

# 1 Philosophy

- Learning algorithms are to compute parameters while complexity analysis focuses on distinguishing different functions from some concept class.

## 2 Weak SQ Dimension

**Definition 2.1.** The (weak) SQ dimension of a class of real valued functions  $\mathcal{F}$  over some domain  $X$  under distribution  $\mathcal{D}$ , denoted  $\text{SQDim}_{\mathcal{F}}^{\mathcal{D}}$ , is the biggest  $d$  such that  $\mathcal{F}$  contains distinct  $f_1, \dots, f_d$  with pairwise correlations between  $-\frac{1}{d}$  and  $\frac{1}{d}$ . Note that correlation between  $f$  and  $g$  is defined by

$$\langle f, g \rangle \triangleq \mathbb{E}_{x \sim \mathcal{D}} f(x)g(x).$$

*Example 2.2.* When consider  $\mathcal{F}$  as set of vectors on  $S^{n-1}$ , inner product as standard inner product and  $\mathcal{D}$  as uniform distribution,  $\text{SQDim}$  is now polynomial; while  $\text{SQDim}$  is  $2^n$  for parity functions under uniform distribution.