

8 containers  
7 packs  
3 bundles  
4 logs

$$8 \times 10^3 + 7 \times 10^2 + 3 \times 10^1 + 4 \times 10^0$$

Base = 10

$\emptyset$   $\cancel{\{ \}}$

Decimal no. system  $\Rightarrow [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]$

Base = 8

Octal no. system  $\Rightarrow [0 - 7]$

Divisibility

$\dots \times^{\text{th}} \Rightarrow x-1$

Eg

$$( \underline{\underline{0}} \underline{1} \underline{3} \underline{2} )_8$$

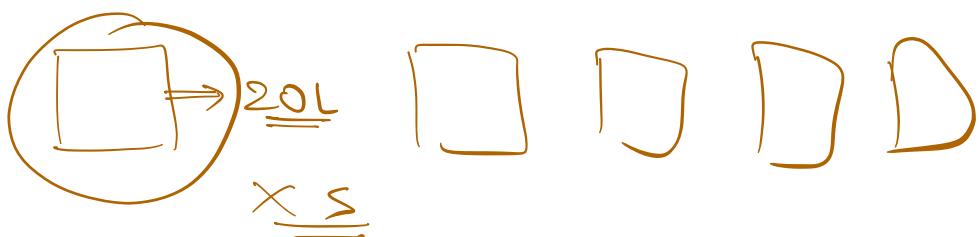
$$0 \times 8^3 + 1 \times 8^2 + 3 \times 8^1 + 2 \times 8^0$$

$$= 64 + 24 + 2 = (90)_{10}$$

	0	1	2	3	4	5	6	7
$\downarrow \rightarrow$	0	1	2	3	4	5	6	7
$\rightarrow 0$	0	1	2	3	4	5	6	7

~~Ex~~ Cr  $\Rightarrow$  Cash

Bundles  $\Rightarrow$  (20L)  $\times$  5



Stone Age (Barter System)

Cut wood in forest

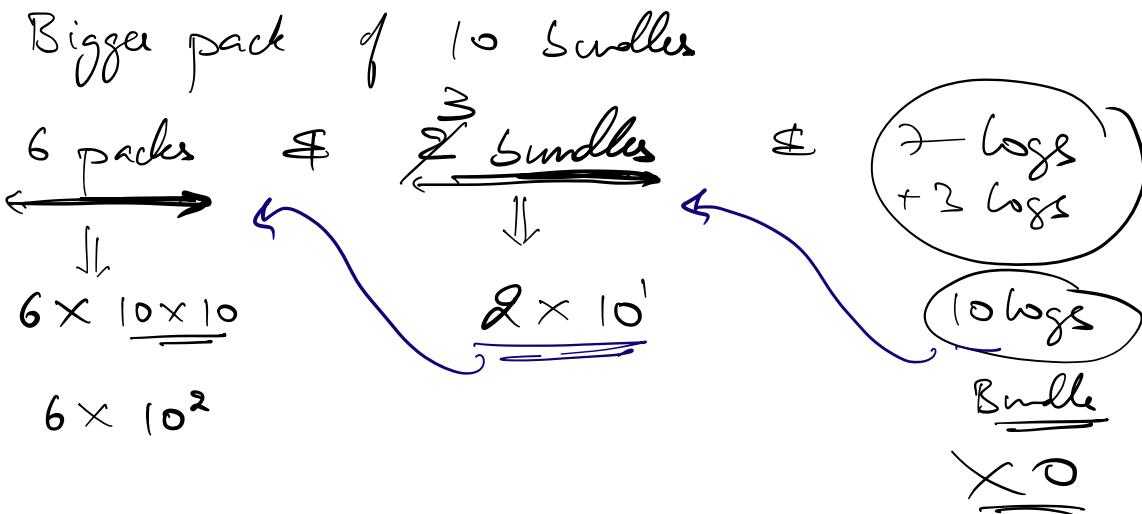
627 pieces of log

Bundles of 10 logs

62 bundles & 7 logs

~~$\underline{\underline{2}}$~~ 

$\curvearrowright$   
 $7 \times 10^0$



~~Bank - 3~~

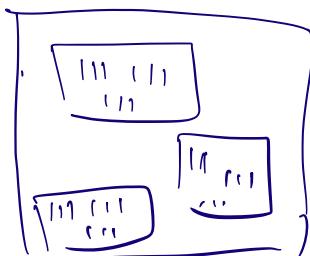
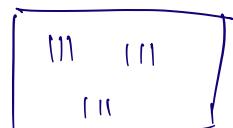
$[0-2]^{0,1,2}$

$$\left( \begin{smallmatrix} 2 & 1 & 0 \\ 1 & 1 & 2 \\ \hline 1 & 1 & 2 \end{smallmatrix} \right)_3 =$$

$$= \frac{1 \times 3^3}{27} + \frac{1 \times 3^2}{9} + \frac{2 \times 3^1}{3} + \frac{0 \times 3^0}{1}$$

$$= \underline{\underline{(42)_{10}}}$$

$\# \quad \#$



$$\text{Ques} \quad (1\underline{2}\underline{5})_8$$

$$= \underline{1 \times 8^2} + \underline{2 \times 8^1} + \underline{5 \times 8^0}$$

$$= \underline{\underline{64}} + \underline{\underline{16}} + \underline{\underline{5}}$$

$$\text{Ques} \quad \text{Octal} \Rightarrow \underline{8} \Rightarrow \begin{array}{c} (0-7) \\ \leftarrow \rightarrow \end{array} \quad \underline{(0,1)}$$

$$(1\underline{0}\underline{0}\underline{0}\underline{0}\underline{0}1)_8 -$$

$$(65\underline{8}2)_x$$

$$\text{Ques} \quad (0\underline{2}\underline{1}\underline{0}\underline{1})_3 \Rightarrow \underline{\text{Base 3}}$$

$$\cancel{0 \times 3^4} + \cancel{2 \times 3^3} + \cancel{1 \times 3^2} + \cancel{0 \times 3^1} + \cancel{1 \times 3^0}$$

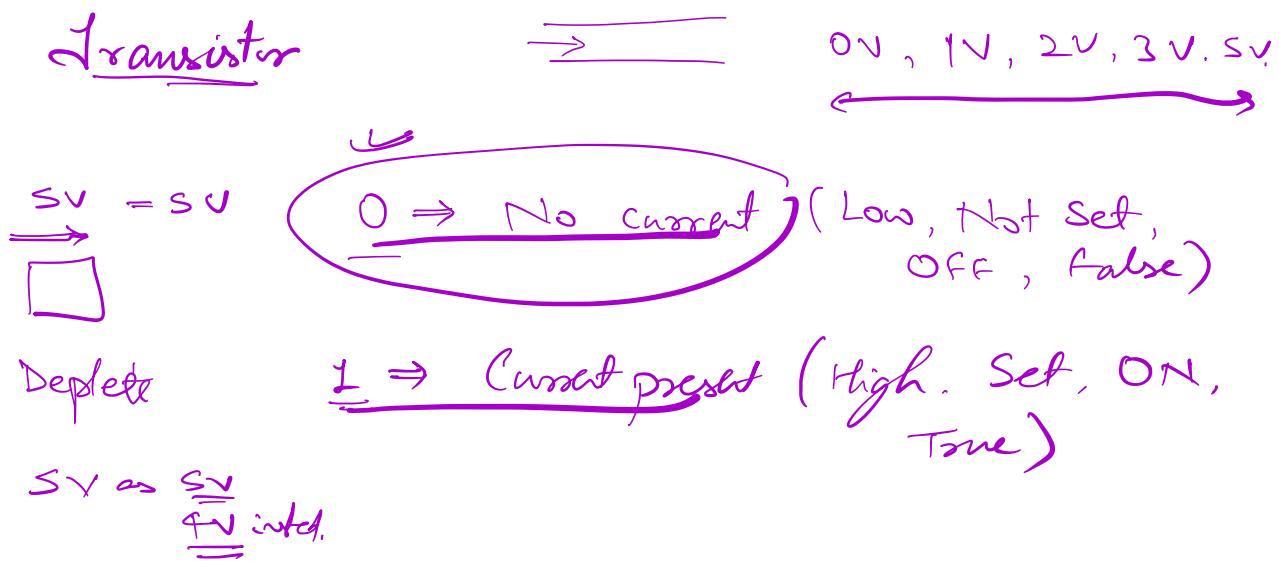
$$= \underline{5} + \underline{9} + \underline{0} + \underline{1}$$

$$= \underline{\underline{(64)}_{10}}$$

Binary Number System (2 unique digits)  
 $[0, 1]$   
 Base = 2

Eg  $\Rightarrow ( \underline{\underline{1}} \underline{\underline{0}} \underline{\underline{1}} \underline{\underline{1}} \underline{\underline{0}} )$

$$\begin{aligned}
 & 1 \times (2)^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\
 & = 16 + 0 + 4 + 2 + 0 \\
 & = (22)_{10}
 \end{aligned}$$



Decimal To Binary (2 logic)

$(28)_{10}$

$$\begin{array}{r}
 2 | 28 \\
 2 | 14
 \end{array}$$

$0 \Rightarrow 0^{\text{th}}$  digit

<del>2</del>	<del>7</del>
<del>2</del>	<del>3</del>
<del>2</del>	<del>1</del>
	0

0 → 1<sup>st</sup> digit  
 1 → 2<sup>nd</sup> digit  
 1 → 3<sup>rd</sup> digit  
 1 → 4<sup>th</sup> digit

11100

Ques      37 in binary

$$\begin{array}{r}
 2 | 37 \\
 2 | 18 \\
 2 | 9 \\
 2 | 4 \\
 2 | 2 \\
 2 | 1 \\
 \hline 0
 \end{array}
 = (100101)_2$$

↑      ←

Q      Binary of  $(25)_{10}$

$$\begin{array}{r}
 2 | 25 \\
 2 | 12 \\
 2 | 6 \\
 2 | 3 \\
 2 | 1 \\
 \hline 0
 \end{array}
 \rightarrow (11001)_2$$

↑      →

# Addition

## ▷ Decimal

mel

Y

1	2	3
4	5	6
7	8	9

$$\begin{array}{cccc}
 & 6 & 13 & 10 \\
 & \downarrow & \downarrow & \downarrow \\
 \underline{6+10} & \underline{13+10} & \underline{10+10} & \text{1 Bundle} \quad \Leftrightarrow \quad 6 \text{ pieces}
 \end{array}$$

16 % 10

## Add



Base = B



$$\begin{aligned}d &= S \% B \\c &= \underline{S / B}\end{aligned}$$

d = digit

# Binary Addition

$$\{0, 1\} \Rightarrow \text{8 bit} \leftarrow \begin{matrix} 0 \\ 1 \end{matrix} \begin{matrix} (\text{Not}) \\ (\text{Set}) \end{matrix}$$

$$\begin{array}{r}
 \text{0} & \text{1} & \overset{2/1}{\text{1}} & \text{0} & \text{0} \\
 \text{1} & \text{0} & \text{1} & \text{1} & \text{0} \\
 \text{0} & \text{0} & \text{1} & \text{1} & \text{1} \\
 \hline
 \text{1} & \text{1} & \underline{\text{3}} & \text{2} & \underline{\text{1}} \\
 & & & & \downarrow 10/02 \\
 & & & & 2/9
 \end{array}
 \Rightarrow \frac{11101}{1/2} = 0$$

$$R \Rightarrow \begin{matrix} 1 & 1 & 1 & \underline{1} & 0 & 1 & - \\ & \underline{3 \times 2} & 2 \times 2 & & & & \\ & 1 \times 2 & & & & & \\ 1 \times 2 & & 1/2 & = 0 & & & \\ & & 1/2 & = 0 & & & \end{matrix}$$

Ques

$$\begin{array}{r}
 a = \begin{smallmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{smallmatrix} \\
 b = \begin{smallmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{smallmatrix} \\
 \hline
 R \Rightarrow \begin{smallmatrix} 1 & 1 & 100 \\ 0 & 1 & 0 \end{smallmatrix}
 \end{array}$$

$$\begin{array}{ccc}
 & C & R \\
 2 \rightarrow 1 & & 0 \\
 2 \% 2 & & \\
 2/2 & & \\
 & C & R \\
 S = 1 & 0 & 1 \\
 1/2 = 0 & & \\
 2 = 1 \% 2 & &
 \end{array}$$

$$S=3 \quad C_4 \quad R_L$$

## Bit Manipulation (S, I, ^, =, &, <<, >>)



$a$	$b$	$a \otimes b$	$a \mid b$	$a^{\wedge} b$
0	0	0	0	0
0	1	0	1	1
1	0	0	1	1
1	1	1	1	0

$\wedge \Rightarrow (a \wedge b)$  is True (1) when both the bits are 1

$a \wedge b \wedge c \wedge d \wedge e \wedge f \dots \Rightarrow$  True if all bits are true.

$\mid \Rightarrow (a \mid b) \Rightarrow$  True if at least 1 is true

$a \mid b \mid c \mid d \mid e \mid f \dots \Rightarrow$  True if atleast one is not 0

$\wedge \rightarrow$  True if exactly 1 bit is True

$a \wedge b$

$a \wedge b \wedge c \wedge d \wedge e \wedge f \dots$  (in some time)

Integer  $\Rightarrow$  32 bits

INT (Assume # bits = 4)

a = 4, b = 3

$a \leq b$        $a = 0100$        $\Rightarrow 0$

$$b = \frac{0011}{0000}$$

$a|b$

$$\begin{array}{r} a = \\ b = \end{array} \begin{array}{r} 0100 \\ 0011 \\ \hline 0111 \\ 2^2 2^2 2^0 \\ 4+2+1 = 7 \end{array} \Rightarrow 7$$

$a^b$

$$\begin{array}{r} a = \\ b = \end{array} \begin{array}{r} 1111 \\ 0100 \\ \hline 0111 \end{array} \Rightarrow 7$$

Quiz

$$\begin{array}{r} a = 13 \\ b = 10 \end{array} \quad \begin{array}{r} 1101 \\ 1010 \\ \hline 1000 \\ 111 \end{array} \quad \Rightarrow 8$$

$$\begin{array}{r} 2 | 13 \\ 2 | 6 \\ 2 | 3 \\ 2 | 1 \\ 0 \end{array} \quad \begin{array}{r} 1101 \\ 1010 \\ \hline 1000 \\ 111 \end{array}$$

$$a|b = 1111 \Rightarrow 15$$

$$a^b = 0111 \Rightarrow 7$$

(4 digits)

Quiz

$$11 \Rightarrow \underline{\underline{1011}} -$$

$$10 \Rightarrow \underline{\underline{1010}} -$$

$$\begin{array}{r} 440 \\ 082 \end{array}$$

$$\begin{array}{r} 1 \\ \times 1 \\ \hline 0 \end{array} = \frac{1011}{0001} \Rightarrow 11$$

Somdatta

$$\begin{array}{r} 1011 \\ \quad \quad \quad \downarrow \\ \begin{array}{r} 1010 \\ 0001 \\ \hline 1011 \end{array} \Rightarrow \underline{\underline{11}} \end{array}$$

$$(a_5 a_4 a_3 a_2 a_1 a_0)_2 = \begin{cases} 0 & (\text{Even}) \\ 1 & (\text{Odd}) \end{cases} \quad (\text{6 digit number})$$

$$a \times \underline{\underline{2^5}} + b \times \underline{\underline{2^4}} + c \times \underline{\underline{2^3}} + d \times \underline{\underline{2^2}} + e \times \underline{\underline{2^1}} + f$$

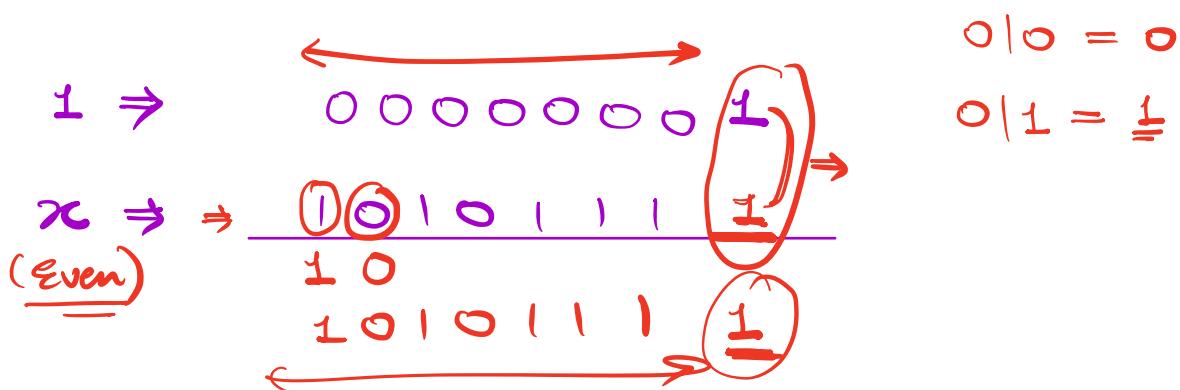
$$\underline{\underline{2^4}} \left( a \times \underline{\underline{2^4}} + b \times \underline{\underline{2^3}} + c \times \underline{\underline{2^2}} + d \times \underline{\underline{2^1}} + e \right) + f$$

Even

$$\underline{\underline{2^4}} + f (1/0)$$

$$f = 1 \Rightarrow \underline{\underline{2^4+1}} \quad \text{Even} + 1 = \text{odd}$$

$$f = 0 \Rightarrow \underline{\underline{2^4+0}} \Rightarrow \text{Even} + 0 = \text{Even}$$



$$x \Rightarrow \text{Even} + \text{Last 6 bits (0)} \\ + \text{Last 5 bits (1)}$$

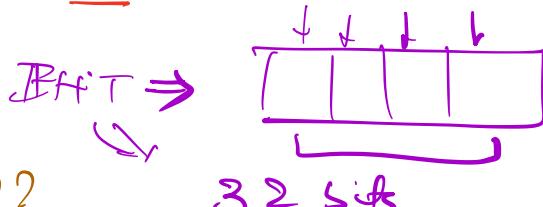
$$x|1 \Rightarrow \underline{\underline{x+1}} \quad (\text{if } x \text{ is even})$$

$x$  is odd

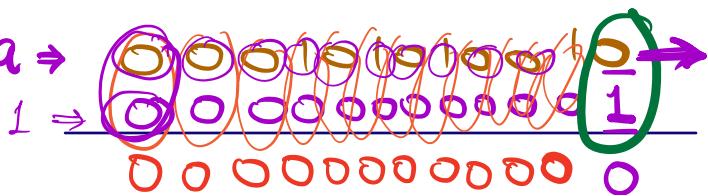
$$x|1 \Rightarrow \text{Same} \Rightarrow \underline{\underline{x}}$$

Quiz

$$\text{INT } \underline{\underline{a}} = \underline{\underline{x}} ??$$



$$\underline{\underline{a}} \underline{\underline{8}} \underline{\underline{1}} \quad 1 \Rightarrow 00000000 \quad \begin{matrix} 1 \\ \swarrow \searrow \end{matrix}$$

$\underline{\underline{a}}$  is Even  $a \Rightarrow$  

~~a~~  $\times \underline{80} \Rightarrow 0$

$$a \& 1 = 0$$

$a$  is odd

$$\begin{array}{r}
 00101010 \\
 00000000 \\
 \hline
 00000000
 \end{array}
 \quad 
 \begin{array}{r}
 1 \Rightarrow \\
 1 \Rightarrow \\
 1
 \end{array}$$

$a \& 1 = 1$

.00

21, 32

Given an integer  $a$ .

Find if its even or odd ??

~~( $a \& 1$ )~~  $\rightarrow$  0 if even  
1 if odd (More efficient)

$(a \% 2 == 0) \Rightarrow$

Doubt

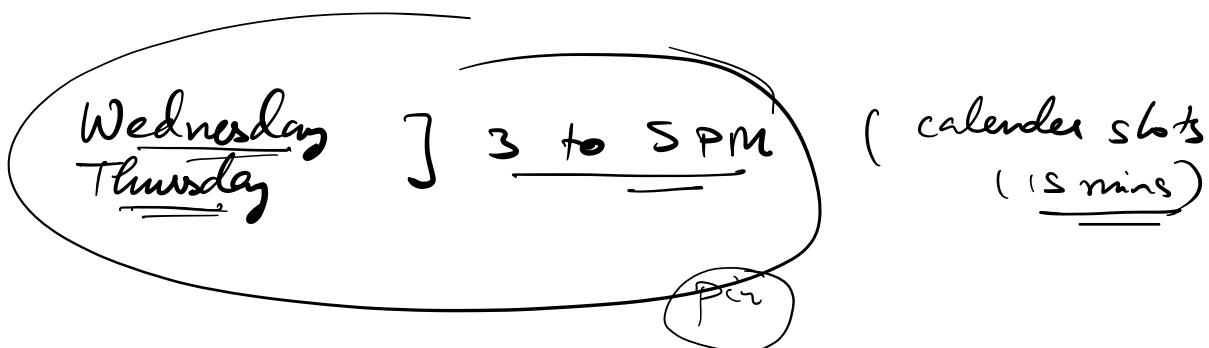
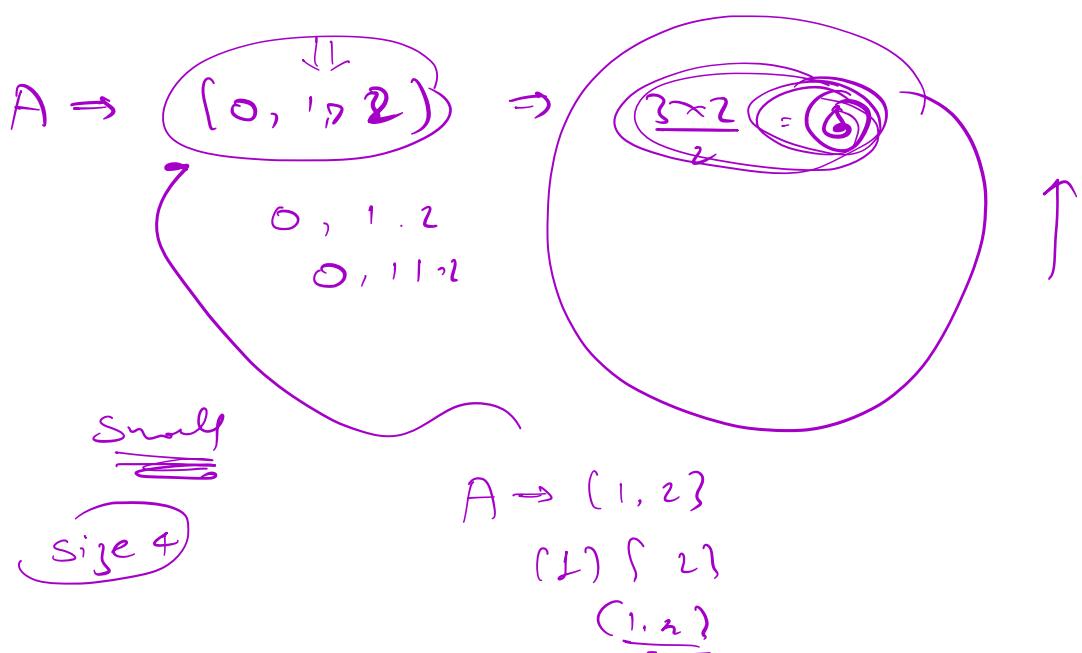
$\downarrow$   
 $\boxed{\quad | \quad | \quad |}$   
3258

24, 31 X

2411  $\Rightarrow$

10 of 10

A 81



Q

Array of size N

1 0 0 1 0 1 0 1 0

