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Q: Given an array of N integers and a no. K . Return true if there exists a pair (i, j) s.t.

$$A[i] + A[j] = K$$

$$(i \neq j)$$

Eg : $A \Rightarrow \{2, 7, 11, 15, 7\}$

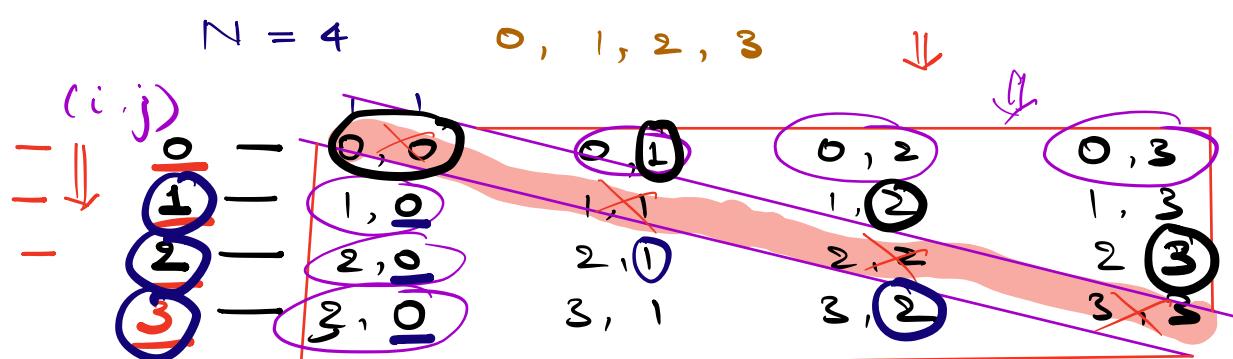
$$K = 18 \Rightarrow \text{True } (1, 2)$$

$$K = 14 \Rightarrow \text{True } (1, 4)$$

$$K = 20 \Rightarrow \text{False.}$$

Solⁿ \Rightarrow Brute force

\Rightarrow Check for all pairs if sum = K



$i \Rightarrow 0 \text{ to } N-1 \Rightarrow \underline{n^2 \text{ possibilities.}}$

\Rightarrow It is okay to solve for one quadrant.

Upper

$\lceil \text{for}(i=0; i < N; i++) \{$

Lower

$\text{for}(i=0; i < N; i++) \{$

$\hookrightarrow // \text{for } (j = \underline{i+1}; j \leq N; j++)\{$ $\Rightarrow \text{for } (j = \underline{0}; j \leq \underline{i}; j++)\{$
 if ($A[i] + A[j] == K$)
 {
 return true;
 }

$$\begin{array}{l} i = \underline{\underline{N-1}} \\ j = \underline{\underline{N}} \end{array}$$

$$\begin{array}{l} i = \underline{\underline{0}} \\ j = \underline{\underline{0}} \end{array}$$

$$\begin{array}{l} \text{T.C.} = O(n^2) \\ \text{s.c.} = O(1) \end{array}$$

2) Can you optimize T.C. ??

$$\Rightarrow i \Rightarrow A[i] + x = K$$

$$x = K - A[i]$$

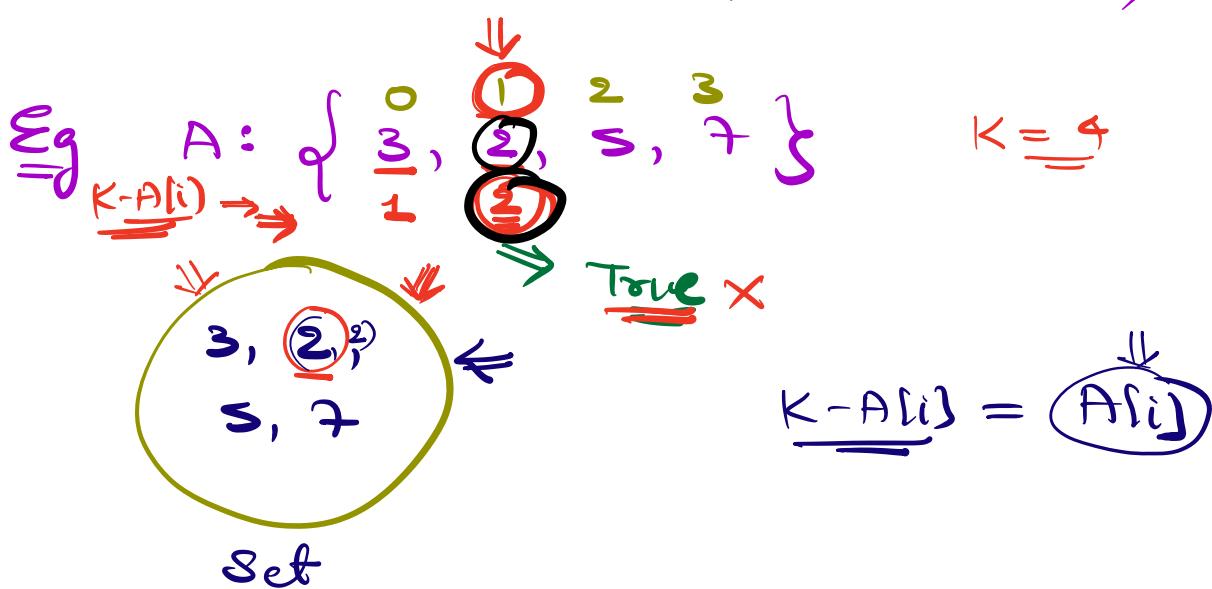
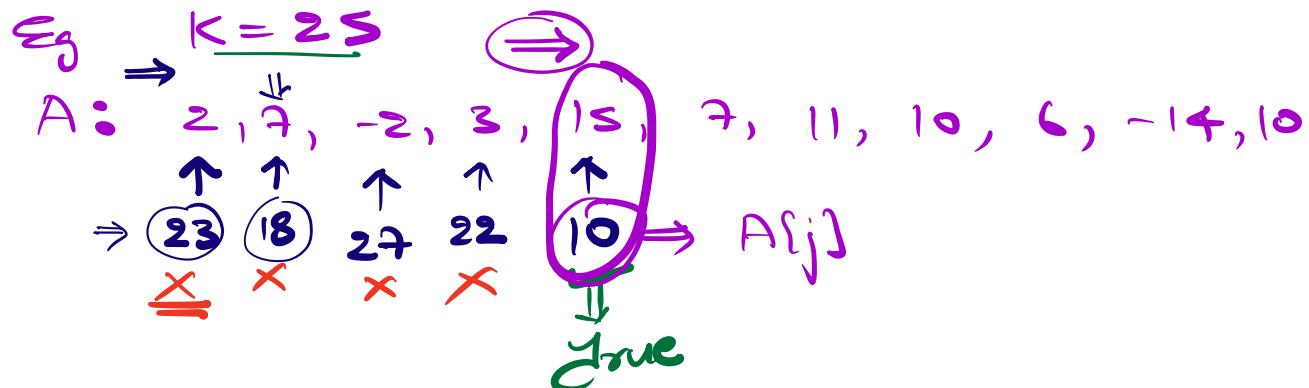
$\forall i$, search for $(K - A[i])$ using hashset

Steps

- 1) Insert all the array elements in a hashset
- 2) Iterate over the array &

$\forall i$, search for $(K - A[i])$ in hashset.

If present, return true. Else false.



Solⁿ

\Rightarrow Hash Map

Step 1 \Rightarrow Create a freq map from the array.
(Hash Map)

L D R T /

Step 2

```
for (i=0; i<N; i++) {
```

```
    x = K - A[i];
```

```
    if ( freqMap.containskey(x) ) {
```

```
        count = freqMap[x];
```

```
        if (A[i] == x) {
```

```
            if (count > 1) {
```

```
                return true;
```

↳
else {
 ↳ return true;

↳

↳
return false;

O-2

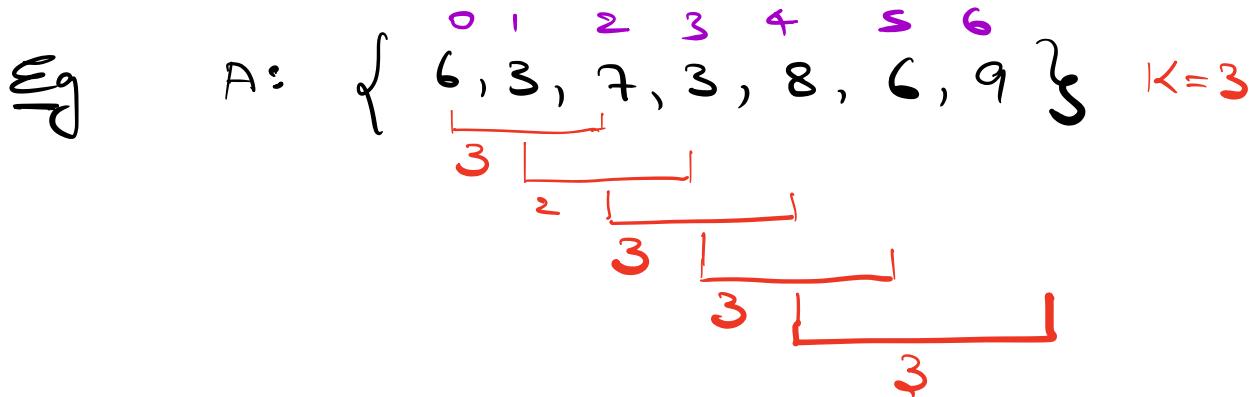
Given an array of size N

Calculate no. of distinct element
in every sliding window of size K.

Eg A: [0, 1, 2, 3, 4] K=2



Return $[1, 2, 1, 2]$



Return $[3, 2, 3, 3, 3]$

$\|Z$

length	start index first	start index last
1	0	$n-1$
2	0	$n-2$
3	0	$n-3$
⋮	⋮	⋮
K	0	$n-K$

1) Hash Set

$$(i, j) \Rightarrow K = j - i + 1$$

$$j = K + i - 1$$

$\Rightarrow \text{for } (i=0; i \leq n-K; i++) \{$

$$D \quad \underline{j} = k+i-1$$

// set <Int> s;

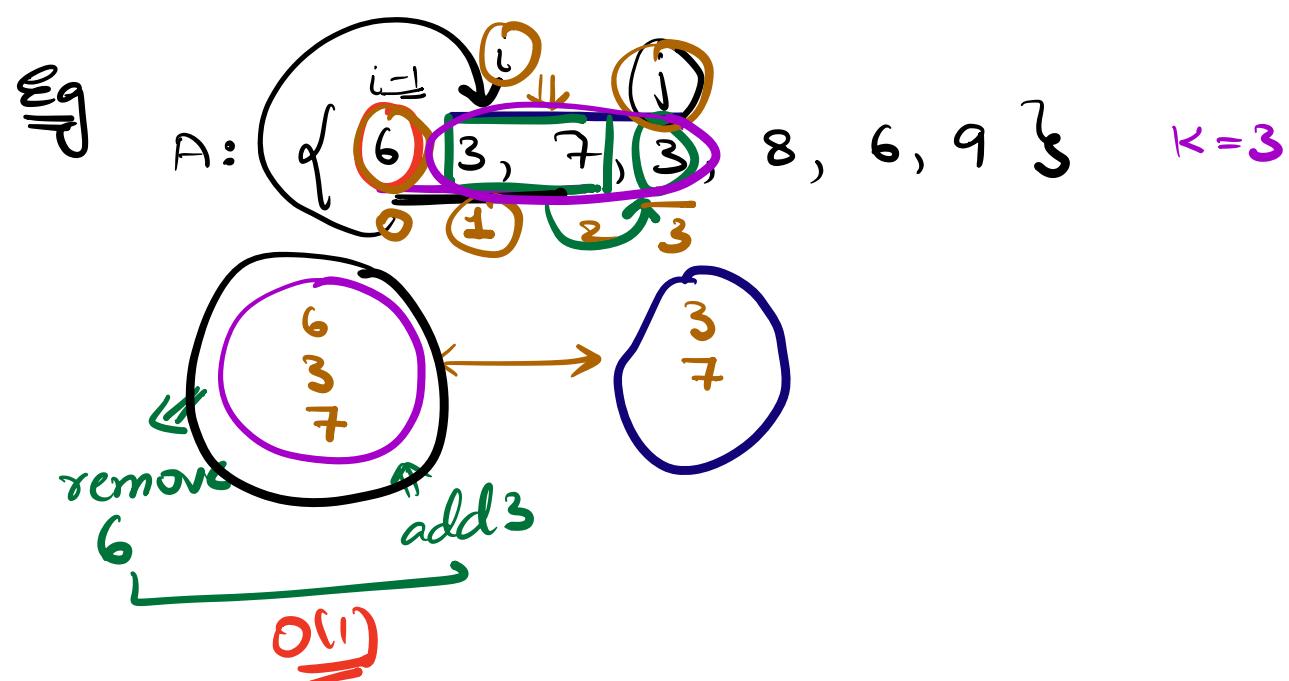
// K \Rightarrow for ($k = i$; $k \leq j$; $k++$) {
 s.add (A[k]); } \Rightarrow

// ans = s.size()

}

$$\begin{aligned} T.C. &= O((n-k) \times k) \\ &= O(nk - \cancel{k^2}) \\ &= O(\underline{nk}) \end{aligned}$$

eg



Code

```
for (i=0; i < K; i++) {  
    set.add(A[i]); } } ) Ans = set.size();
```

\Rightarrow for ($i = 1$; $i \leq (n-k)$; $i++$) {

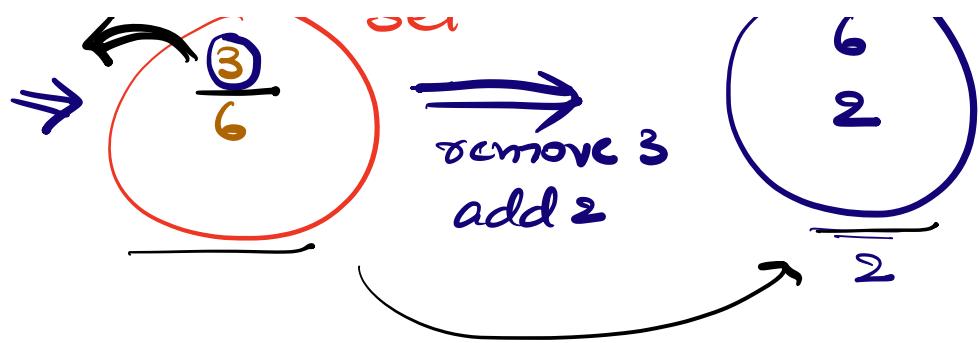
$j = k+i-1;$
 set. remove ($A[\underline{i-1}]$);
 set. add ($A[j]$);
 // ans = set.size()

5

$$\begin{array}{l} T.C = O(N) \\ S.C = O(\bar{N}) \end{array}$$

 Any missing corner cases ??

Ex: $A :=$  $\begin{bmatrix} 1 & 2 & 3 \\ 6 & 3 & 2 \\ 1 & 3 & 5 \end{bmatrix}$



Solⁿ

Hash Map

Eg

A: $\left[\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 3, 6, 2, 2, 1, 3, 5, 7, 9 \end{matrix} \right]$ $K=3$

Element	freq
3	2
2	1

Removing 3
Adding 2

$$\begin{matrix} 0 & 2 \\ \uparrow & \uparrow \\ 0, 2 \Rightarrow 3 \end{matrix}$$

Code

```

for (i=0; i < K; i++) {
    if ( freqMap.contains(A[i]) ) {
        freqMap[A[i]]++;
    } else {
        freqMap.put(A[i], 1);
    }
}

```

}

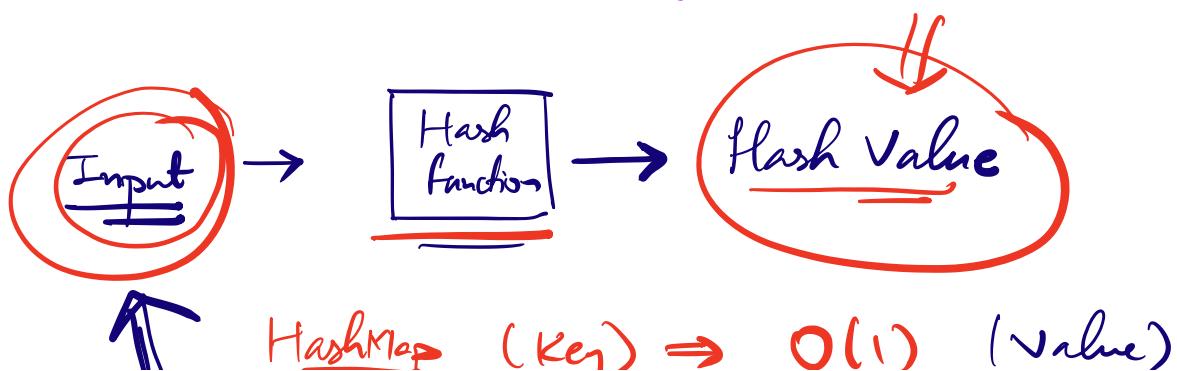
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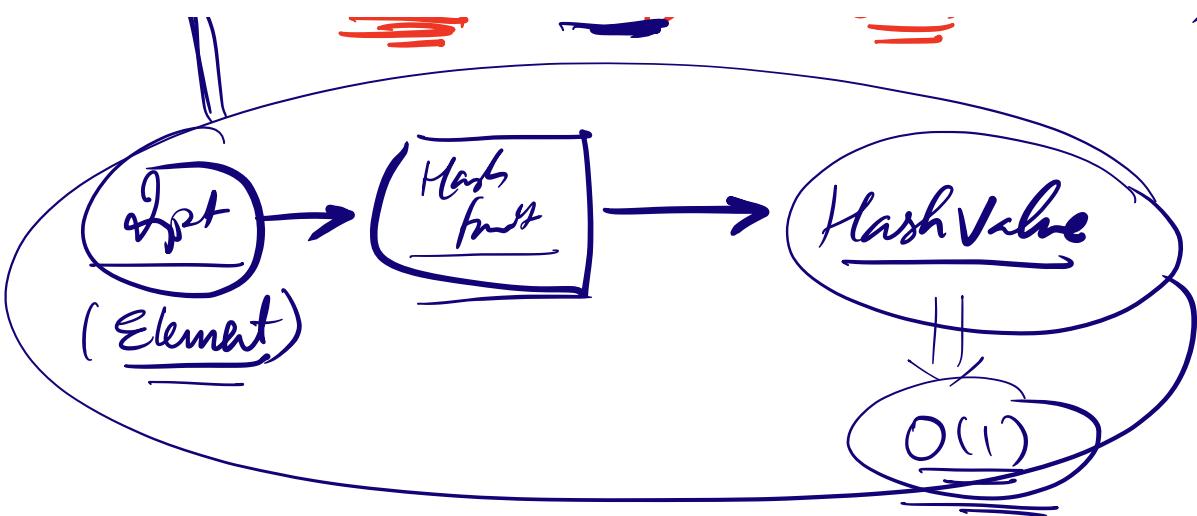
for ( i = 1 ; i <= (n-k) ; i++ ) {
    j = k+i-1;
    freqMap[ A[i-1] ] --;
    if ( freqMap[ A[i-1] ] == 0 ) {
        freqMap.remove( A[i-1] );
    }
    if ( freqMap.contains( A[j] ) ) {
        freqMap[ A[j] ]++;
    } else {
        freqMap.put( A[j], 1 );
    }
}

```

$$T.C = O(n)$$

$$S.C = O(k)$$





$$N \Rightarrow O(N)$$

$$N \Rightarrow O(2N) = \underline{\underline{O(N)}}$$



Given an array of size N

Return TRUE if there exists a subarray with sum = K given

Eg

$$A: [0, 1, 2, 3, 4, 5, 6, 7] \\ 4, 2, -1, 3, 10, 5, 6, 3$$

$$PS: 4, 6, 5, 8, 18, 23, 29, 32$$

$\underline{\underline{K=12}}$

TRUE

$\underbrace{12}_{\text{j}} \quad \underbrace{12}_{\text{i}}$

$j = 4$

$i-1 = 1$
 $i = 2$

Solⁿ

Brute Force

~~for~~ ~~for~~ ~~for~~
for subarrays, check if $\text{sum} = K$
 $O(n^2)$

$$\text{T.C.} = O(n^2)$$

[
 for (i=0, $i < N$, $i++$) {
 sum = 0;
 for (j=i, $j \leq N$, $j++$) {
 sum += A[i];
 if (sum == K) {
 return True;
 }
 }
 }
 return False;

$$\text{T.C. } O(n^2)$$

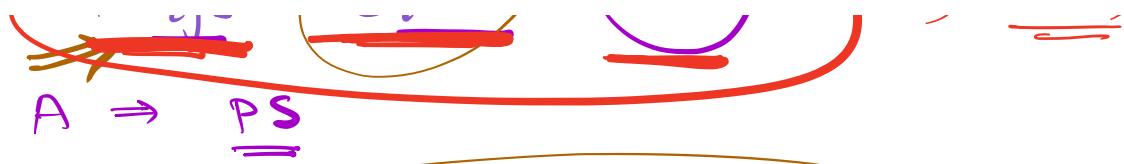
2) Optimise ??

$$\text{Sum}(i, j) \quad \Downarrow \quad \text{Ps}[j] - \text{Ps}[i-1]$$

\approx



$$\text{Ps}[i] - \text{Ps}[i-1] = K \Rightarrow O(N)$$



Find 2 ele from PS array s.t.
 $\text{diff} = k$

H.W.

Ques \leftarrow

$$\underline{\underline{PS[i-1]}} = \underline{k + PS[i-1]}$$

\uparrow