



~~x~~ 10

Degree of connection of
u wrt. v.

$\gamma \gg f_s$

2) BFS → ✓✓

BFS \Rightarrow Reach dest via shortest possible path

Breadth First Search

DS: Duene

7) Add source to queue & mark as visited.

2) While (! queue.is Empty) {

1) Dequeue the first element.

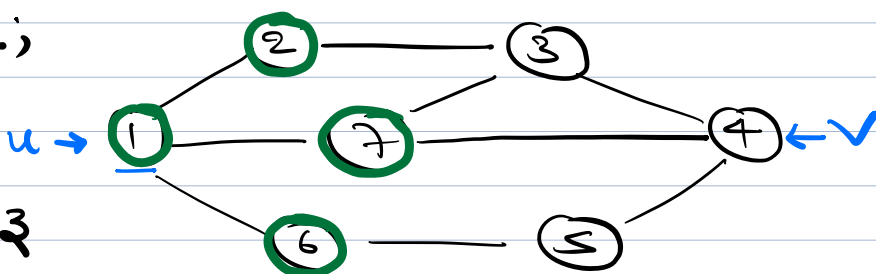
2) Enqueue all unvisited neighbours of this element & also mark them as visited.

$N \rightarrow [1 \text{ to } N]$

visited boolean array of size $N+1$.

Q Given an undirected / unweighted graph & 2 nodes u & v , find the shortest distance b/w u & v .

$d = 1;$



size = 3

1	T
2	T
3	T
4	F
5	F
6	T
7	T

1	2	3		
X	X	X	6	3

Code

(9:45)

bool visited[N+1] = {false};

bfs (source, dest) {

✓ q ⇒ queue

✓ q.push(source);

✓ visited[source] = True;

— int distance = 0;

✓ while (!q.isEmpty()) {

✓ int size = q.size();

✓ for (i = 0; i < size; i++) {

✓ v = q.dequeue();

Adjacency
list of v
↑

✓ for (all ^{unvisited} u connected to v) {

— if (u == dest) {

— return (distance + 1);

— }

✓ visited[u] = True;

✓ q.enqueue(u);

}

}

— distance++;

}

}

V & E

$$T.C. = O(V + E)$$

Depth first Search

→ Select one neighbour. & explore that completely & then go to the next neighbour.

Code

```
bool visited [N+1] = {false};
```

```
dfs ( source ) {
```

```
    visited [source] = True;
```

```
    for ( all u connected to source ) {
```

```
        if ( visited [u] == false ) {
```

```
            dfs (u);
```

```
        }
```

```
    }
```

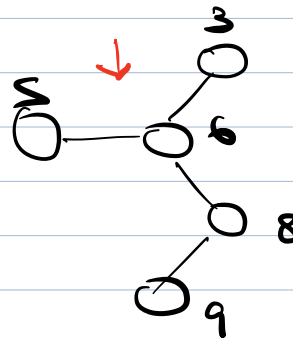
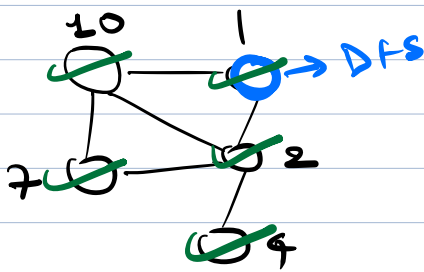
```
    // logic
```

```
}
```

$$T.C. = O(V+E)$$

Q If BFS or DFS is called on any one node of the graph. Is it guaranteed all the nodes will be visited.

NO

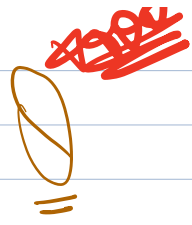


Call BFS/DFS for all unvisited in a loop

visited[N+1] = false

```
for (i = 1; i <= N; i++) {
    if (visited[i] == false) {
        bfs(i);
    }
}
```

Looping over all nodes



Count the total no. of connected component in a graph.

count = 0;

for (all nodes u) {

if (visited[u] == false) {

count ++;

↳ bfs / dfs(u);

}

}



Given a $N \times N$ chessboard.

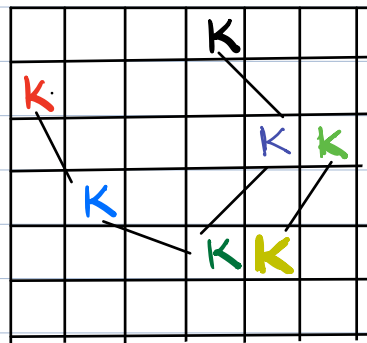
K Knights placed on the chessboard.

Swap 2 Knights if they are reachable from each other.

Find the total no. of ways to arrange these knights.

1

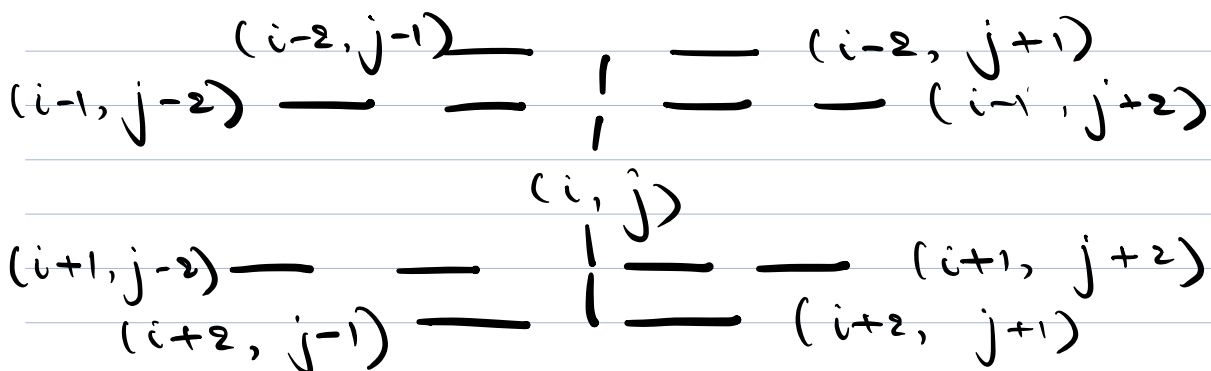
$$\frac{(2!)}{2!} = 1$$



$$5! \times 2!$$

Horse
side
 \downarrow
 $(5!)$
61

$$8 \times 8$$



Solⁿ

ans = 1

Iterate over all connected components: d

Find count

ans = ans \times (count!)

}

H.W. \Rightarrow Code



Given a 2D matrix. (city)

Cell \Rightarrow Residence (R)

Cell \Rightarrow Hospital (H)

For every residence, find the min distance from a hospital.

	0	1	2	2					
0	R	R	R	I		3	2	1	0
1	R	R	I	I	⇒	2	1	0	0
2	R	I	I	R		1	0	0	1
	N x M					N x M			

$O(N \times M)$ residences.

Solⁿ 1) Call BFS from every residence.

$$\begin{aligned} \text{T.C.} &= O(N \times M) \times O(N \times M) \\ &= O(N^2 M^2) \end{aligned}$$

	0	1	2	2
0	R₁	R₂	R₃	H₁
1	R₄	R₅	H ₂	H ₃
2	R₆	H₄	H₅	R₇

$N \times M$

3	2	1	0
2	1	0	0
1	0	0	1

~~$\langle H_1, 0 \rangle$~~ | ~~$\langle H_2, 0 \rangle$~~ | ~~$\langle H_3, 0 \rangle$~~ | ~~$\langle H_4, 0 \rangle$~~ | ~~$\langle H_5, 0 \rangle$~~
 ~~$\langle R_3, 1 \rangle$~~ , ~~$\langle R_5, 1 \rangle$~~ , ~~$\langle R_7, 1 \rangle$~~ , ~~$\langle R_6, 1 \rangle$~~
 ~~$\langle R_2, 2 \rangle$~~ , ~~$\langle R_4, 2 \rangle$~~ , ~~$\langle R_1, 3 \rangle$~~

$\langle H_1, 0 \rangle \rightarrow \langle R_3, 1 \rangle$

$\langle H_2, 0 \rangle \rightarrow \langle R_5, 1 \rangle$

$\langle H_3, 0 \rangle \rightarrow \langle R_7, 1 \rangle$

$\langle H_4, 0 \rangle \rightarrow \langle R_6, 1 \rangle$

$\langle H_5, 0 \rangle \rightarrow$ No unvisited neighbour

$\langle R_3, 1 \rangle \rightarrow \langle R_2, 2 \rangle$

$\langle R_3, 1 \rangle \rightarrow \langle R_4, 2 \rangle$

$\langle R_7, 1 \rangle$ No unvisited neighbour

$\langle R_6, 1 \rangle$ No unvisited neighbour

$\langle R_2, 2 \rangle \rightarrow \langle R_1, 3 \rangle$

T.C. = $O(N \times M)$

→ Multi Sourced BFS

Code