

<https://www.theactuary.com/features/2020/08/05/machine-learning-deep-end>



# **AI and ML - Well, it is all about statistical and probabilistic ideas...**

## **An introduction**

Dr. Pat Ryser-Welch / Oct 2023



# Artificial Intelligence



## Machine Learning



### Deep Learning

Rule Based Systems

Support Vector  
Machines

Game Playing

Linear Regression

Knowledge Representation and Reasoning

MLP

CNN

GAN

RBFN

LSTM

Autoencoders

RNN

Logistic Regression

K-Means Clustering

Gaussian Process  
Regression

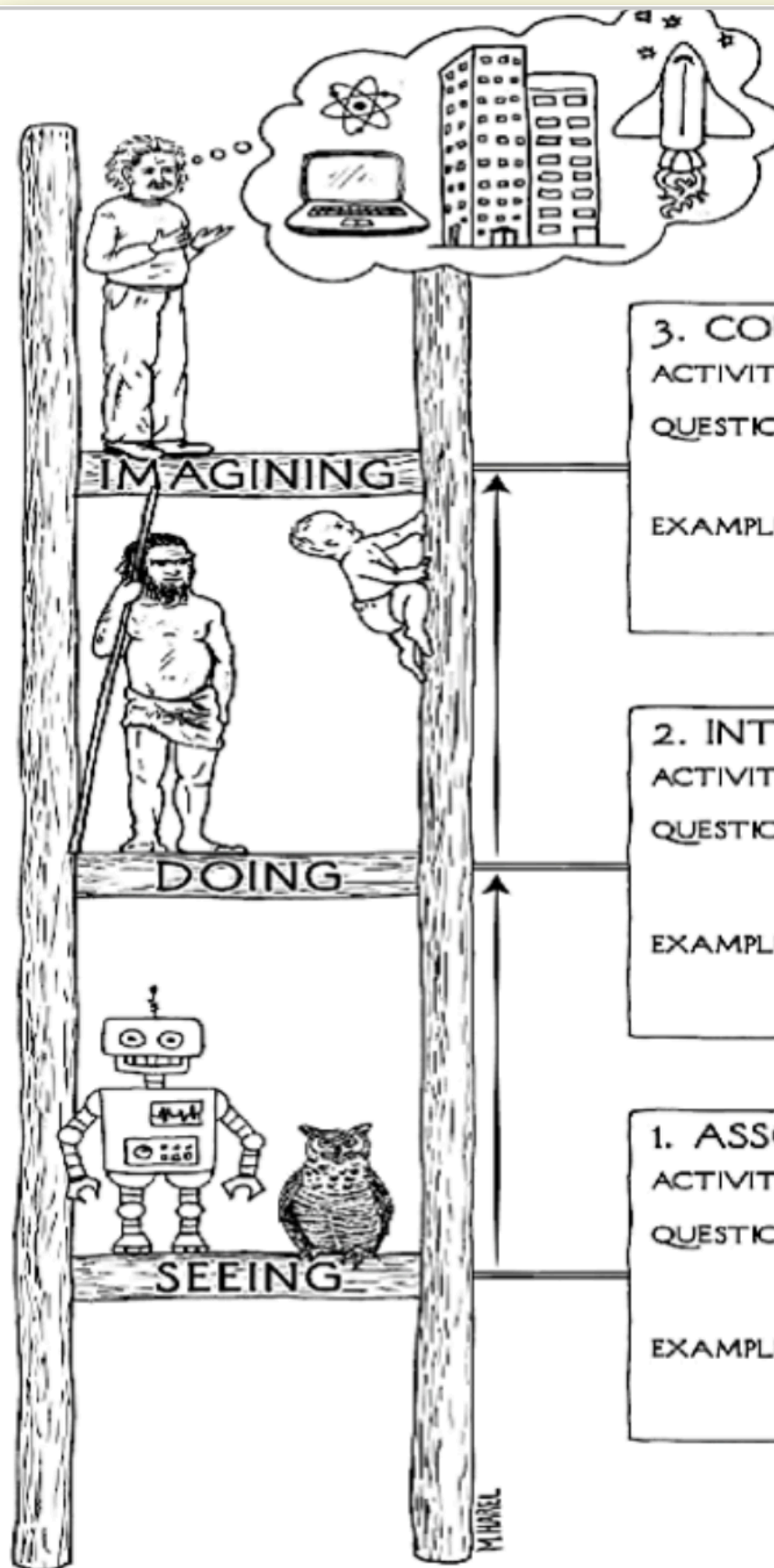
Random Forest

Cognitive Modeling

Planning

Search Algorithms

Propositional Calculus



### 3. COUNTERFACTUALS

ACTIVITY: Imagining, Retrospection, Understanding

QUESTIONS: *What if I had done ...? Why?*  
(Was it X that caused Y? What if X had not occurred? What if I had acted differently?)

EXAMPLES: Was it the aspirin that stopped my headache?  
Would Kennedy be alive if Oswald had not killed him? What if I had not smoked for the last 2 years?

### 2. INTERVENTION

ACTIVITY: Doing, Intervening

QUESTIONS: *What if I do ...? How?*  
(What would Y be if I do X?  
How can I make Y happen?)

EXAMPLES: If I take aspirin, will my headache be cured?  
What if we ban cigarettes?

### 1. ASSOCIATION

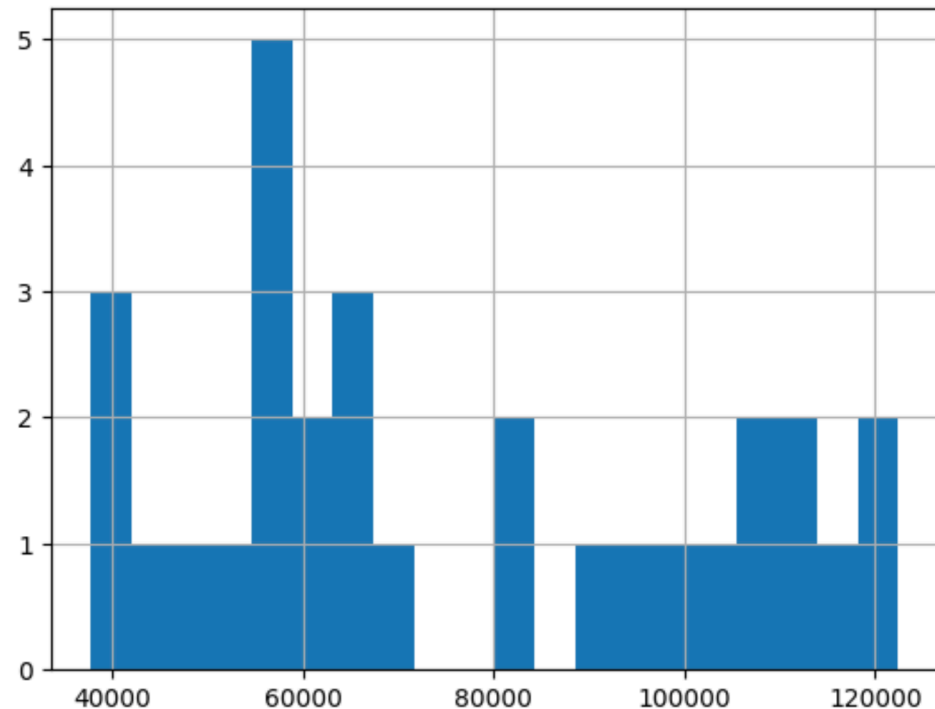
ACTIVITY: Seeing, Observing

QUESTIONS: *What if I see ...?*  
(How are the variables related?  
How would seeing X change my belief in Y?)

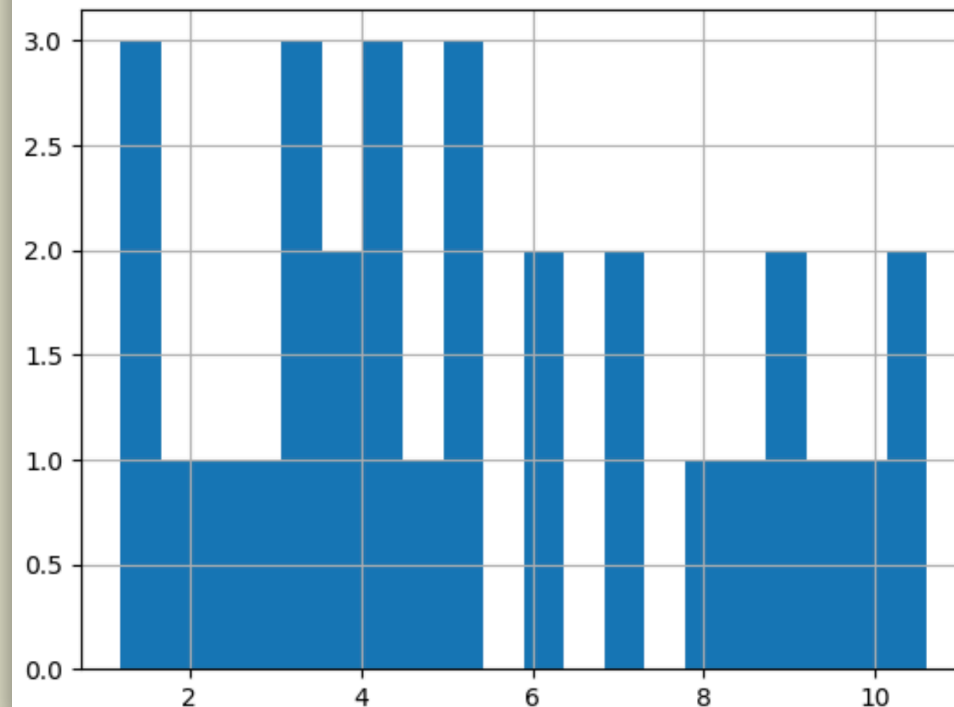
EXAMPLES: What does a symptom tell me about a disease?  
What does a survey tell us about the election results?

# A simple association: Years of experience and Salary

```
Out[141... count      30.000000  
mean       76004.000000  
std        27414.429785  
min        37732.000000  
25%        56721.750000  
50%        65238.000000  
75%       100545.750000  
max       122392.000000  
Name: Salary, dtype: float64
```

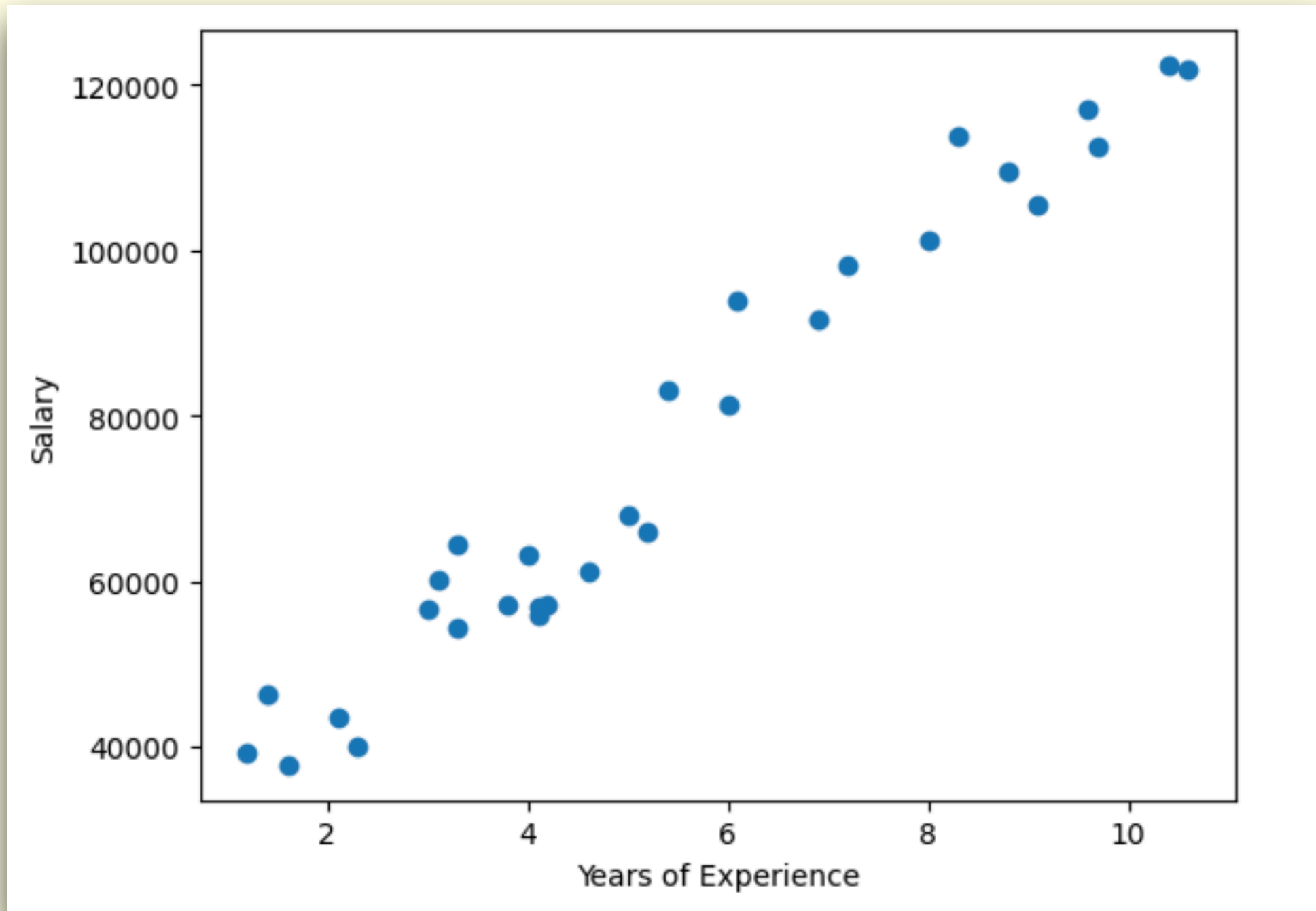


```
count      30.000000  
mean        5.413333  
std         2.837888  
min         1.200000  
25%         3.300000  
50%         4.800000  
75%         7.800000  
max         10.600000  
Name: YearsExperience, dtype: float64
```



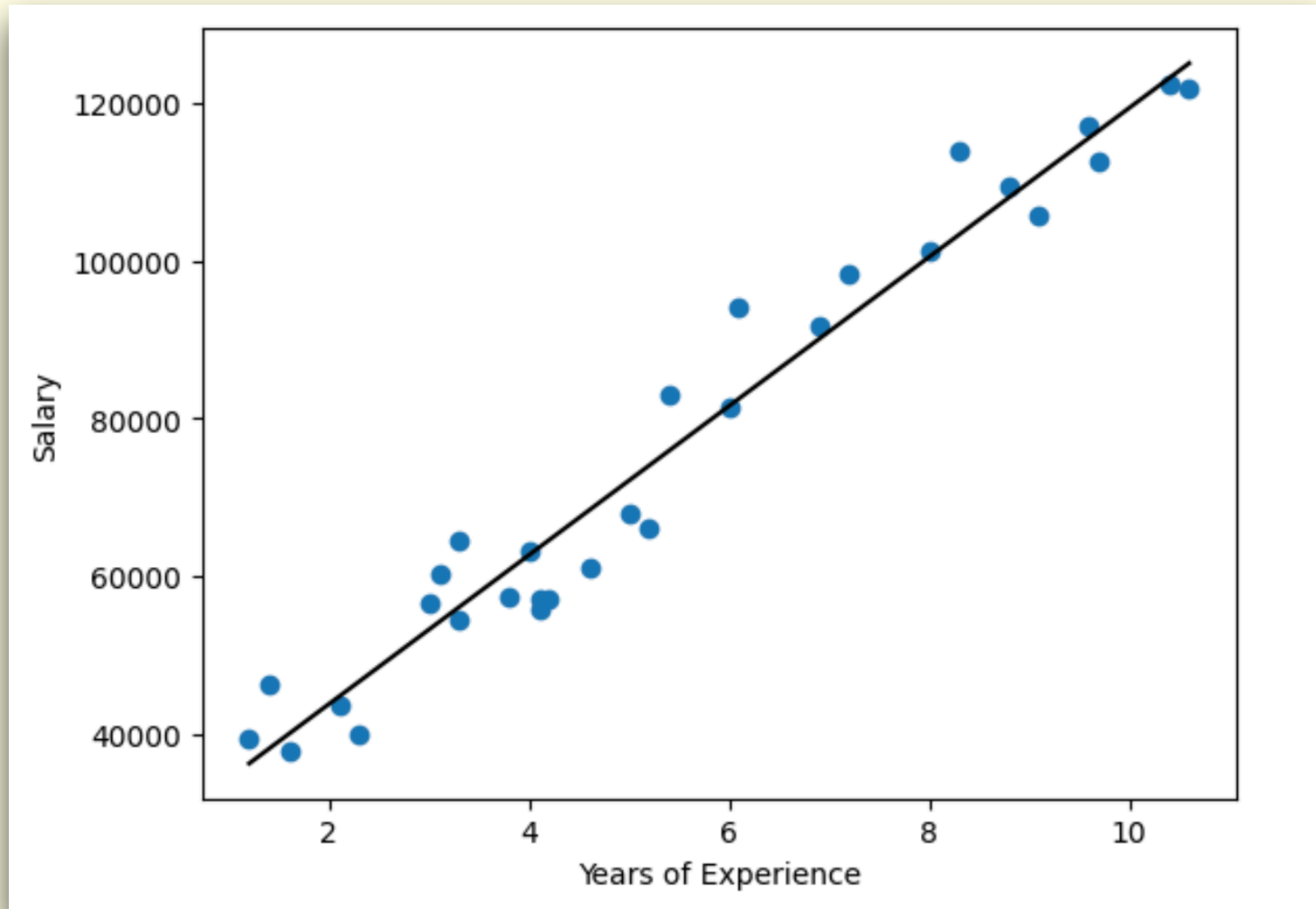
# Years of Experience

In your opinion, what type of pattern may associate the year of experience to the salary?



# Years of Experience

In your opinion, what type of pattern may associate the year of experience to the salary?



# What did we do?

- We have a set of labelled examples - The observed salary.
- We have a set of other values that may be matching the labelled example.
- We constructed a model, based on a hypothesis.
- We use a sample that we surmised represented some properties about years of experience and salary.

$$\text{Model} = \text{data} + \text{error}$$



# Metrics - error and accuracy

In your opinion, would you interpret this percentage error of predictions?

```
3... array([0.07047916])
```

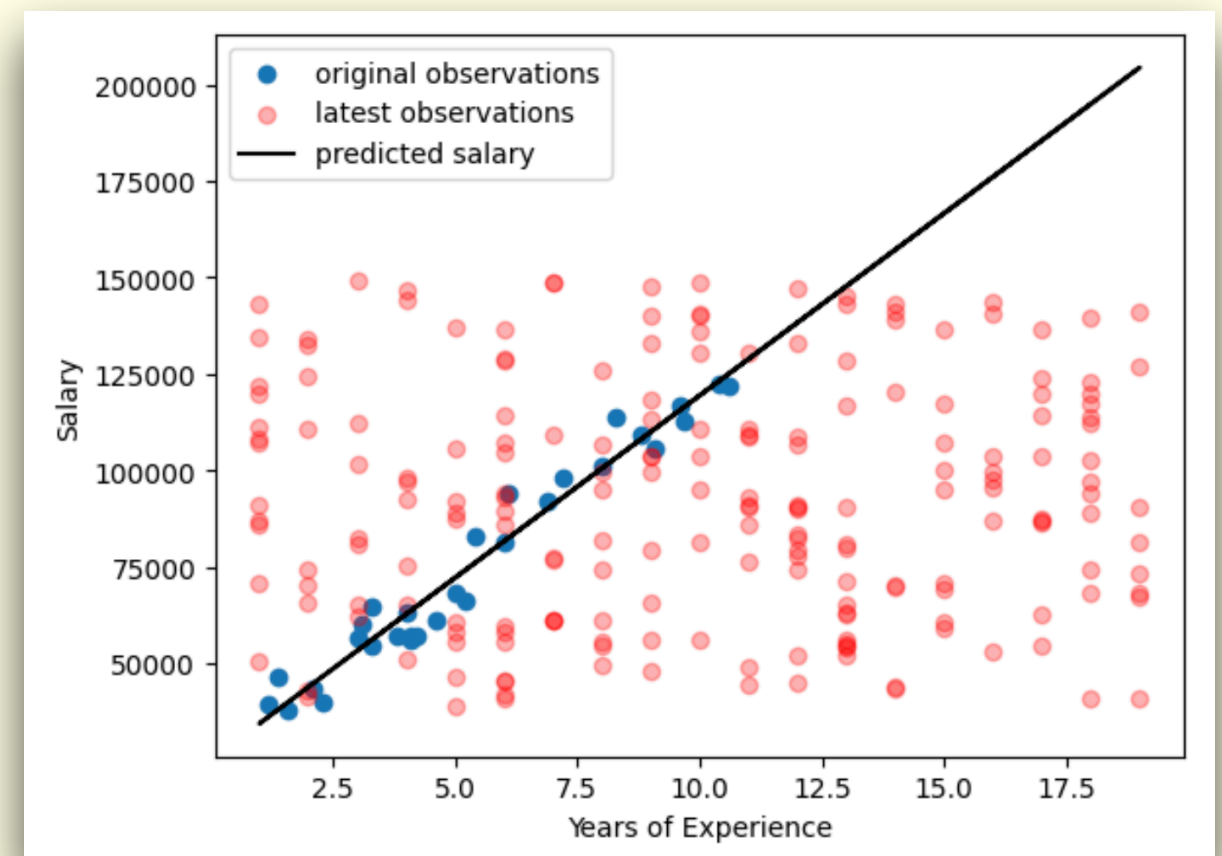
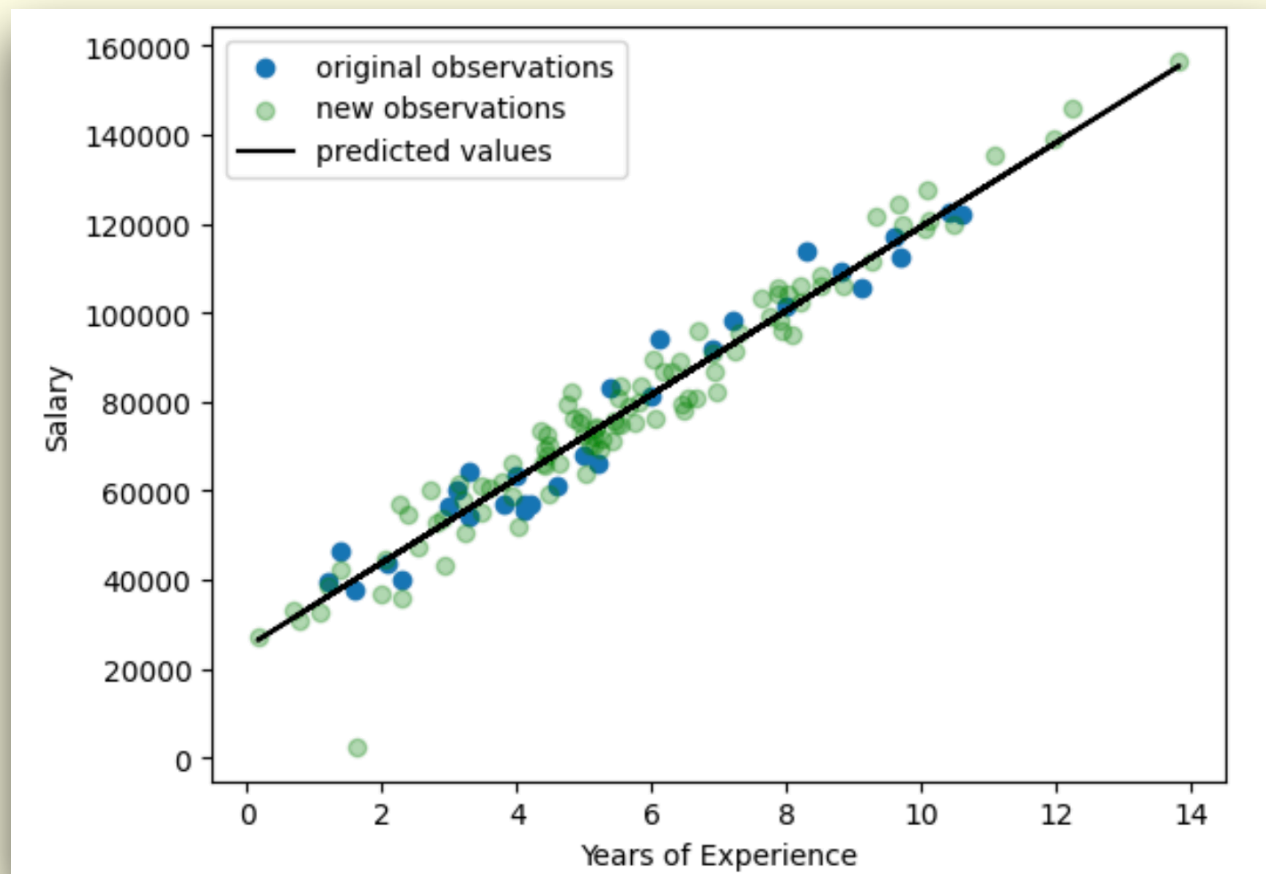
# Metrics - error and accuracy

We use the [mean absolute average error](#) to evaluate the model. The model appears to be quite accurate. The error is less than 10% and, consequently, the accuracy is 90% or greater.

```
3... mape_sum = sum(abs(ys - Y_pred)/ys)
mape = (1/len(Xs)) * mape_sum
mape
```

```
3... array([0.07047916])
```

# Is this model suitable for other observations?



Notebook



# What is PAC learning?

**Definition 1** (*PAC learnability*) Let  $\mathcal{C}$  be a class of boolean functions  $f : \{0,1\}^n \rightarrow 0,1$ . We say that  $\mathcal{C}$  is PAC-learnable if there exists an algorithm  $\mathcal{L}$  such that

- for every  $f \in \mathcal{C}$
- for any probability distribution  $\mathcal{D}$
- for any  $\epsilon$  (where  $0 \leq \epsilon < \frac{1}{2}$ )
- for any  $\delta$  (where  $0 \leq \delta < 1$ )

algorithm  $\mathcal{L}$  on input  $\epsilon$  and  $\delta$  and a set of random examples picked from any probability distribution  $\mathcal{D}$  outputs at least with a probability  $1 - \delta$ , concept  $h$  such that  $\text{error}(h, f) \leq \epsilon$ .

A PAC learning algorithm refers to an algorithm that returns a hypothesis that is PAC.

Using formal methods, a minimum generalization error can be specified for a supervised learning task. The theorem can then be used to estimate the expected number of samples from the problem domain that would be required to determine whether a hypothesis was PAC or not. That is, it provides a way to estimate the number of samples required to find a PAC hypothesis.

“ *The goal of the PAC framework is to understand how large a data set needs to be in order to give good generalization. It also gives bounds for the computational cost of learning ...*

— Page 344, [Pattern Recognition and Machine Learning](#), 2006.

Questions explored in computational learning theory might include:

- How do we know a model has a good approximation for the target function?
- What hypothesis space should be used?
- How do we know if we have a local or globally good solution?
- How do we avoid overfitting?
- How many data examples are needed?