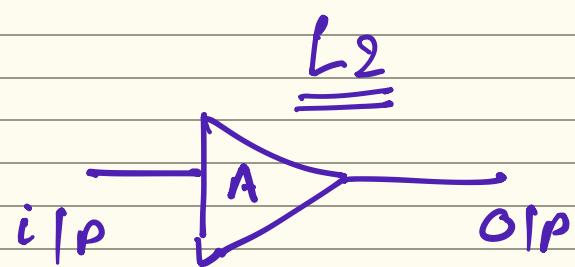


05/01/24

Analog Step

\Rightarrow



$$x \rightarrow A \rightarrow A \cdot x$$

#1

linearity

#

i/I/P

O/I/P

① : Vol.

Vol

② : Vol.

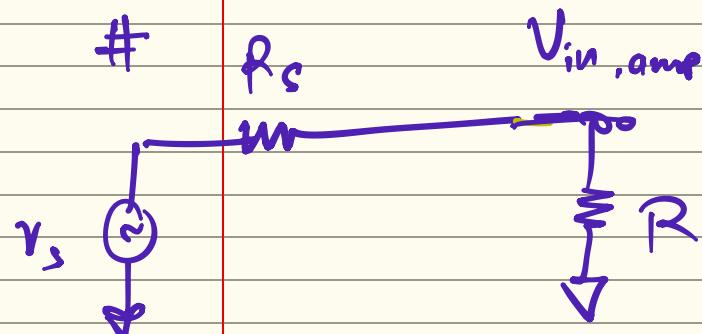
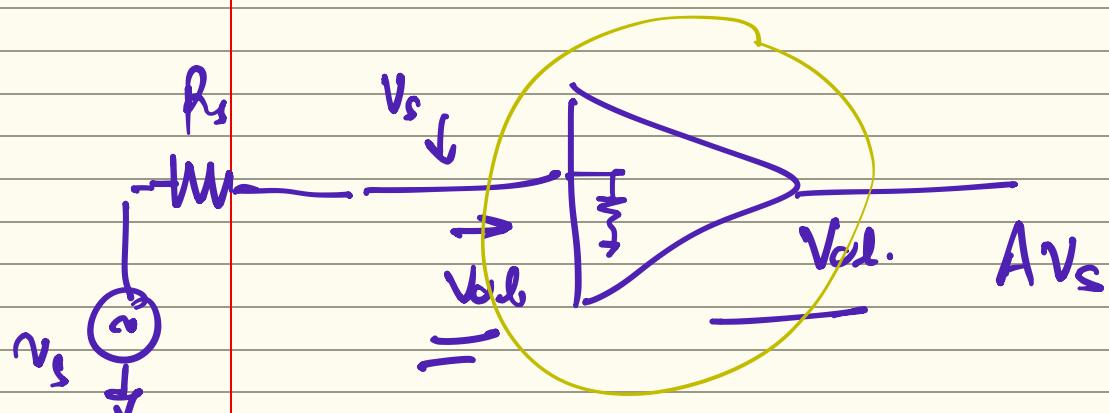
Current

③ : Current

Vol

④ : Current

Current



$$\boxed{V_{in, amp} = V_s}$$

\Rightarrow
 $V_{in, amp} \downarrow$

Either \Rightarrow

$$R_s = 0$$

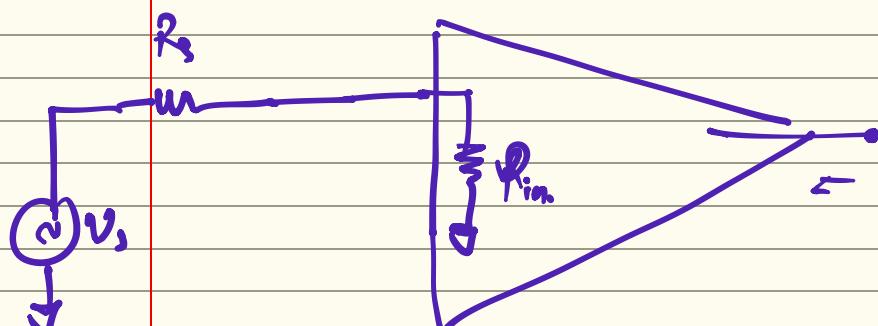
$$\text{or } R_{in,amp} = \infty$$

(1)

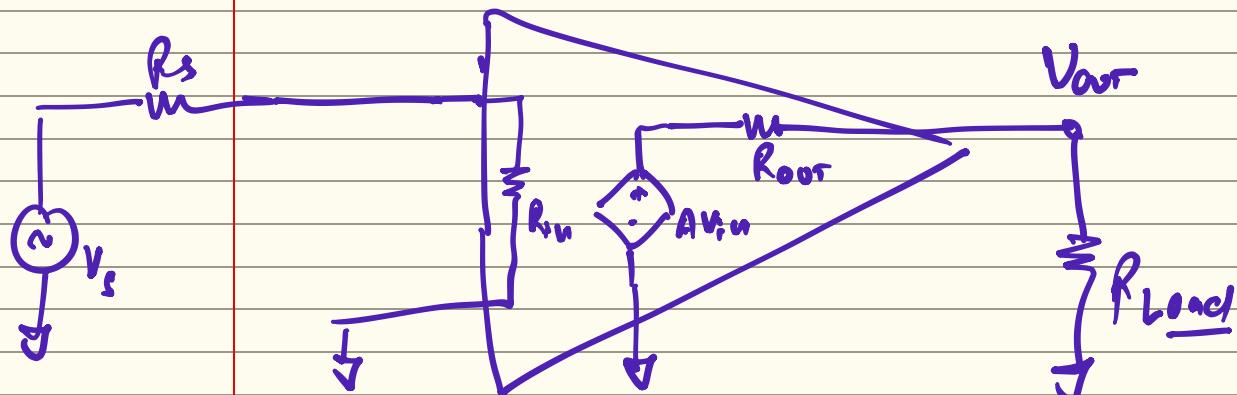
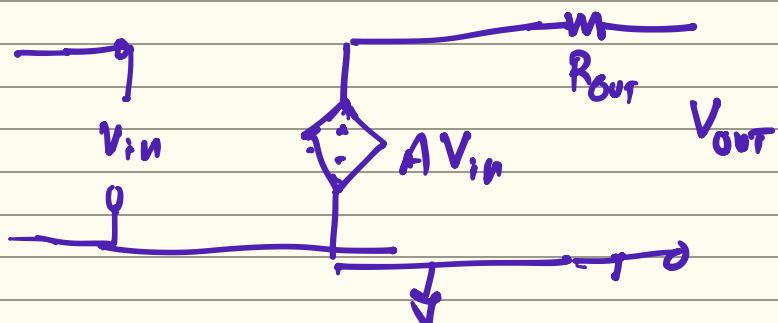
To sense V_{out} at i/p

$R_{in} \Rightarrow \infty$ (or very high)

$R_{in} \ggg R_s$



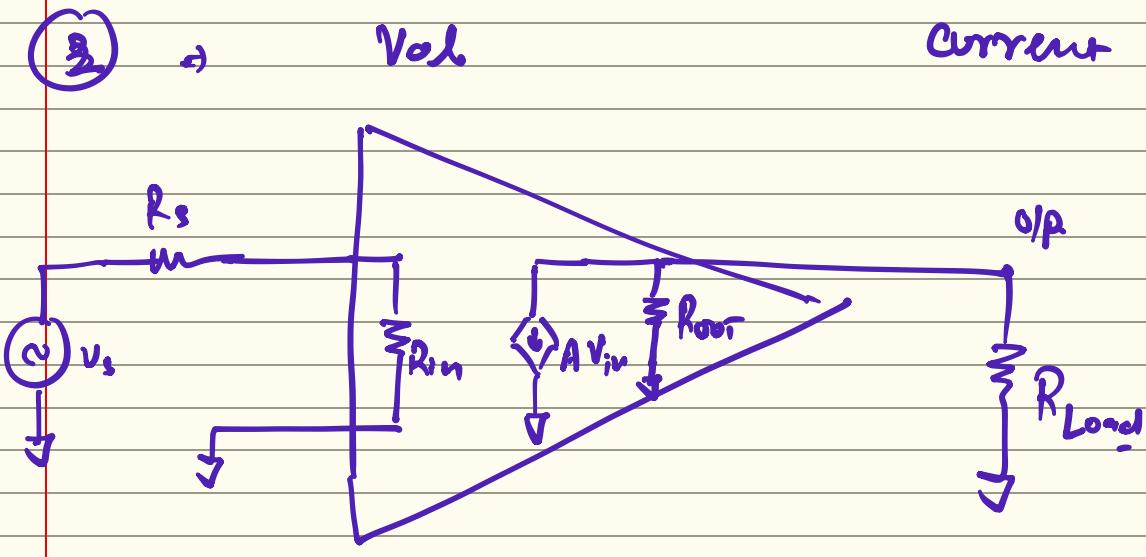
Vol. amp.



$R_{in} \rightarrow \infty$

$R_{out} \rightarrow$ as low as

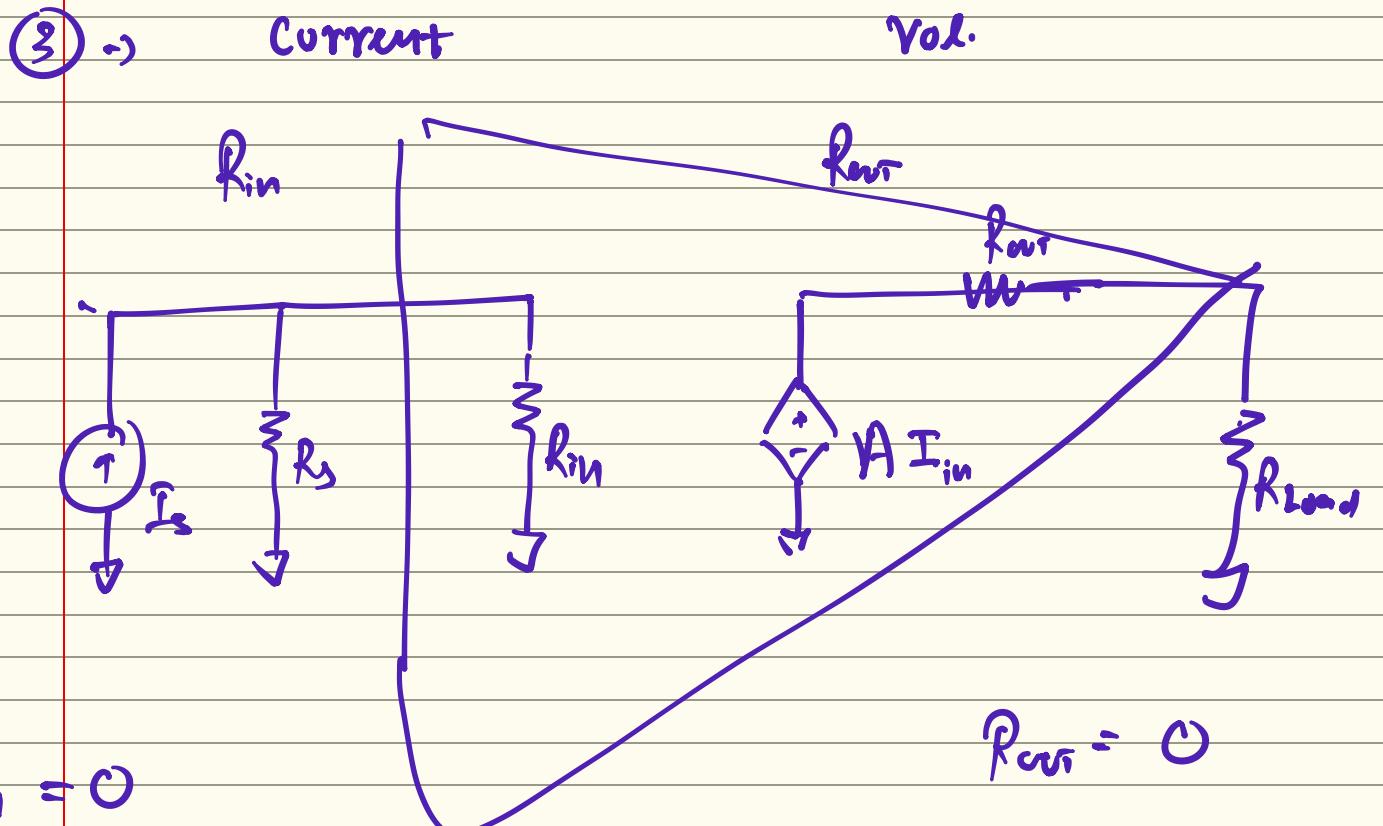
possible or
 0Ω



Vol.

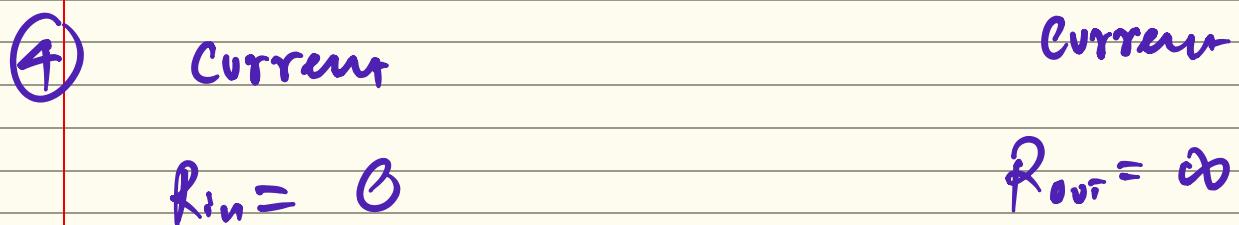
$$R_{in} \Rightarrow 0\Omega$$

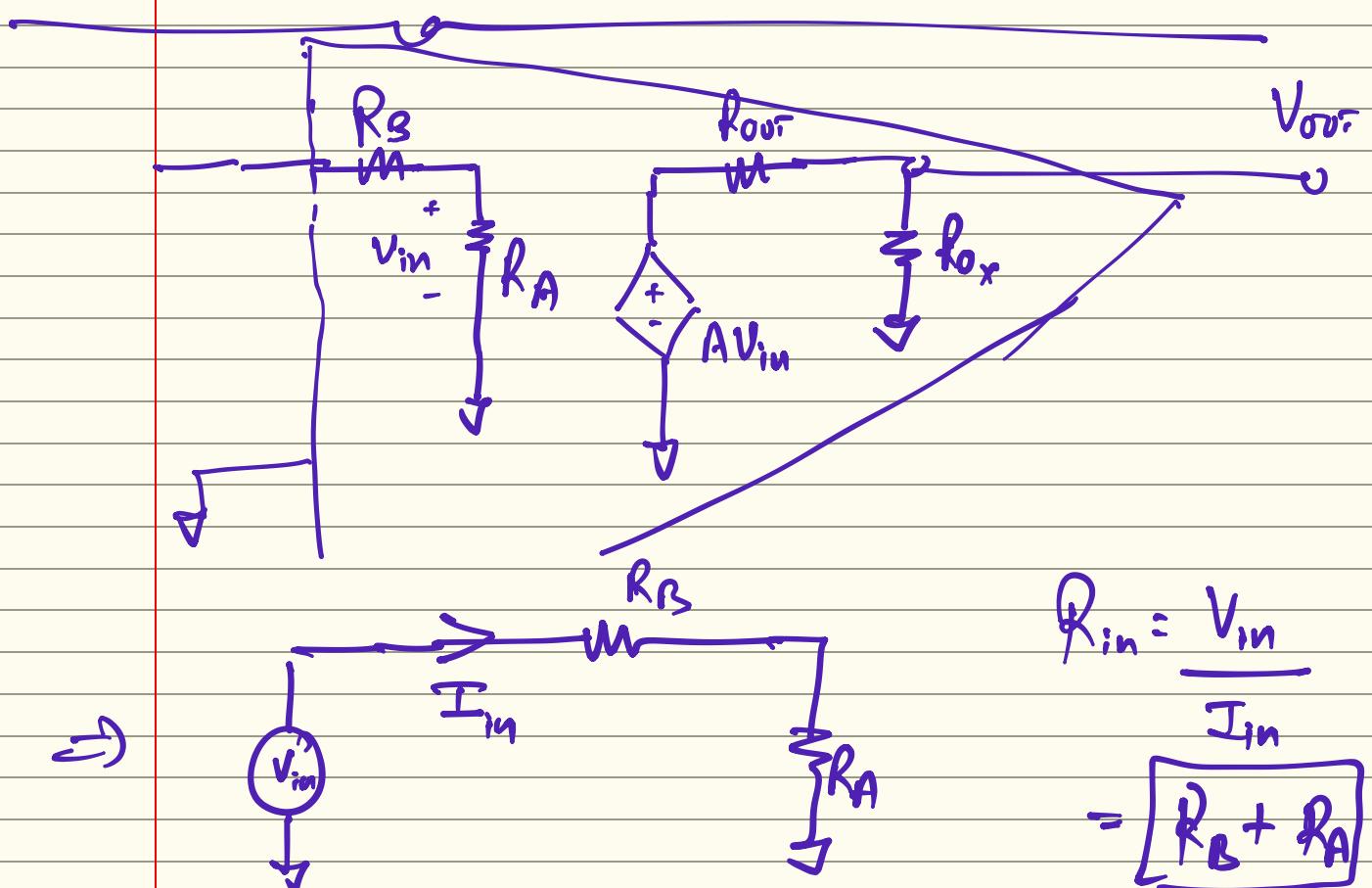
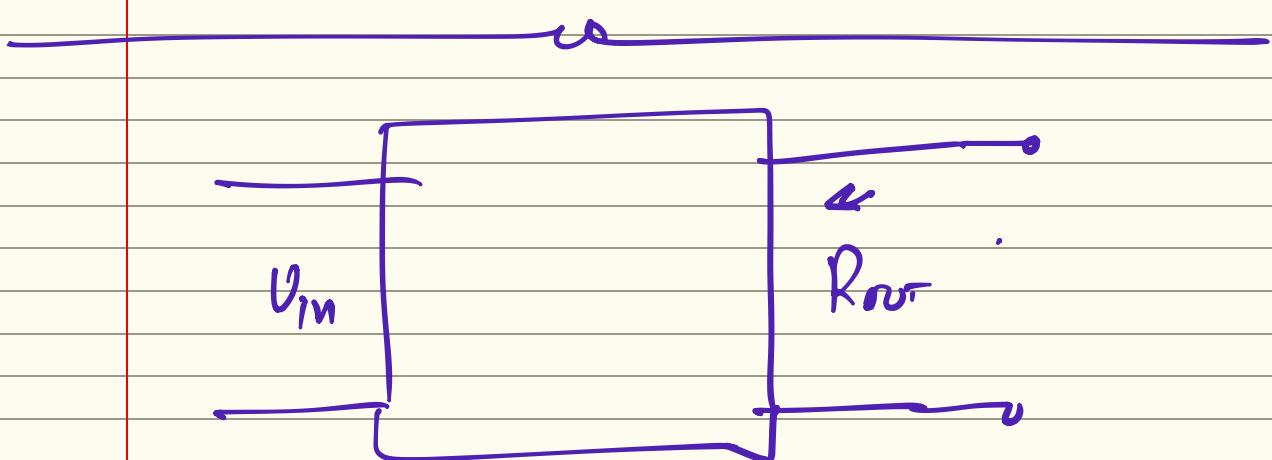
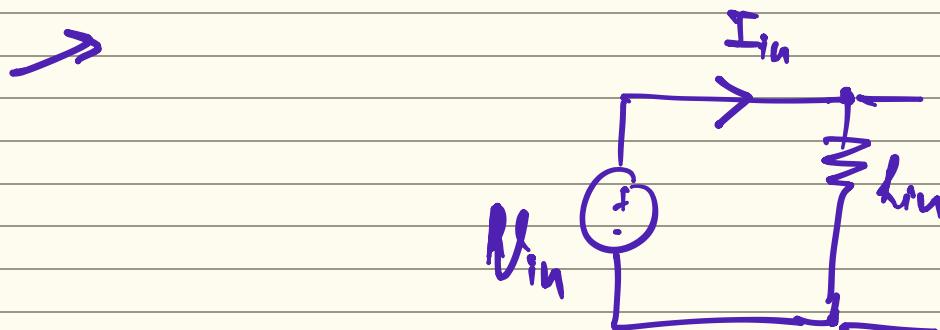
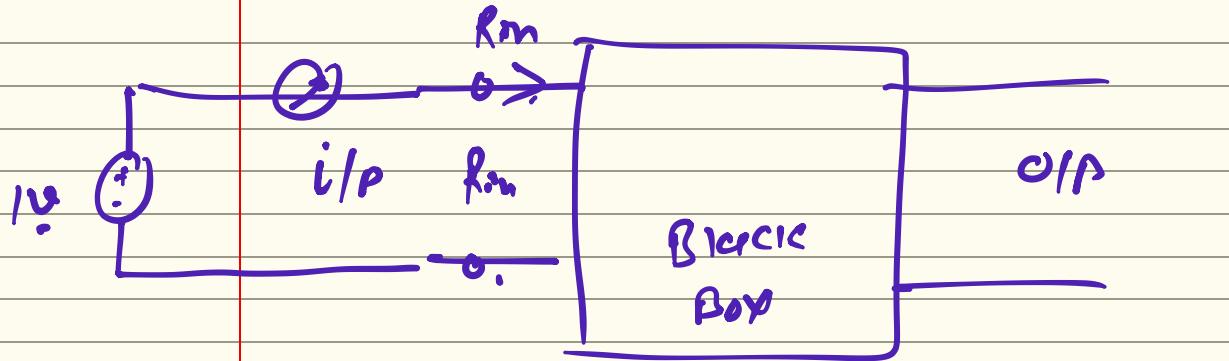
$$R_{out} \Rightarrow \infty$$

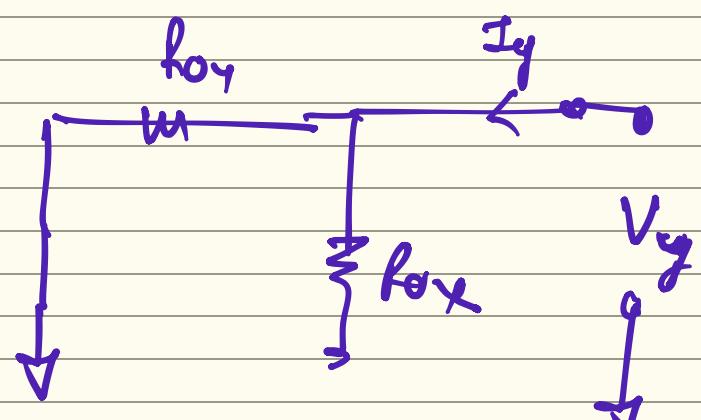
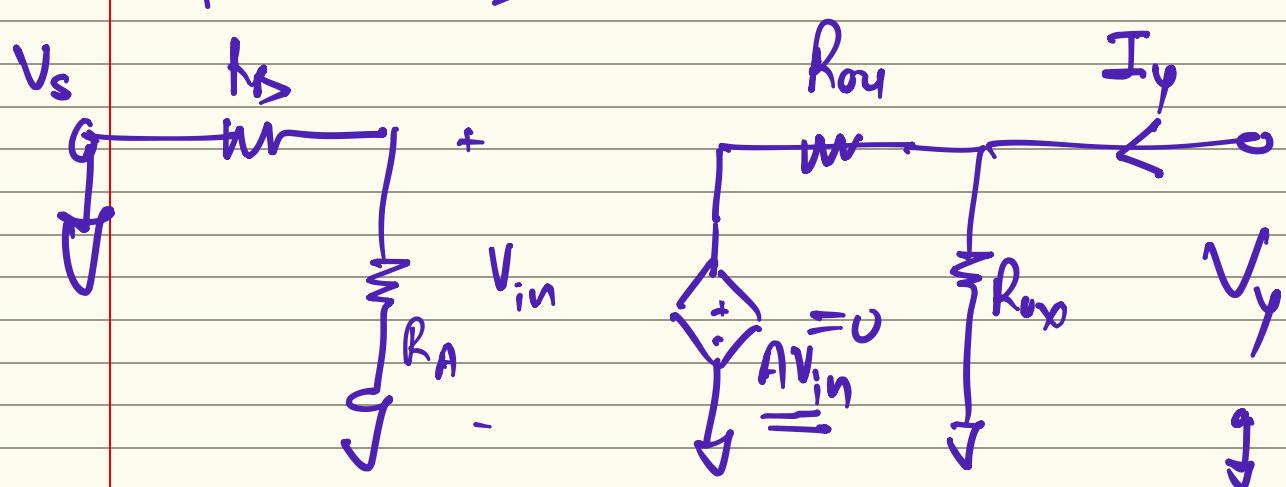
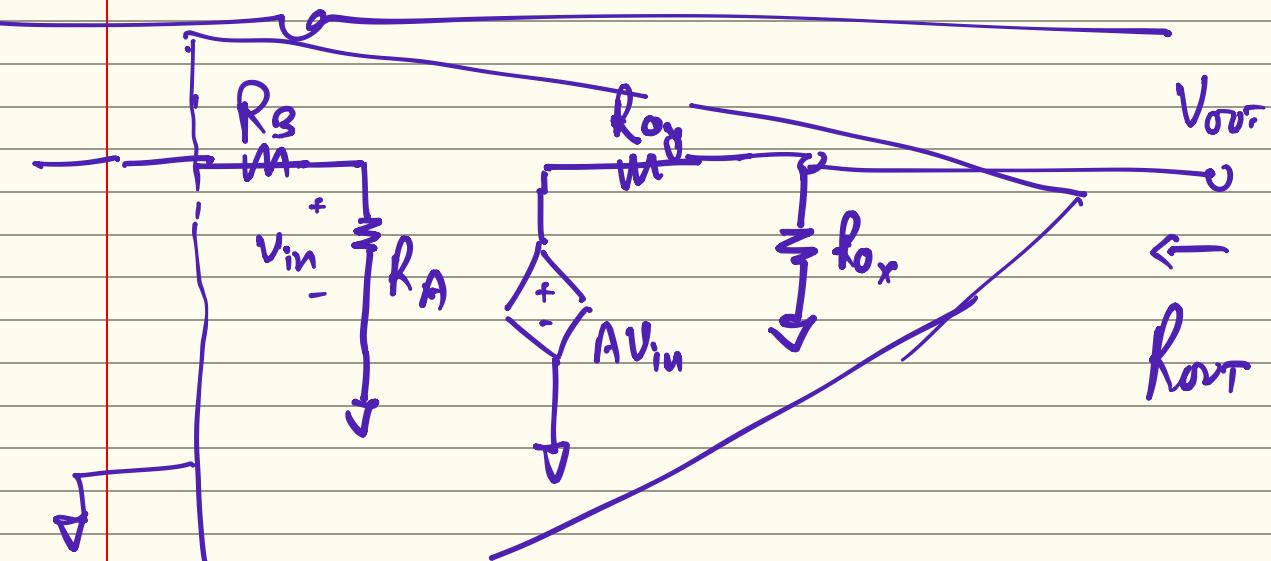


$$R_{in} = 0$$

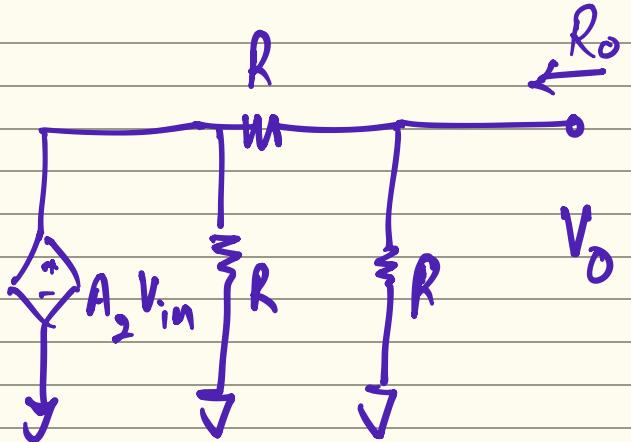
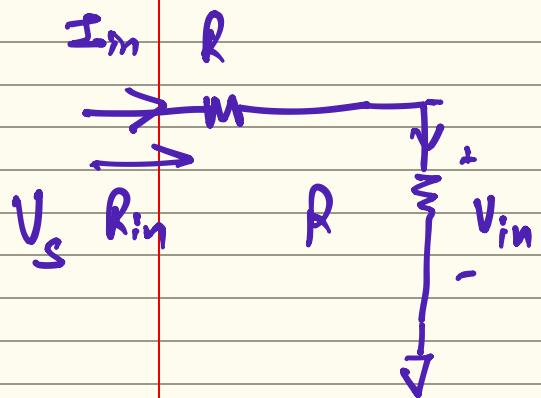
$$R_{out} = \infty$$







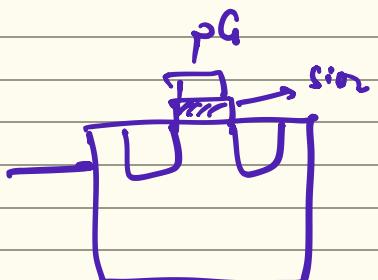
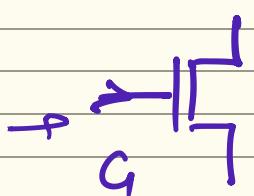
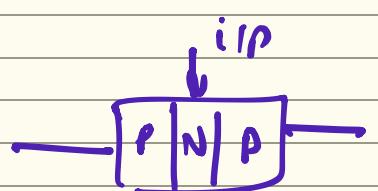
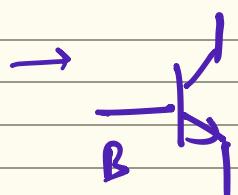
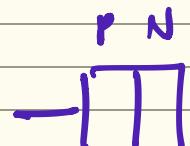
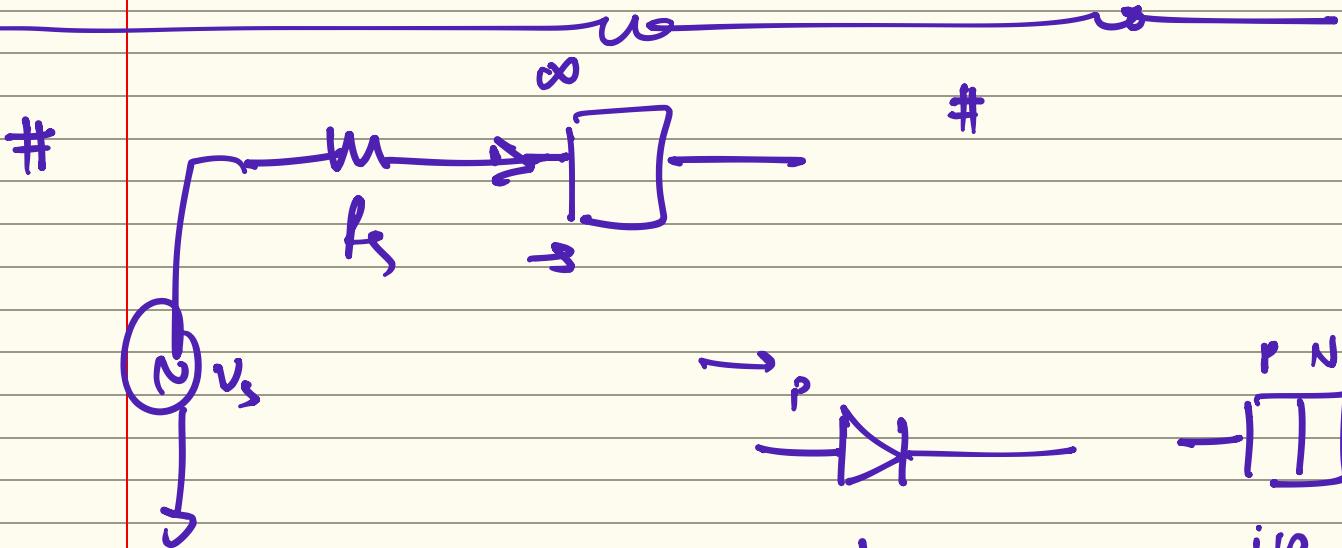
$$\frac{V_y}{I_y} = R_{Ox} \parallel R_{Oy} = R_{out}$$



\Rightarrow

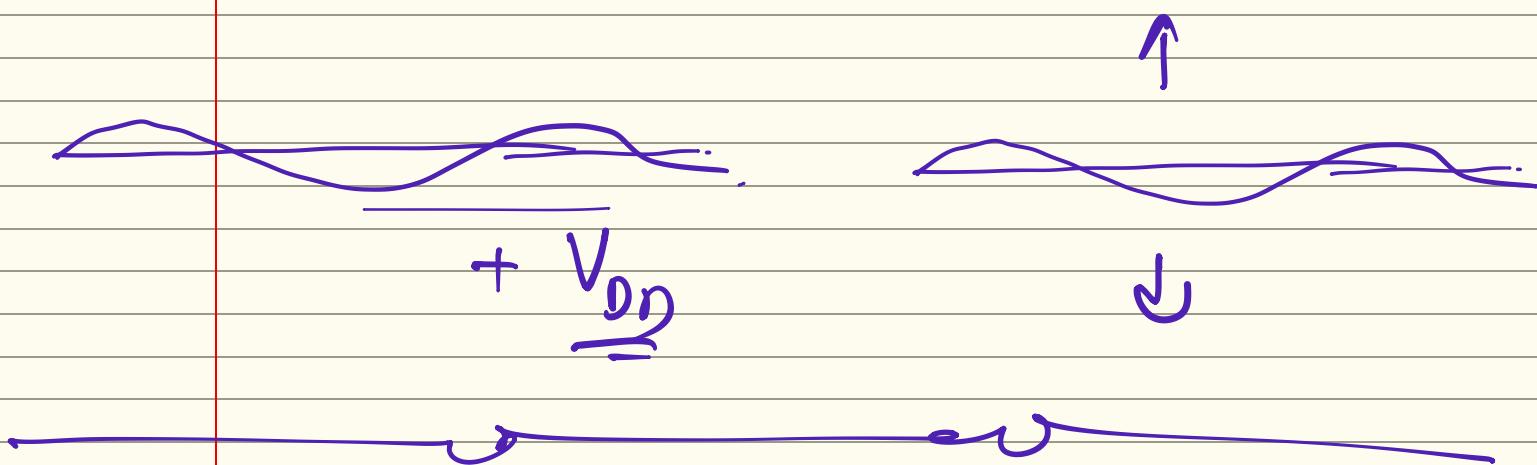
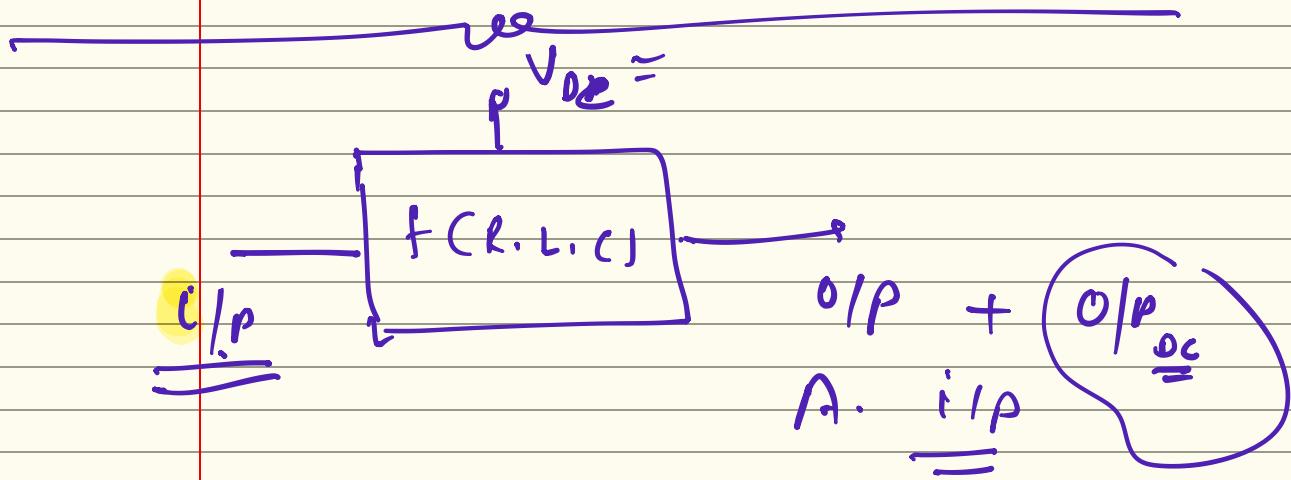
$$R_{in} = \frac{V_s}{I_{in}}$$

$$I_{in} =$$



R, L, C. : Diode
 - - - : BJT, Mos

#



#

Non Linear Elements

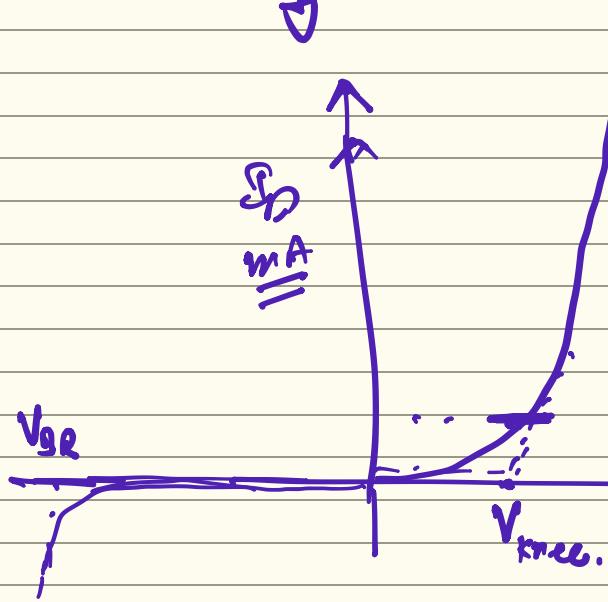
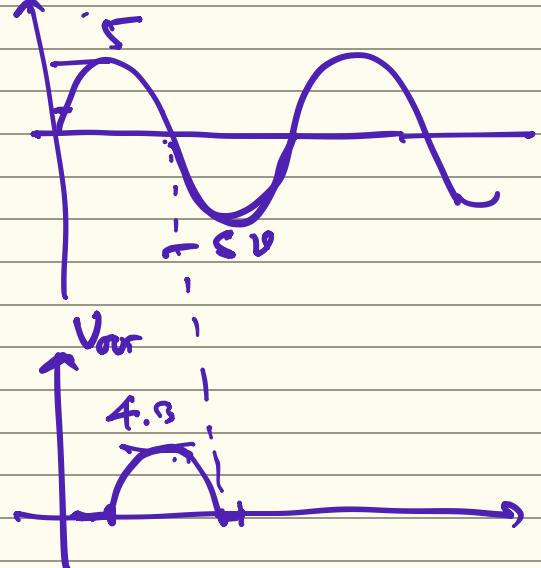
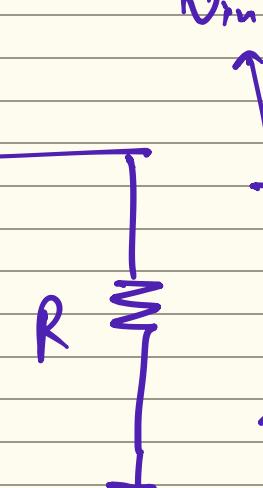
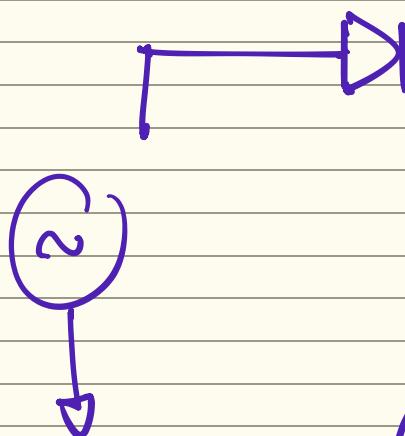
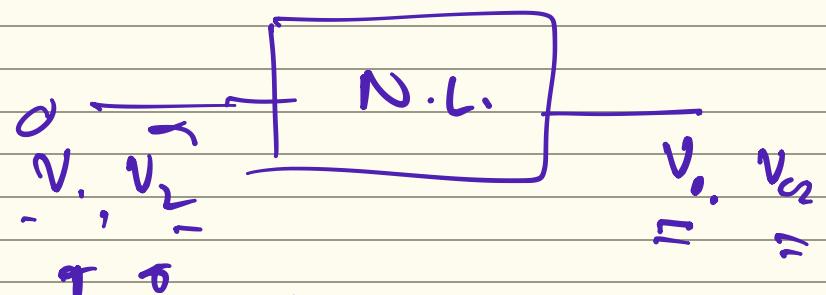
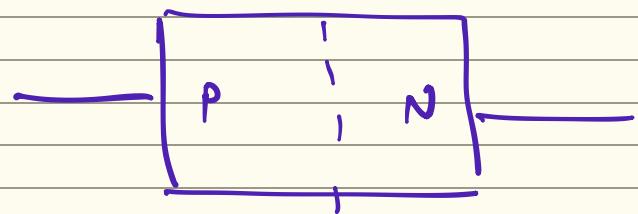
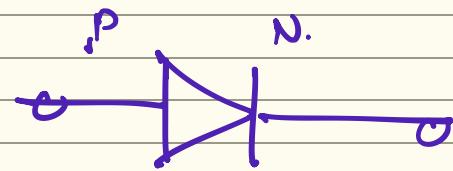
#

Transistor

Transistor

G

Diode



$$I_D = I_0 \left(e^{\frac{V_D}{V_T \cdot n}} - 1 \right)$$

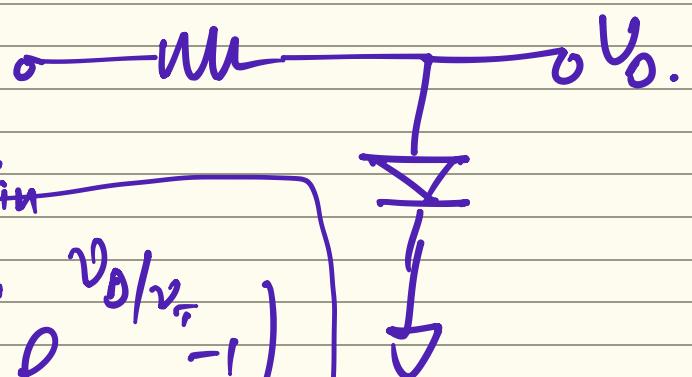
$$\underline{I_D} = I_0 \left(e^{\frac{V_o}{2V_T}} - 1 \right)$$

$$I \text{ mA} = \underline{I_D} \left(e^{0.7 \frac{V_o}{26mV}} - 1 \right)$$

$$\frac{10^{-3}}{e} = \underline{I_D} \left(e \right)$$

$$\boxed{I_D = 2 \text{ mA}}$$

#

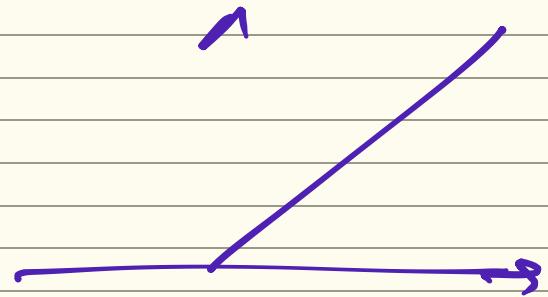


$$\frac{V_{in} - V_D}{R} = I_D \left(e^{\frac{V_D}{2V_T}} - 1 \right)$$

$$R = \text{given} \quad : \quad V_{in} =$$

$$V_D = 26mV \quad |$$

\Rightarrow



$$\frac{V_{in} - V_D}{R} = I_D (e^{V_D/v_r} - 1)$$

$$\frac{V_{in} - V_D}{R} = f(V_D)$$

$$\frac{V_{in} + \Delta V_{in}}{R} - \left(\frac{V_D + \Delta V_D}{R} \right) = f(V_D + \Delta V_D)$$

$$f(V_D + \Delta V_D) = f(V_D) + \Delta V_D f'(V_D)$$

$$+ (\Delta V_D)^2 \underbrace{\frac{f''(V_D)}{2}}_{\textcircled{I}} + \underbrace{\frac{(\Delta V_D)^3 f'''(V_D)}{3}}_{\dots} + \dots$$

H.O.T

when ΔV_D is
very small

hence, $\Delta V_D \gg (\Delta V_D)^2 \gg (\Delta V_D)^3 \dots$

higher order terms can be neglected

$$f(V_D + \Delta V_D) = f(V_D) + \underbrace{\Delta V_D f'(V_D)}_{\text{II}}$$

if II term is a linear one the whole equation becomes linear.

i.e. \rightarrow

$$\frac{V_{in} + \delta V_{in}}{R} - \frac{V_D + \delta V_d}{R} = I_0 (e^{\frac{(V_0 + \delta V_d)}{2V_T}} - 1)$$

$$\approx \frac{V_{in} - V_D}{R} + \frac{\delta V_{in} - \delta V_d}{R} = I_0 \left(e^{\frac{V_0}{n \cdot V_T}} - 1 \right) + \frac{I_0 e^{\frac{V_0}{2V_T}}}{2V_T} \cdot \delta V_d + H.O.T.$$

If δV_d is very small \Rightarrow H.O.T. could be ignored.

$$\Rightarrow \cancel{\frac{V_{in} - V_D}{R}} + \frac{\delta V_{in} - \delta V_d}{R} = \cancel{I_0} \Big|_{V_0} + \frac{I_0 \Big|_{V_0}}{2V_T} \cdot \delta V_d$$

$$\Rightarrow \frac{\delta V_{in} - \delta V_d}{R} = \frac{I_0 \Big|_{V_0}}{2V_T} \cdot \delta V_d$$

Now this is a linear eqnⁿ

\Rightarrow Hence, if we set \downarrow Val. & current (V_{in}, V_D) $(I_0 \Big|_{V_0})$

for a non linear device & then apply small incremental change $(\delta V_{in}, \delta V_d)$ then

System could be treated as linear for

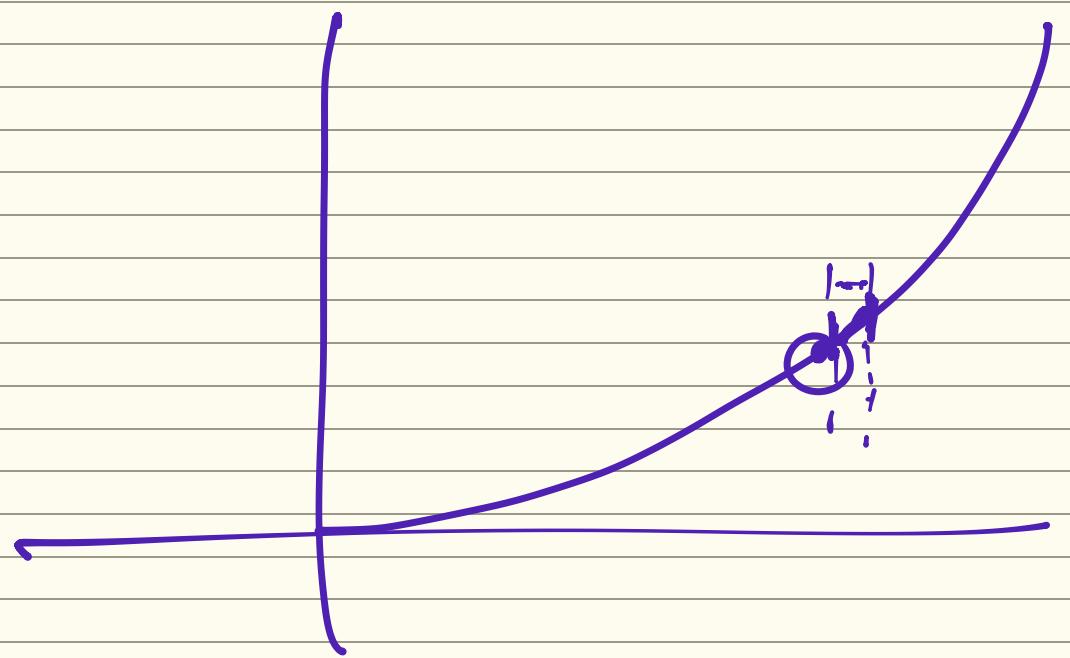
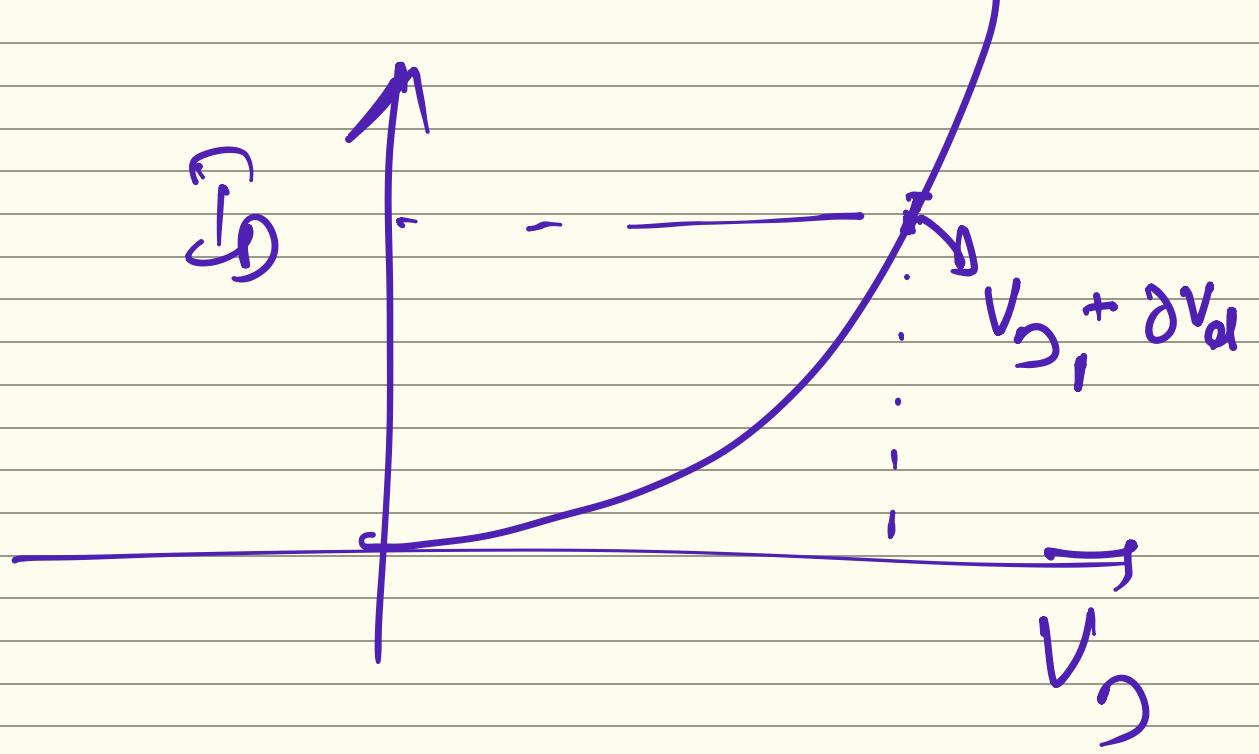
Small range of those small incremental

Changes for them H.O. non linear terms are

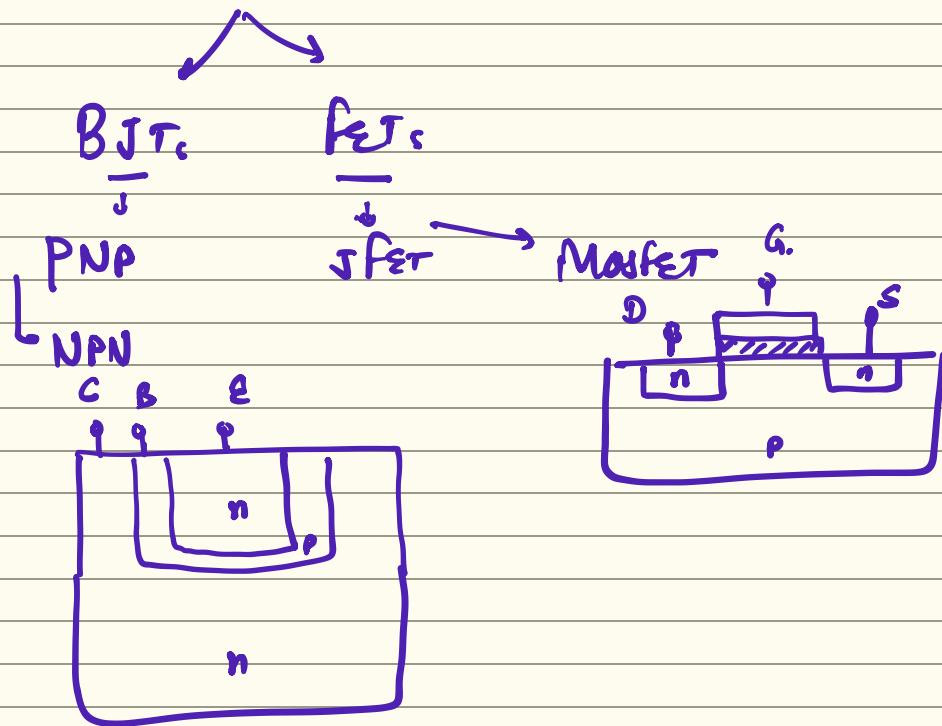
Negligible. For this range of small signal

i/p a non linear system could be

Consider as a linear only.



Transistors



$$I_{mos} = \frac{\mu C_o n}{2} \frac{w}{L} (V_{gs} - V_m)^2 \quad ; \quad I_{ssr} = I_0 (e^{\frac{V_{in}}{V_T}} - 1)$$

$$\frac{\partial I_0}{\partial V_{in}} = \frac{\partial I_{mos}}{\partial V_{gs}} = G_{m,mos} = \frac{\mu C_o n}{L} \frac{w}{L} (V_{gs} - V_m) \quad ; \quad \frac{\partial I_{in}}{\partial V_{in}} = \frac{\partial I_{BJT}}{\partial V_{in}} = G_{m,BJT}$$

$$G_{m,mos} \approx \frac{2 I_{mos}}{V_{gs} - V_m} \quad ; \quad = \frac{I_0}{V_T} e^{\frac{V_{in}}{V_T}}$$

$$V_{gs} - V_m = 150 - 250 \text{ mV}$$

$$\approx \frac{I_{BJT}}{V_T}$$

$$V_T = 26 \text{ mV} @ 27^\circ\text{C}$$

Hence, for some I

$$G_{m,BJT} > G_{m,mos}$$

Which makes BJT a better val. amplifier as Val. amplification is directly proportional to the transconductance of an amplifier.

MOS

- ⇒ More Junctions →
- More parasitic Cap →
- Lesser intrinsic cutoff freq (f_T) → less speed.

BJT

- only 2 junctions →
- better f_T → better speed.

- ⇒ Base Current is non zero (in μA)
- Hence, i/p power is significant.

- ⇒ Gate current is zero (at mos)
- Hence i/p power (at gate) is zero.

- ⇒ Not so compatible for IC fabrication steps
- Hence, Not a suitable candidate for VLSI Tech.

- ⇒ Fabrication steps are compatible for IC design.
- A good candidate for VLSI tech.

(a)