TODO 5

$$p(X = x, \Psi, k | Y = y) \propto$$

$$\frac{1}{\sqrt{2\pi\sigma_{x_s}^2}} \exp\left\{-\frac{1}{2} \sum_{s \in \Omega} \left(\frac{y_s - \mu_{x_s}}{\sigma_{x_s}}\right)^2\right\}$$

$$\times \frac{\exp\left\{-\sum_{s \in \Omega} \left(\beta_{x_s}^{(0)} + \beta^{(1)}V\left(x_s, \eta_s\right)\right)\right\}}{\prod_{s \in \Omega} \sum_{c \in \Lambda} \exp\left\{-\left(\beta_c^{(0)} + \beta^{(1)}V\left(c, \eta_s\right)\right)\right\}}$$

$$\times p_r\left(\beta^{(1)}\right) p_r(k) \prod_{c \in \Lambda} p_r\left(\mu_c\right) p_r\left(\sigma_c\right) p_r\left(\beta_c^{(0)}\right)$$

$$(1)$$

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$$p\left(x_{s}=c|\ y_{s},\eta_{c},\Psi_{c}\right) \propto \frac{1}{\sqrt{2\pi\sigma_{c}^{2}T_{t}}} \exp\left\{-\frac{1}{T_{t}}\left[\frac{1}{2}\left(\frac{y_{s}-\mu_{c}}{\sigma_{c}}\right)^{2}+\left(\beta_{c}^{(0)}+\beta^{(1)}V\left(c,\eta_{s}\right)\right)\right]\right\}$$
(2)

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$$p(\mu_c, \sigma_c | Y, X) \propto \prod_{s:x_s = c} p(y_s | \mu_c, \sigma_c) p_r(\mu_c) p_r(\sigma_c)$$

$$= \frac{1}{\sigma_c (2\pi \sigma_c^2 T_t)^{n_c}} \exp\left\{-\frac{1}{2T_t} \sum_{s:a_{s=c}} \left(\frac{y_s - \mu_c}{\sigma_c}\right)^2\right\}$$
(3)

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$$p\left(\beta_{c}^{(0)}, c \in \Lambda | X\right) = p\left(X | \beta_{c}^{(0)}, c \in \Lambda\right) p_{r}\left(\beta_{c}^{(0)}, c \in \Lambda\right)$$

$$= \prod_{(c \in \Lambda, \psi_{\eta})} \left(\frac{\exp(-\frac{1}{T_{t}} [\beta_{c}^{(0)} + \beta^{(1)} V(c, \eta)])}{\sum_{i \in \Lambda} \exp(-\frac{1}{T_{t}} [\beta_{i}^{(0)} + \beta^{(1)} V(i, \eta)])}\right)^{n_{(c, n)}}$$

$$= \prod_{(c \in \Lambda)} \left(\frac{\exp(-\frac{1}{T_{t}} [\beta_{c}^{(0)}])}{\sum_{i \in \Lambda} \exp(-\frac{1}{T_{t}} [\beta_{i}^{(0)}])}\right)^{n_{c}}$$

$$\times \prod_{(c \in \Lambda, \psi_{\eta})} \left(\frac{\exp(-\frac{1}{T_{t}} [\beta^{(1)} V(c, \eta)]) \sum_{i \in \Lambda} \exp(-\frac{1}{T_{t}} [\beta_{i}^{(0)}])}{\sum_{i \in \Lambda} \exp(-\frac{1}{T_{t}} [\beta_{i}^{(0)} + \beta^{(1)} V(i, \eta)]}\right)^{n_{(c, n)}}$$

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$$\beta_{c1}^{(0)} = \beta_c^{(0)} - T_t \ln (u_1) \quad \beta_{c2}^{(0)} = \beta_c^{(0)} - T_t \ln (1 - u_1)$$

$$\mu_{c1} = \mu_c - u_2 \sigma_c \sqrt{\frac{1 - u_1}{u_1}} \quad \mu_{c2} = \mu_c + u_2 \sigma_c \sqrt{\frac{u_1}{1 - u_1}}$$

$$\sigma_{c1}^2 = u_3 \left(1 - u_2^2\right) \sigma_c^2 \frac{1}{u_1} \quad \sigma_{c2}^2 = (1 - u_3) \left(1 - u_2^2\right) \sigma_c^2 \frac{1}{1 - u_1}$$
(5)

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$$\frac{\partial (\Psi_{c1}, \Psi_{c2})}{\partial (\Psi_{c}, u_1, u_2, u_3)} = \frac{T_t \sigma^2}{u_1^2 (1 - u_1^2) \sqrt{u_3 (1 - u_3)}}$$
(6)

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$$d\left(y^{(1)}, y^{(2)}\right) = \max_{k} \left| \hat{F}_1(k) - \hat{F}_2(k) \right| \tag{7}$$

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$$\frac{p(X = x^{+}, \psi^{+}, k^{+}|Y = y)}{p(X = x, \psi, k|Y = y)} \frac{1}{p_{\beta}(u_{1}) p_{\beta}(u_{2}) p_{\beta}(u_{3})} \times \frac{\partial (\Psi_{c1}, \Psi_{c2})}{p(\text{segmentation})} \left| \frac{1}{\partial (\Psi_{c}, u_{1}, u_{2}, u_{3})} \right|$$
(8)

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$$T_t = (1 + \alpha_1)^{\alpha_2 \left(1 - \frac{t}{N_t}\right)} \tag{9}$$