

D <sup>Addose</sup>

There are  $N$  doors (1 to  $N$ )

In front of each door, one person is standing  
Initially all the doors are closed

1<sup>st</sup> person  $\rightarrow$  1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> ..... N<sup>th</sup> door

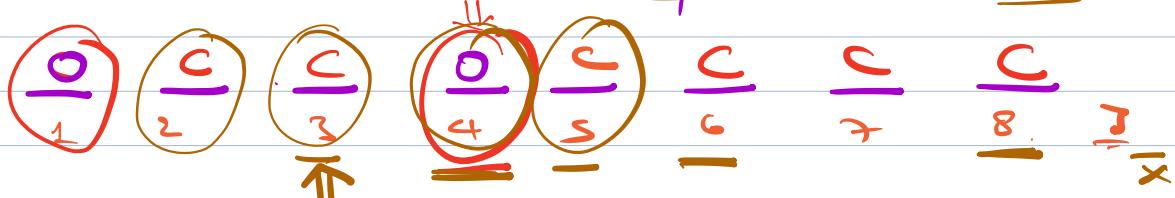
2<sup>nd</sup> person  $\rightarrow$  2<sup>nd</sup>, 4<sup>th</sup>, 6<sup>th</sup>, 8<sup>th</sup> ..... (Toggle)

3<sup>rd</sup> person  $\rightarrow$  3<sup>rd</sup>, 6<sup>th</sup>, 9<sup>th</sup>, 12<sup>th</sup> .....

4<sup>th</sup> person  $\rightarrow$  4<sup>th</sup>, 8<sup>th</sup>, 12<sup>th</sup>, 16<sup>th</sup> .....

⋮  
N<sup>th</sup> person

Return which doors are open at the end.



1	5
2	6
3	7
4	



Initially everything is closed.

for any door  $i$ , if we toggle the door

odd times  $\Rightarrow$  **Open**

Even times  $\Rightarrow$  **Closed.**

$$\underline{9} \Rightarrow \downarrow \frac{1}{i}, \frac{3}{i}, \frac{9}{N/i} \quad (\text{factors of } 9)$$

$\Rightarrow$  for every  $i$ , only the factors of  $i$  can toggle the  $i^{\text{th}}$  door.

If a no. has

odd factors  $\Rightarrow$  OPEN

even factors  $\Rightarrow$  CLOSED

$$N \Rightarrow \text{for } (1 \text{ to } N) \Rightarrow O(N)$$

factors always occurs in pair

$\Rightarrow$   $\underline{i}$  is a factor of  $N$

Except for a  
perfect square

$\Rightarrow$   $\underline{N/i}$  is also a factor.

$$\sim i \in \underline{N/i} \Rightarrow \text{for } (i = 1 \text{ to } \underline{\sqrt{N}})$$

$$\textcircled{9} \Rightarrow \begin{array}{c} 3 \\ | \\ 3 \end{array}$$

Count  $\underline{\underline{+=2}}$  ??

$i \leq n/c$

(Count ++)

2

$$\textcircled{8} \Rightarrow \underline{\underline{=4}}$$

$$\textcircled{8} = \frac{8}{4} = 2$$

$\Rightarrow$  Only perfect squares have odd factors.



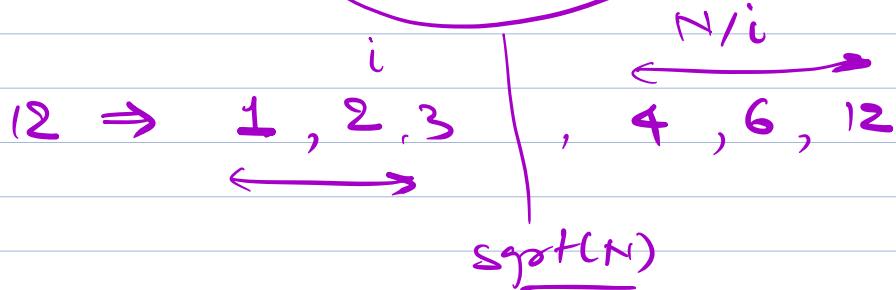
Doors whose index is a perfect square will be open at the end.

Count the no.

of perfect squares (Revise session  $\underline{\underline{1}}$ )

T.C. =

$$\mathcal{O}(\underline{\underline{n \log N}}) \Rightarrow \sqrt{N}$$



$$9 \rightarrow 1, \textcircled{3}, \textcircled{3}, 9$$

$$1 - N \Rightarrow N = \underline{\underline{100}}$$

$\text{sqrt}(N)$

$$\text{sqrt}(100) = 10$$

$$\forall i > 10, \quad i^2 > 100(N)$$

$$\begin{array}{c} 1 - 100 \\ \hline 1 - 10 \end{array}$$

$$1^2 = 1 \quad [1, N]$$

$$2^2 = 4$$

$$3^2 = 9$$

$$4^2 = 16$$

⋮

$$9^2 = 81$$

$$10^2 = \underline{\underline{100}}$$

Iterate from  $(1 \text{ to } \text{sqrt}(N))$   
point  $(i^2)$ ,

5

T.C. =  $\text{sqrt}(N)$

$$11^2 = \underline{\underline{121}} \times$$

$[1, 2]$

$$\underline{\underline{N=8}}$$

$$\Rightarrow \text{sqrt}(8) = \underline{\underline{2}}$$

$$\begin{array}{c} 1^2, 2^2 \\ \downarrow \downarrow \\ 1 \quad 4 \end{array}$$

$$1 \rightarrow \underline{\underline{N}}$$

Amrit

N

Given a no. N.

Return the N<sup>th</sup> magical no.

Magic No  $\Rightarrow$

A no. that can be expressed  
as a sum of unique powers  
of 5.

$$\underline{\underline{1}} \quad \underline{\underline{N=1}}$$

$$S^1$$

$$\underline{\underline{N=1}}$$

$$\underline{\underline{1, 2, 3, 4, S, 6, 7, 8, 9, 10}} \Leftrightarrow$$

$$S^1 + S^0$$

$$\underline{\underline{2}} \quad \underline{\underline{N=2}}$$

$$S^2$$

$$2S$$

$$\underline{\underline{3}} \quad \underline{\underline{N=3}} \Rightarrow S^1 + S^2 \Rightarrow 3S$$

$$\underline{\underline{4}} \quad \underline{\underline{N=4}} \Rightarrow S^3 = 12S$$

$$S \quad \underline{\underline{N=S}} \Rightarrow S^3 + S^2 + S^1 \Rightarrow \underline{\underline{13S}}$$

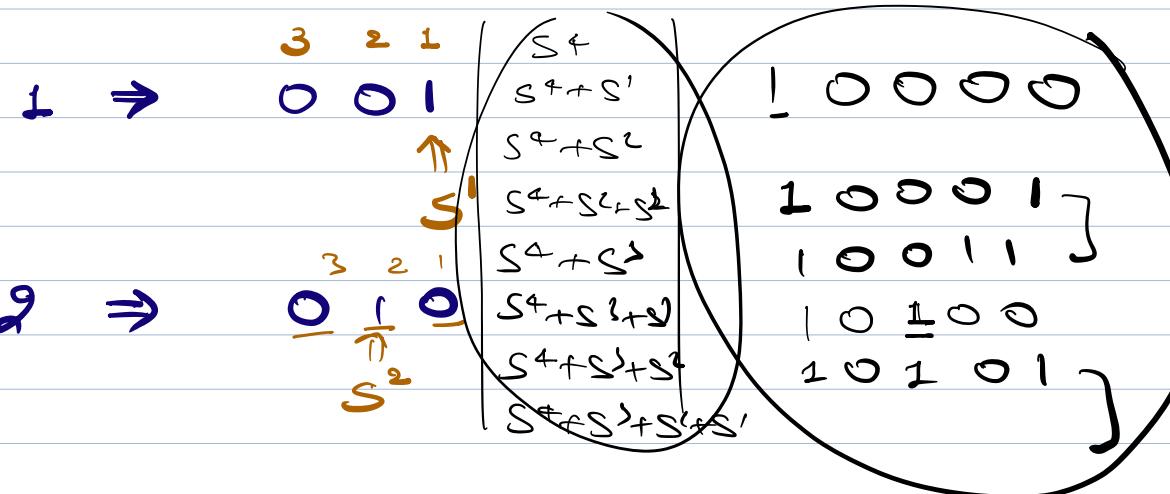
$$N=6 \Rightarrow S^3 + S^2 = 150$$

$$\underline{\underline{7}} \quad \underline{\underline{N=7}} \Rightarrow S^3 + S^2 + S^1 = 155$$

$$N=8 \Rightarrow S^4 =$$

$$10 = \text{ } \left( \text{ } S^{\frac{1}{2}} \text{ } \right) + \text{ } \left( \text{ } S^{\frac{1}{2}} \text{ } \right) \times$$

<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>
$S^1$	$S^2$	$S^3$	$S^4$	$S^5$	$S^6$	$S^7$
$2S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$
$3S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$
$4S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$
$5S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$
$6S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$
$7S$	$S^2 + S^1$	$S^3 + S^2$	$S^4 + S^3 + S^2$	$S^5 + S^4 + S^3 + S^2$	$S^6 + S^5 + S^4 + S^3 + S^2$	$S^7 + S^6 + S^5 + S^4 + S^3 + S^2 + S^1$



$N = 11^{th}$  magical no.

1) Convert to Sinary

$11 \Rightarrow 1011$  (Array)

Code

int generateMagicalNo. (N) {

ans = 0;

power = 1;

$\Rightarrow$  while ( $N \geq 0$ ) { (almost 32 times)

if ( $(N \& 1) == 1$ ) {

ans = ans + S<sup>power</sup>

}

power ++;

$N = N \gg 1$ ;

$N = N/2$

$i = i + 1$   
 $a = a + 1$

$\Rightarrow power$

}

{

T.C. = Constant Time ( $\log N$ )

INT N  $\Rightarrow$  (32)

$\underline{\underline{N \& 1}}$

$N \Rightarrow$

$\underline{\underline{01}}$  0

00000  
↑  
CCCCC

$\underline{\underline{N = 11}}$

66↓↓  
001011  
↓ S<sup>4</sup> S<sup>3</sup> S<sup>2</sup> S<sup>1</sup>

$$\text{Ans} = S + S^1 + S^2 + S^4$$

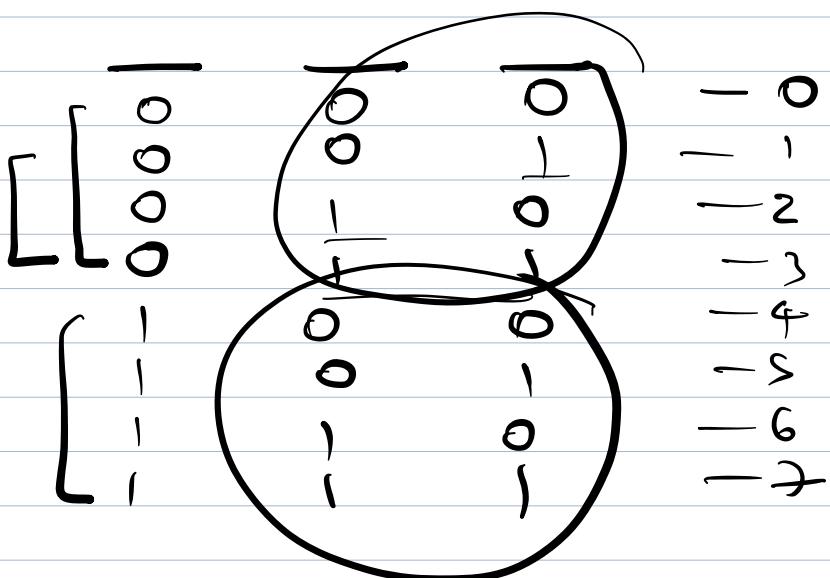
power =  $\lceil \log_2 \text{Ans} \rceil$

$$\begin{array}{r} 001010 \\ \underline{000001} \\ 1 \end{array} \xrightarrow{\leftarrow \uparrow} \quad \begin{array}{r} 000101 \\ \underline{000001} \\ 1 \end{array} \Rightarrow 1$$

$$\begin{array}{r} 000010 \\ \underline{0} \\ 0 \end{array} \Rightarrow 1 \quad \begin{array}{r} 000001 \\ \underline{000001} \\ 1 \end{array} \Rightarrow 1$$

000000

Doubt



A << 1

Yes

A <<= 1

$$N = 11$$

$(N >> 1) \& 1$

Expression

$$\underline{\text{temp}} = (11 >> 1) = (5) \underline{\& 1} = 1$$

$N >> 1$

2

$$a = 3, b = 2$$

if  $((a + b) \& 1 == 1)$

Google

Q

Given an array of size N.

Return if there exists a no. with  
frequency  $> N/2$

Majority element.

No extra  
space  
 $S.C. = O(1)$

A: 1, 6, 1, 1, 2, 1       $N = 6$

$\frac{N}{2} = 3$ , more than 3 times.

Majority = 1

J, , =

Quiz

A: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10  
3, 4, 3, 6, 1, 3, 2, 5, 3, 3, 3

$$N = 11$$

$$N/2 = 5$$

freq >  $\frac{N}{2}$

Quiz

A: 0,  $\frac{1}{6}$ ,  $\frac{2}{5}$ ,  $\frac{2}{3}$ , 4, 5, 6, 7, 8, 9  
4, 5, 5, 6, 4, 4, 4, 4, 4, 4

$$N = 10$$

$$N/2 = 5$$

freq >  $\frac{N}{2}$

freq >  $\frac{N}{2} \Rightarrow$

$\frac{N}{2} + 1$

$N - 1$

$N$

$N - \frac{N}{2} - 1$

$\frac{N}{2} - 1$

Sol<sup>n</sup> ① Brute force

fix the element  $\Leftarrow$  for ( $i = 0$ ;  $i \leq \frac{N}{2}$ ;  $i++$ ) {

Count = 0;

Count,  $A[i] \Leftarrow$  for ( $i = 0$ ;  $i < N$ ;  $i++$ ) {

for "b" -> D J J J

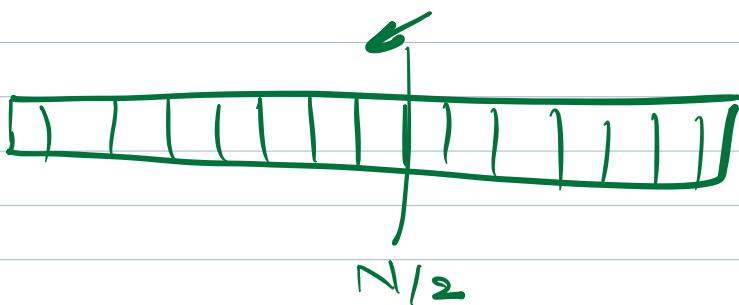
if  $(A[i] == A[i+1]) \{$   
    count++;

$\Rightarrow b$

if  $(count > N/2) \{$   
    return  $A[i]$ ;

b

z



$$T.C. = O(n^2)$$

Approach 2  $\Rightarrow$  Sorting

A: 4, 6, 5, 3, 4, 5, 6, 4, 4, 4

A: 3, 4, 4, 4, 4, 4, 4, 5, 5, 5, 6.  
Count = 1 2 3 4 5 6 7 8 9 10 11 12 13

Count = 1  
for ( $i = 1$ ;  $i < N$ ;  $i++$ ) {  
    if  $(A[i-1] == A[i]) \{$   
        count++;

$N/2 + 1$

$\Rightarrow$   
    if  $(A[i-1] == A[i]) \{$   
        count++;

b

else if  
count = 1;

if (count >  $\frac{N}{2}$ )  
return A[i];

$$T.C. = O(N + N \log N)$$

$$= O(N \log N)$$

$$= O(N)$$

Sorting  $\Rightarrow$  ↵

Array  $\Rightarrow$   $\mathbb{Z}$

$$\left( \frac{N}{2} + 1 \right) \Rightarrow \left( \frac{N}{2} - 1 \right)$$

free of  
majority

free of  
all

remaining  
elements.

$$\left( \frac{N}{2} + 1 \right) \pm - 1 \left( \frac{N}{2} - 1 \right) \pm \pm$$

$$= 2$$

(=)

$N = 9$ ,  $\text{Ter} = 5$

A<sub>o</sub>: 5, 5, 2, 3, 5, 1, 2, 5, 5

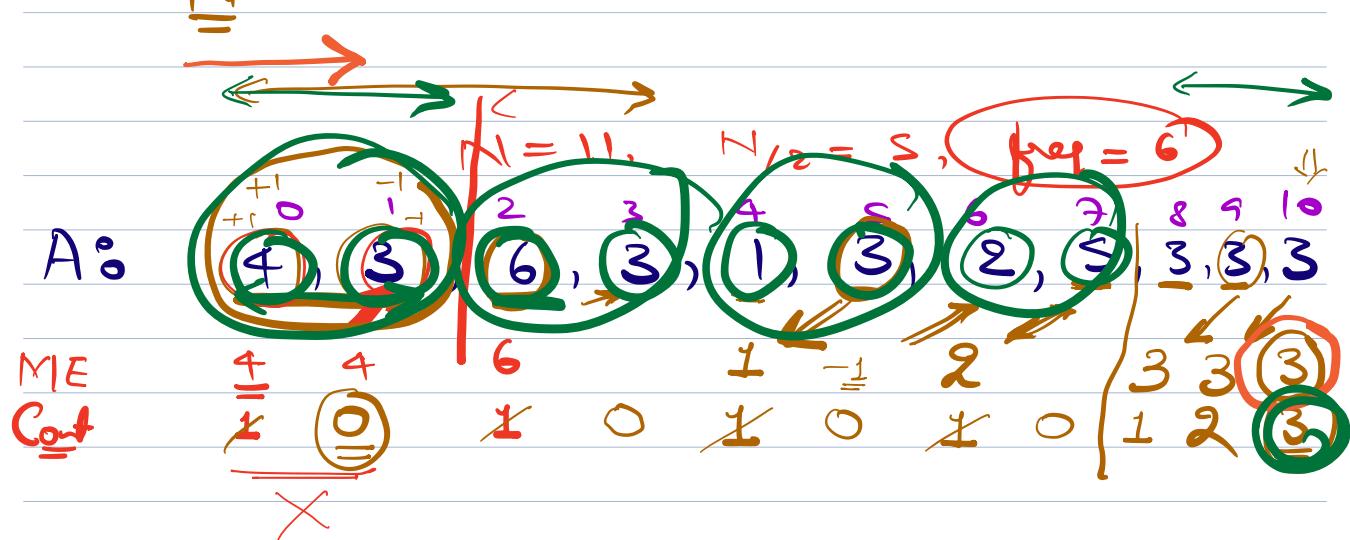
ME: 5, 5, 5

Count: 1, 2, 1

3  $\Rightarrow$  2 of them are 5

1 of them is 2

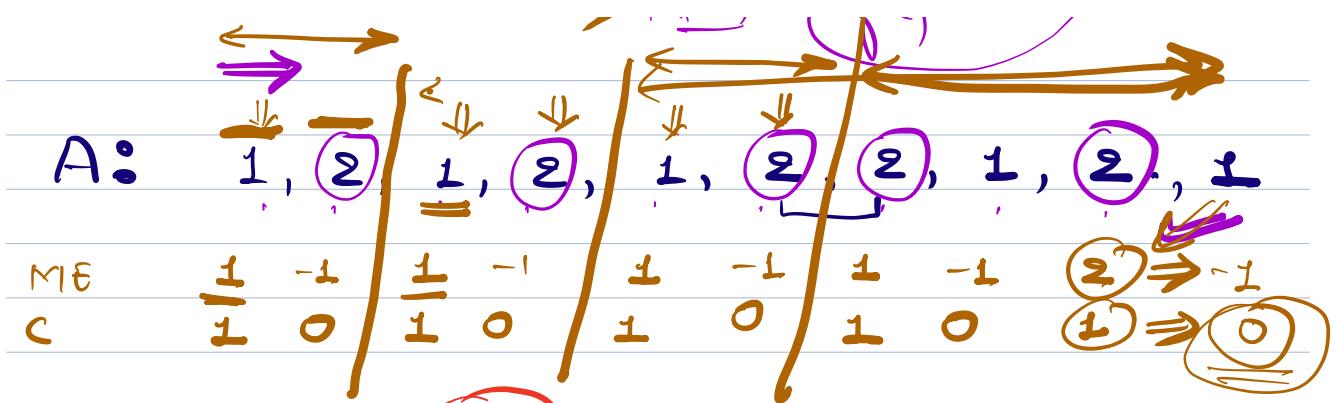
$= N$



for an array, as long as count is +ve.

majority element may be present

$\longleftrightarrow N = 9$ ,  $\text{Ter} = 5$



$\rightarrow$   
 $\text{A}^o: \underline{1}, \underline{2}, \underline{3}, \underline{4}, \underline{1}, \underline{2}, \underline{1}, \underline{1}, \underline{3}, \underline{1}, \underline{1}, \underline{2}$

NE C  $1 \times \underline{3} \times \underline{1} \times \underline{1} \times \underline{1} \underline{1}$

$i = 3$   
 $N = 7$   
 $N/2 = 3$ ,  $fcr = 4$

A:  $1, 2, \underline{3}, \underline{4}, \underline{5}, \underline{6}, \underline{7}$

ME C  $1 \times \underline{3} \times \underline{1} \times \underline{0} \quad \underline{1} \times \underline{0} \quad \underline{1} \times \underline{0}$

$\text{A}^o: \cancel{4, 3, 6, 3, 1, 3, 2, 5}$

$\rightarrow N = 10 \quad fcr = \underline{6}$

A:  $\underline{3}, \underline{3}, \underline{2}, \underline{3}, \underline{3}, \underline{3}, \underline{3}, \underline{2}, \underline{5}, \underline{7}$

ME  $3 \quad 3 \quad 3 \quad \underline{3} \quad 3 \quad 3 \quad 3 \quad 3 \quad 3 \quad \cancel{3}$

C 1 2 1 2 3 4 5 4 3 (2)

## Code

$$m = A[0]$$

$$c = 1$$

```
for (i=1; i < N; i++) {  
    if (A[i] == m) {  
        - c++;  
        - continue;  
    }  
    else {  
        c--;  
    }  
    if (c == 0) {  
         $\Rightarrow$  i++;  
        if (i < N) {  
            M = A[i]  
            c = 1;  
        }  
    }  
}
```

if ( $c > 0$ ) {

count = 0;

for ( $i = 0$ ;  $i < N$ ;  $i++$ ) {

D      if ( $A[i] == m$ ) {  
          count++;  
      }

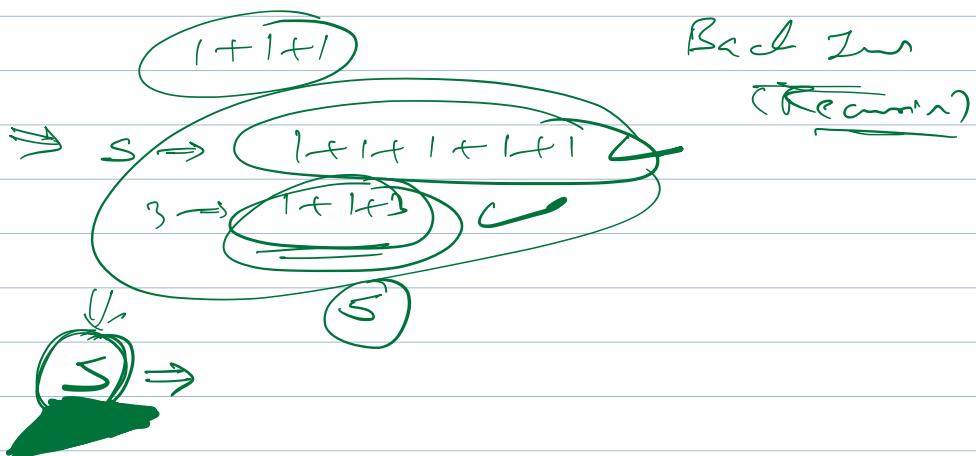
      if (count > N/2)  
          return m;  
    }

$$T.C. = O(2n) = \underline{O(n)}$$

$$S.C. = \underline{\underline{O(1)}}$$

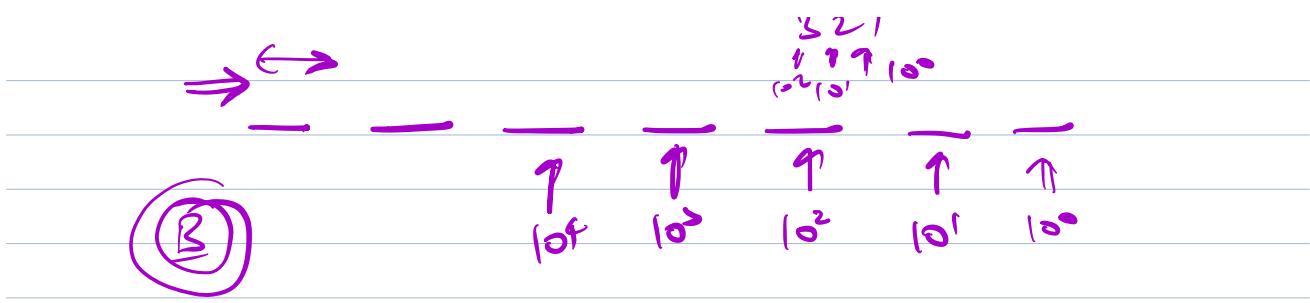
Doubt

$$N=3$$



$$N \Rightarrow N^k \text{ function}$$





Sum of all  $N$  nos

$$\frac{(N)(N+1)}{2}$$



lass

X^A

1 → N

$$\frac{(N)(N+1)}{2} - X + A =$$

$$\frac{(N)(N+1)}{2}$$

X - 2A

2A - X

X - A =

B^A

N = 10

1, 2, 3, 4, 5, 6, 7, 8, 9, 10

$$A = 7 \\ B = 4$$

Ach BK

$$\underline{A \cdot B} = 0$$

$$0 - \textcircled{1} \textcircled{0} \textcircled{0} \Rightarrow A^{\wedge}B = \textcircled{0} - \textcircled{2}$$

$(A^{\wedge}B) \wedge (\neg(A^{\wedge}B) \rightarrow)$

