

Given an array A of N integers. The value of subarray is defined as bitwise OR of all elements in it.

Return the sum of value of all the subarrays.

ex: $[1, 2, 3, 4]$

$[1]$ → 1

$[1, 2]$ → 3

$[1, 2, 3]$ → 3

$[1, 2, 3, 4]$ → 7

$[2]$ → 2

$[2, 3]$ → 3

$[2, 3, 4]$ → 7

$[3]$ → 3

$[3, 4]$ → 7

$[4]$ → 4

$N \leq 10^5$

$A[i] \leq 10^8$

return result.

$$\text{ans} = 1 + 3 + 3 + 7 + 2 + 3 + 7 + 13 + 7 + 4,$$

$$= 40$$

1 | 1 2 | 3

$$3 | 3 = 3.$$

OR

0 0 0

0 1 1

1 0 1

1 1 1

7 → 111
4 → 100

BF

1. Find all subarrays. $O(N^2)$

2. Take the OR of each subarray (N)

3. Take & return sum. ($O(N)$)

$Tc \rightarrow O(N^2)$

10^5

$\cancel{10^5}$

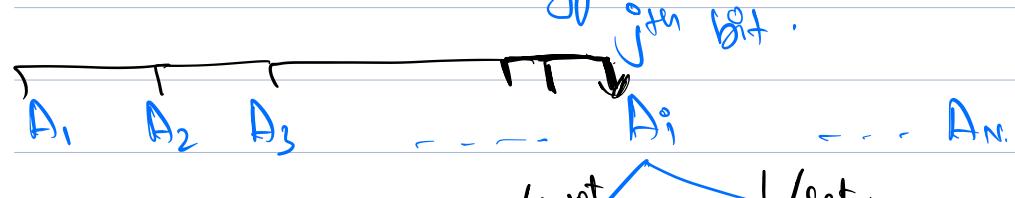
$O(N)$

$N \log N$

$10^8 \rightarrow 31 \text{ or } 32$ $N(\text{approx})$
 $2^{10} \approx 1024 \approx 10^3$
 $2^{20} \approx 10^6$
 $2^{30} \approx 10^9$

30 bits.

Contribution strategy



0/unset 1/set

of subarray = i
contribution = $i \times 2^j$

		jth bit
A ₁	(1 st)	0
A ₂	(2 nd)	0
A ₃	(3 rd)	1
A ₄	(4 th)	1
A ₅	5	0
A ₆	6	0
A ₇	7	0
A ₈	8	0

jth →

$A = [1, 2, 3, 4]$
 $\xrightarrow{\text{group}} 2^0$
1 → 0 0 1
2 → 0 1 0
3 → 0 1 1 ← j
4 → 1 0 0

subarray → 3

subarrays = 6

set Subarray = 4

$\# 2^0 * 3 = 1 * 3$
 $\underline{\text{count}}$ $2^j * i \rightarrow$ bit is set

\downarrow \Rightarrow  \oplus

lastSetIndex (LSI)

contribution = $LSI * 2^j$ If bit is unset.

	0	1	2	3	4
1	0 0 1				
2	0 1 0				
3	0 1 1				
4	1 0 0				

$2^0 \times i = 2^0 \times 1 = 1$
 $2^0 \times LSI = 2^0 \times 1 = 1$
 $2^0 \times i = 2^0 \times 3 = 3$
 $2^0 \times LSI = 2^0 \times 3 = \frac{3}{8}$

0th bit $\rightarrow 8$ 

1	0	$\rightarrow 2^1 \times 0$
2	1	$\rightarrow 2^1 \times 2 = 4$
3	1	$\rightarrow 2^1 \times 3 = 6$
4	0	$\rightarrow 2^1 \times 3 = 6$

$$1^{st} \text{ bit} = 16$$

$$1 \quad 0 \rightarrow 0 \times 2^2$$

$$2 \quad 0 \rightarrow 0 \times 2^2$$

$$3 \quad 0 \rightarrow 0 \times 2^2$$

$$4 \quad 1 \rightarrow 4 \times 2^2 = 4 \times 4 = 16$$

$$2^{nd} \text{ bit} = 16$$

16 + 16 + 8 = 40

Given a sorted array A of distinct integers. Return all possible subsets of A

ex: $A = [1, 2, 3]$

$\{ \quad [] \quad \}$ } Subsets.

$[1, 2]$

$[1, 2, 3]$

$[1, 3]$

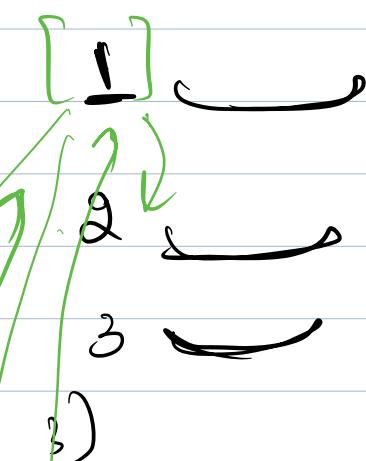
$[2]$

$[2, 3]$

$[3]$

Notes:

↳ Subsets \uparrow len of arr
↳ No duplicates in sol.



$[1, 2]$

$[1, 3]$

$[1, 2, 3]$

Pseudo code.

ans = {}

temp = {}

findSubset(A, idx)

```
ans.add(temp) //  
for(i = idx; i < A.length; i++) {  
    temp.add(A[i]) // do  
    findSubset(A, i+1)  
    temp.removeLast() // undo.  
}
```

findSubset(A, 0)

ans = {} [1] [1, 2] [1, 2, 3] temp = {} [1, 2, 3]

~~ans~~ → findSubset(A, 1)

fS(A, 2)

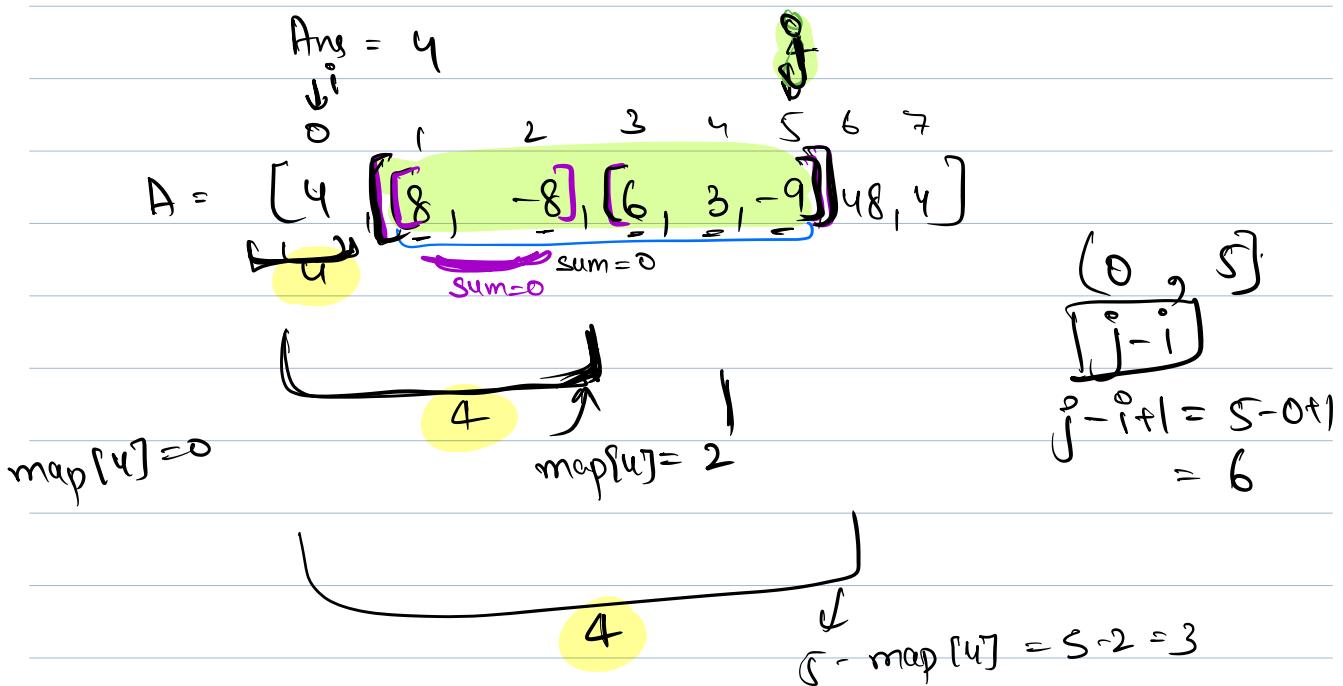
fS(A, 3)

Q prefix Sum.

Q Given an array A of N integers

Find the largest continuous subsequence in the array which sums to zero & return length.

ex: $A = [1, 2, -2, 4, -4]$



1. Find prefix sum

2. Hashmap: to find if that sum had already occurred, if yes at what index.

Code:

```
prefixSum[0] = A[0]
for (i=0; i < A.size(); i++)
    prefixSum[i] = A[i-1];
```

\sum |
 sum Index.

```

HashMap<int, int> map = new HashMap<>
ans = 0;
for(i=0 ; i < A.size() ; i++) {
  if (map.contains(pfixSum[i])) {
    ans = max(ans, i - map.get(psi[i]))
    continue;
  }
  map[psi[i]] = i
}
  
```

Code for Q1

long setBit[N][31]

\leftarrow 28

```

for(j=0 ; j < 30 ; j++) {
  int lsi = 0
}
  
```

```

for(i=0 ; i < A.length ; i++) {
  if((A[i] & (1 << j)) > 0)
    setBit[i][j] = i+1
    lsi = i+1
}
  
```

$\} \text{ else}$

$\| \text{ Bit is unset}$

$\text{setBit}[i][j] = lsi \quad |$

$(10^9 + 7) \mod$

\downarrow

$\text{ans} += ((1 << j) * \text{setBit}[i][j])$

\downarrow

\downarrow

000
001
010
011

↓ ↓
 \downarrow^{12}

[1] [2] [1,2]

[1] [1,2] [2]

Q Given an array A comprising of 0's & 1's & an integer B. Find indices s.t. there are B alternating 0 & 1 on left of that idx.

0 1 2 3 4 5

ex: $\underset{x}{[1, 0, 1, 0, 1, 1]}$
 $B=0$

[0, 1, 2, 3, 4]

$B=1$

[1, 2, 3, 4]

$B=2$

[2, 3, 4]

0 1 2 3 4 5 6

ex: [0, 0, 0, 1, 1, 0, 1]

$B=1$

[5, 6]

1

B.F. for every idx, check sequence on left
 $O(N^2)$

$\underbrace{010101}_{6 \neq} \overbrace{00}^{\text{different}} \rightarrow$
 $010101 \overbrace{1}^{\text{same}} \rightarrow$

same \rightarrow start from 0
 different \rightarrow add 1 to prev.
 i.e. $\text{count}[i-1] + 1$

$010101 \overbrace{00}^{\text{different}}$
 $\text{count} = [0 1 2 3 4 5 6 0]$
 \rightarrow

$01010 \overbrace{0}^{\text{different}} \rightarrow$
 $01011 \overbrace{1}^{\text{same}} \rightarrow$
 $010101 \overbrace{0}^{\text{different}}$
 $sc(5) + 1$
 $010100 \overbrace{0}^{\text{different}}$

Code:

```

segCount = [0 1 1 1 1 1]
segCount[0] = 0;
for(i=1 ; i < A.length ; i++) {
    if(A[i] != A[i-1])
        segCount[i] = segCount[i-1] + 1
    else
        segCount[i] = 0
    }

```

$$a = a + 1$$

$$a++$$

Q Given an array A comprising of 0's & 1's & an integer B. Find indices s.t. there are B alternating 0 & 1 on right of that ido.

$\begin{array}{r} 1 3 2 1 0 \\ | 0 1 0 1 0 \\ | 0 3 2 1 0 \\ | 1 0 1 0 \\ \hline \end{array}$

$\text{segCount} = [0 \ 1 \ 1 \ 1 \ 1]$

$\text{segCount}[0] = 0;$

for($i = A[\text{length}-2]; i >= 0; i--$) {

 if($A[i] \neq A[i+1]$)

$\text{segCount}[i] = \text{segCount}[i+1] + 1$

 else

$\text{segCount}[i] = 0$

Q - Given an array A of length N consisting of 0's & 1's & an integer B . Find indices of A that can be treated as a center for $2*B+1$ length of alternating 0-1 subarray.

$A: [1 \ 0 \ 1 \ 0 \ 1]$

$B=2$

$B=1$

$2*B+1$

$2*1+1=3$

$2*B+1$

[2]

[1, 3, 2]

Q A of N integers & an element B .

$A = [5, -2, 3, 1, 1, 2]$

$B \geq 3$

$\downarrow^S \quad \downarrow^{e-B} \quad \downarrow^e$

$5, -2, 3, 1, 1, 2, 5, -2, 3, 1, 1, 2$

$\therefore (i+1) \% \text{A.size}$

$B \leq A.size$.

$i = 1$

$i = 2$

$i = 3$
 $i = 4$

$i = 5$

$i = 6$

$i = 7$

$\frac{1}{4}$
0

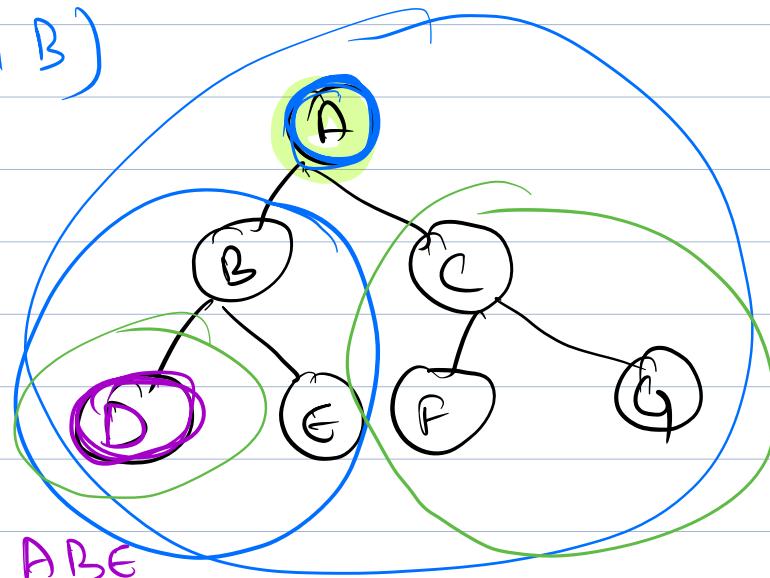
1

2

3

$(-3, 3)$

$(-B, B)$



ABD

A BE

array = { };

traverse(A) { → point path of return.

// If A null return.

array.push(A) // did

{ traverse(A.left) } } // recursion.

{ traverse(A.right) } }

array.removeLastElement(); // undo.

}.

array = { A B ~~E~~ E };

A B D ✓
A B D ✓
[]

J

D B D T

