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Candidate surname		Other names
Centre Number Candidate No		
Pearson Edexcel Inter Thursday 8 June 202		al GCSE
Tharsaay o June 202		
Morning (Time: 2 hours)	Paper reference	4PM1/02R
Further Pure Mat PAPER 2R	hema	tics

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
 - there may be more space than you need.
- You must NOT write anything on the formulae page.
 Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶



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International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times \text{slant height}$

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to *n* terms, $S_n = \frac{n}{2} [2a + (n-1)d]$

Geometric series

Sum to *n* terms,
$$S_n = \frac{a(1-r^n)}{(1-r)}$$

Sum to infinity, $S_{\infty} = \frac{a}{1-r} |r| < 1$

Binomial series

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$$
 for $|x| < 1, n \in \mathbb{Q}$

Calculus

Quotient rule (differentiation)

$$\frac{\mathrm{d}}{\mathrm{d}x} \left(\frac{\mathrm{f}(x)}{\mathrm{g}(x)} \right) = \frac{\mathrm{f}'(x)\mathrm{g}(x) - \mathrm{f}(x)\mathrm{g}'(x)}{\left[\mathrm{g}(x)\right]^2}$$

Trigonometry

Cosine rule

In triangle *ABC*: $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1	$f(x) = 2x^2 + (k+8)x + k$	
	Show that for all values of k , the equation $f(x) = 0$ has distinct real roots.	
		(4)
	(Total for Question 1 is	4 marks)

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2	Find	the	set	of	values	of <i>x</i>	for	which

(a)
$$2(x+1) < 5x - 2$$

(2)

(b)
$$3x^2 - x \le 10$$

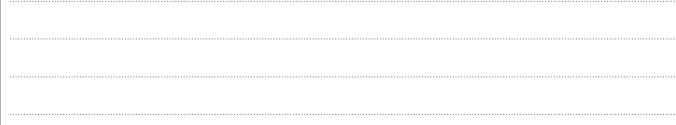
(3)

(c) **both**
$$2(x+1) < 5x - 2$$
 and $3x^2 - x \le 10$

(1)

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Question 2 continued
(Total for Question 2 is 6 marks)
(Total for Question 2 is o marks)



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(5)

Figure 1

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Figure 1 shows the sector *OAB* of a circle with centre *O*.

The radius of the circle is r cm and the angle AOB is θ radians.

 $r \, \mathrm{cm}$

The area of the sector is 675 cm²

(a) Show that the perimeter of the sector, P cm, is given by

$$P = 2r + \frac{1350}{r} \tag{3}$$

Given that r can vary,

(b) find, using calculus, the minimum value of PGive your answer in the form $a\sqrt{b}$ where a is an integer and b is a prime number.

(c) Justify that the value of P you found in (b) is a minimum. (2)



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Question 3 continued
(Total for Question 3 is 10 marks)



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4	O, A and B	are fixed	points	such that

$$\overrightarrow{OA} = 5\mathbf{i} + 7\mathbf{j}$$
 $\overrightarrow{AB} = a\mathbf{i} + 16\mathbf{j}$ and $\left| \overrightarrow{OB} \right| = 5\sqrt{29}$

(a) Find the possible values of a

(4)

Given that a > 0

(b) find a unit vector that is parallel to \overrightarrow{AB}

(2)

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Question 4 continued
(Total for Question 4 is 6 marks)
(Total for Question 4 is o marks)



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5	A particle <i>P</i> is moving along the <i>x</i> -axis.	
	At time t seconds, $t \ge 0$, the velocity, v m/s, of P is given by	
	$v = 2t^2 - 19t + 35$	
	(a) Find the acceleration of P when $t = 5$	
		(2)
	The particle comes to instantaneous rest at the points A and B at times t_1 seconds and t_2 seconds respectively, where $t_1 < t_2$	
	(b) Find the value of t_1 and the value of t_2	
		(2)
	(c) Use calculus to find the distance AB	(3)

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Question 5 continued
(Total for Question 5 is 7 marks)
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 $f(x) = 2x^2 + 5x - p$

The equation f(x) = 0 has roots α and β

Given that $\alpha^3 + \beta^3 = -\frac{215}{8}$

(a) find the value of p

(5)

Without solving the equation f(x) = 0

(b) form a quadratic equation, with integer coefficients, that has roots

$$\frac{\alpha+\beta}{\alpha^2}$$
 and $\frac{\alpha+\beta}{\beta^2}$

(5)

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Question 6 continued	



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Question 6 continued
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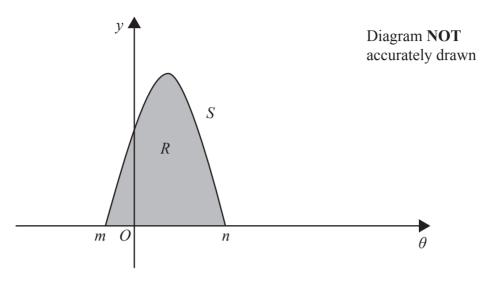


Figure 2

Figure 2 shows part of the curve S with equation $y = \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right)^{\frac{1}{2}}$

where $m \le \theta \le n$

The curve S meets the x-axis at the point with coordinates (m, 0) and at the point with coordinates (n, 0)

(a) Find the exact value of m and the exact value of n

(3)

The finite region R, shown shaded in Figure 2, is bounded by the curve S, and the x-axis in the region $m \le \theta \le n$

The region R is rotated through 2π radians about the theta-axis.

(b) Use calculus to find the exact volume of the solid generated.

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Question 7 continued		



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Question 7 continued
(Total for Question 7 is 7 marks)



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- 8 The points A and B have coordinates (1,5) and (9,9) respectively.
 - (a) Find an equation of line AB, giving your answer in the form ax + by + c = 0, where a, b and c are integers to be found.

(3)

The line l is perpendicular to AB and passes through the point X which lies on AB such that AX: XB = 3:1

(b) Show that an equation of *l* is y = -2x + 22

(5)

The point C has coordinates (6, p)

Given that C lies on l

(c) find the value of p

(1)

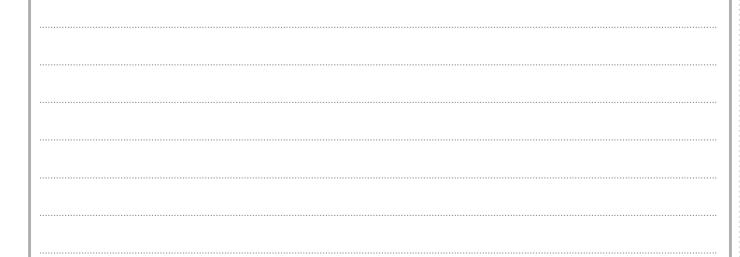
ABCD is a parallelogram where the x coordinate of D is negative.

(d) Find the coordinates of the point D

(3)

(e) Find the area of the parallelogram ABCD

(4)



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Question 8 continued	



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Question 8 continued	
	(Total for Question 8 is 16 marks)



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- 9 A curve C has equation $y = \frac{3-2x}{x+6}$ where $x \neq -6$
 - (a) Write down an equation of the asymptote to C that is parallel to the
 - (i) x-axis
- (ii) y-axis

(2)

- (b) Find the coordinates of the point where C crosses the
 - (i) x-axis
- (ii) y-axis

(2)

(c) Using the axes opposite, sketch the graph of C, showing clearly its asymptotes and the coordinates of the points where C crosses the coordinate axes.

(3)

(d) Show that the gradient of the tangent to C is always negative.

(3)

A tangent to C has equation $y = -\frac{3}{5}x + k$ where k > 0

(e) Find the value of k

(5)

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Question 9 continued	
<i>y</i> 4	
0	x



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Question 9 continued
(Total for Question 9 is 15 marks)



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10 Solve the equation	
$\log_4 x^3 + 8\log_x 64 = 22$	(7)
	(7)

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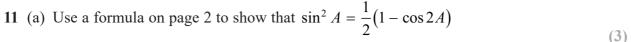
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Question 10 continued
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(3)

(b) Show that
$$\sin^4 x + \cos^4 x = \frac{3 + \cos 4x}{4}$$

(5)

(c) Hence solve, in degrees to one decimal place, the equation

$$8\sin^4\left(\frac{\theta}{2}\right) + 8\cos^4\left(\frac{\theta}{2}\right) = 5\sin(2\theta) + 6 \quad \text{for} \quad 0^\circ \leqslant \theta < 180^\circ$$
(4)

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Question 11 continued

