

1. Two microstrip lines are fabricated end-to-end on a 2mm-thick wafer of lithium niobate ( $\epsilon'_r = 4.8$ ). Line 1 has a width of 4mm; Line 2 (due to fabrication error) has a width of 5mm. Determine the power loss in dB for waves transmitted through the junction.

2. Find  $R$ ,  $L$ ,  $C$ , and  $G$  for a coaxial cable with

inner radius  $a = 0.25mm$ , Shield inner radius  $b = 2.50mm$ , Outer radius  $c = 3.30mm$ ,

$\epsilon_r = 2.0$ ,  $\mu_r = 1$ ,  $\sigma_c = 1.0 \times 10^7 \text{ S/m}$ ,  $\sigma = 1.0 \times 10^{-5} \text{ S/m}$ ,  $f = 300MHz$ .

3. A transmission line constructed from perfect conductors and an air dielectric is to have a maximum cross-section dimension of 8mm. The line is to be used at high frequencies. Specify the dimensions if it is

- (a) a two-wire line with  $Z_0 = 300$ ,
- (b) a planar line with  $Z_0 = 15$ ,
- (c) a 72 coax having a zero-thickness outer conductor.

Note: Refer Transmission lines with arbitrary cross section (any reference textbook)

4. Each conductor of a two-wire transmission line has a radius of 0.5mm; their center-to-center separation is 0.8cm. Let  $f = 150MHz$  and assume  $\sigma = \sigma_c = 0$ . Find the dielectric constant of the insulating medium if

- (a)  $Z_0 = 300$ ,
- (b)  $C = 20pF/m$ ,
- (c)  $v_p = 2.6 \times 10^8 \text{ m/s}$ .

5. The parameters of a certain transmission line operating at  $\omega = 6 \times 10^8 \text{ rad/s}$  are

$$L = 0.350 \mu\text{H/m}, \quad C = 40 \text{ pF/m}, \quad G = 0, \quad R = 15.0 \Omega/\text{m}.$$

Find the attenuation constant  $\alpha$ , the phase constant  $\beta$ , the wavelength  $\lambda$ , and the characteristic impedance  $Z_0$ .

6. A 50 lossless line of length  $0.4\lambda$  is operated at 300MHz. A load  $Z_L = 40 + j30 \Omega$  is connected at  $z = 0$ , and the Thevenin-equivalent source at  $z = -l$  is  $12\angle 0^\circ \text{ V}$  in series with  $Z_{Th} = 50 \Omega$ . Find:

- (a) the reflection coefficient  $\Gamma$ ,
- (b) the standing-wave ratio  $s$ ,
- (c) the input impedance  $Z_{in}$ .

7. Let  $Z_L = 100 + j150 \Omega$  and  $Z_0 = 100 \Omega$ . Find the shortest length  $d_1$  of a short-circuited stub and the shortest distance  $d$  that it may be located from the load to provide a perfect match on the main line to the left of the stub. Repeat for an open-circuited stub. Express all answers in wavelengths. (Refer Reading assignment: Smith chart)
8. Two lossless transmission lines having different characteristic impedances are to be joined end-to-end. The impedances are  $Z_{01} = 100 \Omega$  and  $Z_{03} = 25 \Omega$ . The operating frequency is 1GHz.
- Find the required characteristic impedance  $Z_{02}$  of a quarter-wave section that will impedance-match the joint.
  - The capacitance per unit length of the intermediate line is  $100\text{pF/m}$ . Find the shortest length in meters of this line that satisfies the matching condition.
  - The frequency is now doubled to 2GHz. Find the input impedance at the line-1-line-2 junction, seen by waves incident from line 1.
  - Under these conditions, evaluate the standing-wave ratio measured in line 1 and the fraction of incident power reflected back to the input.
9. A voltage pulse propagates within a lossless transmission line of characteristic impedance  $Z_0 = 50 \Omega$ . The pulse is Gaussian in shape, with voltage envelope

$$V(t) = V_0 e^{-t^2/(2T^2)}$$

where  $V_0 = 10V$  and  $T = 20\text{ns}$ . The pulse is incident on a  $100 \Omega$  load at the far end of the line. Determine the energy in joules that is dissipated by the load.

10. In the transmission line as shown in figure,  $Z_0 = 50 \Omega$ , and  $R_L = R_s = 25 \Omega$ . The switch is closed at  $t = 0$  and is opened again at time  $t = l/(4v)$ , thus creating a rectangular voltage pulse in the line. Construct an appropriate voltage reflection diagram for this case and use it to make a plot of the voltage at the load resistor as a function of time for  $0 < t < 8l/v$  (note that the effect of opening the switch is to initiate a second voltage wave, whose value is such that it leaves a net current of zero in its wake).

