

Expression Evaluation {Stack & Queue}

Level (1)

- Infix Evaluation + Conversion
- Postfix Evaluation + Conversion
- Prefix Evaluation + Conversion (HW)

Level (2)

- Basic Calculator - $1, 11, 111$
- Expression Tree - Construction & Evaluation

①

2
-3
8
4
-2
-1
0

Infⁿ Evaluation

Infⁿ → operand operator operand

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
5 + 2 * (3 - 4 + 2 / 3) * 4 + 2

b
a
3
2
-1
4
3
2
5

operand

+
*
/
+
-
(
*
+

operator

Precedence

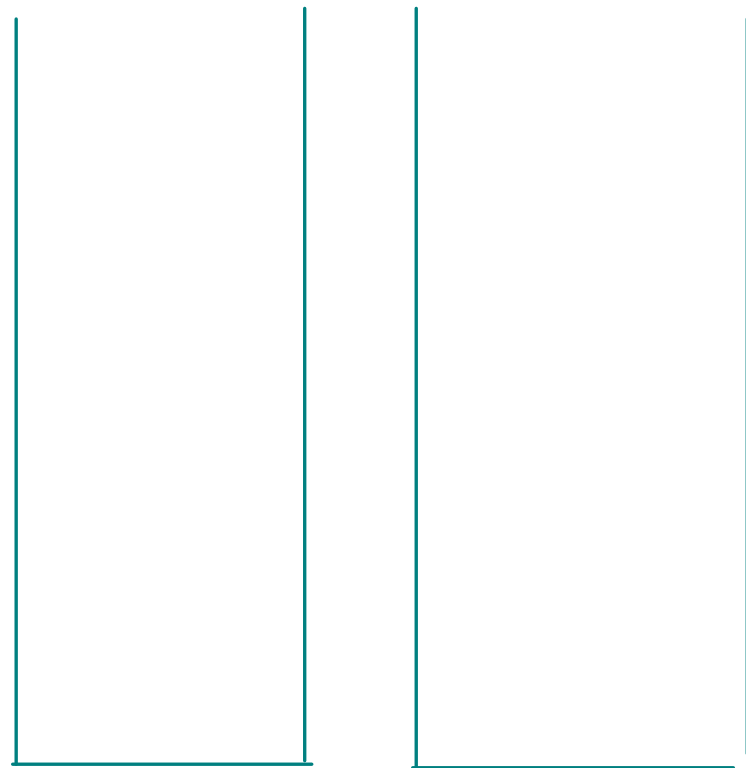
① Brackets

① Division & Multiplication
(/, *)

② Addition & Subtraction
(+, -)

Equal Precedence
"Left to right associativity"
(+, -, /, *)

$\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
 $5 + 2 * (3 - 4 + 2 / 3) * 4 + 2$



if ($ch \geq '0' \ \&\& \ ch \leq '9'$)

operand: push(ch)

else if ($ch == '('$)

operator: push(ch)

else if ($ch == ')'$)

}

pop until '(' on top, perform, res push operand

pop '(' also

else {

while ($stk\text{-}size > 0 \ \&\& \ stk.peek() \neq '('$
 $\&\& \ prec(stk.peek()) \geq prec(ch)$)

pop & push

push yourself ;

}

```

public static int precedence(char ch){
    if(ch == '/' || ch == '*') return 2;
    if(ch == '+' || ch == '-') return 1;
    return 0;
}

public static int performOp(int a, char op, int b){
    if(op == '+'){
        return a + b;
    } else if(op == '-'){
        return a - b;
    } else if(op == '*'){
        return a * b;
    } else {
        return a / b;
    }
}

```

```

} else if(ch == '+' || ch == '-' || ch == '*' || ch == '/'){
    // operator -> + or - or * or /
    while(operator.size() > 0 && operator.peek() != '('
        && precedence(operator.peek()) >= precedence(ch)){
        int b = operand.pop();
        int a = operand.pop();
        char op = operator.pop();
        operand.push(performOp(a, op, b));
    }
    operator.push(ch);
}

```

- ① Precedence
- ② Associativity

$O(N)$

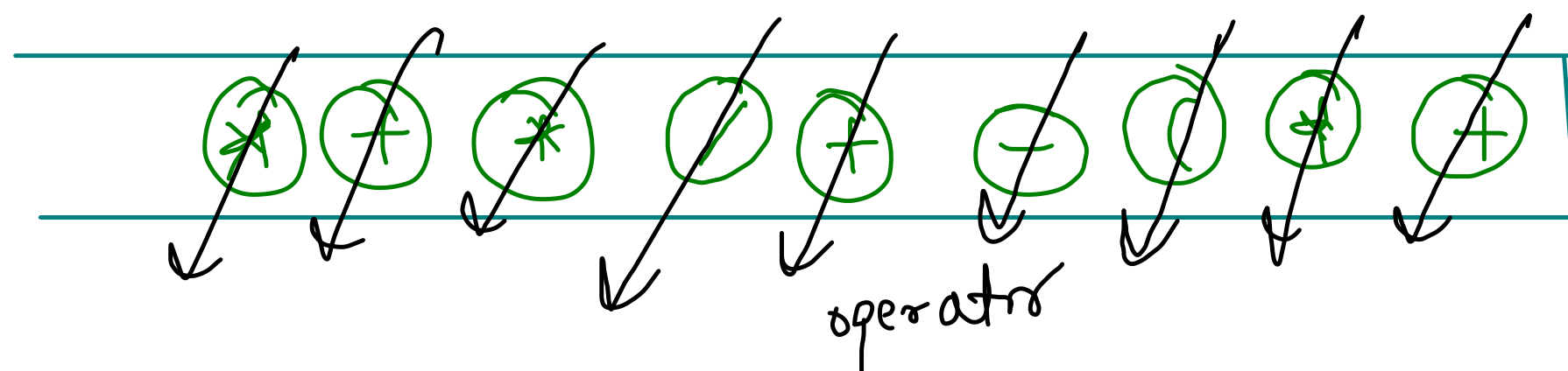
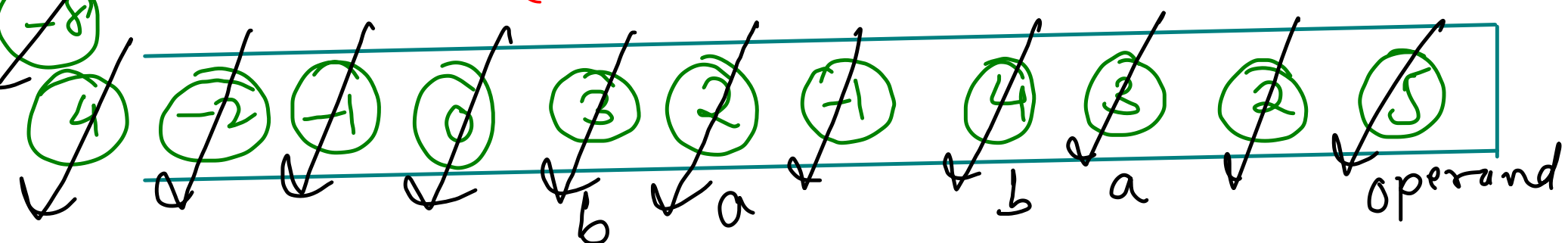
```

for(int i=0; i<exp.length(); i++){
    char ch = exp.charAt(i);

    if(ch >= '0' && ch <= '9'){
        // operand -> push in operand wali stack
        operand.push(ch - '0');
    } else if(ch == '('){
        operator.push(ch);
    } else if(ch == ')'){
        while(operator.peek() != '('){
            int b = operand.pop();
            int a = operand.pop();
            char op = operator.pop();
            operand.push(performOp(a, op, b));
        }
        operator.pop(); // pop opening braces as well
    }
}

```

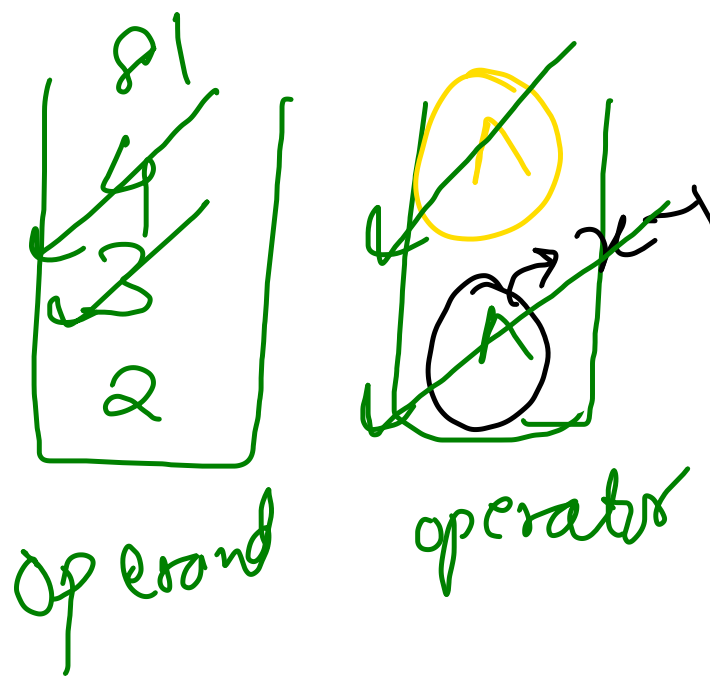
↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
 5 + 2 * (3 - 4 + 2 / 3) * 4 + 2 * 3



$$2^{3^4} \rightarrow (2^3)^4 = (8)^4 = 4096 \quad \checkmark$$

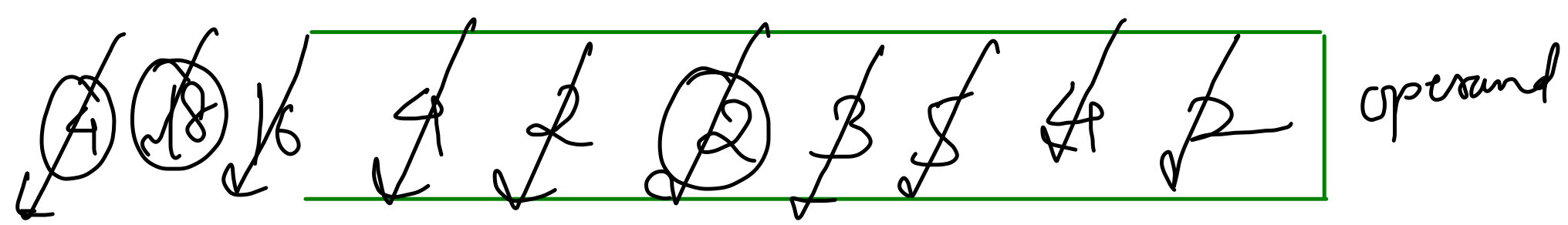
$$2^{(3^4)} = 2^{81} = \checkmark \dots$$

$$\begin{array}{c} \downarrow \downarrow \downarrow \downarrow \downarrow \\ 2^{\wedge} 3^{\wedge} 4 \\ \hline \end{array}$$

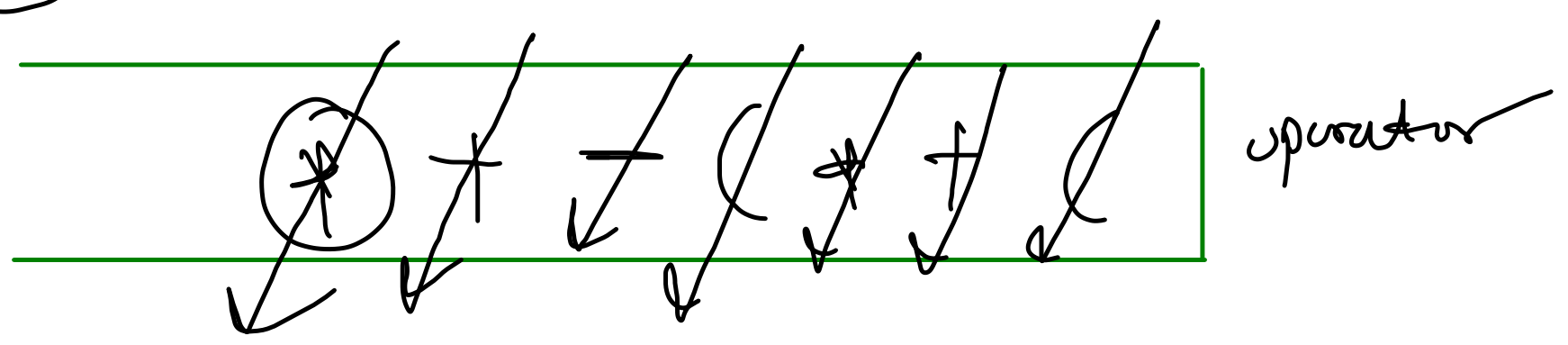


$$\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$$

$$(2 + 4 * (5 - 3 + 2)) * 4$$



$$18 * 4 = 72$$



Infix Conversion
 $a \text{ operator } b$

\rightarrow Prefix \rightarrow Operator $a \ b$
 \rightarrow Postfix $\rightarrow a \ b \text{ operator}$

$\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
 $5 + 2 * (3 - 4 + 2 / 3) * 4$

$* * 2 + - 3 4 / 2 3 4$
 $(4) \quad (2 + - 3 4 / 2 3) \quad (+ - 3 4 / 2 3)$
 $(4) \quad (2 3 4 - 2 3 / +) \quad (3 4 - 2 3 / +)$
 $2 3 4 - 2 3 / + * 4 *$

*	/	+	-	(*	+
1 2 3	3	2	- 3 4	4	3	2
2 3	3	2	3 4 -	4	3	2

operator <Character>

prefix <String>

Postfix <String>

Prefix $\Rightarrow + 5 * * 2 + - 3 4 / 2 3 4$

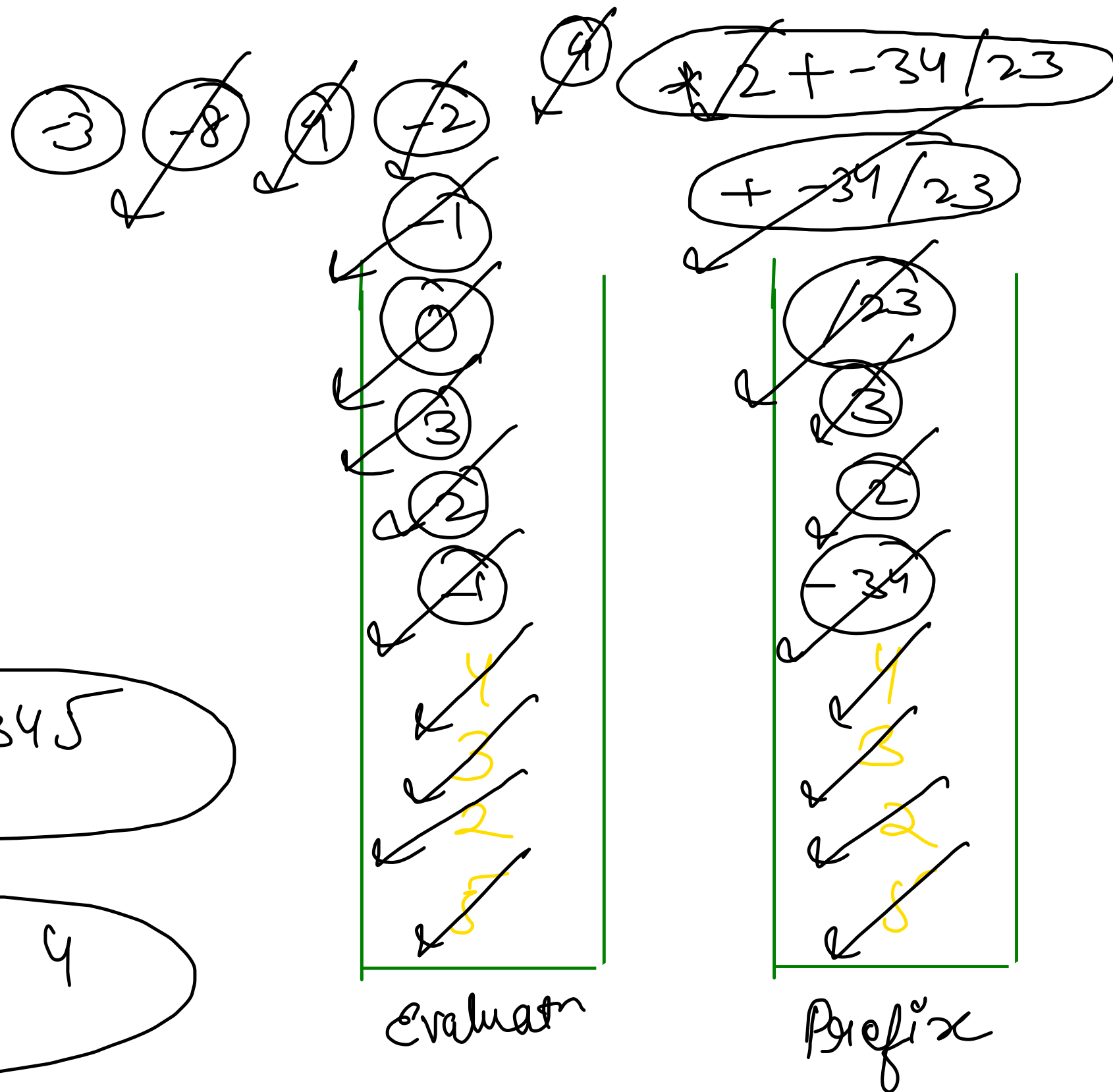
Postfix $\Rightarrow 5 2 3 4 - 2 3 / + * 4 * +$

Postfix Evaluation & Conversion

5 2 3 4 - 2 3 / + * 4 * +
 ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

+ * 2 + - 3 4 / 2 3 4 5

* * 2 + - 3 4 / 2 3 4



Postfix 2 3 4 - 2 3 / + *

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

$(2 * ((3 - 4) + (2 / 3))) + -34 / 23$ -2

$((3 - 4) + (2 / 3)) + -34 / 23$

$(2 / 3)$

2
3
4
-
3
2

Infix

23

3
2
-
34
4
3
2

Postfix

$0.$

3
2
-
4
3
2

Evaluate

Basic Calculator - I, II, III

Processing

1 " $- 3 + (- 5 - (+ 5 - (- 2)))$ "

res = " $0 - 3 + (0 - 5 - (5 - 2))$ "

71 digit

(2)

2 35 + 478
↑ ↑↑ ↑ ↑↑↑

$$\text{curr} = 2 \times 10 + 3 = 23 \times 10 + 5 = 235$$

$$\text{curr} = 4 \times 10 + 7 = 47 \times 10 + 8 = 478$$

