

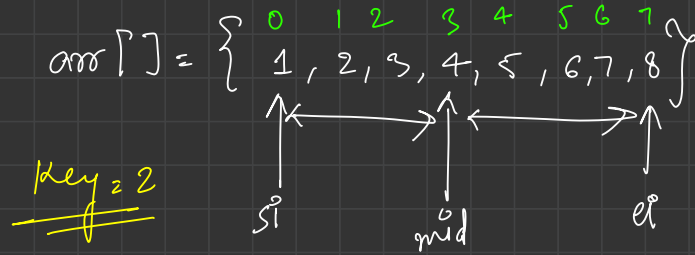


## # Infinite Sorted Array

$$\text{arr}[] = \{ 1, 2, 3, 4, \dots, \infty \}$$

$$\text{Key} = \underline{\underline{10}}$$

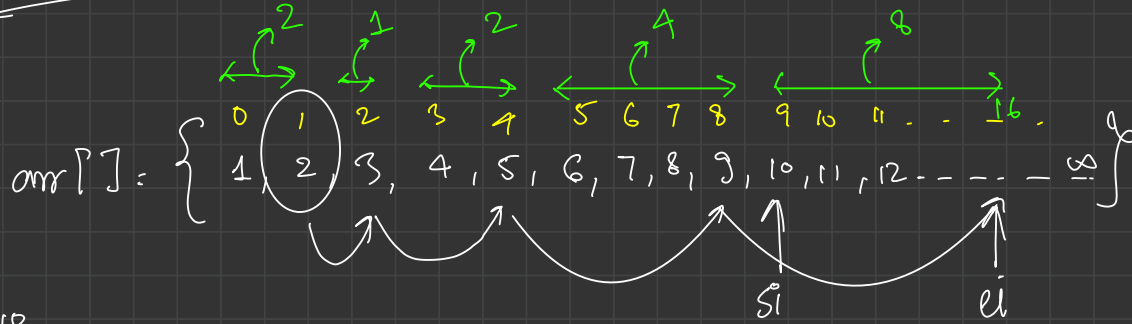
# Binary Search



TC:  $O(\log N)$

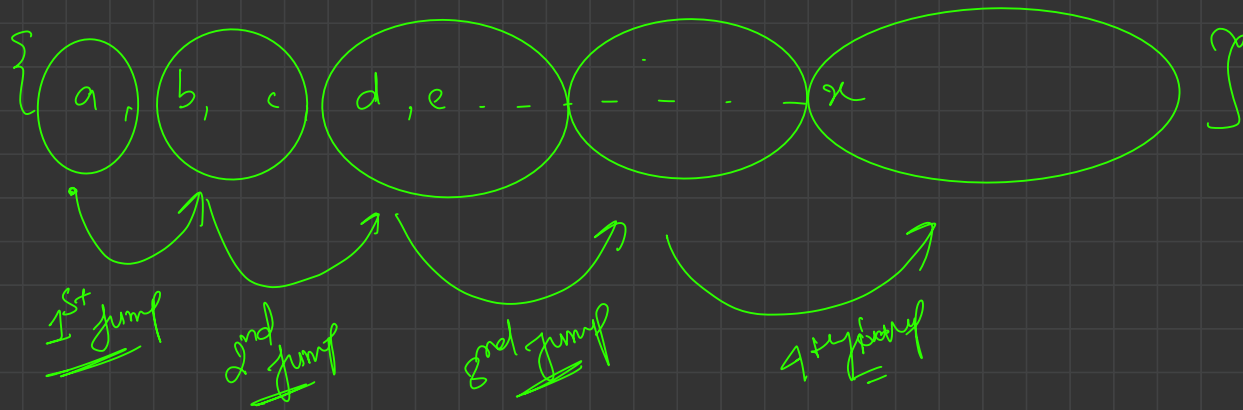
Size of the Array

# Search In Infinite Sorted Array



Key = 10

$$\begin{cases} si = ei + 1; \\ ei = 2 \times ei \end{cases}$$



$$\text{arr}[ ] = \{ 1, 2, 3, 4, 5, \dots, \overset{(p)^{\text{th}}}{x}, \dots, \infty \}$$

$\uparrow$   
 $(p-1)^{\text{th}}$

$$\left. \begin{array}{l} s_i \rightarrow p \\ e_i \rightarrow 2(p-1) \end{array} \right\}$$

$$\begin{aligned} \text{Number of elements} &= \overset{e_i - s_i + 1}{\sqrt{2(p-1) - p + 1}} \\ &= 2p - 2 - p + 1 = \underline{\underline{(p-1) \text{ elements}}} \end{aligned}$$

TC: of BS  $O(\log p)$   $\left\{ \begin{array}{l} \text{index of} \\ \text{target} \end{array} \right\}$

←



$$2^{K-1} = 2^{(p-1)}$$

$$\frac{2^{K-1}}{2} = (p-1)$$

$$2^{K-2} = (p-1)$$

$$\log_2 2^{(K-2)} = \log_2 (p-1)$$

$$(K-2) = \log_2 (p-1)$$

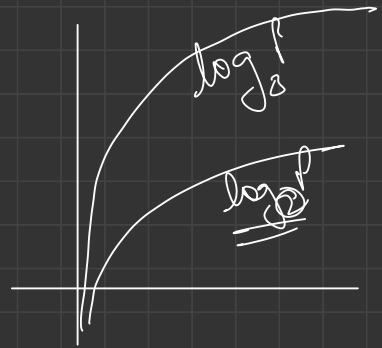
$$K \approx \log_2 p$$

$$TC: O(K)$$

$$: \underline{\underline{O(\log_2 p)}}$$

Total TC:

TC. to find Range + TC. to find Key



$$\log_2 P + \log_2 P$$

$$2 \log_2 P = \boxed{O(\log_2 P)}$$

→ index of key  
in infinite  
sorted array



```

int find (int[] arr, int target)
{
    if (target < arr[0])
        return -1;
}

```

$\left\{ \begin{array}{l} TC: O(\log P) \\ SC: O(1) \end{array} \right.$

```

int s1 = 0;
int e1 = 1;

```

```

while (arr[e1] < target)
{
    s1 = e1 + 1;
    e1 = 2 * e1;
}

```

$\int \rightarrow K \text{ jumps} \rightarrow \log P$

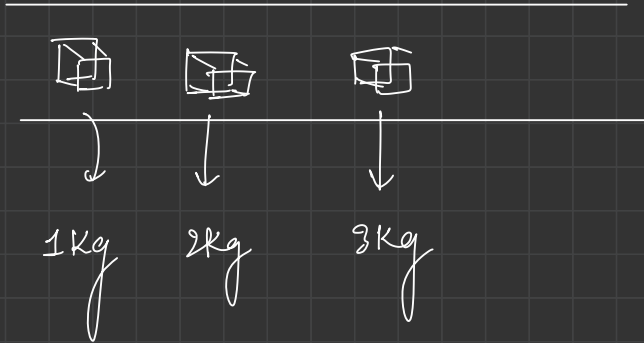
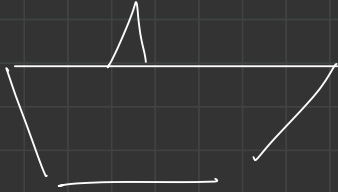
```

int idx = BinarySearch(arr, s1, e1, target);
System.out.println(idx);
}

```

$\rightarrow TC: O(\log P)$

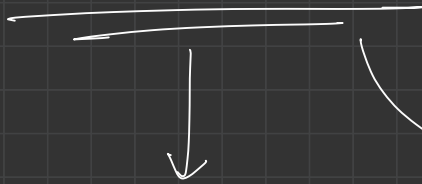
# Capacity to ship packages within 6 days



2 days

$A[] = [ \overset{0}{1}, \overset{1}{2}, \overset{2}{3}, \overset{3}{4}, \overset{4}{5}, \overset{5}{6}, \overset{6}{7}, \overset{7}{8}, \overset{8}{9}, \overset{9}{10} ]$

B = 5 days



1 day

10 days

{1} {2} ... {10}

{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

cap story

10 kg  
cap

Ans = ~~8~~ ~~2~~ ~~1~~ (15) → 15kg



cap 32kg

$A[] = [$   
0 1 2 3 4 5 6 7 8 9  
1, 2, 3, 4, 5, 6, 7, 8, 9, 10]  
↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

day 1 → 1 + 2 + 3 + 4 + 5 + 6 + 7  
day 2 → 8 + 9 + 10

days = 2

cap = 20kg

$A[i] = [ \begin{array}{cccccccccc} & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 1, & 2, & 3, & 4, & 5, & 6, & 7, & 8, & 9, & 10 \end{array} ]$   
 $\uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$

day 1 = 1 + 2 + 3 + 4 + 5  
day 2 = 6 + 7  
day 3 = 8 + 9  
day 4 = 10

days = 4

cap 14 kg

$A[] = [ \overset{0}{1}, \overset{1}{2}, \overset{2}{3}, \overset{3}{4}, \overset{4}{5}, \overset{5}{6}, \overset{6}{7}, \overset{7}{8}, \overset{8}{9}, \overset{9}{10} ]$

Day 1  $\rightarrow 1 + 2 + 3 + 4$

Day 2  $\rightarrow 5 + 6$

Day 3  $\rightarrow 7$

Day 4  $\rightarrow 8$

Day 5  $\rightarrow 9$

day = 10 kg

6 days

cap = 17kg

$A[] = [ \overset{0}{1}, \overset{1}{2}, \overset{2}{3}, \overset{3}{4}, \overset{4}{5}, \overset{5}{6}, \overset{6}{7}, \overset{7}{8}, \overset{8}{9}, \overset{9}{10} ]$

Day 1  $\rightarrow 1 + 2 + 3 + 4 + 5$

Day 2  $\rightarrow 6 + 7$

Day 3  $\rightarrow 8 + 9$

Day 4  $\rightarrow 10$

Day 4

cap = 15 kg

$A[] = [ \overset{0}{1}, \overset{1}{2}, \overset{2}{3}, \overset{3}{4}, \overset{4}{5}, \overset{5}{6}, \overset{6}{7}, \overset{7}{8}, \overset{8}{9}, \overset{9}{10} ]$

day 1  $\rightarrow 1 + 2 + 3 + 4 + 5$

day 2  $\rightarrow 6 + 7$

day 3  $\rightarrow 8$

day 4  $\rightarrow 9$

day 5  $\rightarrow 10$

day 25



# Minimum limit of balls in a bag

$$\text{arr}[1] = \{2, 4, 8, 2\} \quad \underline{\text{maxOpt} = 4}$$

→ (2, 2) (1, 3) ✓

$$\{2, 1, 3, 8, 2\} \quad \boxed{3}$$

→ (1, 7) (2, 6) (3, 5) (4, 4) ✓

$$\{2, 1, 3, 4, 4, 2\} \quad \boxed{2}$$

→ (1, 3) (2, 2) ✓

$$\{2, 1, 3, 1, 3, 4, 2\} \quad \boxed{1}$$

→ (1, 3)

$\{2, 1, 3, 1, 3, 1, 3, 2\}$

ans = 3

arr[] =  $\{2, 4, 8, 2\}$   
                    ↓  
                    4, 4

max opt = 4

$\{2, 4, 4, 4, 2\}$  [3]

$\{2, 2, 2, 4, 4, 2\}$  [2]

$\{2, 2, 2, 2, 2, 4, 2\}$  (1)

$\{2, 2, 2, 2, 2, 2, 2, 2\}$  [0]

2 = ans

$$\text{arr}[j] = \{ 2, 4, 8, 2 \}$$

$$\text{max opt} = 4$$

$$\boxed{\text{opt} = 0}$$

$$\boxed{\text{penalty} = 8}$$



$$\boxed{\text{opt} = \infty}$$

$$\boxed{\text{penalty} = 1}$$



$$\text{pens} = \cancel{4} 2$$



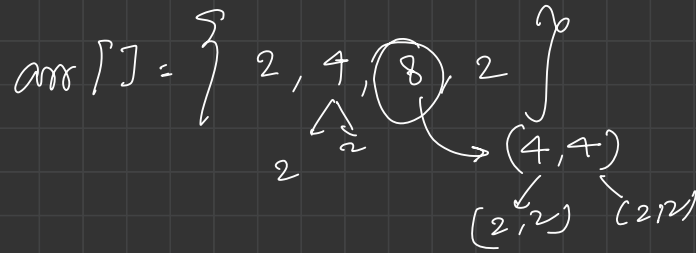
$$\text{arr}[1] = \{ 2, 4, 8, 2 \}$$

$$\{ 2, 4, 4, 4, 2 \}$$

$$\text{penalty} = 4$$

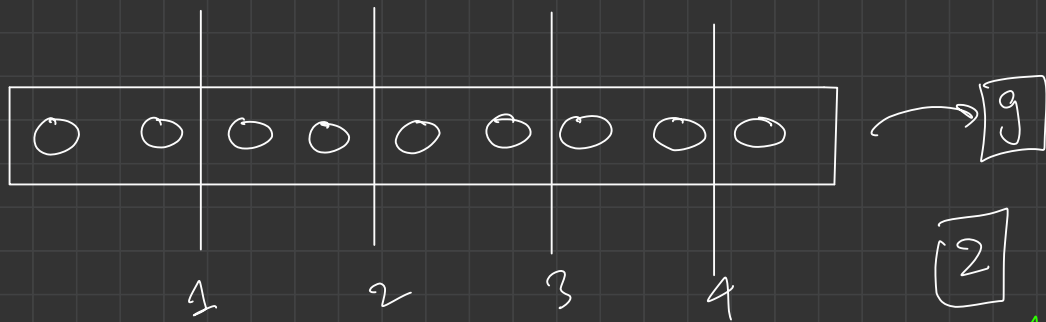
$$\boxed{4} \checkmark$$

$$\boxed{\text{opt} = 1}$$

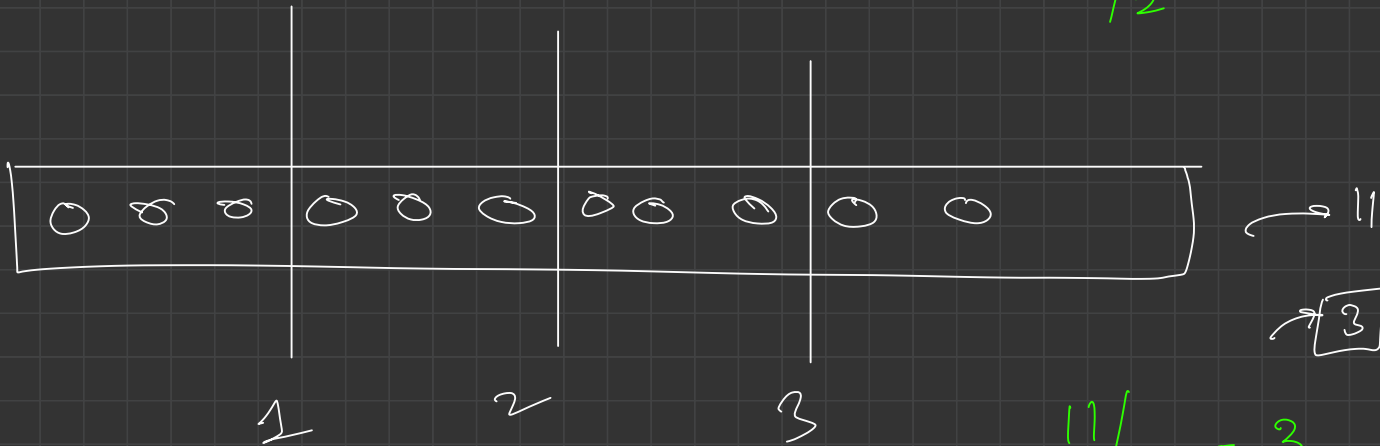


$$\boxed{\text{opt} = 1 + 3}$$

$$\text{penalty} = 2$$



$$9/2 = 4$$



$$11/3 = 3$$





$$15/4 = 3$$

15

$$\begin{cases} (7, 11) \\ (4, 4, 7) \\ (4, 7, 7, 3) \end{cases}$$



$$\checkmark \text{ min}^m \text{ no. of opt} = \frac{\text{Balls in a Bag}}{\text{max}^m \text{ one can hold}}$$

$$0 \ 0 \mid 0 \ 0 \mid 0 \ 0 \mid 0 \ 0 \quad x=8 \quad 2$$

$$8/2 = 4$$

$$0 \ 0 \ 0 \mid 0 \ 0 \ 0 \mid 0 \ 0 \ 0 \quad x=9$$

$$p=3$$

$$9/3 = \boxed{3}$$

if  $x \% p == 0$   
ans = (x/p) - 1

else  
ans = (x/p)

} Ps Possible

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End!

Binary Trees

Stacks  
Queue  
Hashing

Binary Search

Friday Sat Sund Mon

Th Wed