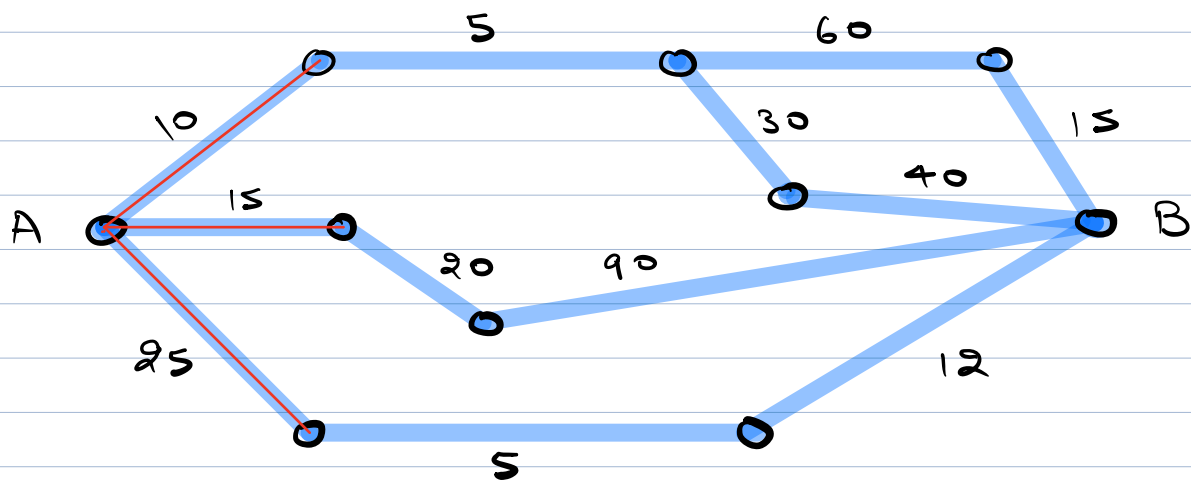


- 1) Greedy
- 2) When to apply greedy.
- 3) Problems.

	<u>⊗ (40L)</u>	⊗ (40L)	⊗ (41L)
Recruiter	⊗ (50L)	⊗ (56L)	⊗ (36L)
Google	⊗ (55L)	⊗ (67L)	⊗ (38L)
		<u>⊗ (35L)</u>	<u>⊗ (35L)</u>
	Jan	Feb	Mar

Goal: Reduce the overall annual hiring cost.

- 1) Best choice locally leads to best global solution
- 2) Current local choice will not affect any future decisions.



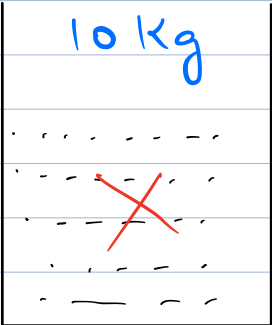
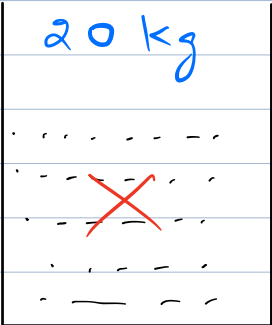
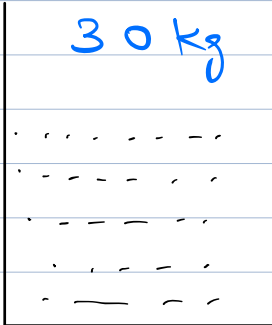
* If greedy fails, explore all possibilities (Recursion)

Fractional Knapsack

Given N items $\begin{cases} \text{Weight} \\ \text{Cost (value)} \end{cases}$

Given a bag with weight capacity W
Pick some items s.t. the value stored in the bags is maximised / minimised.

Super Market

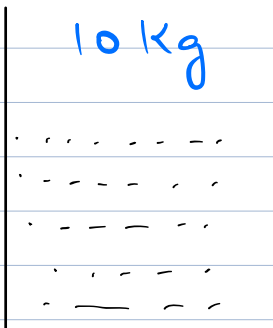
10 kg	20 kg	30 kg
		
Rice	Wheat	Pulse
60 \$	100 \$	120 \$
6 \$	5 \$	4 \$
	<div>20 kg Pulse 20 kg Wheat</div>	80 \$ 100 \$

$$\boxed{10 \text{ Kg}}$$

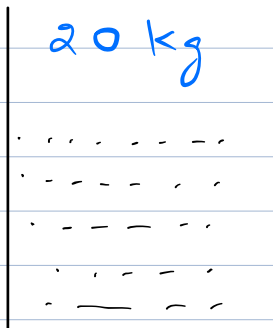
$$W = 50$$

$$\frac{60 \$}{240 \$}$$

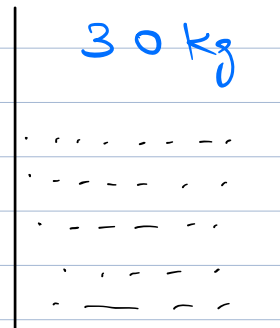
Const. : Either select all or select nothing



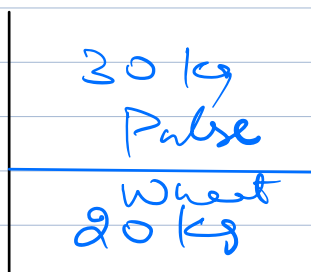
Rice
60 \$
6 \$



Wheat
100 \$
5 \$



Pulse
120 \$
4 \$



$W = 50$

220 \$

0/1 Knapsack \Rightarrow DP

Steps:

- 1) Sort all the items on the basis of per unit cost

2) Iterate, pick the best & keep updating the seg capacity.

$$\begin{aligned} T.C. &= O(N \log N + N) \\ &= O(N \log N) \end{aligned}$$

Q Aniruddha (CEO) (famous)
BMW approaches Aniruddha
Special sale.

N cars.

$A \Rightarrow A[i] =$ Time till which i^{th} car is free of cost (sale is active)

$B \Rightarrow B[i] =$ Beauty of i^{th} car.

\Rightarrow Maximize the overall beauty value of the cars purchased.

\Rightarrow It takes 1 unit of time to purchase 1 car.

	0	1	2	3	4
$A \Rightarrow$	<u>3</u>	1	<u>3</u>	2	<u>3</u>
$B \Rightarrow$	<u>6</u>	5	<u>3</u>	1	<u>9</u>
	X	X	X	X	X

$T = 0$
 $T = 1$
 $T = 2$
 $T = 2$

9
 6
 3
18

5
 6
 9
20 Ans

2) Sort the cars on the basis of the sale end time

A: 1, 5, 5, 5, 3, 3, 3
 B: 5, 4, 3, 8, 20, 7, 10

A: 1, 3, 3, 3, 5, 5, 5
 B: 5, 20, 7, 10, 4, 3, 8, ↑

$T = 0$
 $T = 1$
 $T = 2$
 $T = 3$
 $T = 4$
 $T = 5$

~~0 (5)~~ 3 (10)
 1 (20)
 2 (7)
 4 (4)
~~5 (3)~~ 6 (8)

min Beauty
 ↓
 Min Heap

Code

1) Sort the cars (H.W.)

```

int t = 0;
min Heap m;
  
```

total Beauty = 0;

for (i = 0; i < N; i++) {

if (t < A[i]) {

m.insert(B[i]);
total Beauty += B[i];
t++;

}

else {

if (B[i] > m.peek()) {

total Beauty -=
m.deleteMin();
m.insert(B[i]);
total Beauty += B[i];

}

}

}

T.C. = $O(N \log N + N \log N)$

= $O(N \log N)$

S.C. = $O(\underline{N})$