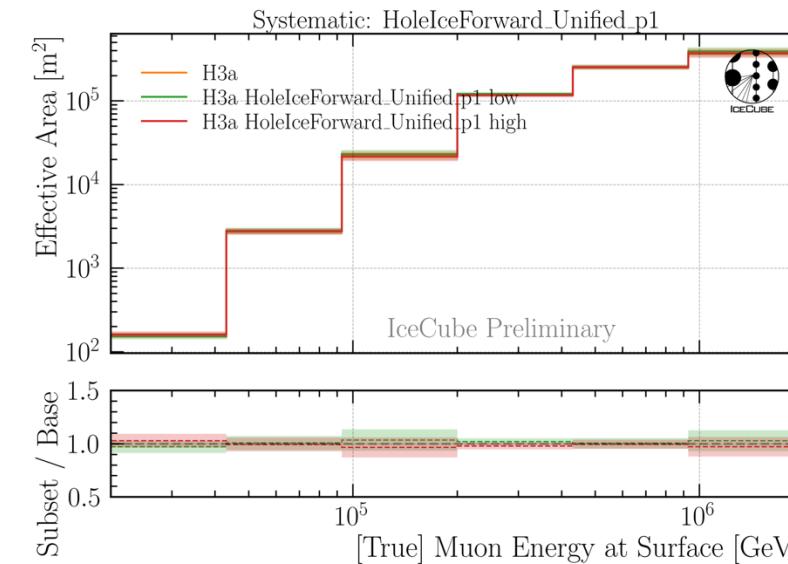
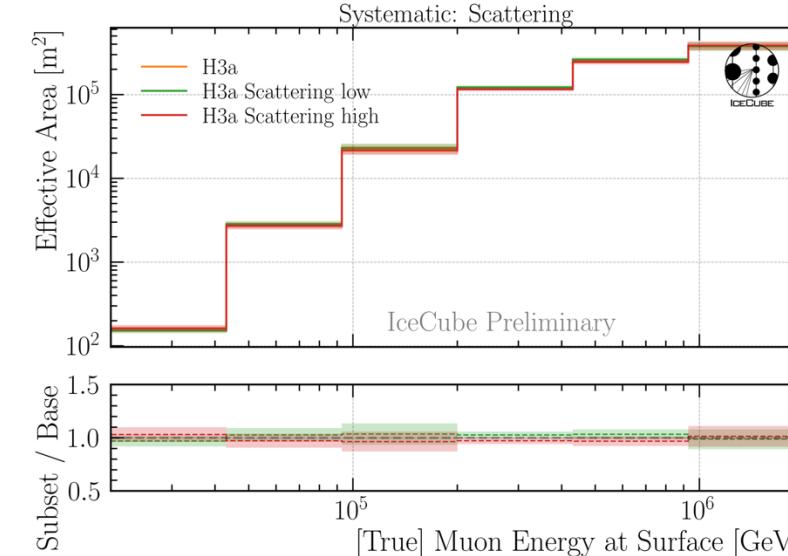
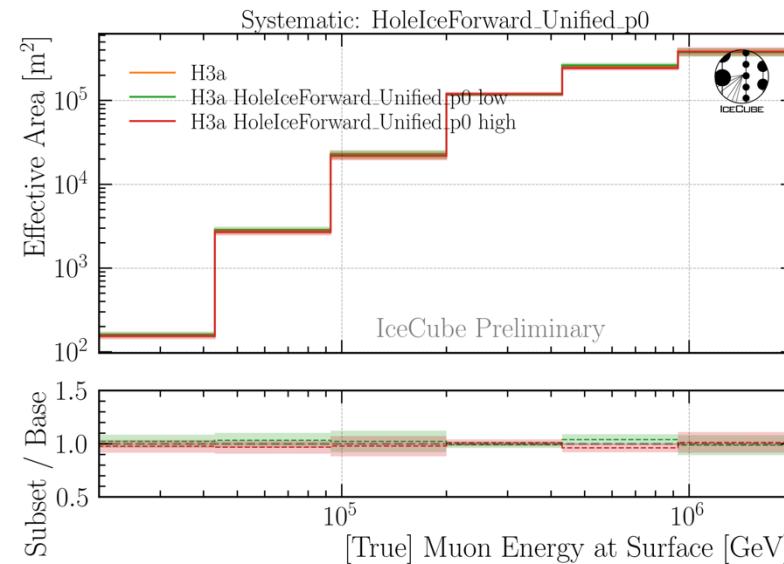
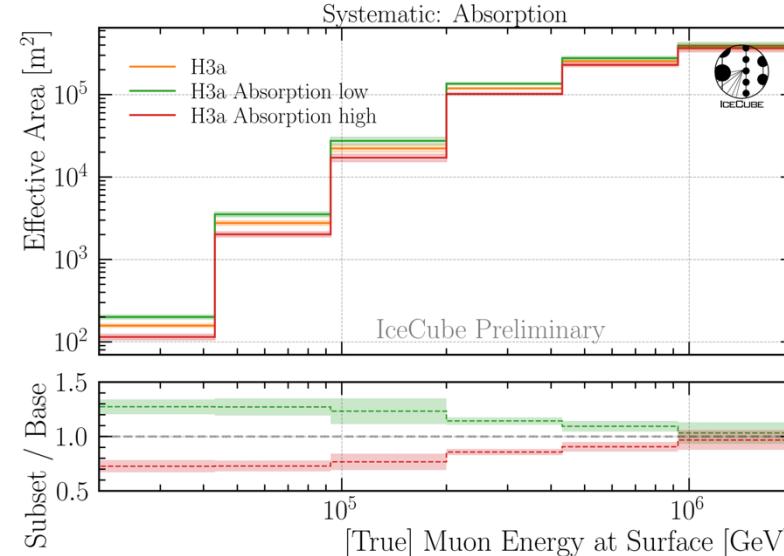
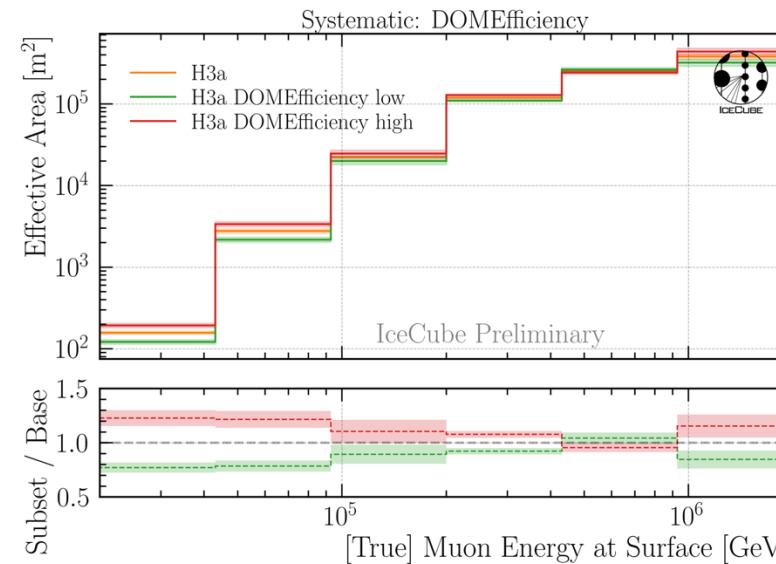
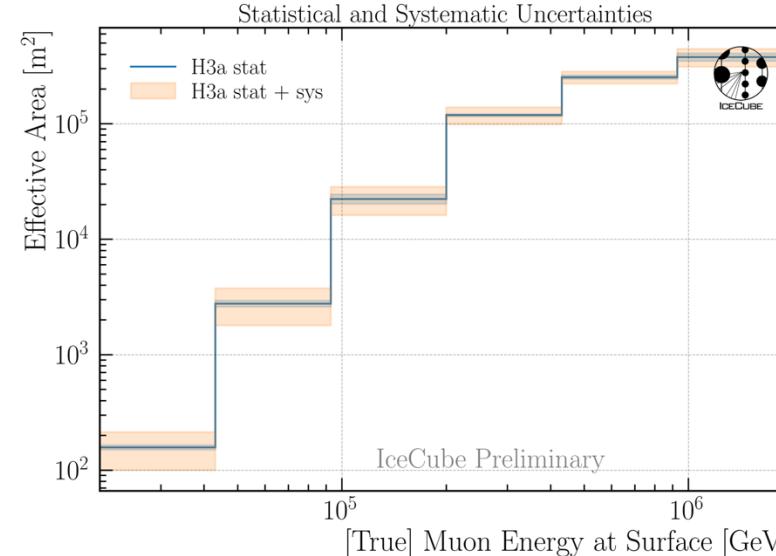


funfolding
by M. Börner

Muon Flux Unfolding

- ❑ Effective area
- ❑ Systematics
- ❑ Proxy that correlates with target
- ❑ Regularization
 - Unfolding

Ice & Detector Systematics

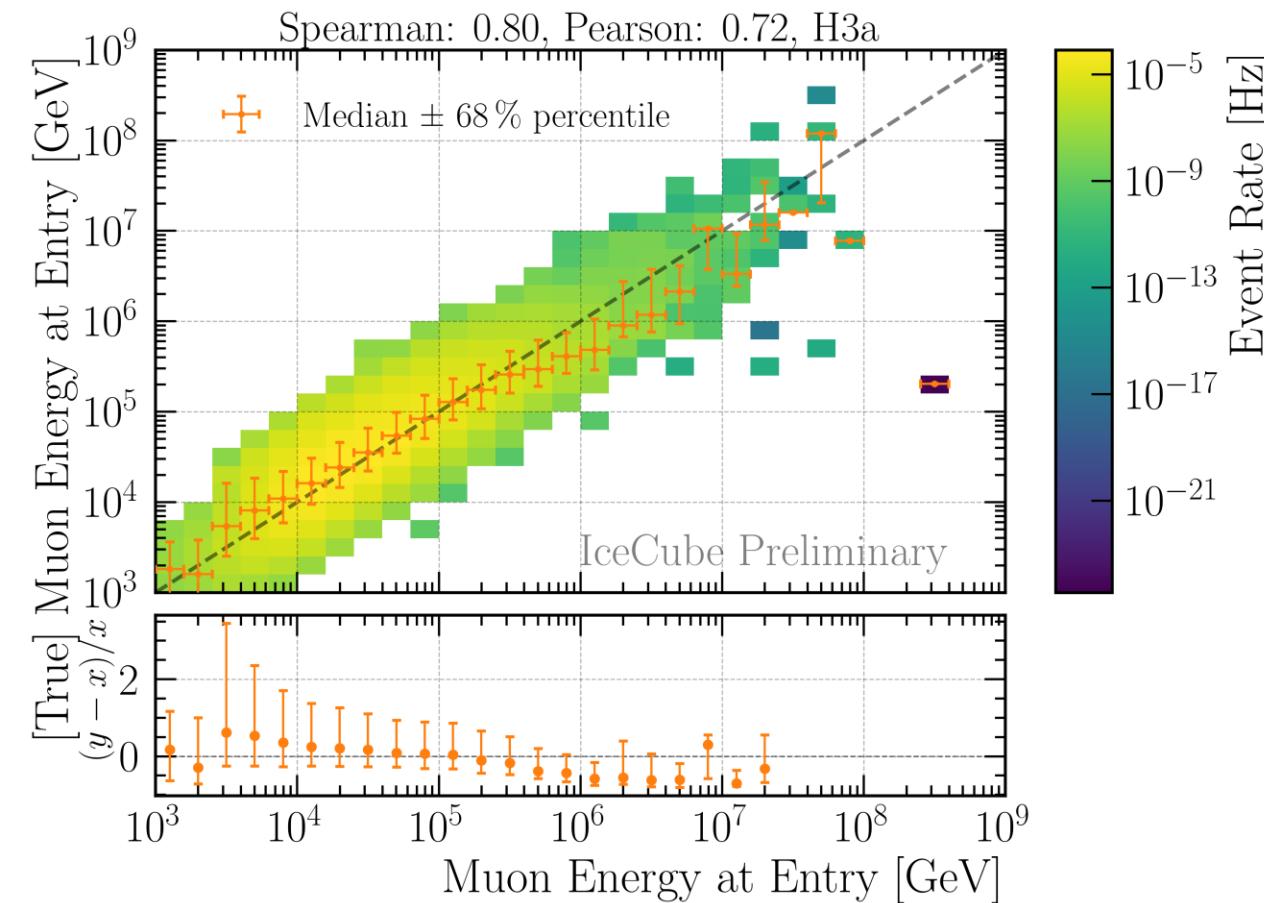


- Baseline: entire set
- Subset: above/below center

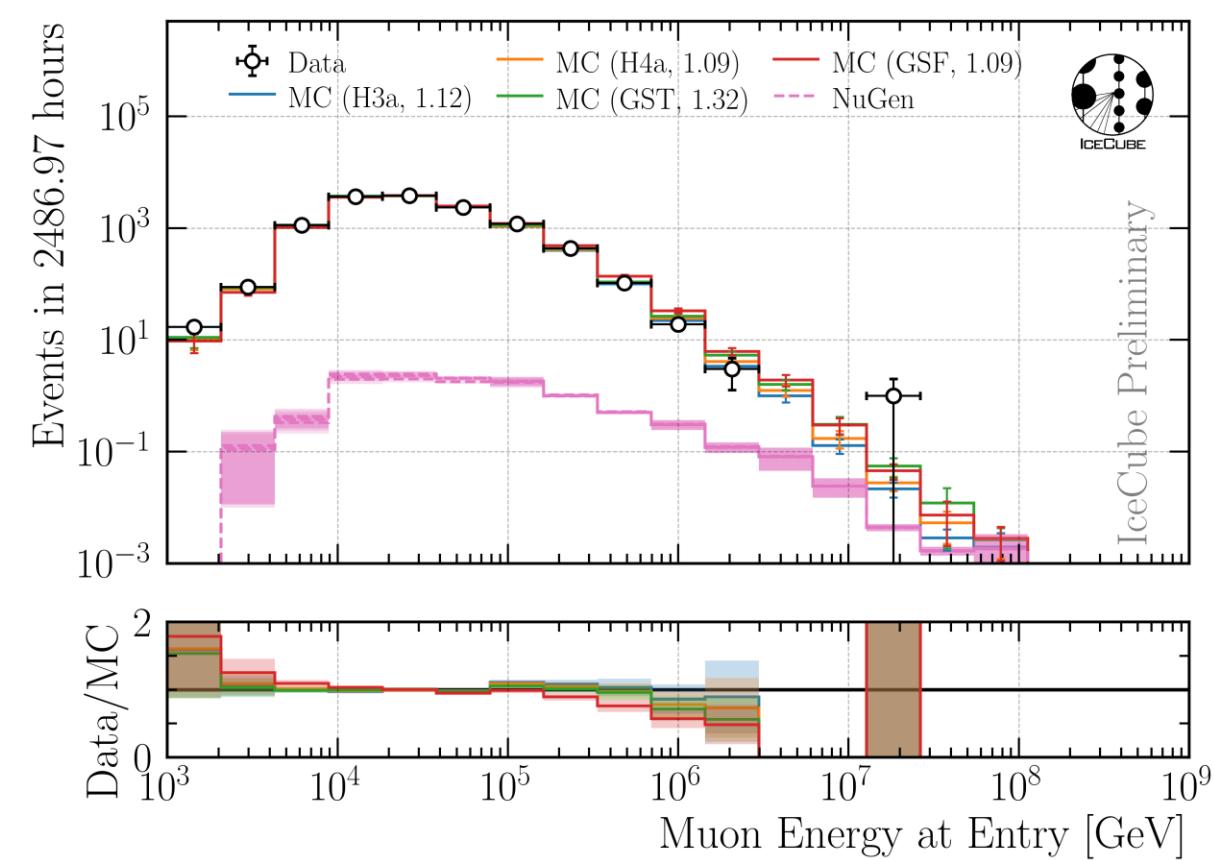
$$\sigma_{\text{tot}} = \sqrt{\sigma_{\text{stat}}^2 + \sum_i \sigma_i^2}, i: \text{scat, abs, DOME, holeice p0, p1}$$

Reconstruction and Data—MC: Leading Muons

- Good reconstruction of leading muon energy → proxy

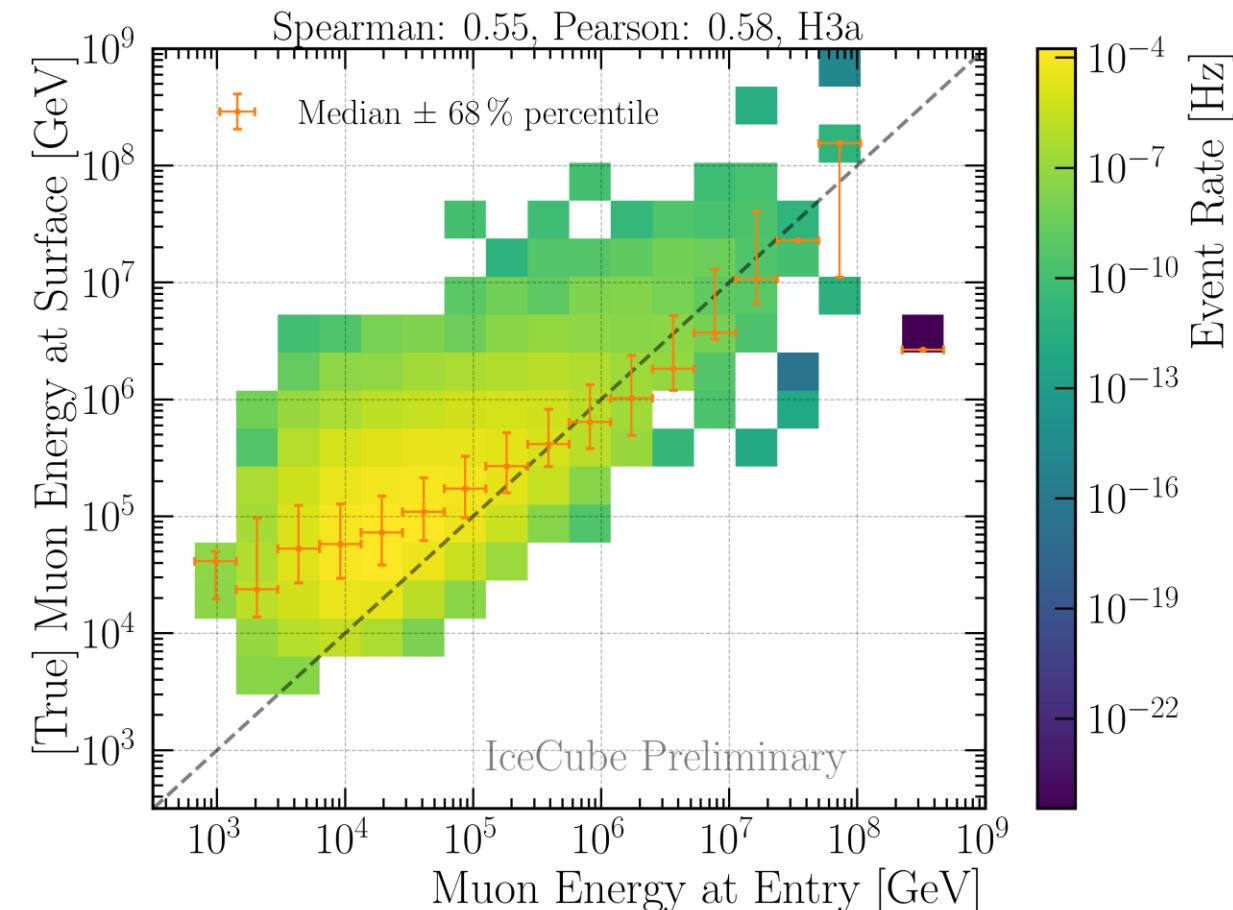


- Good data—MC agreement
- Global offset → upscale MC by 12%

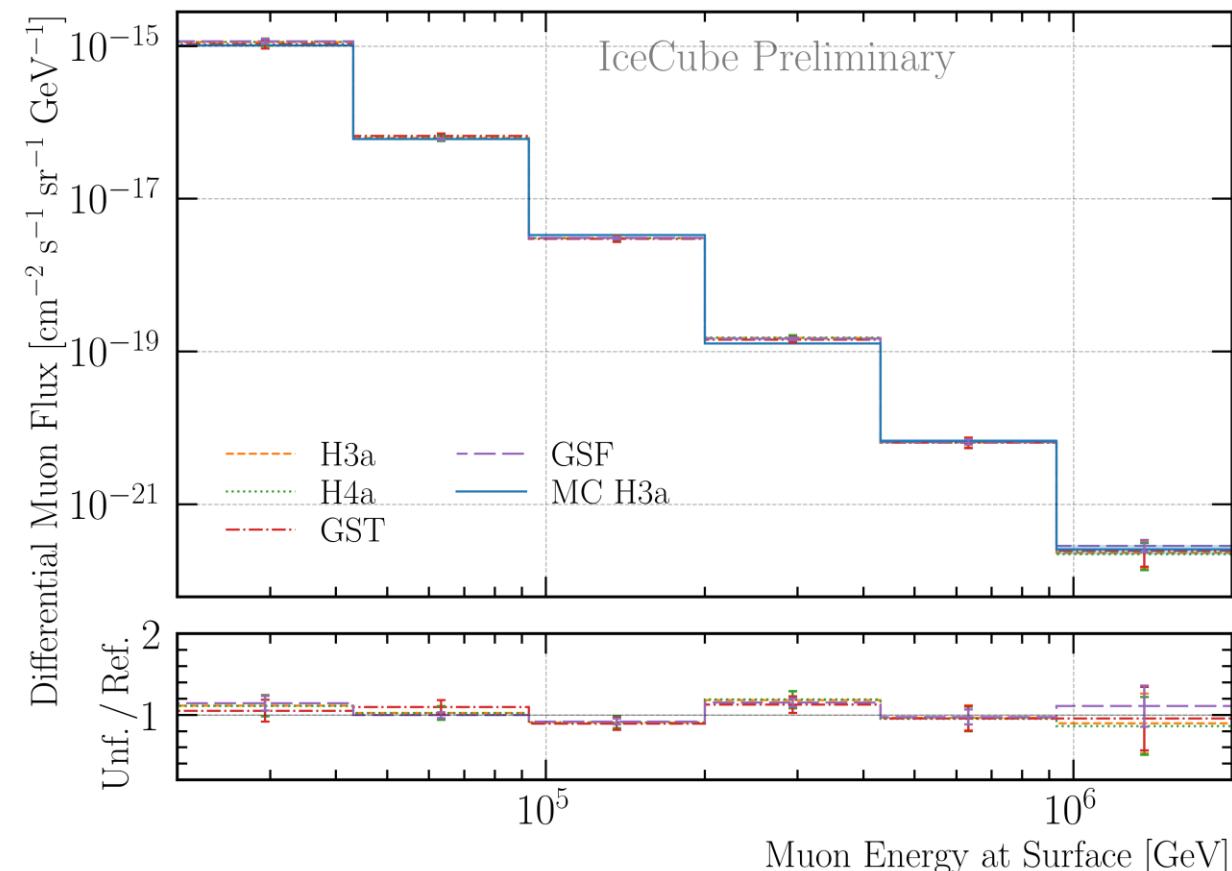


Correlation and Robustness Test: Leading Muons

- Correlation between proxy and target



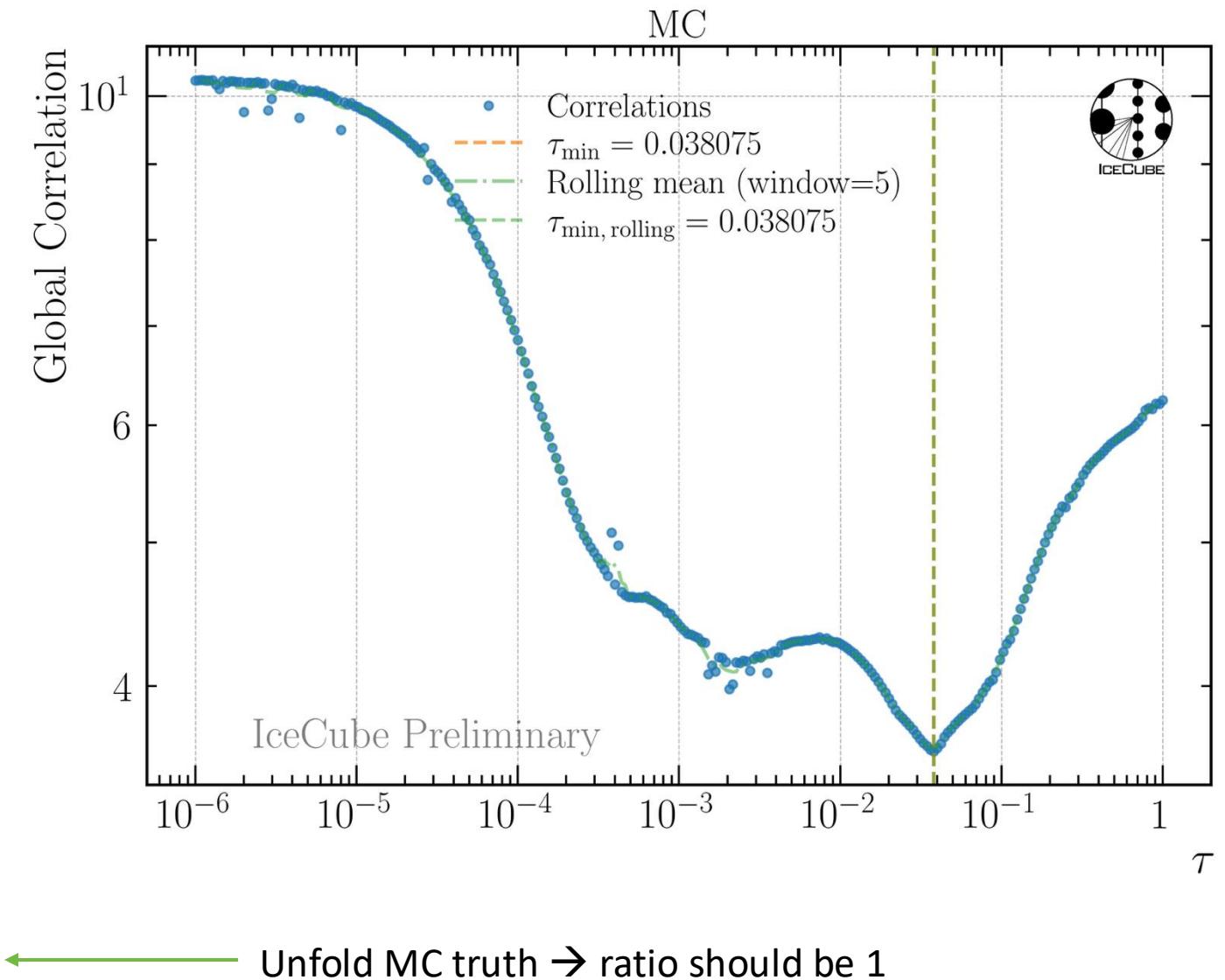
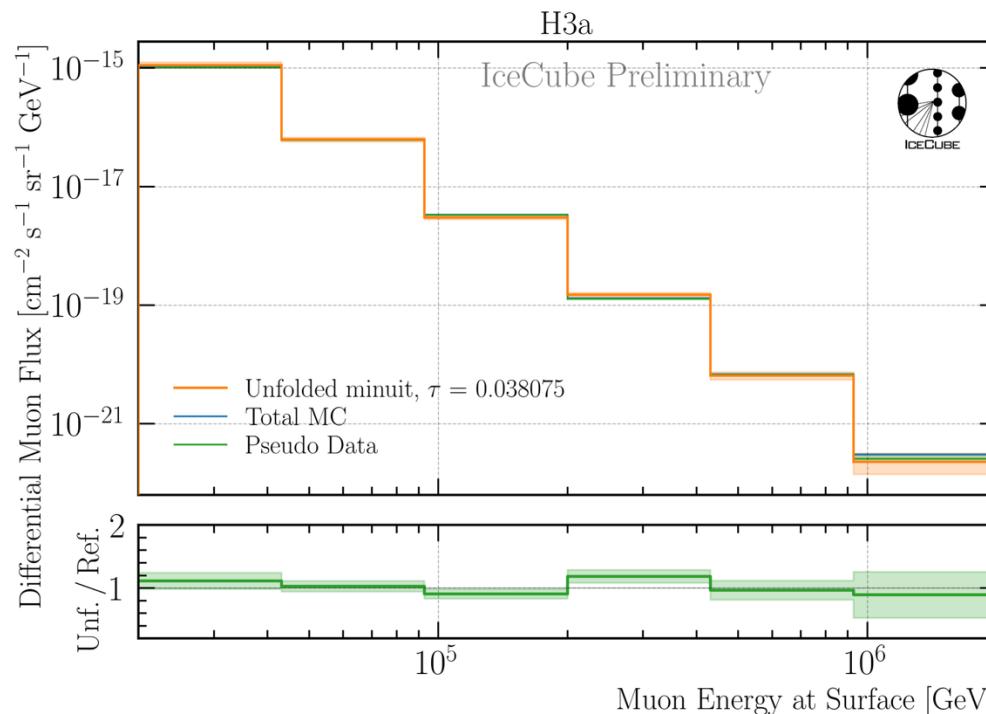
- Build unfolding matrix on H3a, H4a, GST & GSF
- Unfold H3a as test set
- Results are within uncertainties → robust



Determine Regularization

- Find regularization τ with minimal bin-to-bin correlation
- LLH minimization (unfolding) provides full covariance matrix V

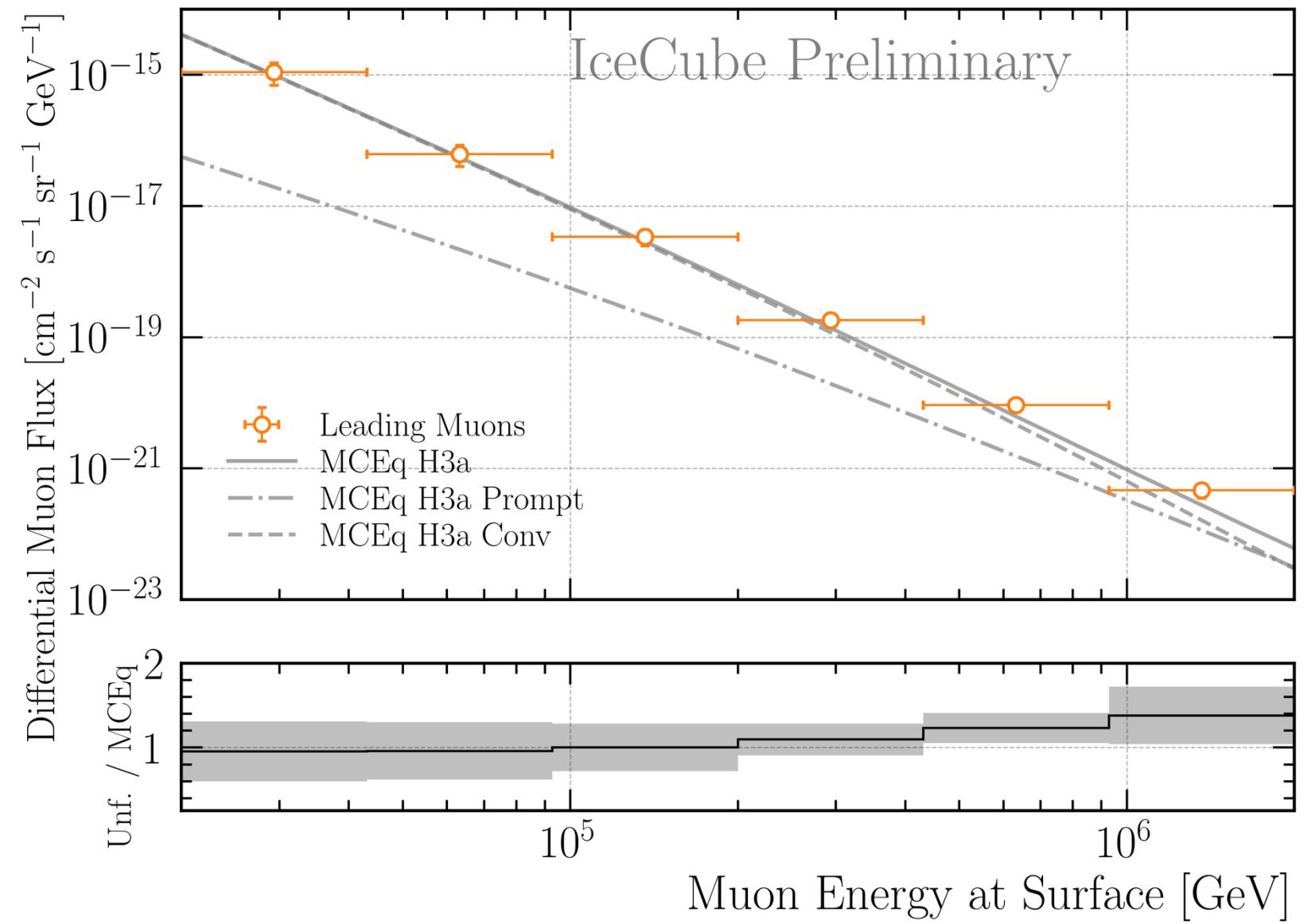
➤ Minimize global correlation $\rho = \sum_{i > i} V_{ij}$



Burnsample Unfolding

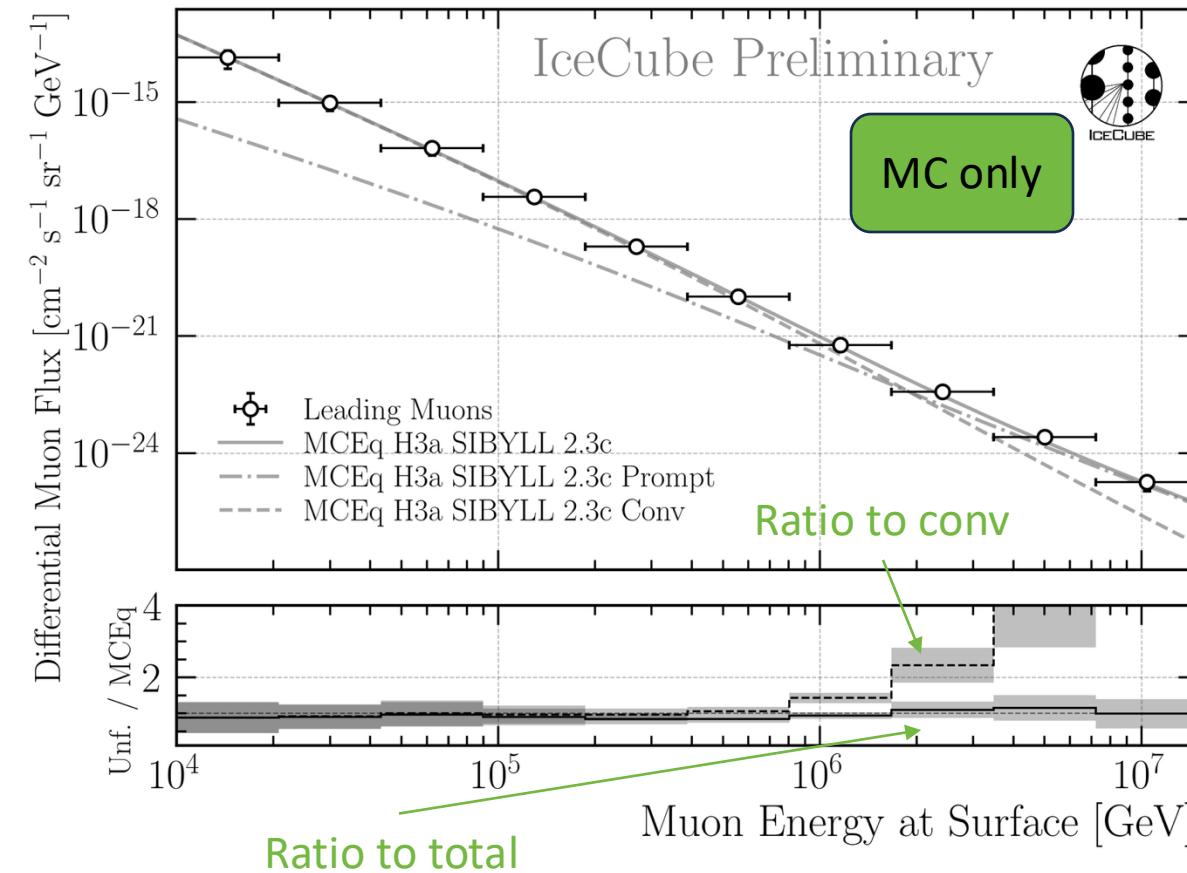
Leading muons

- 2487 h IceCube data
- 12754 events
- Agrees with MCEq

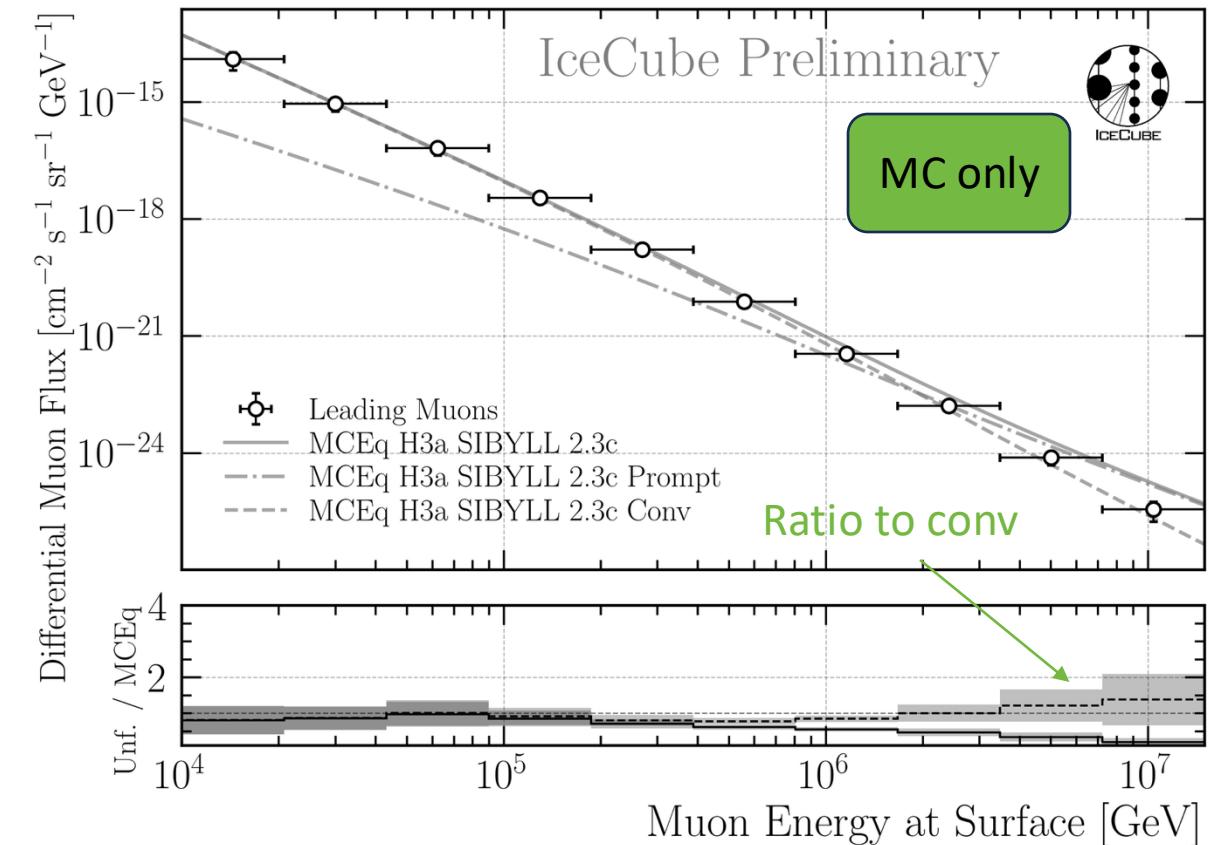


Prediction: 12 Years of IceCube Data Unfolding

Pseudo Sample has prompt



Pseudo Sample has NO prompt



➤ Unfolding is sensitive to the prompt component

Event Rate to Flux → Effective Area

- Unfolding estimates an event rate
- Transfer event rate to flux

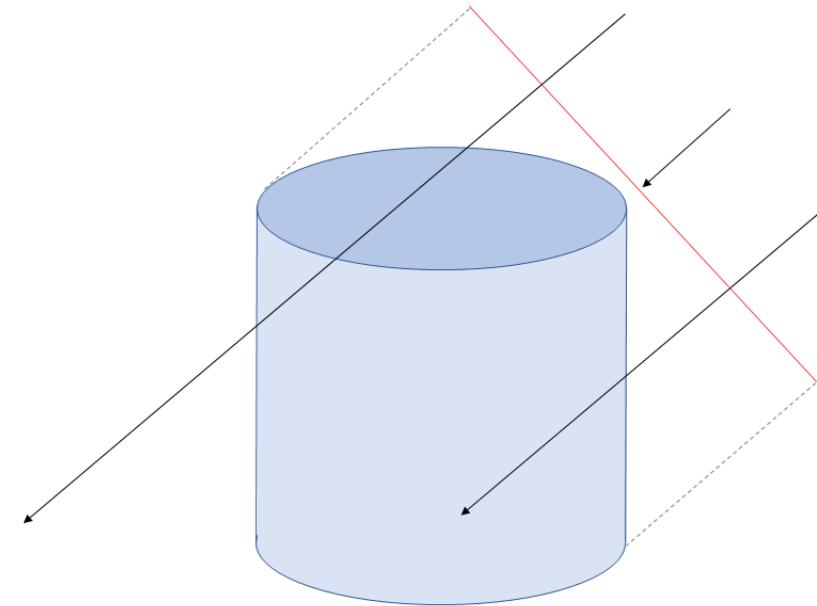
$$\Phi_i = \frac{N_i}{T \cdot \Delta L_i \cdot \Omega_i \cdot A_{\text{eff},i}}$$

- with solid angle

$$\Omega_i = 2\pi \cdot (\cos \Theta_{\min,i} - \cos \Theta_{\max,i})$$

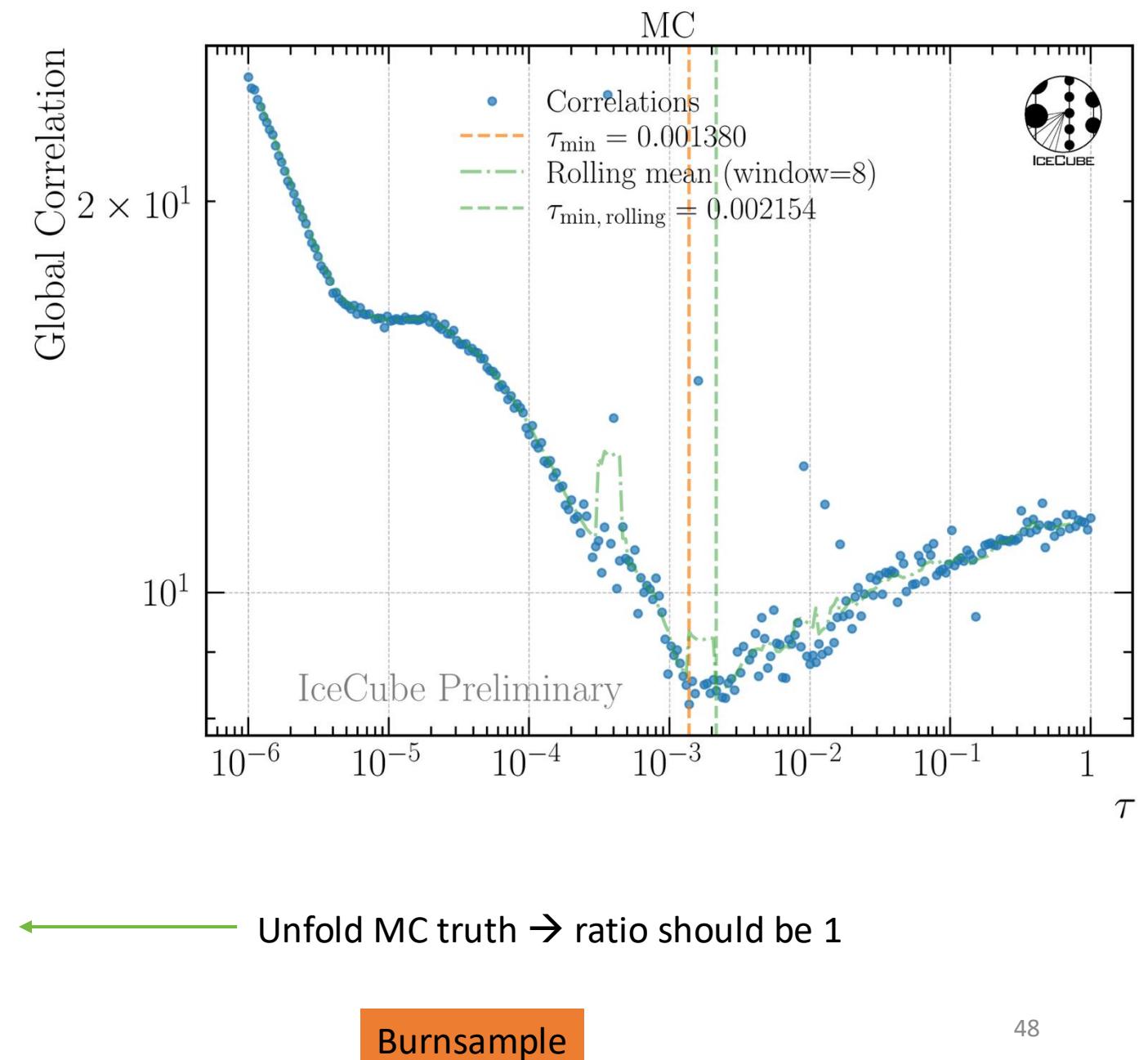
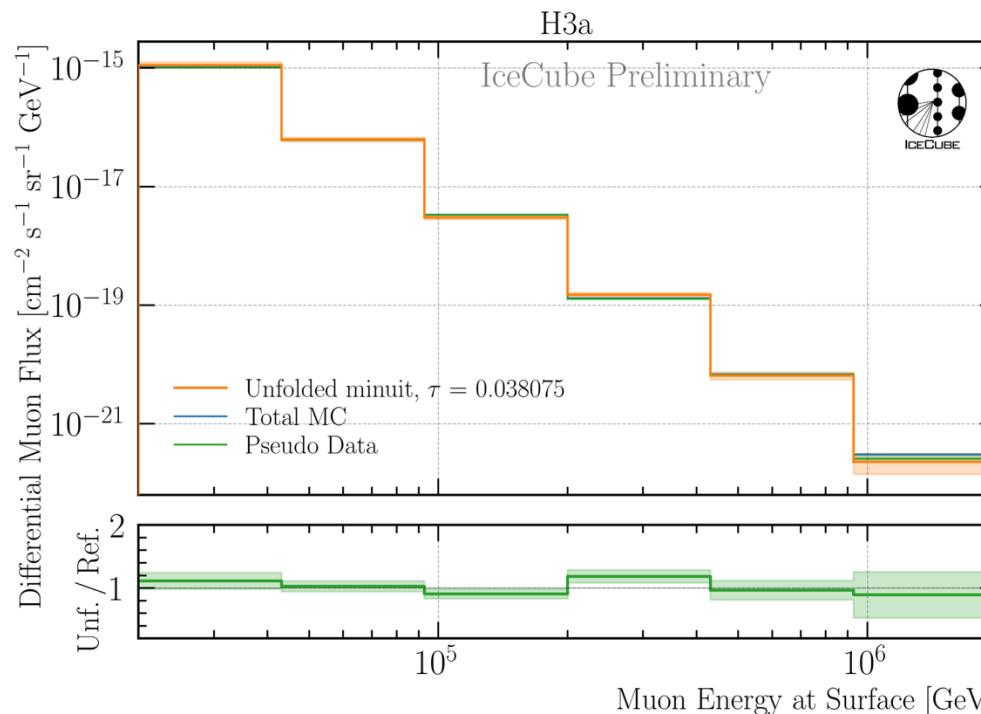
- and effective area

$$A_{\text{eff}} = A_{\text{sim}} \frac{N_{\text{sel}}}{N_{\text{gen}}}$$



Determine Regularization

- Find regularization τ with minimal bin-to-bin correlation
 - LLH minimization (unfolding) provides full covariance matrix V
- Minimize global correlation $\rho = \sum_{i > i} V_{ij}$



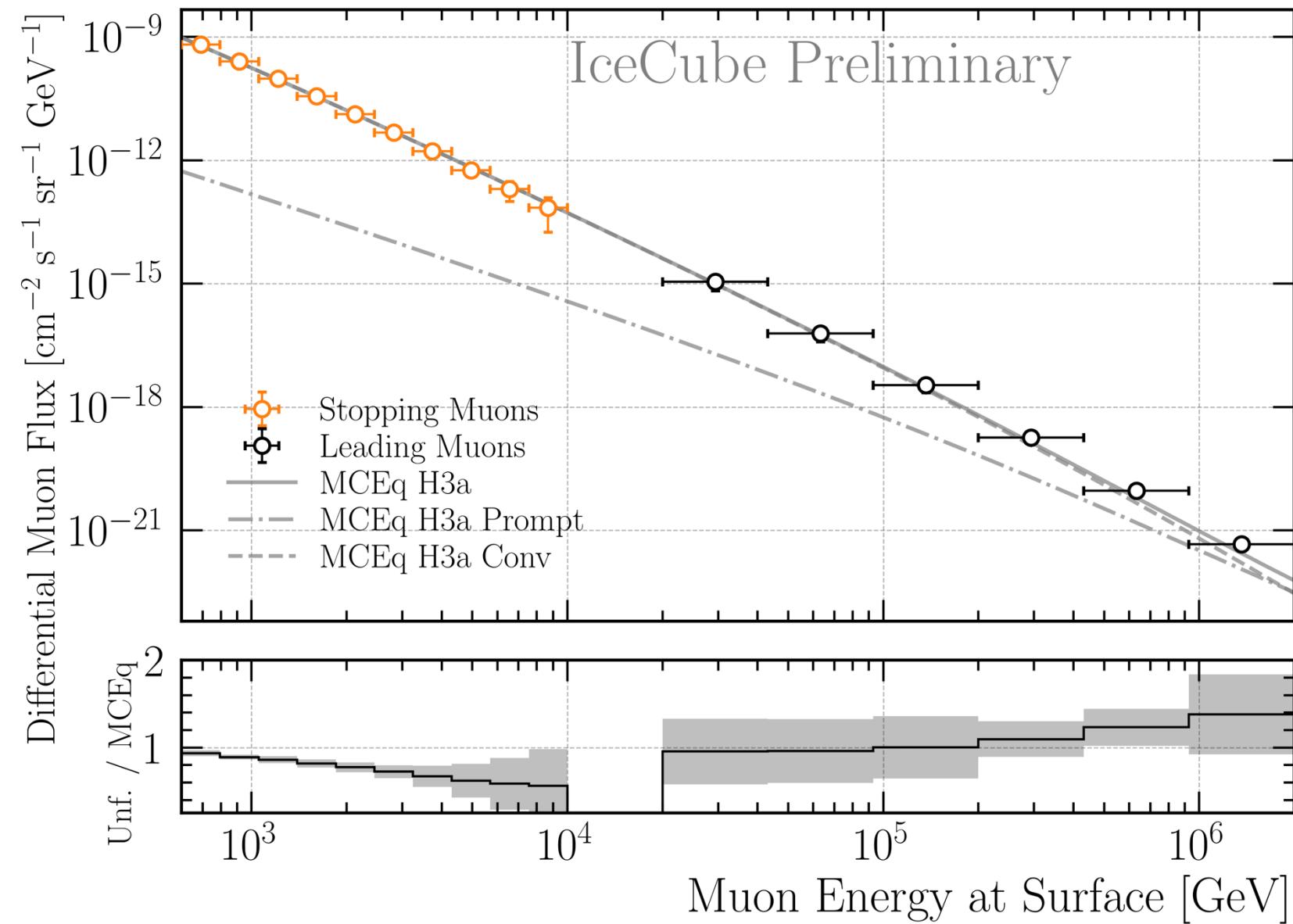
Muon Flux Unfolding

Leading muons

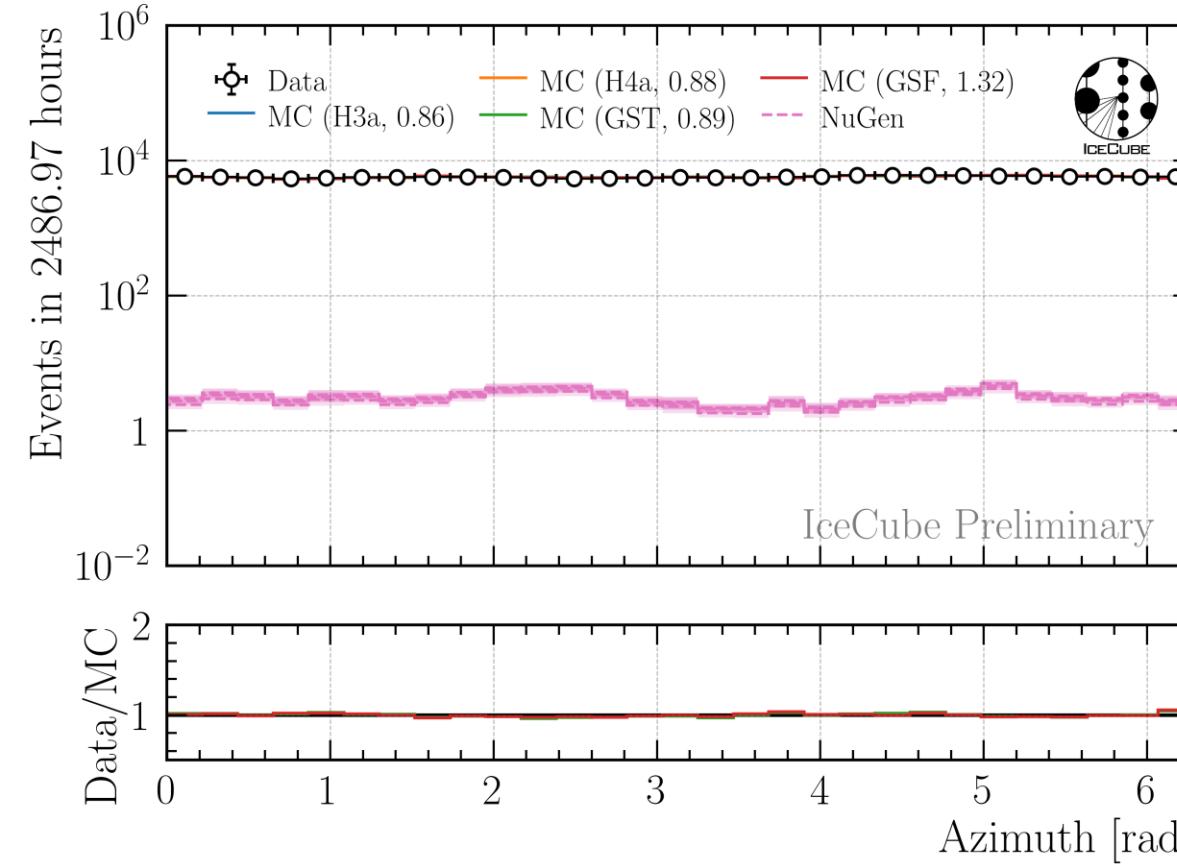
- 2487 h IceCube data
- 12754 events
- Agrees with MCEq

Stopping muons

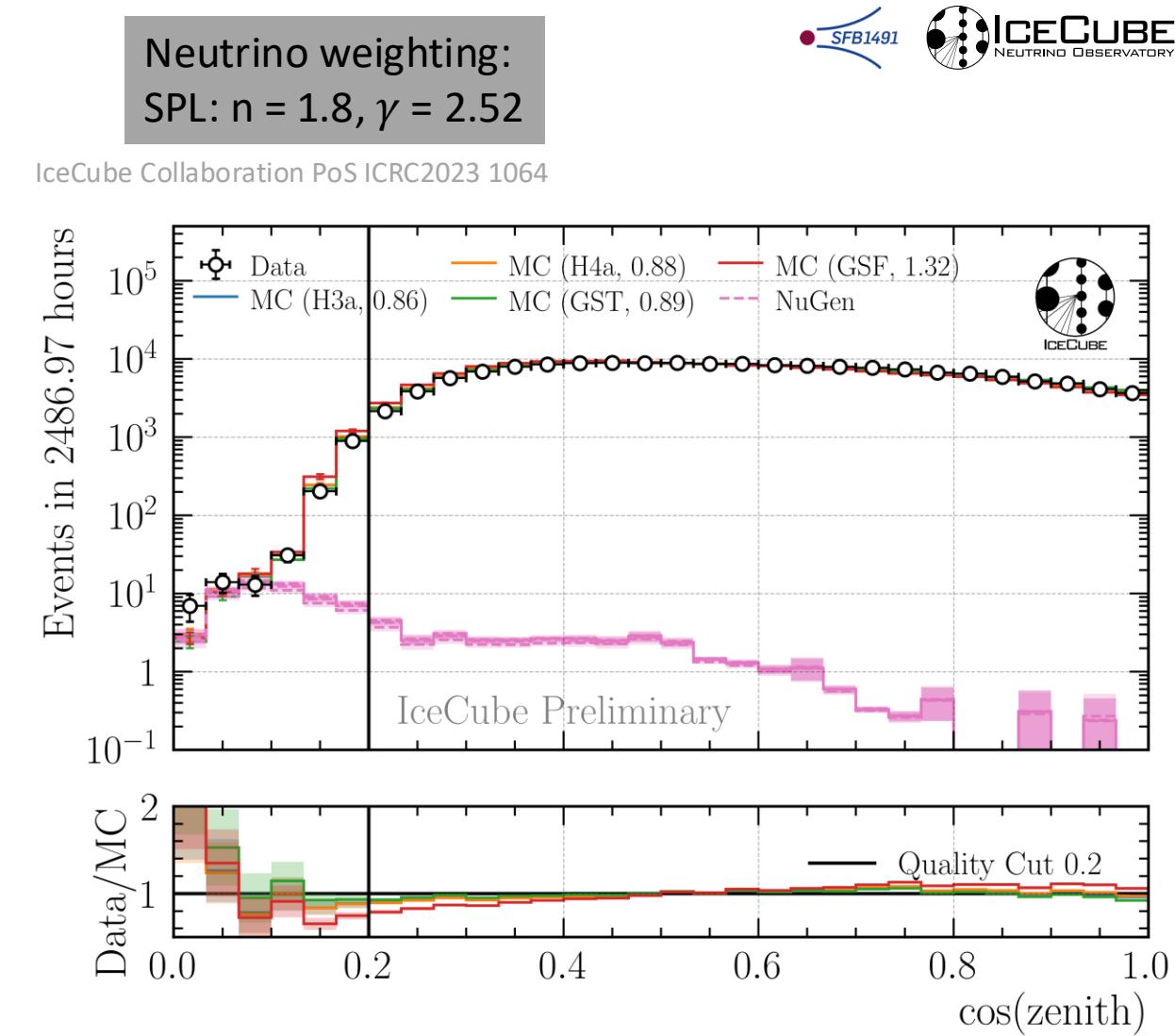
- 47 min IceCube data
- 32943 events
- Below MCEq prediction



Level 5: Data/MC Quality Cuts

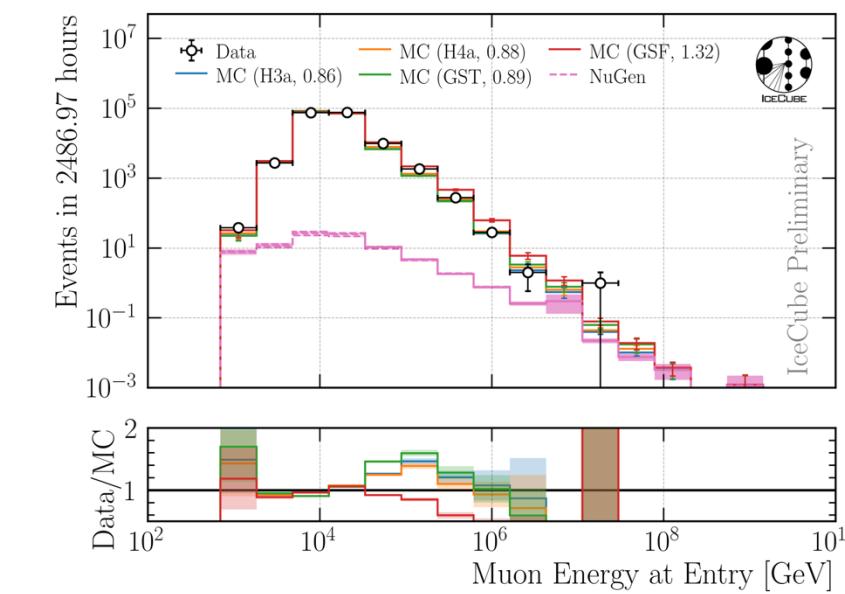
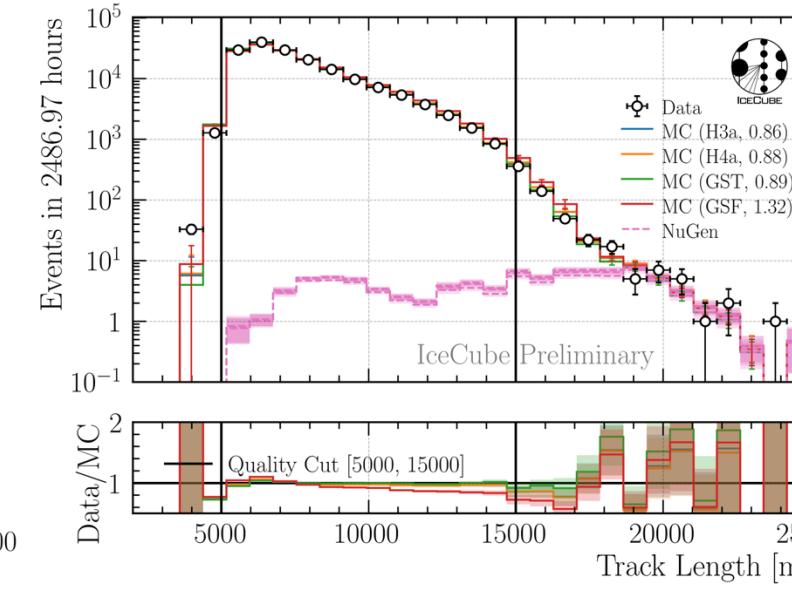
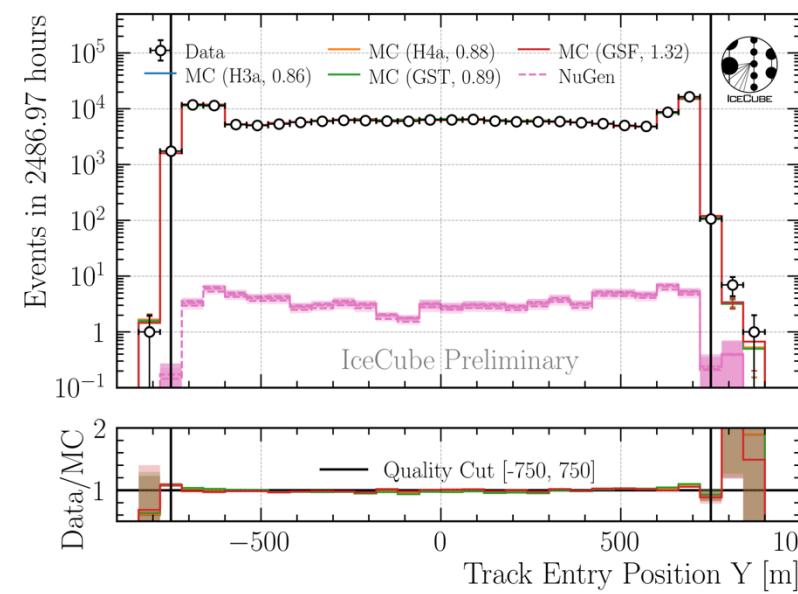
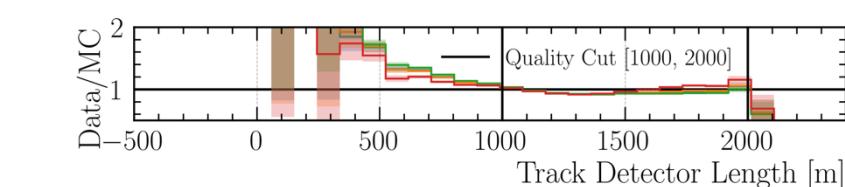
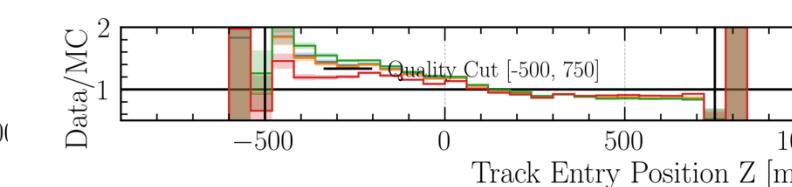
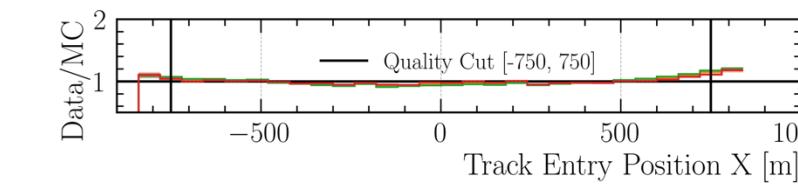
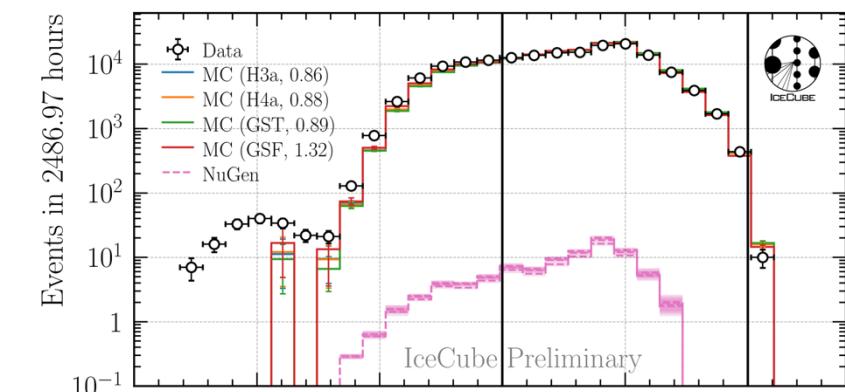
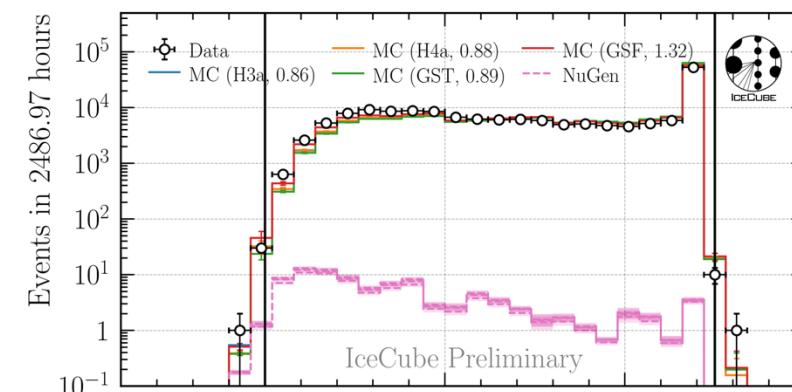
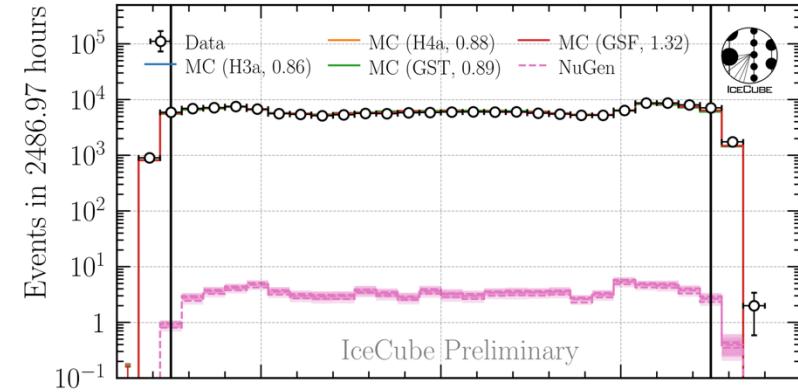


- Good directional reconstruction
- Cut: $\cos(\text{zenith}) > 0.2$

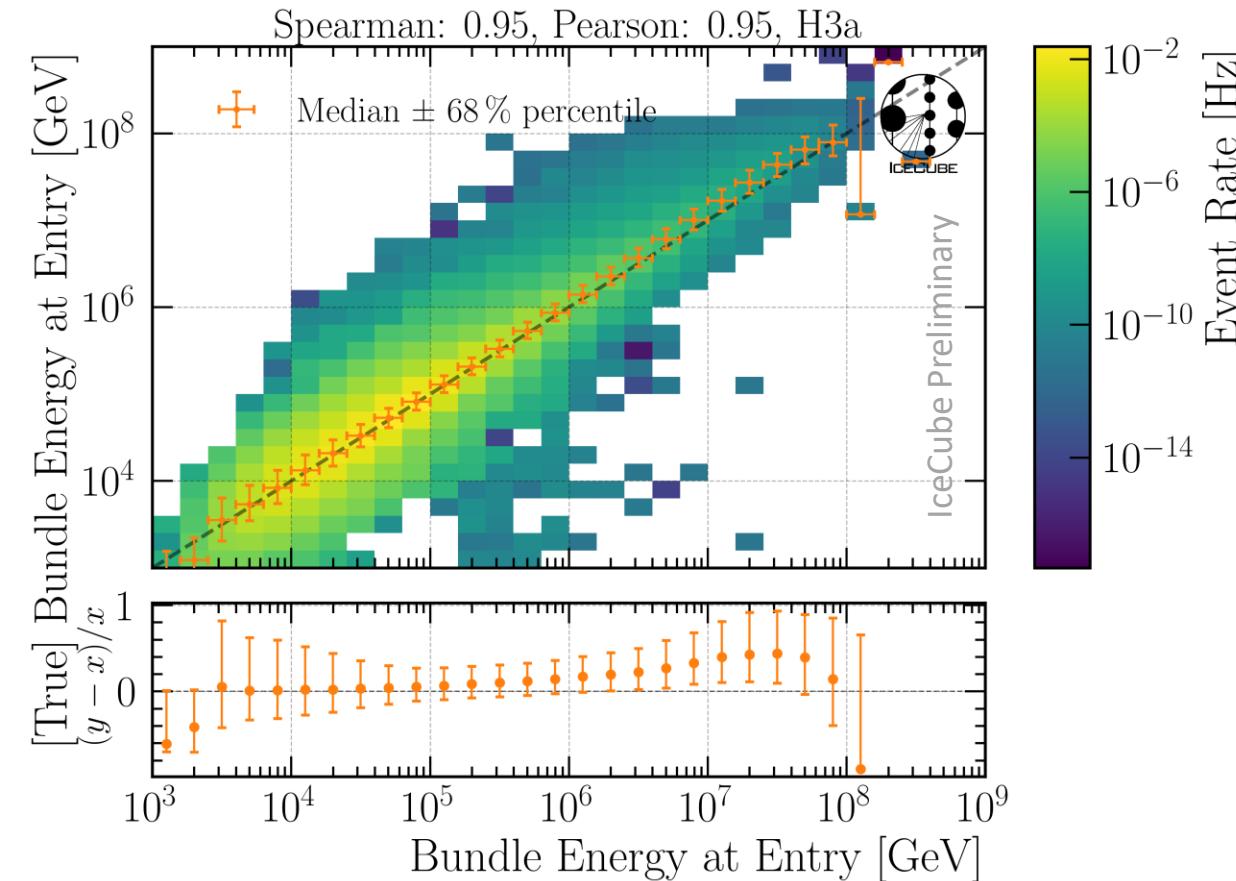
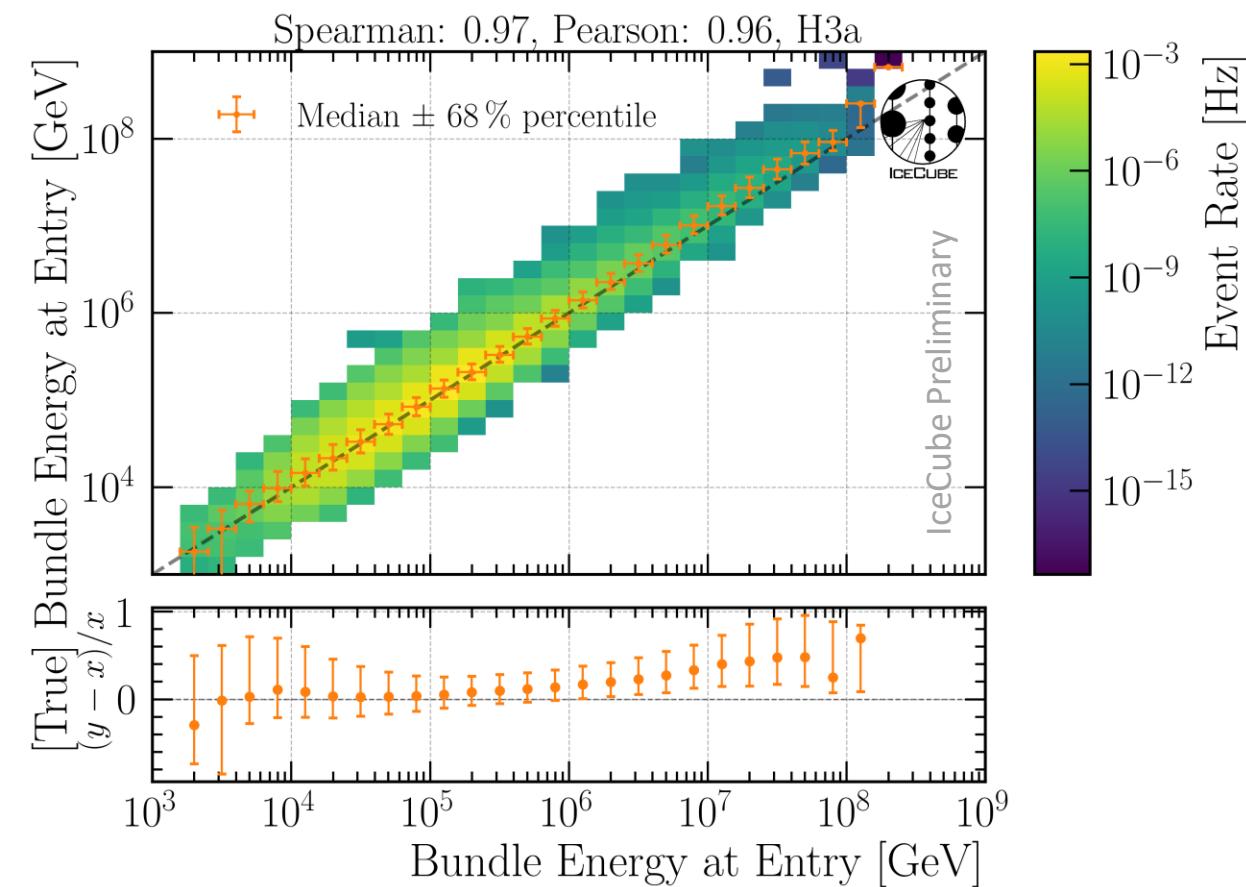


- Remove outliers
- Depth—dependent slope (no analysis relevance)
- CR—model impact on energy reconstruction
- 23 quality cuts in total

Level 5: Data/MC Quality Cuts



Bundle Energy Reconstruction

Level 4**Level 5**

Muon Filter

MuonFilter The I3MuonFilter_13 selects events based on reconstructed track quality and charge brightness, using criteria that depend on the reconstructed zenith angle. It requires three inputs: a cleaned pulse series map, a reconstructed track, and the log-likelihood fit parameters associated with the track. From the pulse series map, the number of hit DOMs N_{ch} and the total charge Q_{tot} , defined as the sum of the pulse charges over all DOMs, is determined. Then, the logarithmic charge $\ell = \log_{10}(Q_{\text{tot}})$ is calculated. The cosine of the reconstructed zenith angle is computed as $\cos(\theta)$, and the per-DOM log-likelihood value is retrieved from the fit parameters.

Events are classified into three angular zones based on the value of $\cos(\theta)$:

- Zone 1: $-1.0 < \cos \theta \leq 0.2$
- Zone 2: $0.2 < \cos \theta \leq 0.5$
- Zone 3: $0.5 < \cos \theta \leq 1.0$

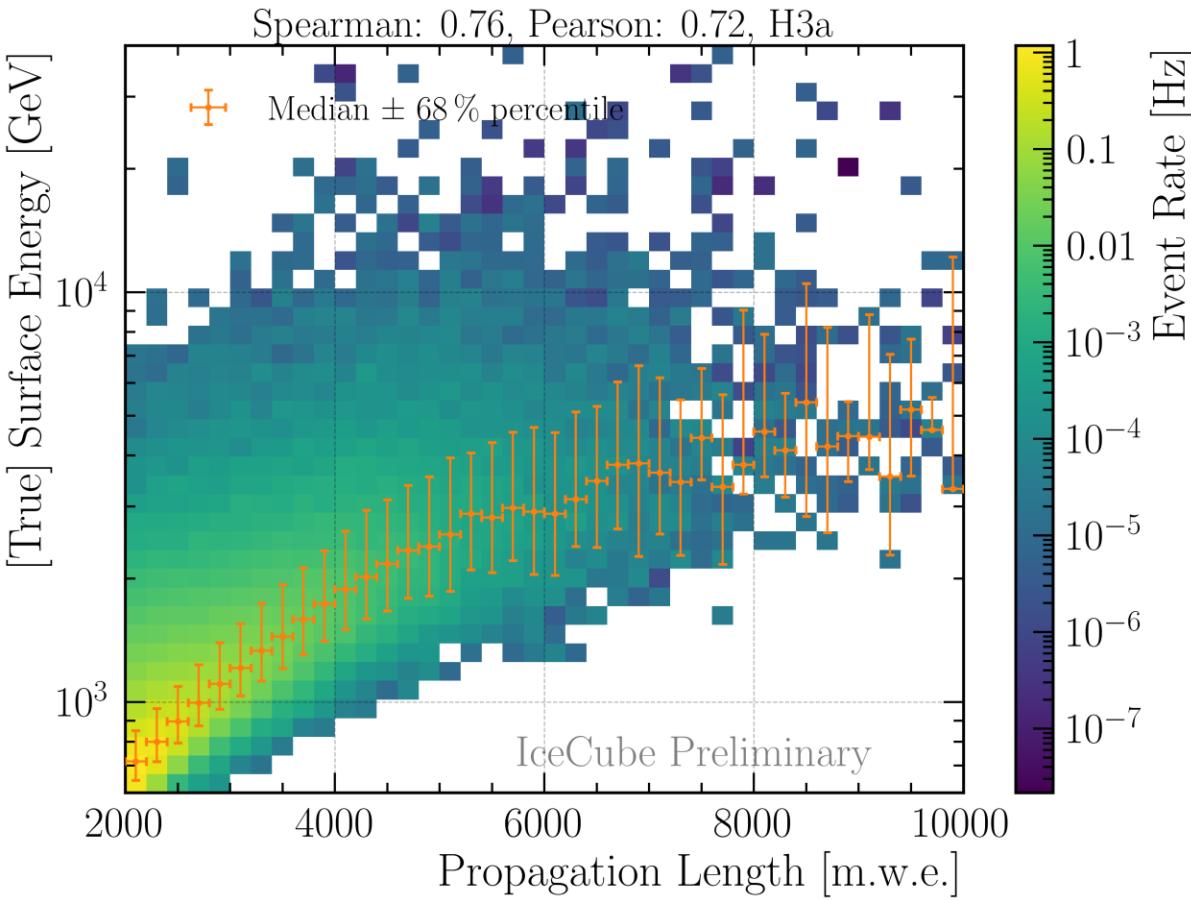
Each zone applies a different selection criterion:

- Zone 1: the filter computes a scaled log-likelihood value $\tilde{\lambda} = \text{rlogl} \cdot \frac{N_{\text{ch}} - 5}{N_{\text{ch}} - 3}$, and accepts the event if $\tilde{\lambda} \leq 8.7$.
- Zone 2: the filter applies a brightness-based cut and accepts the event if $\ell > 3.9 \cdot \cos \theta + 0.65$.
- Zone 3: a similar brightness cut is used with a shallower slope $\ell > 0.6 \cdot \cos \theta + 2.3$.

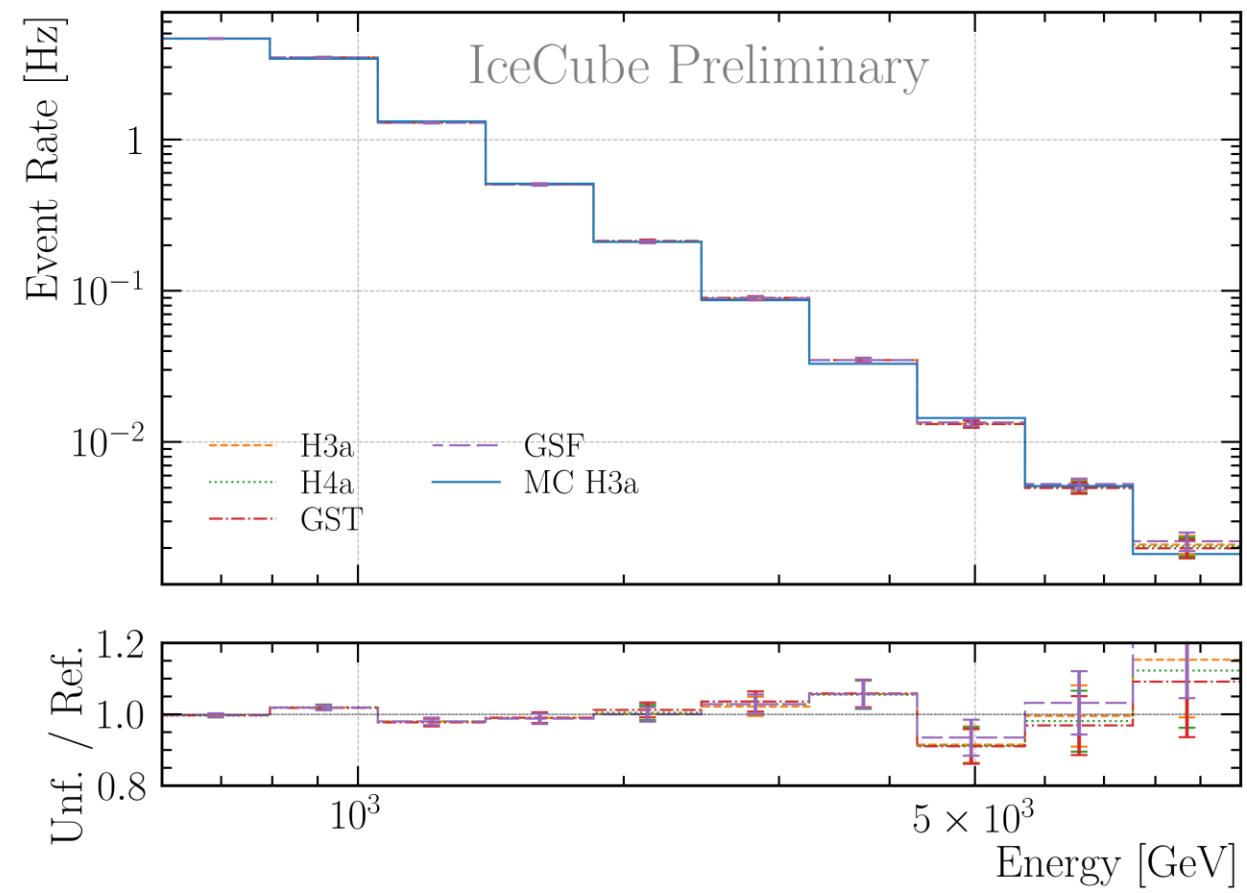
The event is accepted if it passes the selection criteria for any of the three zones. This design ensures that events are selected based on fit quality in the near-horizontal region and on brightness in the vertical direction, balancing background suppression with high signal efficiency across the full zenith range.

Correlation and Robustness Test: Stopping Muons

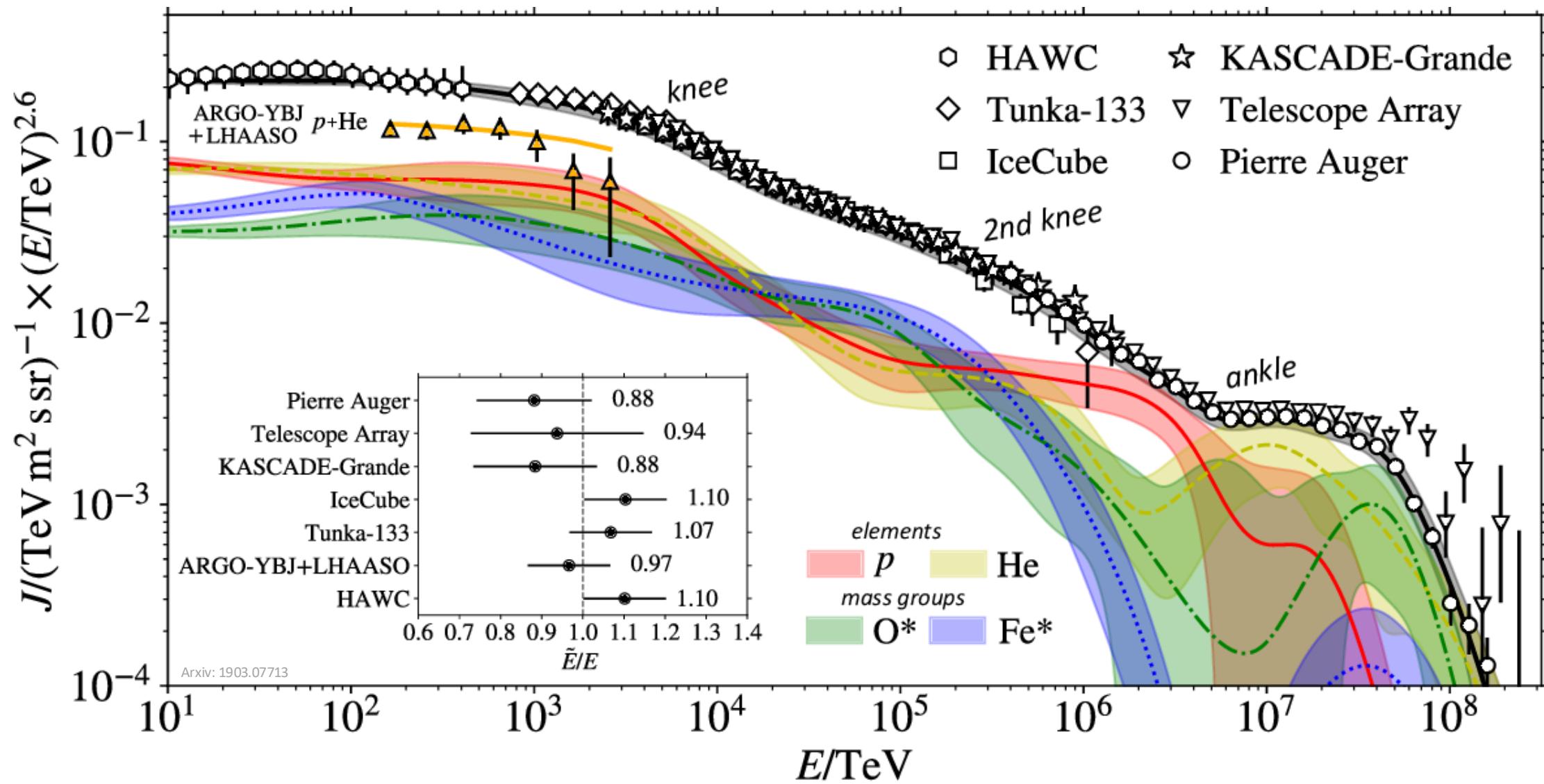
- Correlation between proxy and target



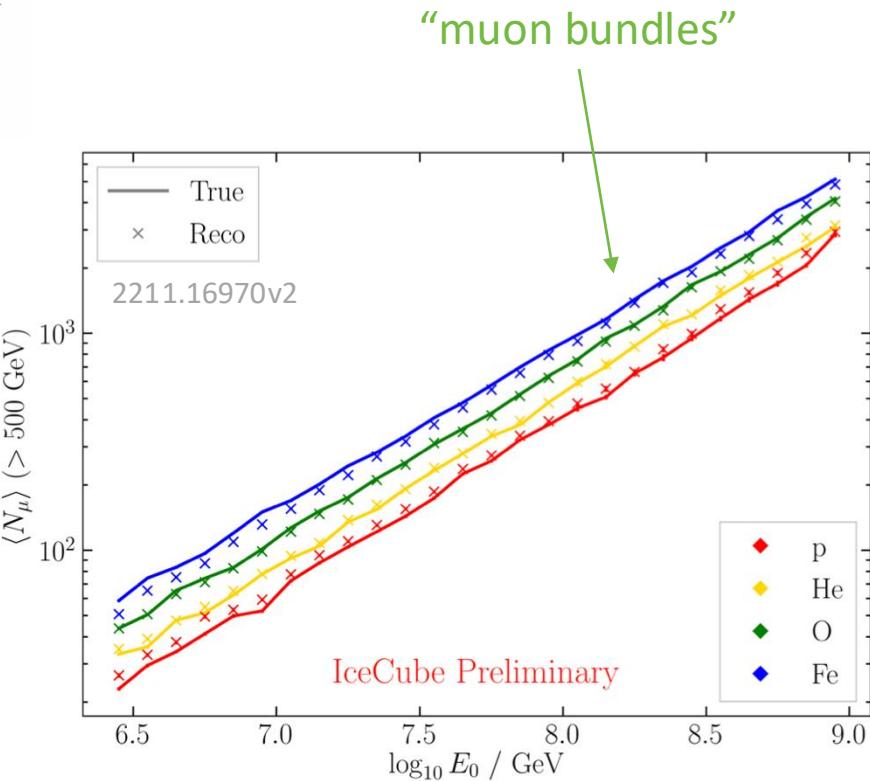
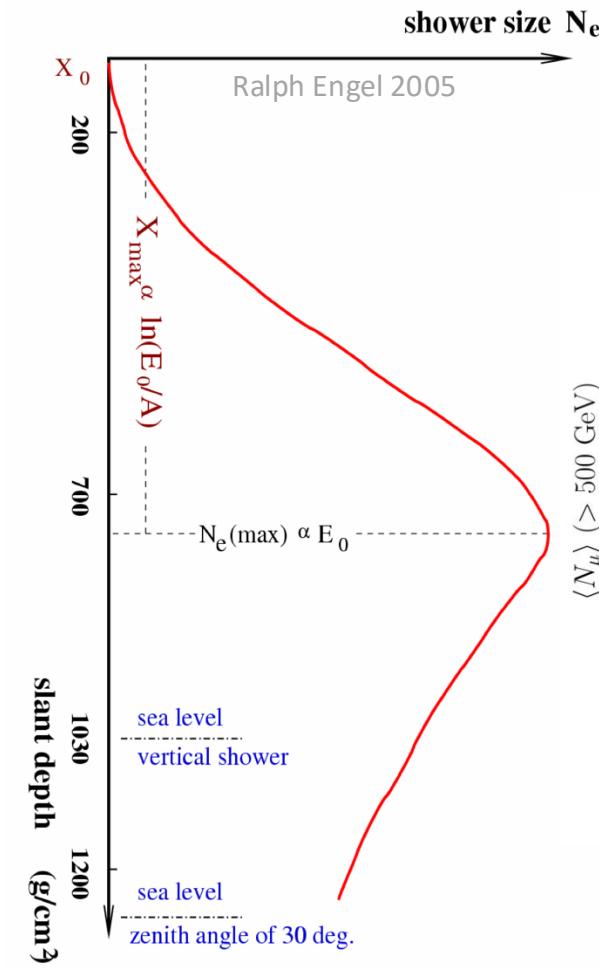
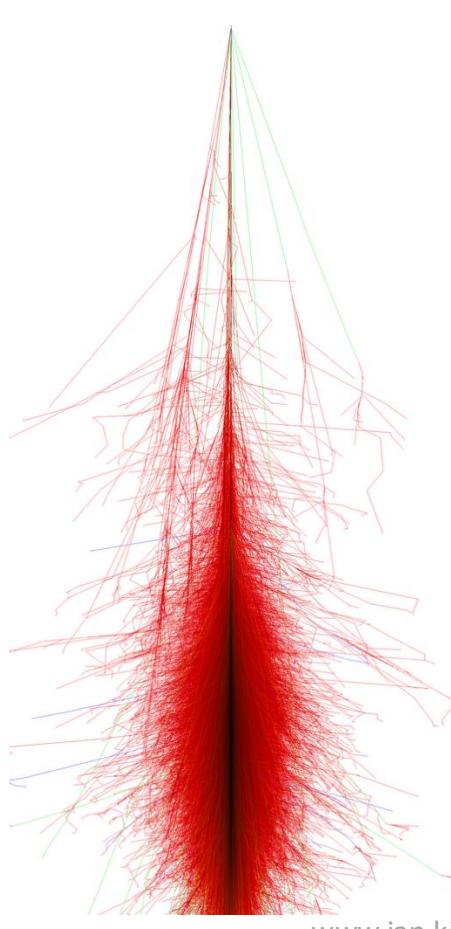
- Build unfolding matrix on H3a, H4a, GST & GSF
- Unfold H3a as test set
- Results are within uncertainties → robust



Cosmic ray flux

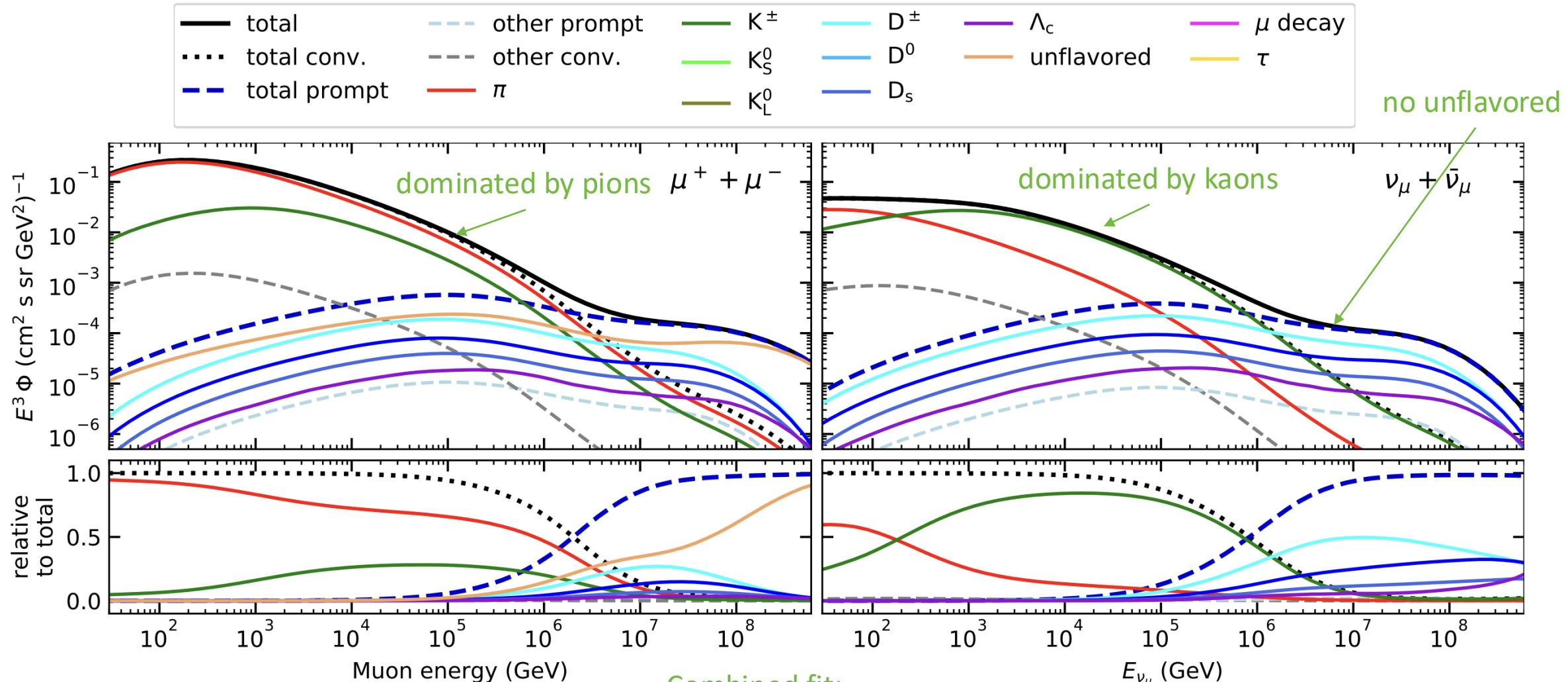


Air shower – 10 TeV



Prompt atmospheric muons and neutrinos

10.1103/PhysRevD.100.103018

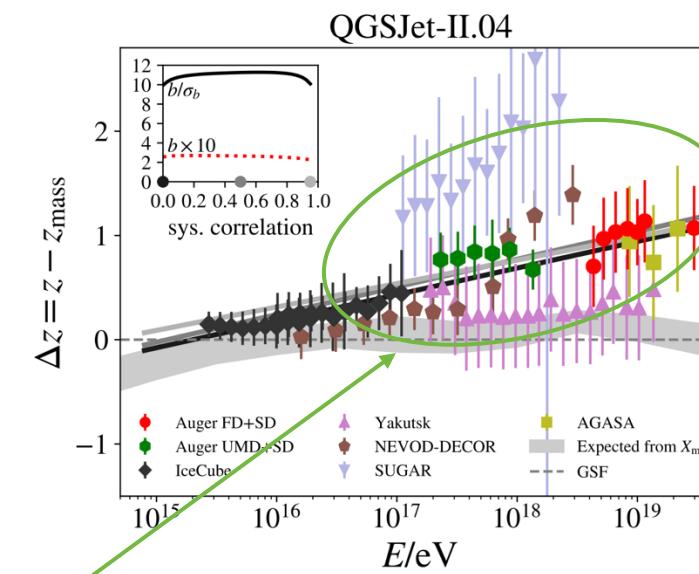
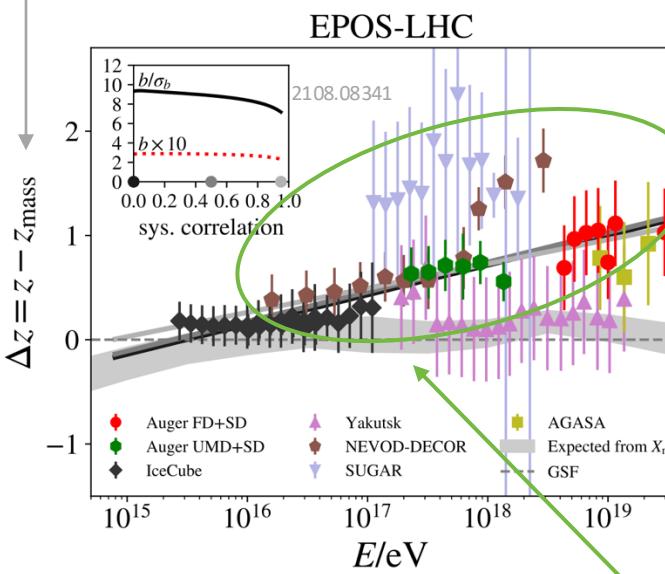


Muon puzzle and model uncertainties

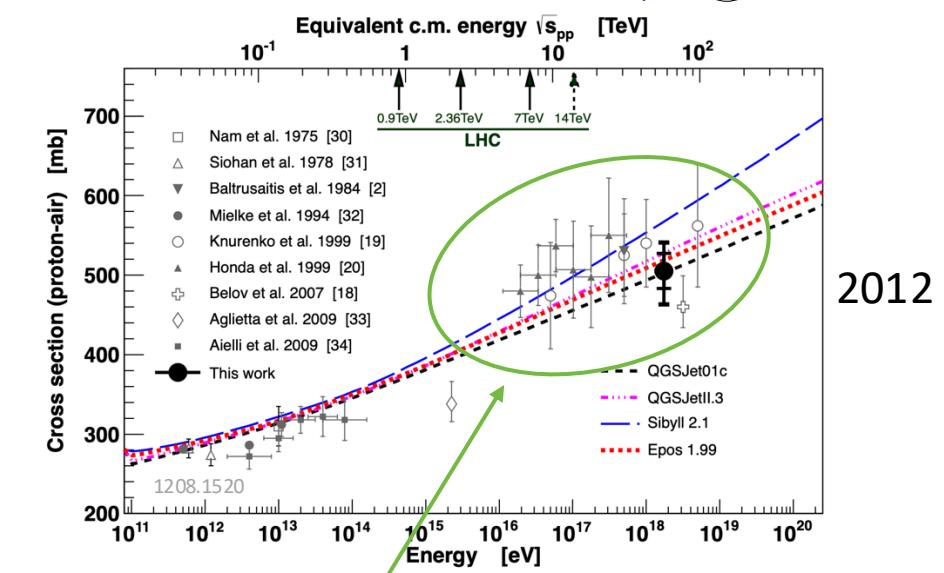
"muon number"

$$z = \frac{\ln\langle N_\mu \rangle - \ln\langle N_\mu \rangle_p}{\ln\langle N_\mu \rangle_{\text{Fe}} - \ln\langle N_\mu \rangle_p}$$

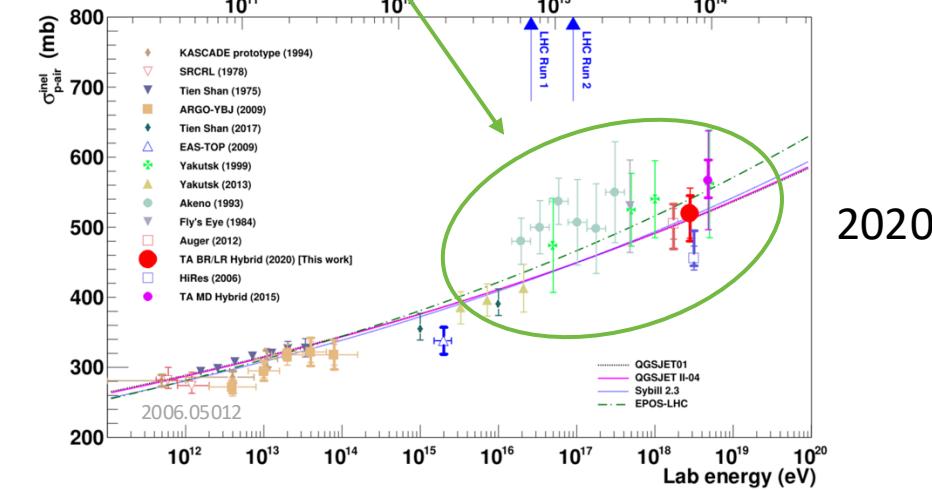
Expected z
("muon number")



➤ More muons measured than simulated for $E > 40 \text{ PeV} \sim \text{ cms } 8 \text{ TeV}$

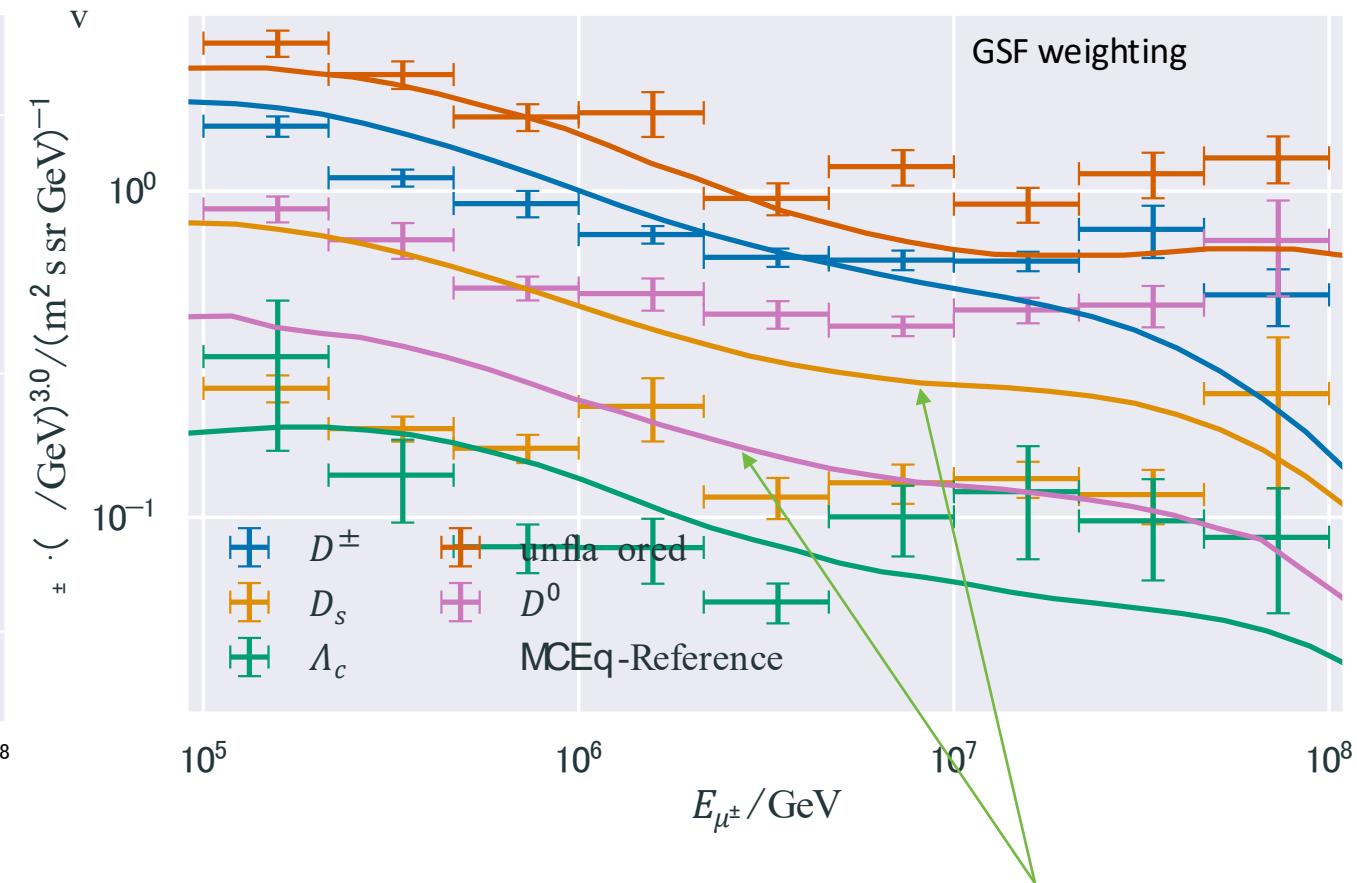
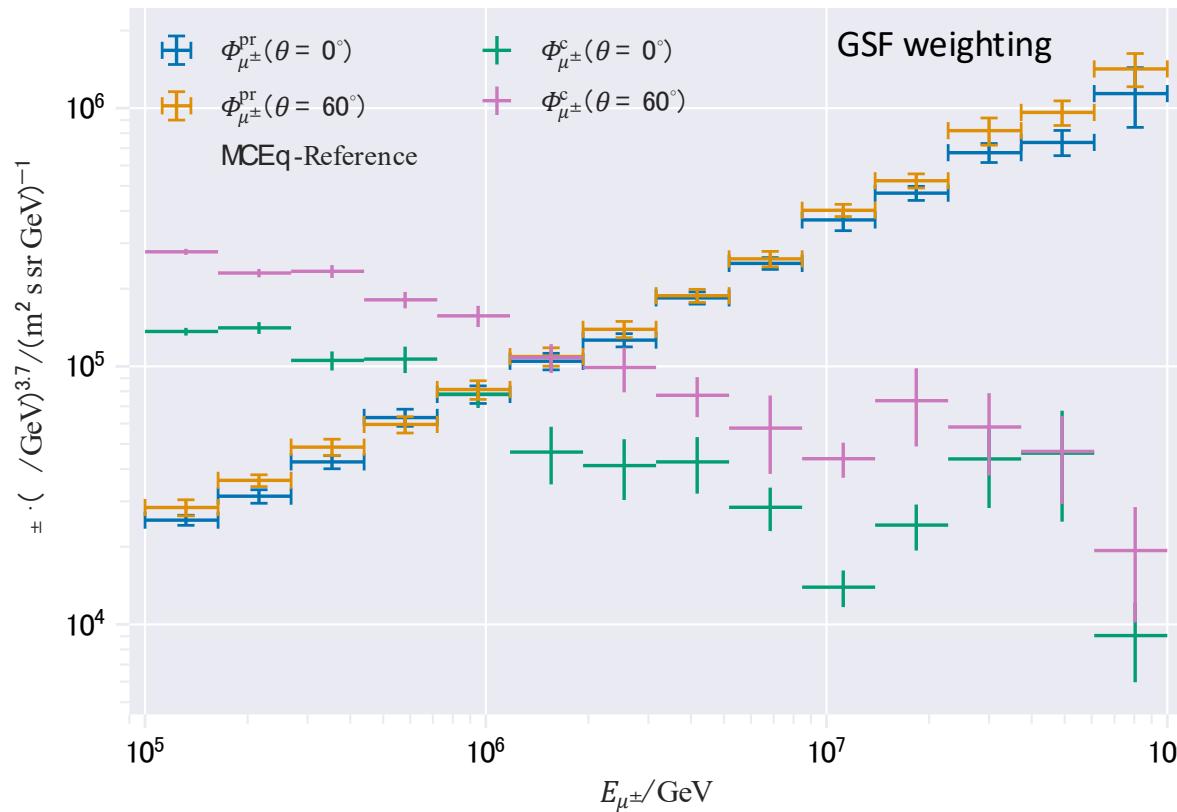


➤ Uncertainties at $E > 10 \text{ PeV}$



CORSIKA 7 tagging and MCEq comparison

MCEq: tool to numerically solve the cascade equations that describes the evolution of particle densities as they propagate through a gaseous, dense medium
<https://github.com/mceq-project/MCEq>

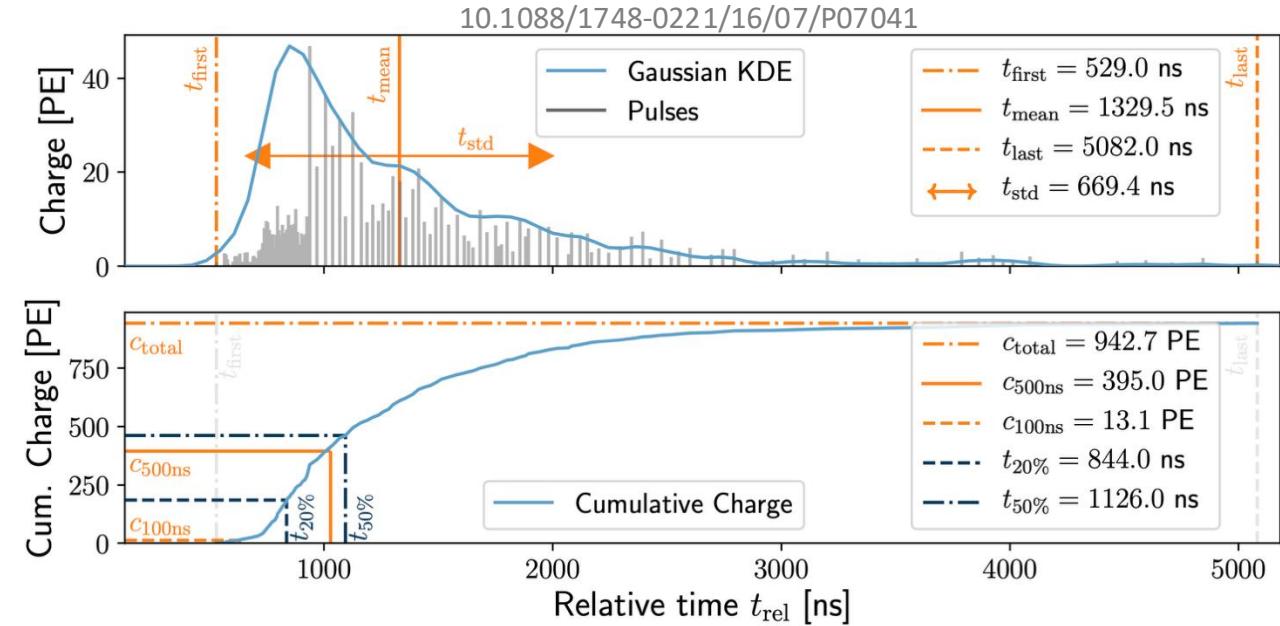
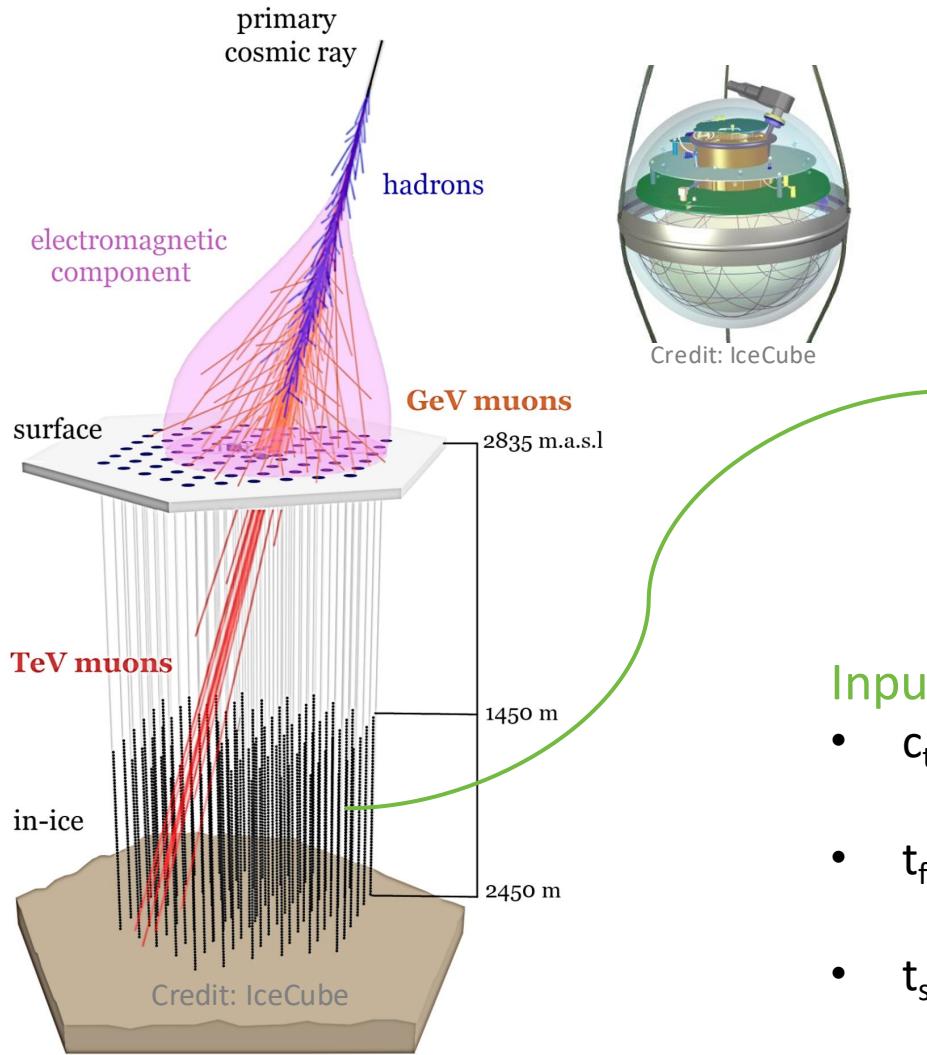


➤ Good agreement in total prompt and conv muon flux

mention panama

➤ D^0 and D_s are swapped here but this is fixed in MCEq

Machine Learning Reconstructions



Convolutional Neural Network

Inputs

- c_{total} : Total charge
 - Sum of charge
- t_{first} : Relative time of first pulse
 - Relative to total time offset
- t_{std} : Standard deviation of first pulse
 - Charge weighted standard deviation of pulse times

Outputs

- Direction
- Stopping point
- Entry point
- Energy at entry/surface
- ...

Level5: quality cuts

containment cuts	>	<
length in detector	1000 m	2000 m
entry pos x, y	-750 m	750 m
entry pos z	-500 m	750 m
center pos x, y	-550 m	550 m
center pos z	-650 m	650 m

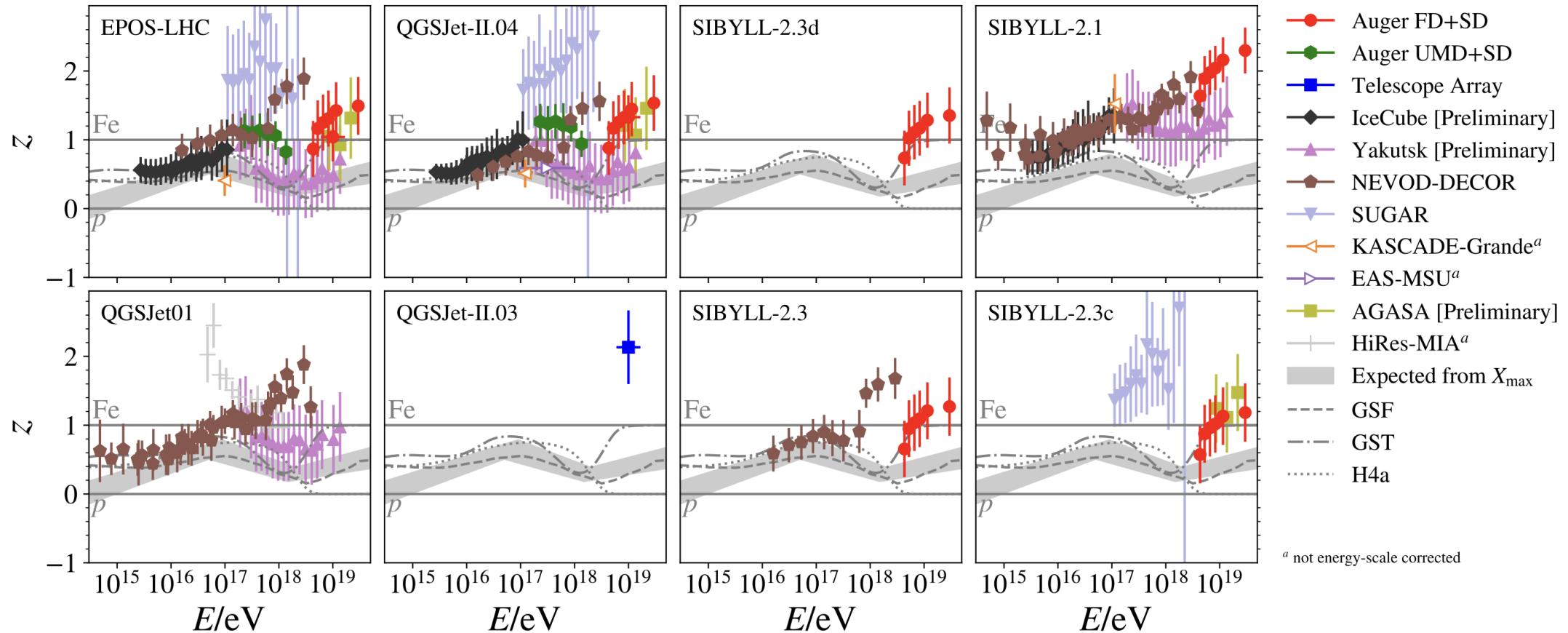
neutrino cuts	>	<
$\cos(\text{zenith})$	0.2	
length	5000 m	15000 m

uncertainty cuts	<
bundle energy at entry	$0.9 \log_{10}(\text{GeV})$
bundle energy at surface	$2.0 \log_{10}(\text{GeV})$
zenith	0.1 rad
azimuth	0.2 rad
entry pos x, y, z	42 m
center pos x, y, z	50 m
entry pos time	200 ns
center pos time	600 ns
length in detector	160 m
length	2000 m

The Muon Puzzle

"muon number"

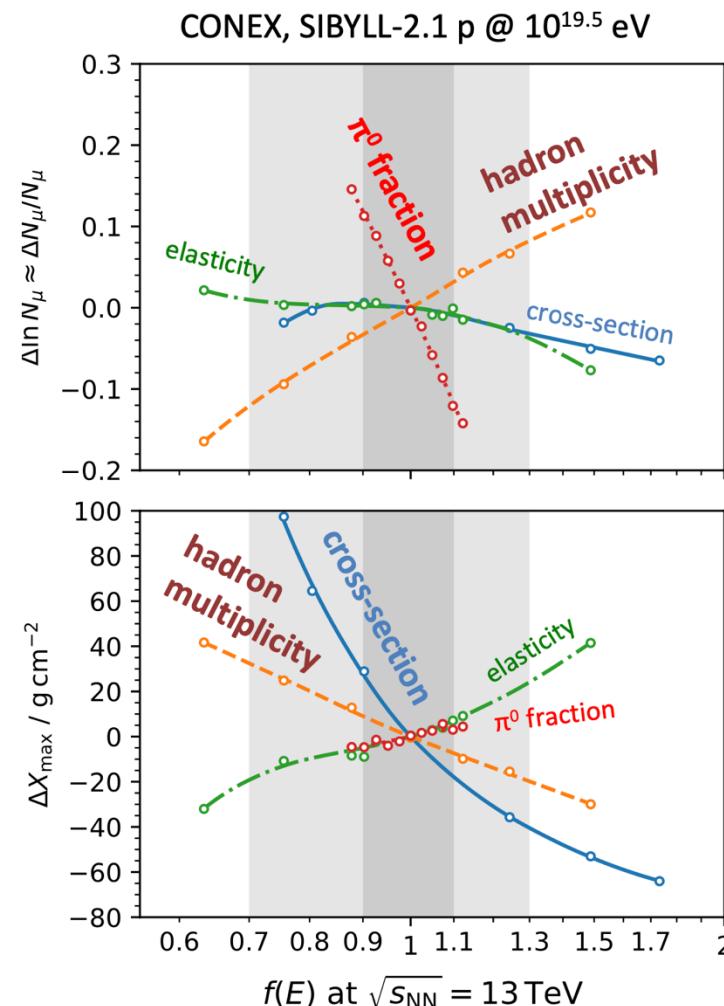
$$z = \frac{\ln\langle N_\mu \rangle - \ln\langle N_\mu \rangle_p}{\ln\langle N_\mu \rangle_{\text{Fe}} - \ln\langle N_\mu \rangle_p}$$



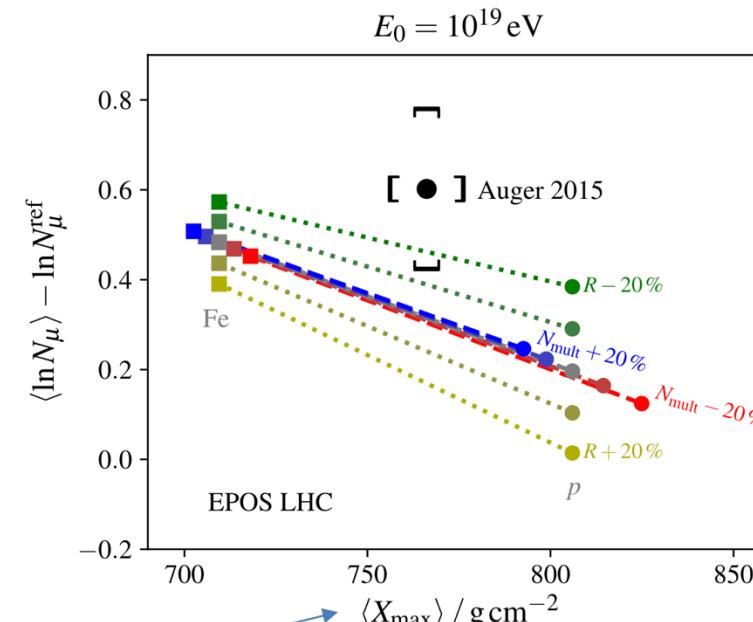
Arxiv: 2108.08341

Possible Solutions

R. Ulrich, R. Engel, M. Unger, PRD 83 (2011) 054026



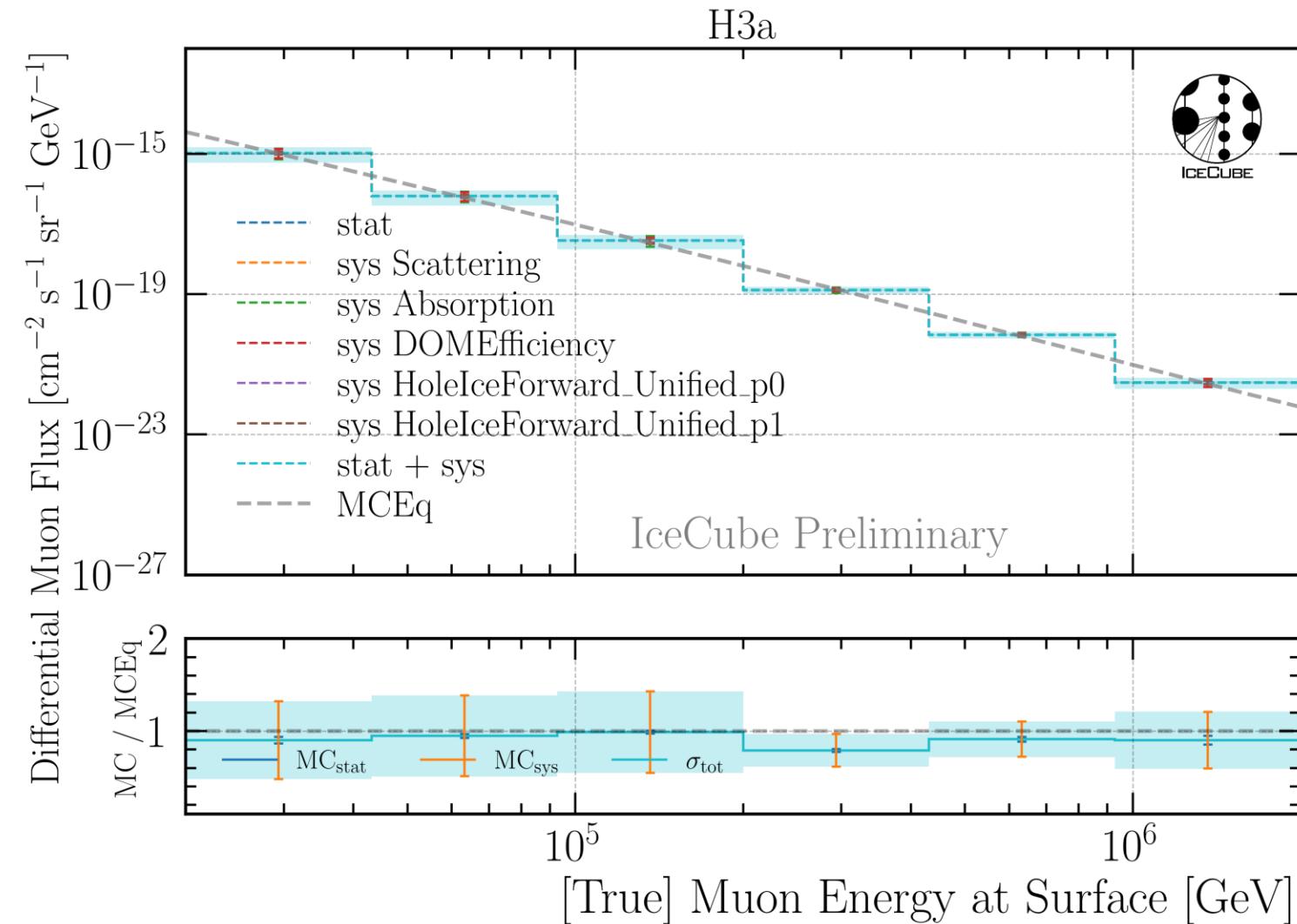
S. Baur, HD, M. Perlin, T. Pierog, R. Ulrich, K. Werner,
arXiv:1902.09265



$$R = \frac{E_{\pi^0}}{E_{\text{other hadrons}}}$$

- Only changes to R can solve muon puzzle
- Small changes have large effect,
 R needs to be known to about 5 %

MCEq vs CORSIKA



Overview

