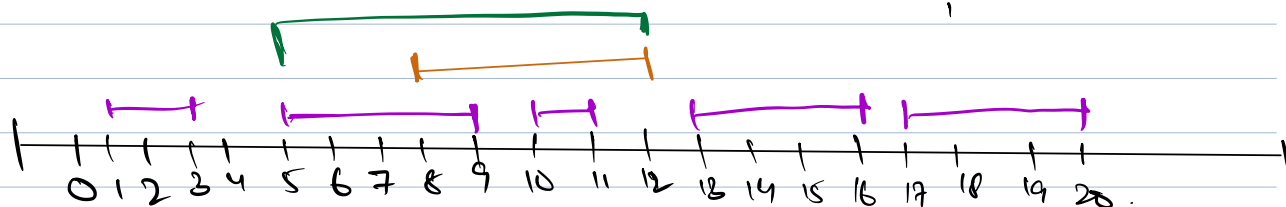


Q Merging intervals

Given a sorted set of non-overlapping intervals. Insert a new interval. st resulting interval is also sorted & non-overlapping

ex: $s \rightarrow [1 \quad 5 \quad 10 \quad 13 \quad 17]$
 $e \rightarrow [3 \quad 9 \quad 11 \quad 16 \quad 20]$



Insert $\rightarrow [8, 12]$

$s \rightarrow [1 \quad 5 \quad 13 \quad 17]$
 $e \rightarrow [3 \quad 12 \quad 16 \quad 20]$

$l_1 \quad r_1$

l_2

Non-overlapping.

$$(r_1 < l_2 \text{ or } r_2 < l_1)$$

Non-overlapping.

$l_1 \quad r_1$

$l_2 \quad r_2$

$l_2 \quad r_2$

$l_1 \quad r_1$

Overlapping

$$!(r_1 < l_2 \text{ or } r_2 < l_1)$$

Traverse from left to right & check for overlapping intervals with the new interval (we want to insert)

$i \rightarrow$ first overlapping idn(interval)

$j \rightarrow$ last overlapping idn/interval.

\rightarrow Non-overlapping \rightarrow put directly in ans.

start $\rightarrow \min(s[i], s_{\text{new}})$

end $\rightarrow \max(e[i], e_{\text{new}})$

TC = $O(N)$
SC = $O(1)$

arr = $[[1, 2], [3, 6], [5, 10], [2, 15]]$
0 1 2 3
[1, 3, 5, 2]
[2, 6, 10, 15]

s_{new} s_{end}

for($i=0$; $i < N$; $i++$) {

// overlap check.
if (!((arr[i][0] < s_{new}) || (s_{end} < arr[i][0])))

Q Given N distinct arr[i]; when $0 \leq \text{arr}[i] < N$
replace arr[i] = arr[arr[i]]

[0, N-1]

ex: $\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ \text{[} & \cancel{3} & \cancel{2} & \cancel{4} & \cancel{0} & \text{]} \\ & \downarrow & & \uparrow & \\ & \text{arr[arr[0]]} & & & \\ & \text{arr[3]} & & & \\ & = 1 & & & \end{matrix}$ $\text{arr}[i] = \text{arr}[\text{arr}[i]]$

[1, 4, 0, 2, 3]

$$\text{arr}[1] = \text{arr}[\text{arr}[1]] = \text{arr}[2] = 4$$

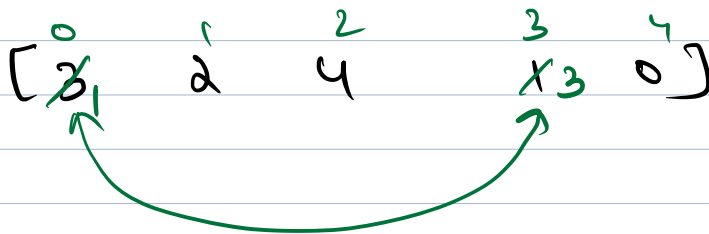
$$\text{arr}[2] = \text{arr}[\text{arr}[2]] = \text{arr}[4] = 0$$

$$\text{arr}[3] = \text{arr}[\text{arr}[3]] = \text{arr}[1] = 2$$

$$\text{arr}[4] = \text{arr}[\text{arr}[4]] = \text{arr}[0] = 3$$

Do you think I will let you use an extra Array?

→ Can't use an extra array.



$$\text{arr}[4] = \text{arr}[\text{arr}[4]] = \text{arr}[0] = \text{X}$$

3

→ Cannot swap

ex: $\text{arr}[7] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ \text{[} & 3 & 1 & 4 & 6 & 5 & 0 & 2 & \text{]} \end{matrix}$

Ans - $\text{[6, 1, 5, 2, 0, 3, 4]}$

ex: $\text{arr}[7] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ \text{[} & 1 & 6 & 3 & 5 & 4 & 2 & 0 & \text{]} \end{matrix}$

Hint: Somehow at $a[i]$, we need to store both new & old value.

Big Bang Theory.

Day
0

Hour.
0

23

0

23

40

1

16

100

4

4

125

5

5

200

8

8

x

$x/24$

$x \% 24$

↳ Aren't we storing 2 values in a single variable.

$\frac{x}{24} \rightarrow$ Quotient \rightarrow days.

$x \% 24 \rightarrow$ Remainder \rightarrow hour.

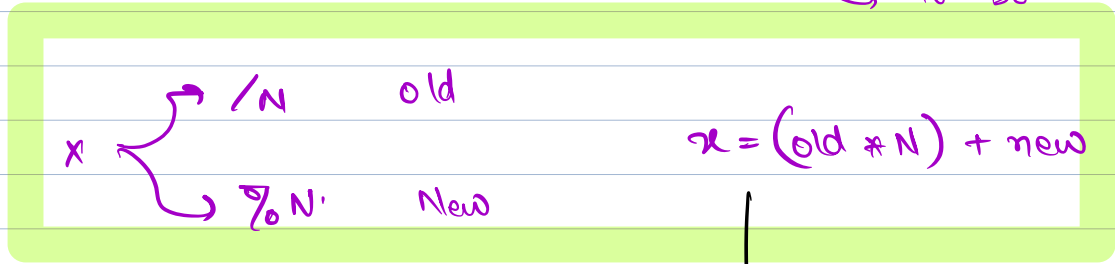
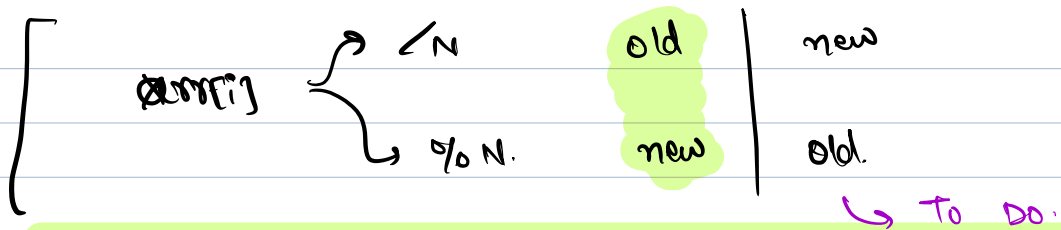
$$0 \leq x < 24$$

$$0 \leq a[i] < N. \leftarrow$$

↳ $[0, N-1]$

All values in $A[i]$ will be $\% N$.

$x \left\{ \begin{array}{l} / 24 \\ \% 24 \end{array} \right.$



Derivation of old and new from x :

- $x / N = \text{old}$
- $x \% N = \text{new}$

Equation for x :

$$\frac{\text{old} * N + \text{new}}{N} < N$$

Boxed equations:

$$\frac{x}{N} = \text{old}$$

$$x = \text{old} * N$$

Equation for $(N+x) \% N$:

$$(N+x) \% N = (N + \text{new}) \% N$$

↓ new

$$= \text{old}$$

Equation for $\frac{\text{old} * N}{N}$:

$$\frac{\text{old} * N}{N} = \text{old}$$

greater than 1
or
less than 1

Equation for $\frac{N-1}{N}$:

$$\frac{N-1}{N}$$

Equation for $\frac{\text{old} * N}{N}$:

$$\frac{\text{old} * N}{N}$$

Equation for $\frac{\text{old}}{N}$:

$$\frac{\text{old}}{N} = 0$$

$$(old * N + new) \% N = new$$

$$(old * N) \% N + (new \% N)$$

$$(4 * 10) \% 10 = 0$$

$$40 \% 10 = 0$$

new

$$x = (old * N) + new$$

$$arr[7] = [\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ 3*7 & 1*7 & 4*7 & 6*7 & 5*7 & 0*7 & 2*7 \\ +6 & +1 & +5 & +2 & +0 & +3 & +4 \end{matrix}]$$

→ Multiply all values by 7

→ Old value → /7
→ New value → %7

$$arr[0] = arr[arr[0]]$$

$$\begin{matrix} \text{idx.} \\ 2 \div 7 = 3 \\ \hline arr[3] \end{matrix}$$

$$\begin{matrix} \text{value} \\ arr[3] = 6 \\ \hline \end{matrix}$$

$$arr[1] = arr[arr[1]]$$

$$\begin{matrix} arr[1] = 1 \\ \hline 7 \end{matrix}$$

$$\begin{matrix} arr[1] = 1 \\ \hline 7 \end{matrix}$$

$$arr[2] = arr[arr[2]] = \begin{matrix} arr[2] = 4 \\ \hline 7 \end{matrix}$$

$$\begin{matrix} arr[4] = 5 \\ \hline 7 \end{matrix}$$

$$21 + 6 = 27 \% 7 = 6$$

$$\begin{matrix} 27 \\ \hline 7 \end{matrix} = 3$$

TC → O(N)

SC → O(1)

Break = 11:03

Q → Given a string of distinct chars. Find the sorted. permutation rank of that string
 ex: BCDA → 10 ~~A B C D~~

1. A B C D
2. A B D C
3. A C B D
4. A C D B
5. A D B C
6. A D C B

$$\begin{array}{c} \text{A} \\ \hline \uparrow \end{array} \quad \overline{3} \times \overline{2} \times \overline{1} = 3!$$

$$\rightarrow \begin{array}{c} \text{B} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{C} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{D} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{A} \\ \hline \uparrow \end{array} = 2! = 1!$$

7. B A C D
8. B A D C
9. B C A D
10. B C D A

$$\begin{array}{c} 3! \\ 6 \end{array} + \begin{array}{c} 2! \\ 2 \end{array} + \begin{array}{c} 1! \\ 1 \end{array} + \begin{array}{c} 1! \\ 1 \end{array} = 10$$

sorted → RST

sto → STRR:

1. RST
2. RTS
3. SRT
4. STR

$$\begin{array}{c} \text{R} \\ \hline \uparrow \end{array} \quad \text{---} \quad \text{---} \quad \text{---} \quad 2!$$

$$\begin{array}{c} \text{S} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{R} \\ \hline \uparrow \end{array} \quad \text{---} \quad \text{---} \quad 1!$$

$$\begin{array}{c} \text{S} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{T} \\ \hline \uparrow \end{array} \quad \begin{array}{c} \text{R} \\ \hline \uparrow \end{array} \quad \text{---} \quad +1$$

$$2! + 1! + 1 = 2 + 1 + 1 = 4$$

①

$$\begin{array}{c} \text{R} \\ \hline \uparrow \end{array} \quad \text{---} \quad \text{---} \quad \text{---} \quad \left(\frac{3!}{2!} \right) \quad \% 3000$$

Inverse Modulo

② $\begin{array}{c} \text{S} \\ \hline \uparrow \end{array} \quad \text{---} \quad \text{---} \quad \text{---}$