

Mark Scheme (Results)

January 2020

Pearson Edexcel International GCSE In Further Pure Mathematics (4PM1) Paper 01R

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January 2020
Publications Code 4PM1_01R_2001_MS
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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
 - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

Types of mark

- o M marks: method marks
- A marks: accuracy marks can only be awarded when relevant M marks have been gained
- o B marks: unconditional accuracy marks (independent of M marks)

Abbreviations

- o cao correct answer only
- o cso correct solution only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o awrt answer which rounds to
- o eeoo each error or omission

No working

If no working is shown then correct answers may score full marks
If no working is shown then incorrect (even though nearly correct) answers
score no marks.

With working

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question: eg. uses 252 instead of 255; follow through their working and deduct 2A marks from any gained provided the work has not been simplified. (Do not deduct any M marks gained.)

If there is a choice of methods shown, then award the lowest mark, unless the subsequent working makes clear the method that has been used

Examiners should send any instance of a suspected misread to review (but see above for simple misreads).

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

General Principles for Further Pure Mathematics Marking

(but note that specific mark schemes may sometimes override these general principles)

Method mark for solving a 3 term quadratic equation:

1. Factorisation:

$$(x^2+bx+c)=(x+p)(x+q)$$
, where $|pq|=|c|$ leading to $x=...$
 $(ax^2+bx+c)=(mx+p)(nx+q)$ where $|pq|=|c|$ and $|mm|=|a|$ leading to $x=...$

2. Formula:

Attempt to use the **correct** formula (shown explicitly or implied by working) with values for a, b and c, leading to x =

3. Completing the square:

$$x^{2} + bx + c = 0$$
: $(x \pm \frac{b}{2})^{2} \pm q \pm c = 0$, $q \ne 0$ leading to $x = ...$

Method marks for differentiation and integration:

1. <u>Differentiation</u>

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration:

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula:

Generally, the method mark is gained by **either**

quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values

or, where the formula is <u>not</u> quoted, the method mark can be gained by implication

from the substitution of <u>correct</u> values and then proceeding to a solution.

Answers without working:

The rubric states "Without sufficient working, correct answers <u>may</u> be awarded no marks".

General policy is that if it could be done "in your head" detailed working would not be required. (Mark schemes may override this eg in a case of "prove or show...."

Exact answers:

When a question demands an exact answer, all the working must also be exact. Once a candidate loses exactness by resorting to decimals the exactness cannot be regained.

Rounding answers (where accuracy is specified in the question)

Penalise only once per question for failing to round as instructed - ie giving more digits in the answers. Answers with fewer digits are automatically incorrect, but the is rule may allow the mark to be awarded before the final answer is given.

MARK SCHEME

Question number	Scheme	Marks
1	$\frac{\left(a+\sqrt{3}\right)}{\left(2-\sqrt{3}\right)} \times \frac{\left(2+\sqrt{3}\right)}{\left(2+\sqrt{3}\right)} = \frac{2a+\sqrt{3}\left(a+2\right)+3}{1}$	M1
	$2a + \sqrt{3}(a+2) + 3 = 11 + b\sqrt{3} \Rightarrow 11 = 2a+3, b = a+2$	M1M1
	Solves the equations in a and $b \Rightarrow a = 4$, $b = 6$ ALT	A1 [4]
	$\frac{a+\sqrt{3}}{2-\sqrt{3}} = 11 + b\sqrt{3} \Rightarrow a+\sqrt{3} = (2-\sqrt{3})(11+b\sqrt{3})$	{M1}
	$\Rightarrow a + \sqrt{3} = (22 - 3b) + (2b - 11)\sqrt{3}$	(M1) (M1)
	$\Rightarrow a = 22 - 3b \text{ and } 1 = 2b - 11$	{M1}{M1}
	Solves the equations in a and $b \Rightarrow a = 4, b = 6$	{A1} [4]
	T	otal 4 marks
(a)		
M1	Multiply by $\frac{\left(2+\sqrt{3}\right)}{\left(2+\sqrt{3}\right)}$	
M1	For either $11 = 2a + 3$ or $b = a + 2$	
M 1	For $11 = 2a + 3$ and $b = a + 2$	
A1	a = 4, b = 6	
M1		
M1 M1 M1 A1 ALT M1	Multiply by $\frac{\left(2+\sqrt{3}\right)}{\left(2+\sqrt{3}\right)}$ For either $11=2a+3$ or $b=a+2$	[4]

Question number	Scheme	Marks
2 (a)	$7+4x-x^2=11-(x-2)^2$	M1A1A1
	[a = 11, b = 1, c = -2]	[3]
	ALT	
	$7 + 4x - x^2 = a - b(x^2 + 2cx + c^2)$	{M1}
	$a-bc^2 = 7$ $b=1$ $bc = 4$ So $a = 11, b = 1, c = -2$	{A1}{A1}
	$7 + 4x - x^2 = 11 - (x - 2)^2$	[3]
(b)	(i) 11	B1ft
	(ii) 2	B1ft
	То	[2] tal 5 marks
(a)	10	tai S iliai Ks
M1	An attempt to factorise to make x^2 positive e.g. $-(x \pm p)^2 \pm q$	
A1	Complete the square to obtain an expression in the form $-(x \pm 2)^2 \pm a$	NB Any
AI	expression in this form will score M1A1	
A1	$11 - (x - 2)^2$ or $a = 11, b = 1, c = -2$	
ALT		
M1	Expands $a - b(x + c)$	
A1	$a - bc^2 = 7 \qquad b = 1 \qquad bc = 4$	
A1	$11 - (x - 2)^2$ or $a = 11, b = 1, c = -2$	
(b) (i)	Mark parts b(i) and b(ii) together	
B1ft	11 follow through their a	
(b) (ii) B1ft	2 follow through their a	
DIII	2 follow through their c NB Answer of Max = (2, 11) score B1B1	

Question number	Scheme	Marks
3(a)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 2\mathrm{e}^{2x}\left(x^2 + 1\right) + \mathrm{e}^{2x}\left(2x\right)$	M1A1A1 [3]
(b)	When $x = 0$ $\frac{dy}{dx} = 2 \times 1 \times 1 + 1 \times 0 = 2$ $y = e^{2 \times 0} (0 + 1) = 1$	B1B1
	$y-1=2(x-0) \Rightarrow y=2x+1$	B1 [3]
	<u>T</u> '0	tal 6 marks
(a) M1	Attempted use of the product rule. Sum of two terms (either way roun $x^n \to x^{n-1}$ (Condone e^{2x} instead of $2e^{2x}$) Once the correct answer is This mark may be implied by the sum of two terms with one of the two correct.	seen ISW.
A1	Either term correct	
A1	Both terms correct	
(b)		
B1	When $x = 0$ $\frac{dy}{dx} = 2$	
B 1	When $x = 0$ $y = 1$	
B1	y = 2x + 1	

Question number	Scheme	Marks
4 (a)	$f(2) = 2 \times 2^3 + a \times 2^2 + b \times 2 + 18 = 0$	M1
	$f'(x) = 6x^2 + 2ax + b \Rightarrow f'(2) = 6 \times 2^2 + 2 \times a \times 2 + b = 5$	M1M1
	4a + 2b + 34 = 0	1,111,11
	4a+b+19=0	A1
	$\Rightarrow b = -15, \ a = -1$	M1A1 [6]
(b)	$2x^2 + 3x - 9$	M1
	$x-2)2x^{3}-x^{2}-15x+18$	
	$2x^2 + 3x - 9 = (x+3)(2x-3)$	
	$\Rightarrow (x-2)(x+3)(2x-3)$	M1A1 [3]
(c)	$x=2, -3, \frac{3}{2}$	B2ft [2]
	Tot	al 11 marks
(a)		
M1	f(2) = 0 leading to an equation in a and b	
M1	Attempt to differentiate	
M1	f'(2) = 5 leading to an equation in a and b	
A1	4a + 2b + 34 = 0 and $4a + b + 19 = 0$	
M1	Solving simultaneously	
A1	$b = -15, \ a = -1$	
(b)	District Amo	
M1 M1	Dividing by $x-2$ to obtain a 3TQ	
A1	Factorising the 3TQ All 3 terms correct	
(c)	An 5 terms correct	
B2 ft	$x = 2, -3, \frac{3}{2}$ (B1 for 2 correct)	

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Question number	Scheme	Marks
ALT $\log_4 32 = a \implies 4^a = 32 \implies a = \frac{5}{2} *$ $\log_2 x - \log_4 32 + \frac{1}{4} \log_x 16 = 0$ Let $\log_2 x = y$ $y - \frac{5}{2} + \frac{1}{4} \left(\frac{\log_2 16}{\log_2 x} \right) = 0 \text{or} y - \frac{5}{2} + \frac{1}{\log_2 x} = 0$ $\implies y - \frac{5}{2} + \frac{1}{y} = 0$ $\implies y - \frac{5}{2} + \frac{1}{y} = 0$ $\implies y = \log_2 x = \frac{1}{2} \text{ or } 2$ $\implies y = \log_2 x = \frac{1}{2} \text{ or } 2$ $\implies x = 2^{\frac{1}{2}} = \sqrt{2} \text{and} x = 2^2 = 4$ M1A1 [7] Total 9 marks (a) M1 For $\log_4 32 = \frac{\log_3 32}{\log_2 4}$ or $\log_4 32 = \log_4 4^{\frac{5}{2}}$ or $\log_4 32 = \log_2 2^5$ ALT M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_a x = \frac{\log_b x}{\log_b a}$ or $\log_a b = \frac{1}{\log_b a}$ M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or $z = 2^2 = 4$ M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$		_	
Let $\log_2 x - \log_4 32 + \frac{1}{4} \log_x 16 = 0$ Let $\log_2 x = y$ $y - \frac{5}{2} + \frac{1}{4} \left(\frac{\log_2 16}{\log_2 x} \right) = 0$ or $y - \frac{5}{2} + \frac{1}{\log_2 x} = 0$ $\Rightarrow y - \frac{5}{2} + \frac{1}{y} = 0$ $\Rightarrow 2y^2 - 5y + 2 = 0$ $\Rightarrow y = \log_2 x = \frac{1}{2} \text{ or } 2$ $\Rightarrow x = 2^{\frac{1}{2}} = \sqrt{2} \text{and} x = 2^2 = 4$ M1 M1 For $\log_4 32 = \frac{\log_2 32}{\log_2 4}$ or $\log_4 32 = \log_4 4^{\frac{5}{2}}$ or $\log_4 32 = \log_{2^2} 2^5$ ALT M1 A1 cso (b) M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$		ALT	cso
$\Rightarrow 2y^{2} - 5y + 2 = 0$ $\Rightarrow (2y - 1)(y - 2) = 0$ $\Rightarrow y = \log_{2} x = \frac{1}{2} \text{ or } 2$ $\Rightarrow x = 2^{\frac{1}{2}} = \sqrt{2} \text{and} x = 2^{2} = 4$ M1 M1A1 [7] Total 9 marks (a) M1 For $\log_{4} 32 = \frac{\log_{2} 32}{\log_{2} 4}$ or $\log_{4} 32 = \log_{4} 4^{\frac{5}{2}}$ or $\log_{4} 32 = \log_{2^{2}} 2^{5}$ ALT M1 For $4^{a} = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_{a} x = \frac{\log_{b} x}{\log_{b} a}$ or $\log_{a} b = \frac{1}{\log_{b} a}$ M1 Forming a 3TQ A1 $2y^{2} - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_{2} x = \frac{1}{2}$ or $z = 2^{\frac{1}{2}} = \sqrt{2}$ or $z = 2^{\frac{1}{2}} = 4$	(b)	Let $\log_2 x = y$ $y - \frac{5}{2} + \frac{1}{4} \left(\frac{\log_2 16}{\log_2 x} \right) = 0 \text{or} y - \frac{5}{2} + \frac{1}{\log_2 x} = 0$	M1
$\Rightarrow x = 2^{\frac{1}{2}} = \sqrt{2} \text{and} x = 2^2 = 4$ $\Rightarrow x = 2^{\frac{1}{2}} = \sqrt{2} \text{and} x = 2^2 = 4$ $\text{M1A1} [7]$ Total 9 marks (a) $\text{M1} \text{For } \log_4 32 = \frac{\log_2 32}{\log_2 4} \text{ or } \log_4 32 = \log_4 4^{\frac{5}{2}} \text{ or } \log_4 32 = \log_2 2^5$ $\text{ALT} \text{M1} \text{For } 4^a = 32$ $\text{Obtains the given answer with no errors in the working}$ (b) $\text{M1} \text{Use of } \log_a x = \frac{\log_b x}{\log_b a} \text{ or } \log_a b = \frac{1}{\log_b a}$ $\text{M1} \text{Forming a 3TQ}$ $\text{M1} \text{Solving the 3TQ}$ $\text{M1} \text{For } y = \log_2 x = \frac{1}{2} \text{ or } 2$ $\text{M1} \text{Either } x = 2^{\frac{1}{2}} = \sqrt{2} \text{or } x = 2^2 = 4$		$\Rightarrow 2y^2 - 5y + 2 = 0$ $\Rightarrow (2y - 1)(y - 2) = 0$	
(a) M1 For $\log_4 32 = \frac{\log_2 32}{\log_2 4}$ or $\log_4 32 = \log_4 4^{\frac{5}{2}}$ or $\log_4 32 = \log_{2^2} 2^5$ ALT M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_a x = \frac{\log_b x}{\log_b a}$ or $\log_a b = \frac{1}{\log_b a}$ M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$		$\Rightarrow x = 2^{\frac{1}{2}} = \sqrt{2}$ and $x = 2^2 = 4$	M1A1 [7]
M1 For $\log_4 32 = \frac{\log_2 32}{\log_2 4}$ or $\log_4 32 = \log_4 4^{\frac{5}{2}}$ or $\log_4 32 = \log_{2^2} 2^5$ ALT M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_a x = \frac{\log_b x}{\log_b a}$ or $\log_a b = \frac{1}{\log_b a}$ M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	(a)		otal 9 marks
ALT M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_a x = \frac{\log_b x}{\log_b a}$ or $\log_a b = \frac{1}{\log_b a}$ M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	(a)	log 32 5	
ALT M1 For $4^a = 32$ Obtains the given answer with no errors in the working (b) M1 Use of $\log_a x = \frac{\log_b x}{\log_b a}$ or $\log_a b = \frac{1}{\log_b a}$ M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	M1	For $\log_4 32 = \frac{\log_2 32}{\log_4 4}$ or $\log_4 32 = \log_4 4^2$ or $\log_4 32 = \log_{2^2} 2^5$	
M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	M1 A1 cso	For $4^a = 32$ Obtains the given answer with no errors in the working	
M1 Forming a 3TQ A1 $2y^2 - 5y + 2 = 0$ M1 Solving the 3TQ M1 For $y = \log_2 x = \frac{1}{2}$ or 2 M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	M1	Use of $\log_a x = \frac{\log_b x}{\log_a a}$ or $\log_a b = \frac{1}{\log_a a}$	
M1 Either $x = 2^{\frac{1}{2}} = \sqrt{2}$ or $x = 2^2 = 4$	A1 M1	Forming a 3TQ $2y^2 - 5y + 2 = 0$ Solving the 3TQ	
		2	
A1 Roth $r = 2^{\frac{1}{2}} = \sqrt{2}$ and $r = 2^2 = 4$	A1	Both $x = 2^{\frac{1}{2}} = \sqrt{2}$ and $x = 2^2 = 4$	

Question number	Scheme								Marks		
6 (a)											
		х	0.5	1	1.5	2	3	4	5	6	
		у	-11.5	-2	0.2	1.3	2.7	3.8	4.9	5.9	B2
					ļ						[2]
(b)	Points plott Points joine				_						B1ft B1ft [2]
(c)	$\frac{x^3 - 3}{x^2} = ax$	+ b =	$\Rightarrow x^3 - 3 =$	$=ax^3+$	$-bx^2 =$	$\Rightarrow 0 = x$	$c^3(a-1)$	1)+bx	$x^2 + 3$		M1
	Comparing	coe	fficients								
	$x^3(a-1)-$	$x^{3}(a-1)-bx^{2}+3=2x^{3}+6x^{2}+3$									
	$\Rightarrow a = 3, b = -6$ so line required is $y = 3x - 6$							M1A1			
	Draws the line $y = 3x - 6$ and identifies two intersections with the						M1				
	curve when $x = 0.8 / 0.9$ and $x = 2.8 / 2.9$							A1 (both) [5]			
	ALT										
	$2x^3 - 6x^2 + 3 = 0 \Rightarrow 2x - 6 = -\frac{3}{x^2}$								{M1}		
	$3x - 6 = x - \frac{3}{x^2}$ so line required is $y = 3x - 6$							{M1}{A1}			
	Draws the line $y = 3x - 6$ and identifies two intersections with the							{M1}			
	curve when $x = 0.8 / 0.9$ and $x = 2.8 / 2.9$								{A1} both [5]		
	•									To	otal 9 marks

()	
(a)	
B2	All 4 points correct
	(B1 for 3 points correct)
(b)	
B1ft	Points plotted ft their table allow half a square tolerance
B1ft	Points joined together with a smooth curve ft their table
(c)	
M1	Setting $x - \frac{3}{x^2} = ax + b$ and simplifying to $x^3(a-1) + bx^2 + 3$
M 1	Comparing coefficients
A1	Identifying that the line required is $y = 3x - 6$
M1	y = 3x - 6 drawn intersecting the curve in two places
A1	x = 0.8/0.9 and $x = 2.8/2.9$
ALT	
M1	Subtracting 3 from both sides and dividing by x^2
M1	Adding x to both sides
A1	Identifying that the line required is $y = 3x - 6$
M1	y = 3x - 6 drawn intersecting the curve in two places
A1	x = 0.8/0.9 and $x = 2.8/2.9$

Question number	Scheme	Marks
7 (a)(i)	a + 4d = 4x + 6	
	a + 7d = 7x + 3	M1A1cso
	$\Rightarrow 3d = 3x - 3 \Rightarrow d = x - 1*$	
(ii)	$a + 7(x-1) = 7x + 3 \Rightarrow a = 10$ or $a + 4(x-1) = 4x + 6 \Rightarrow a = 10$	M1A1 [4]
(b)	$42 = 10 + 8(x-1) \Rightarrow x = 5$	M1A1 [2]
(c)	$d = x - 1 \Rightarrow d = 5 - 1 = 4$	B1
	$S_{n+1} = 12U_n + 18 \Rightarrow \frac{n+1}{2} (2 \times 10 + [(n+1)-1]4) = 12[10 + (n-1)4] + 18$	M1
	$\Rightarrow n^2 - 18n - 40 = 0$	M1
	$\Rightarrow (n-20)(n+2) = 0 \Rightarrow n = 20$	M1A1
		[5]
	Tota	l 11 marks
(a) (i)		
M1 A1 cso	a+4d=4x+6 and $a+7d=7x+3Obtains the given answer with no errors in the working$	
(a) (ii)	Obtains the given answer with no criois in the working	
M1	Substitution of $d = x - 1$	
A1	a = 10	
(b)		
M1	Use of $a + 8d = 42$	
A1	x = 5	
(c) B1	d=4	
M1	Use of $\frac{n}{2}(2a+(n-1)d)$	
M1	Simplifying to $n^2 - 18n - 40 = 0$	
M1	Solving the 3TQ	
A1	n = 20 if shown must reject $n = -2$	

Question	Scheme	Marks
number		
8	$s = \int (3 + 5t - 2t^2) dt = 3t + \frac{5t^2}{2} - \frac{2t^3}{3} + c$	M1
	when $t = 0$ $s = 5$ 5 = 0 + 0 - 0 + c	
	5 = 0 + 0 - 0 + c	B1
	$s = 5 + 3t + \frac{5t^2}{2} - \frac{2t^3}{3}$	A1
	When $s = x$	
	$\frac{\mathrm{d}x}{\mathrm{d}t} = 3 + 5t - 2t^2 = 0 \Longrightarrow (2t+1)(t-3) = 0 \Longrightarrow t = 3$	M1A1
	$\Rightarrow x = 5 + 3 \times 3 + \frac{5 \times 3^2}{2} - \frac{2 \times 3^3}{3} = \frac{37}{2}$ oe	A1
	$\frac{d^2x}{dt^2} = 5 - 4t$ when $t = 3$ $\frac{d^2x}{dt^2} = -7 \Rightarrow \max$	M1A1
	$\mathrm{d}t^{-}$ $\mathrm{d}t^{-}$	[8]
	To	tal 8 marks
M1	Attempt to integrate	
B 1	c=5	
A1	$s = 5 + 3t + \frac{5t^2}{2} - \frac{2t^3}{3}$	
M1	Solving $3 + 5t - 2t^2 = 0$	
A1	$t = 3$ if shown must reject $t = -\frac{1}{2}$	
A1	$x = \frac{37}{2} \text{ oe}$	
M1	Differentiates to obtain $\left(\frac{d^2x}{dt^2}\right) = 5 - 4t$	
A1	Establish that the maximum has been obtained and give a conclusion	

Question number	Scheme	Marks
9 (a)	$a = -1, \ b = -2$	B1,B1 [2]
(b)	Gradient of $l_1 = -2, \Rightarrow$ Gradient of $l_2 = \frac{1}{2}$	B1,B1
	$180 = (x+1)^2 + (y-6)^2$	M1
	$\frac{1}{2} = \frac{y - 6}{x + 1} \Rightarrow x = 2y - 13$	M1
	Solves simultaneous equations; $180 = ([2y-13]+1)^2 + (y-6)^2 \Rightarrow 0 = 5y^2 - 60y$ or $180 = (x+1)^2 + (\frac{1}{2}x + \frac{13}{2} - 6)^2 \Rightarrow 0 = x^2 + 2x - 143 = 0$	M1M1
	$y = 0, y = 12 \Rightarrow x = -13, x = 11$ or $x = -13, x = 11 \Rightarrow y = 0, y = 12$ Coordinates are $(-13, 0)$ and $(11, 12)$	A1A1 [8]
(c)	Area of triangle PQR $PQ = \sqrt{(6+2)^2 + (-1-3)^2} = 4\sqrt{5}$	M1
	Area = $\frac{1}{2} \times 4\sqrt{5} \times 6\sqrt{5} = 60 \text{ (units)}^2$	M1A1 [3]
	ALT $Area = \frac{1}{2} \begin{pmatrix} -13 & -1 & 3 & -13 \\ 0 & 6 & -2 & 0 \end{pmatrix} = \frac{1}{2} (-78 + 2 + 0 - 0 - 18 - 26) = -60$ $\Rightarrow 60 \text{ (units)}^2$	{M1} {M1} {A1} [3]
(d)	Coordinates of R required are $(-13, 0)$	[0]
	$\angle RPQ = 90^{\circ}$ so RQ is a diameter	
	$\left(\frac{-13+3}{2},\frac{0-2}{2}\right) \Rightarrow (-5, -1)$	M1A1 [2]
	То	tal 15 marks
(a) B1 B1	a = -1 $b = -2$	

```
(b)
           Gradient of l_1 = -2
 B1
           Gradient of l_2 = \frac{1}{2}
 B1
           Use of PR = 6\sqrt{5} to obtain an equation
M1
           Use of gradient of the perpendicular to obtain an equation
M1
            Solves simultaneously
M1
            Simplifies to 5y^2 - 60y = 0 or x^2 + 2x - 143 = 0
M1
            All 4 values identified 0, 12, -13, 11
A1
            (11, 12) and (-13, 0) (must be paired correctly and if written as a coordinate
A1
            then must be in the correct order)
 (c)
           PQ = 4\sqrt{5}
M1
           Use of Area = \frac{1}{2} \times PQ \times PR
M1
            60 \text{ (units)}^2
A1
ALT
           Use of Area = \frac{1}{2}\begin{pmatrix} -13 & -1 & 3 & -13 \\ 0 & 6 & -2 & 0 \end{pmatrix} ft R provided e < 0
M1
            \frac{1}{2}(-78+2+0-0-18-26) ft R provided e < 0
M1
            60 \text{ (units)}^2
A1
(d)
           \left(\frac{-13+3}{2}, \frac{0-2}{2}\right) ft R provided e < 0
M1
            \left(-5, -1\right)
A1
```

10 (a) (b) (c)	$AB = AO + OB = -(2\mathbf{a} - \mathbf{b}) + 3\mathbf{a} + \mathbf{b} = \mathbf{a} + 2\mathbf{b}$ $C = OB + BC = 3\mathbf{a} + \mathbf{b} - \mathbf{a} + 3\mathbf{b} = 2\mathbf{a} + 4\mathbf{b} = 2(\mathbf{a} + 2\mathbf{b})$ unit Complysion required, some direction and OC is a multiple of AB	M1A1 [2] M1
	CARL CRAW	
(c)	CARL CRAW	1
(c)	Conclusion required; same direction and OC is a multiple of AB therefore OC is parallel to AB .	A1 [2]
	$AC = AB + BC = \mathbf{a} + 2\mathbf{b} + (-\mathbf{a} + 3\mathbf{b}) = 5\mathbf{b}$	B1 B1
	$AX = \mu AC = \mu 5\mathbf{b}$ ULLY $AX = AO + OX = -(2\mathbf{a} - \mathbf{b}) + \lambda(3\mathbf{a} + \mathbf{b})$ $\Rightarrow \mu 5\mathbf{b} = -(2\mathbf{a} - \mathbf{b}) + \lambda(3\mathbf{a} + \mathbf{b})$	M1 M1
	$\Rightarrow -2 + 3\lambda = 0 \Rightarrow \lambda = \frac{2}{3}$	M1
	$\Rightarrow 5\mu = 1 + \lambda \Rightarrow \mu = \frac{1}{3}$	A1
	$\Rightarrow AX: XC = 1:2$	A1
L	Tot	al 11 marks
(a) M1 A1	Use of $AB = AO + OB$ $\mathbf{a} + 2\mathbf{b}$	
(b) M1		

(a)
M1
Use of
$$AB = AO + OB$$
A1
 $a + 2b$

(b)
M1
Use of $OC = OB + BC$

Correct conclusion i.e. $OC = 2AB$ $\therefore OC$ is parallel to AB

(c)
B1
 $AC = 5b$ may be implied by 2^{nd} B1
 $AX = \mu 5b$ or $XC = \lambda 5b$

A correct vector for AX or OX or BX or CX or BC including an unknown multiple of a vector e.g. $AX = -(2a - b) + \lambda(3a + b)$

M1
Equate 2 forms of the same vector e.g. $\mu 5b = -(2a - b) + \lambda(3a + b)$

M1
Comparing coefficients
A1
 $AX : XC = 1: 2$

Question number	Scheme	Marks
11 (a)	at P $b = \sqrt{a-2} \Rightarrow b^2 = a-2*$	M1A1cso [2]
(b)	At $P \ y = b \Rightarrow y^2 = b^2 \Rightarrow y^2 = a - 2$	B1
	$V = \pi \int_{a}^{16} \left(\sqrt{x - 2} \right)^{2} dx - \pi \int_{a}^{16} (a - 2) dx = \pi \int_{a}^{16} (x - 2) dx - \pi \int_{a}^{16} (a - 2) dx$	M1
	$\Rightarrow \pi \int_{a}^{16} (x-a) dx \text{or} \pi \int_{a}^{16} \left(\sqrt{x-2}\right)^{2} dx - \pi (a-2)(16-a)$	
	$50\pi = \pi \left[\frac{x^2}{2} - ax \right]_a^{16}$ or $50\pi = \pi \left[\frac{x^2}{2} - 2x \right]_a^{16} - \pi (a - 2)(16 - a)$	depM1A1
	$50\pi = \pi \left[\left(\frac{256}{2} - 16a \right) - \left(\frac{a^2}{2} - a^2 \right) \right]$	depM1
	or $50\pi = \pi \left[\left(96 - \frac{a^2}{2} + 2a \right) - \left(18a - a^2 - 32 \right) \right]$	
	$\Rightarrow a^2 - 32a + 156 = 0$	M1
	$\Rightarrow (a-6)(a-26) = 0 \Rightarrow a < 16 \text{ so } a = 6$	
	$b^2 = a - 2 \Rightarrow b^2 = 4 \Rightarrow b = 2$	M1A1 A1
		[9]
(a)	lota	l 11 marks
M1	$b = \sqrt{a-2}$	
A1 cso	Obtains the given answer with no errors in the working	
(b)		
B 1	$y^2 = a - 2$	
M1	Use of $V = \pi \int_{a}^{16} (\sqrt{x-2})^{2} dx - \pi \int_{a}^{16} (a-2) dx$ or $V = \pi \int_{a}^{16} (x-a) dx$ or $\pi \int_{a}^{16} (\sqrt{x-2})^{2} dx - \pi (a-2)(16-a)$ Ignore limits	
depM1 A1 depM1 M1	Attempts to integrate. Ignore limits (Dependent on previous M1) Correct integration. Ignore limits Correct substitution of limits (Dependent on previous M1) Obtaining the 3TQ Solving the 3TQ	
A1 A1	$ \begin{array}{l} a = 6 \\ b = 2 \end{array} $	