

Problem 1.4.3

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Verify that \mathbf{O} satisfies (1.4.1.1). \mathbf{O} is known as the circumcentre.

Solution: Let \mathbf{A} , \mathbf{B} , and \mathbf{C} be the vectors representing the vertices of triangle ABC, and let \mathbf{O} be the circumcentre of the triangle. We want to verify the

Calculating the required known vectors:

$$\frac{\mathbf{B} + \mathbf{C}}{2} = \begin{pmatrix} -\frac{7}{2} \\ \frac{1}{2} \end{pmatrix} \quad (6)$$

$$\mathbf{B} - \mathbf{C} = \begin{pmatrix} -1 \\ 11 \end{pmatrix} \quad (7)$$

Putting (2), (6) and (7) in condition (1):

$$\left(\begin{pmatrix} -\frac{53}{12} \\ \frac{5}{12} \end{pmatrix} - \begin{pmatrix} -\frac{7}{2} \\ \frac{1}{2} \end{pmatrix} \right)^T \begin{pmatrix} -1 \\ 11 \end{pmatrix} = 0 \quad (8)$$

$$\Rightarrow \begin{pmatrix} -\frac{11}{12} & -\frac{1}{12} \end{pmatrix} \begin{pmatrix} -1 \\ 11 \end{pmatrix} = 0 \quad (9)$$

$$\Rightarrow \frac{11}{12} - \frac{11}{12} = 0 \quad (10)$$

Thus, we showed that \mathbf{O} satisfies the required condition (1).

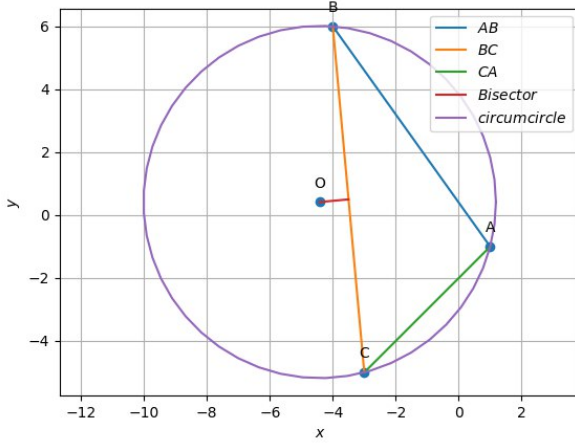


Fig. 0. Plot

condition (1.4.1.1) of the question:

$$\left(\mathbf{x} - \frac{\mathbf{B} + \mathbf{C}}{2} \right)^T (\mathbf{B} - \mathbf{C}) = 0 \quad (1)$$

Substituting the values obtained in the previous problem:

$$\mathbf{x} = \mathbf{O} = \begin{pmatrix} -\frac{53}{12} \\ \frac{5}{12} \end{pmatrix} \quad (2)$$

$$\mathbf{A} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad (3)$$

$$\mathbf{B} = \begin{pmatrix} -4 \\ 6 \end{pmatrix} \quad (4)$$

$$\mathbf{C} = \begin{pmatrix} -3 \\ -5 \end{pmatrix} \quad (5)$$