Faithful Model Explanations through Energy-Constrained Conformal Counterfactuals

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Pick your Poison

All of these counterfactuals are valid explanations for the model's prediction.

Which one would you pick?



Figure 1: Turning a 9 into a 7: Counterfactual explanations for an image classifier produced using *Wachter* (Wachter, Mittelstadt, and Russell 2017), *Schut* (Schut et al. 2021) and *REVISE* (Joshi et al. 2019).

Faithfulness first, plausibility second.

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We propose *ECCCo*: a new way to generate faithful model explanations that are as plausible as the underlying model permits.

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- **Method**: constrain the model's energy and predictive uncertainty for the counterfactual.
- Result: faithful counterfactuals that are as plausible as the model permits.
- Benefits: enable us to distinguish trustworthy from unreliable models.

Counterfactual Explanations

$$\min_{\mathbf{Z}' \in \mathcal{Z}^L} \{ \mathsf{yloss}(M_{\theta}(f(\mathbf{Z}')), \mathbf{y}^+) + \lambda \mathsf{cost}(f(\mathbf{Z}')) \}$$

Counterfactual Explanations (CE) explain how inputs into a model need to change for it to produce different outputs.



Figure 2: Gradient-based counterfactual search.

Reconciling Faithfulness and Plausibility

Plausibility

Definition (Plausible Counterfactuals)

Let $\mathcal{X}|\mathbf{y}^+ = p(\mathbf{x}|\mathbf{y}^+)$ denote the true conditional distribution of samples in the target class \mathbf{y}^+ . Then for \mathbf{x}' to be considered a plausible counterfactual, we need: $\mathbf{x}' \sim \mathcal{X}|\mathbf{y}^+$.

Why Plausibility?

Plausibility is positively associated with actionability, robustness (Artelt et al. 2021) and causal validity (Mahajan, Tan, and Sharma 2020).



Figure 3: Kernel density estimate (KDE) for the conditional distribution, $p(\mathbf{x}|\mathbf{y}^+)$, based on observed data. Counterfactual path as in Figure 2.

Faithfulness

Definition (Faithful Counterfactuals)

Let $\mathcal{X}_{\theta}|\mathbf{y}^+ = p_{\theta}(\mathbf{x}|\mathbf{y}^+)$ denote the conditional distribution of \mathbf{x} in the target class \mathbf{y}^+ , where θ denotes the parameters of model M_{θ} . Then for \mathbf{x}' to be considered a faithful counterfactual, we need: $\mathbf{x}' \sim \mathcal{X}_{\theta}|\mathbf{y}^+.$

Trustworthy Models

If the model posterior approximates the true posterior $(p_{\theta}(\mathbf{x}|\mathbf{y}^+) \to p(\mathbf{x}|\mathbf{y}^+))$, faithful counterfactuals are also plausible.



Figure 4: KDE for learned conditional distribution, $p_{\theta}(\mathbf{x}|\mathbf{y}^+)$. Yellow stars indicate conditional samples generated through SGLD for a joint energy model (JEM).

ECCCo

Key Idea

Use the hvbrid objective joint ergy models (JEM) and a model-agnostic penalty for predictive uncertainty: Energy-Constrained $(\mathcal{E}_{\mathcal{A}})$ Conformal (Ω) Counterfactuals (ECCCo).

ECCCo objective¹:

$$\begin{split} \min_{\mathbf{Z}' \in \mathcal{Z}^L} \{ L_{\text{clf}}(f(\mathbf{Z}'); M_{\theta}, \mathbf{y}^+) + \lambda_1 \text{cost}(f(\mathbf{Z}')) \\ + \lambda_2 \mathcal{E}_{\theta}(f(\mathbf{Z}') | \mathbf{y}^+) + \lambda_3 \Omega(C_{\theta}(f(\mathbf{Z}'); \alpha)) \} \end{split}$$

Figure 5: Gradient fields and counterfactual paths for different generators.

Results

Results

Visual Evidence



Figure 6: Turning a 9 into a 7. *ECCCo* applied to MLP (a), Ensemble (b), JEM (c), JEM Ensemble (d).

ECCCo generates counterfactuals that

- faithfully represent model quality (Figure 6).
- achieve state-of-the-art plausibility (Figure 7).











Figure 7: Results for different generators (from 3 to 5).

The Numbers

- Large benchmarks on a variety of models and datasets from various domains.
- ECCCo achieves state-of-the-art faithfulness across models and datasets and approaches state-of-the-art plausibility for more trustworthy models.

		California Housing			GMSC		
Model	Generator	Unfaithfulness \downarrow	Implausibility \downarrow	Uncertainty \downarrow	Unfaithfulness \downarrow	Implausibility \downarrow	Uncertainty ↓
MLP Ensemble	ECCCo ECCCo+ ECCCo (no CP) ECCCo (no EBM) REVISE Schut Wachter	3.69 ± 0.08** 3.88 ± 0.07** 3.70 ± 0.08** 4.03 ± 0.07 3.96 ± 0.07* 4.00 ± 0.06 4.04 ± 0.07	1.94 ± 0.13 1.20 ± 0.09 1.94 ± 0.13 1.12 ± 0.12 $0.58 \pm 0.03**$ 1.15 ± 0.12 1.13 ± 0.12	0.09 ± 0.01** 0.15 ± 0.02 0.10 ± 0.01** 0.14 ± 0.01** 0.17 ± 0.03 0.10 ± 0.01** 0.16 ± 0.01	3.84 ± 0.07** 3.79 ± 0.05** 3.85 ± 0.07** 4.08 ± 0.06 4.09 ± 0.07 4.04 ± 0.08 4.10 ± 0.07	2.13 ± 0.08 1.81 ± 0.05 2.13 ± 0.08 0.97 ± 0.08 0.63 ± 0.02 ** 1.21 ± 0.08 0.95 ± 0.08	0.23 ± 0.01** 0.30 ± 0.01* 0.23 ± 0.01** 0.31 ± 0.01* 0.33 ± 0.06 0.30 ± 0.01* 0.32 ± 0.01
JEM Ensemble	ECCCo ECCCo+ ECCCo (no CP) ECCCo (no EBM) REVISE Schut Wachter	1.40 ± 0.08** 1.28 ± 0.08** 1.39 ± 0.08** 1.70 ± 0.09 1.39 ± 0.15** 1.59 ± 0.10* 1.71 ± 0.09	0.69 ± 0.05** 0.60 ± 0.04** 0.69 ± 0.05** 0.99 ± 0.08 0.59 ± 0.04** 1.10 ± 0.06 0.99 ± 0.08	0.11 ± 0.00** 0.11 ± 0.00** 0.11 ± 0.00** 0.11 ± 0.00* 0.14 ± 0.00* 0.25 ± 0.07 0.09 ± 0.00 ** 0.14 ± 0.00	1.0 ± 0.06* 1.01 ± 0.07** 1.21 ± 0.07* 1.31 ± 0.07* 1.01 ± 0.07** 1.34 ± 0.07 1.31 ± 0.08	0.78 ± 0.07** 0.70 ± 0.07** 0.77 ± 0.07** 0.97 ± 0.10 0.63 ± 0.04 ** 1.21 ± 0.10 0.95 ± 0.10	0.38 ± 0.01 0.37 ± 0.01 0.39 ± 0.01 0.32 ± 0.01** 0.33 ± 0.07 0.26 ± 0.01 ** 0.33 ± 0.01

Table 1: Results for tabular datasets: sample averages +/- one standard deviation across valid counterfactuals. The best outcomes are highlighted in bold. Asterisks indicate that the given value is more than one (*) or two (**) standard deviations away from the baseline (Wachter).

Questions?

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With thanks to my co-authors Mojtaba Farmanbar, Arie van Deursen and Cynthia C. S. Liem.



Code

The code used to run the analysis for this work is built on top of CounterfactualExplanations.jl.

There is also a corresponding paper, *Explaining Black-Box Models through Counterfactuals*, which has been published in JuliaCon Proceedings.



Figure 8: Trustworthy AI in Julia: github.com/JuliaTrustworthyAI

Questions?

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