

In the following Examples we see how the general binomial expansion  $(a + b)^n$  may be put to use.

**Example 2****Self Tutor**

Use  $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$  to find the binomial expansion of:

a  $(2x + 3)^3$

b  $(x - 5)^3$

- a In the expansion of  $(a + b)^3$  we substitute  $a = (2x)$  and  $b = (3)$ .

Brackets are essential!

$$\therefore (2x + 3)^3 = (2x)^3 + 3(2x)^2(3) + 3(2x)^1(3)^2 + (3)^3 \\ = 8x^3 + 36x^2 + 54x + 27$$

- b We substitute  $a = (x)$  and  $b = (-5)$

$$\therefore (x - 5)^3 = (x)^3 + 3(x)^2(-5) + 3(x)(-5)^2 + (-5)^3 \\ = x^3 - 15x^2 + 75x - 125$$

**Example 3****Self Tutor**

Find the:

- a 5th row of Pascal's triangle

- b binomial expansion of  $\left(x - \frac{2}{x}\right)^5$ .

a  $1 \quad 1$  ← the 1st row, for  $(a + b)^1$

$1 \quad 2 \quad 1$

$1 \quad 3 \quad 3 \quad 1$

$1 \quad 4 \quad 6 \quad 4 \quad 1$

$1 \quad 5 \quad 10 \quad 10 \quad 5 \quad 1$  ← the 5th row, for  $(a + b)^5$

- b Using the coefficients obtained in a,  $(a + b)^5 = a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5$

Letting  $a = (x)$  and  $b = \left(\frac{-2}{x}\right)$ ,

$$\begin{aligned} & \left(x - \frac{2}{x}\right)^5 \\ &= (x)^5 + 5(x)^4\left(\frac{-2}{x}\right) + 10(x)^3\left(\frac{-2}{x}\right)^2 + 10(x)^2\left(\frac{-2}{x}\right)^3 + 5(x)\left(\frac{-2}{x}\right)^4 + \left(\frac{-2}{x}\right)^5 \\ &= x^5 - 10x^3 + 40x - \frac{80}{x} + \frac{80}{x^3} - \frac{32}{x^5} \end{aligned}$$