

Department of Physics, Chemistry and Biology

Master's Thesis

# **Search for Dark Matter in the Upgraded High Luminosity LHC at CERN**

**Impact of ATLAS phase II performance on a mono-jet analysis**

**Sven-Patrik Hallsjö**

Thesis work performed at Stockholm University

Linköping, June 4, 2014

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## **Abstract**

If your thesis is written in English, the primary abstract would go here while the Swedish abstract would be optional.





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I wish to dedicate this thesis to my mathematics teacher Ulf Rydmark without whom I would not have studied physics.

A big thank you to my family, fiancée and friends who have supported me throughout my education. A warm thank you to my friend Joakim Skoog who altered some of the images for me.

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*Linköping, June 2014*  
*Sven-Patrik Hallsjö*



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# Contents

<b>Notation</b>	<b>ix</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Research goals . . . . .	2
1.2 Theoretical Background . . . . .	3
1.2.1 Quantum mechanics and quantum field theory . . . . .	3
1.2.2 Nuclear, particle and subatomic particle physics . . . . .	4
1.2.3 The standard model of particle physics . . . . .	4
1.2.4 Dark matter . . . . .	5
1.2.5 Effective field theory . . . . .	6
1.2.6 Search for WIMPS . . . . .	8
1.3 Experimental overview . . . . .	10
1.3.1 LHC . . . . .	10
1.3.2 ATLAS . . . . .	11
1.3.3 Coordinate system . . . . .	12
1.3.4 Reconstructing data . . . . .	12
1.3.5 Pile-up . . . . .	13
1.3.6 Mono-jet analysis . . . . .	13
1.3.7 Phase II high luminosity upgrade . . . . .	14
1.3.8 Monte Carlo simulation . . . . .	15
<b>2 Validation of smearing functions</b>	<b>17</b>
2.1 Smearing functions . . . . .	18
2.2 Validation . . . . .	18
2.3 Results . . . . .	19
2.3.1 Leptons and photon . . . . .	19
2.3.2 Jets . . . . .	19
2.3.3 Missing Energy . . . . .	19
2.3.4 Expected results . . . . .	19
2.4 Discussion . . . . .	20
2.5 Conclusion . . . . .	20
2.5.1 Validation . . . . .	20
2.5.2 Some smearing independent on pile-up . . . . .	20

<b>3</b>	<b>Evaluating dark matter signals</b>	<b>21</b>
3.1	Signal to background ratio . . . . .	21
3.1.1	Selection criteria . . . . .	22
3.2	Comparing with published papers . . . . .	22
3.3	Figures of merit . . . . .	22
3.4	D5 operators . . . . .	22
3.5	Light vector mediator models . . . . .	23
3.6	Other selection criteria and observables . . . . .	23
3.7	Mitigating the effect of the high luminosity . . . . .	23
3.8	Results . . . . .	23
3.8.1	Limit on $M^*$ . . . . .	23
3.8.2	Previous results . . . . .	23
3.8.3	Limit on mediator mass . . . . .	23
3.9	Discussion . . . . .	23
3.10	Conclusion . . . . .	23
<b>4</b>	<b>Results and Conclusions</b>	<b>25</b>
4.1	Validation of smearing functions . . . . .	25
4.2	Signal to background ratio . . . . .	25
4.3	Other selection criteria and observables . . . . .	25
4.4	Mitigating the effect of the high luminosity . . . . .	25
4.5	Recommendations to mitigate the effect of the high luminosity . .	25
4.6	Suggestions for future research . . . . .	25
<b>A</b>	<b>Datasets</b>	<b>29</b>
A.1	Background processes . . . . .	29
A.2	D5 signal processes . . . . .	29
A.3	Light vector mediator processes . . . . .	29
	<b>Bibliography</b>	<b>31</b>

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# Notation

## NOTATIONS

Notation	Explanation
barn(b)	1 barn(b)= 10 <sup>-24</sup> cm <sup>2</sup>
$\oplus$	$a \oplus b = \sqrt{a^2 + b^2}$ , $a \oplus b \oplus c = \sqrt{a^2 + b^2 + c^2}$

## ABBREVIATIONS

Abbreviation	Expansion
ATLAS	A large Toroidal LHC ApparatuS
CERN	Organisation européenne pour la recherche nucléaire <sup>1</sup>
LHC	Large Hadron Collider
SM	the Standard Model of particle physics
WIMP	Weakly Interacting Massive Particle
WIMPS	Weakly Interacting Massive ParticleS
QED	Quantum ElectroDynamics
QFT	Quantum Field Theory
QM	Quantum Mechanics

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<sup>1</sup>Originally, Conseil Européen pour la Recherche Nucléaire



# 1

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## Introduction

Discrepancies in measurements of the rotations of galaxies indicate the presence of a large amount of matter which interacts through gravity, though not electromagnetically making it invisible to our telescopes. This matter is commonly referred to as dark matter. Since no known or hypothesised particle in the standard model of particle physics can be used as a candidate for dark matter, this has opened the door for new physics. Aside from dark matter there are other phenomena, such as the neutrino mass and the hierarchy problem, that can not be explained today.

At the Organisation européenne pour la recherche nucléaire (CERN) the interest now lies to discover any evidence of so called weakly interacting massive particles (WIMPS) which may be a candidate for dark matter. It is usually impossible to detect any interaction of dark matter candidates on the subatomic scale, however through looking at proposed interactions, searching for assumed decay channels and inconsistencies in momentum conservation it is hoped that signs will be found. Though as of April 8, 2014, none have been found.

Both these experiments and current theories now show that higher energies are required at the LHC to be able to see any signs. This is why the LHC and all detectors are undergoing a vast upgrading program [1]. In this thesis focus will be on the last part of the upgrade due for completion in 2023, known as the high luminosity-LHC phase II upgrade; and also on the ATLAS detector. The method used in this thesis focuses on looking at data which emulate conditions at the upgraded LHC.

## 1.1 Research goals

This research took place at Stockholm University from January 7th until **when?** During the research period the following tasks were set up and performed/answered:

- Implement a C++ programme that loops over the collisions inside the signal and background datasets.
- For each collision retrieve the relevant observables (variables used to extract the signal over the background) and apply "smearing functions" to emulate the effect of the high luminosity on the observables.
- For both signal and background datasets, compare observables before and after smearing. What observables are the least/most affected?
- Implement selection criteria that selects the signal collisions efficiently while reduces significantly the background. In a first step the selection criteria should be taken from existing studies.
- Selection criteria can be evaluated and compared with each other using a figure of merit  $P$ , that measures the sensitivity of the experiment to the dark matter signal. Calculate  $P$  for the given selection criteria before and after smearing.
- What is the effect of the high luminosity (smearing) on the value of  $P$ ?
- Investigate other selection criteria and observables, to mitigate the effect of high luminosity. Use  $P$  to rank different criteria after smearing.
- Conclude on the effect of the high luminosity on the sensitivity for dark matter and possible ways to mitigate its effects using alternative observables and selection criteria.



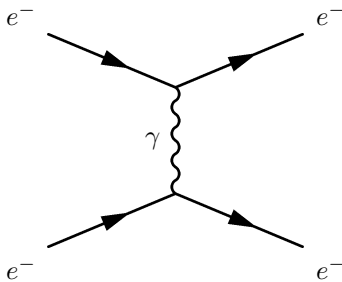
## 1.2 Theoretical Background

### 1.2.1 Quantum mechanics and quantum field theory

In the beginning of the 20th century, some physical phenomena could not be explained by classical physics, for example the ultra-violet disaster of any classical model of black-body radiation, and the photoelectric effect [2]. It was these phenomena that led to the formulation of quantum mechanics (QM), where energy transfer is quantized and particles can act as both waves and particles at the same time [3].

Combining QM with classical electromagnetism proved harder than expected, colliding a photon(em-field) and an electron (particle/wave) is quite tricky. This can be seen when trying to calculate the scattering between them both in a QM schema. One idea that came from this was to explain them both in the same framework, field theory. Also, trying to incorporate special relativity into QM suggested a field description where space-time is described using the metric formalism from differential geometry. The culmination of both of these problems is the first part of a Quantum field theory (QFT), Quantum electrodynamics (QED) which with incredible precision explains electromagnetic phenomena including effects from special relativity[4]. It is in this merging that antimatter was theorised, since it is a requirement for the theory to hold. After the discovery of antimatter, the theory was set in stone. Since this the theory has been altered somewhat to explain more and more experimental data. This is discussed more in subsection 1.2.2 and subsection 1.2.3.

To be able to calculate properties in QFT one uses the Lagrangian formalism [5]. Which gives a governing equation for the different physical processes. In general the Lagrangian used for the Standard model is quite complicated, one can thus focus on one of the different terms corresponding to a specific force. This can be done to calculate the so called cross-section for a process, which is related to the probability that that process will occur. A step to simplify the calculations is to use the so called Feynman diagrams, an example of which is given in figure 1.1.



**Figure 1.1:** An example of a Feynman diagram explaining an electron-electron scattering using QED.

Through the figure, which comes with certain rules, and knowing what the major process (in this case QED) one can calculate the cross-section [4]. it is this that is needed to predict is one will be able to detect new particles.

## 1.2.2 Nuclear, particle and subatomic particle physics

Many could argue that these branches of physics started after Ernest Rutherford famous gold foil experiment [6], where he discovered that matter is composed of matter with a nucleus, a lot of empty space and electrons.

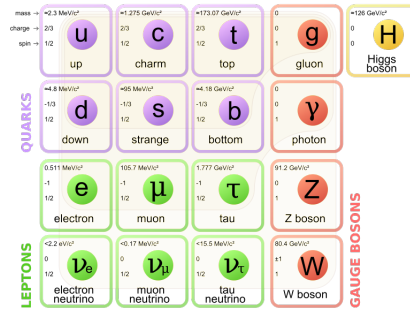
It was the that sparked the curiosity to see what the nucleus is made of and what forces govern the insides of atoms. After this, and the combination of the theoretical description given by QM, a lot more has been discovered and still more has been predicted. The newest of these is of course the Higgs particle, which was predicted through QFT and then discovered by CERN [7].

The discovered particles are often divided into different groups depending on the fundamental particles that build them up. For instance, particles build up of three quarks are known as hadrons. Particles with an integer spin are known as bosons whereas half-integer particles are known as fermions.

## 1.2.3 The standard model of particle physics

The standard model of particle physics, referred to simply as the standard model (SM), is the particle zoo which tries to categorize all the particles and that have been discovered experimentally. QFT has tried its best to explain the interactions between these particles and it has also predicted several particles by including symmetries [6]. Regarding SM, Gauge bosons are the force carriers for the different forces, quarks are the and leptons are the fundamental blocks that we know of so far. The difference between the later two is if they interact via the strong force or not.

**Figure 1.2:** The standard model of particle physics where the three first columns represent the so called generations, starting with the first. [8].



SM is today the pinnacle of particle physics and can be used to explain almost everything that occurs around us. There are however some problems [9]:

- No QFT for general relativity! Thus there is no link between gravity and the SM.
- Experimentally it has been shown that neutrinos have mass, though in SM they do not!
- Asymmetry between matter and antimatter can not fully be described.

- No dark matter candidate!
- No explanation that can contain dark matter.

In this thesis focus lies with dark matter, some more introduction to possible dark matter and different candidates in extensions to SM are explained in subsection 1.2.4.

### 1.2.4 Dark matter

A very quick introduction was given in the beginning of this chapter. Dark matter is the name given to the solution to the discrepancies of galactic rotations.

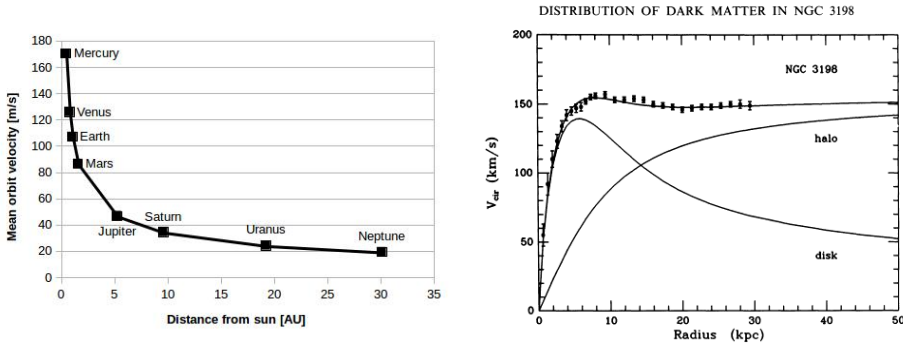
To explain this, focus on matter in a galaxy which are rotating around the center of the galaxy. Through Newtons law of gravity and the centrifugal force one can calculate the rotation speed dependent on the distance to the center of the galaxy. Since one of these forces is attractive and the other repulsive, if the matter is in a stable orbit around the galactic center (which they are) they must be equal and give us an expression for the speed depending on the distance. Newtons law can be written as the following:

$$F_{Gravitational} = G \frac{Mm}{r^2} = G_M \frac{m}{r^2} \quad F_{Centrifugal} = m \frac{V^2}{r} \quad (1.1)$$

where  $G$  is the gravitational constant,  $M$  the mass of the centre object,  $m$  the mass of the matter,  $r$  the distance between the two and  $V$  is the rotation speed. It has been simplified using  $G_M$  since all matter orbits the same galactic center. Setting the equations in (1.1) results in:

$$G_M \frac{m}{r^2} = m \frac{V^2}{r} \Leftrightarrow V^2 = \frac{G_M}{r} \Rightarrow V = \sqrt{\frac{G_M}{r}} \propto \frac{1}{\sqrt{r}} \quad (1.2)$$

where the speed is assumed to be positive and  $\propto$  means proportional. Through these simple calculations it shown that the rotation speed should decrease with and increased distance. The same reasoning can be applied to, our solar system where this is the case figure 1.3a. The relation in these units is  $V = \frac{107}{\sqrt{r}}$  where 107 can be used in (1.2) to calculate the mass of the sun. However when looking at galaxies, even when taking into account that one has to see the galaxies as a mass distribution and that the above is only true when outside of the inner mass half, this is not the case! In figure 1.3b experimental data can be seen from the galaxy NGC3198 with a fitted curve which does not decrease with the distance but is instead constant. This is the discrepancy which is solved by postulating the existence of dark matter. After this the big question arises, what could this dark matter consist of? What is known so far lies in the name. Dark since no electromagnetic interaction and matter since gravitational interaction. This means that it can not be made up of any barionic matter or anything in the Standard Model apart from neutrinos. The main topic and also the main contributor to the rotational discrepancies is known as cold dark matter. This is due to the matter having as low kinetic energy and have mass in the GeV scale [9, 12, 13]. This means however that neutrinos can not be a candidate, thus the standard model is



(a) Rotation speed of planets in our solar system. Based on data from [10].

(b) Rotation speed of matter in NGC3198 with a curve fitting and three different models, if only a dark model halo existed, if there was no dark matter and the correct, if both exist [11].

**Figure 1.3:** Different rotation curves, both for planets in our solar system and matter in the NGC3198 galaxy.

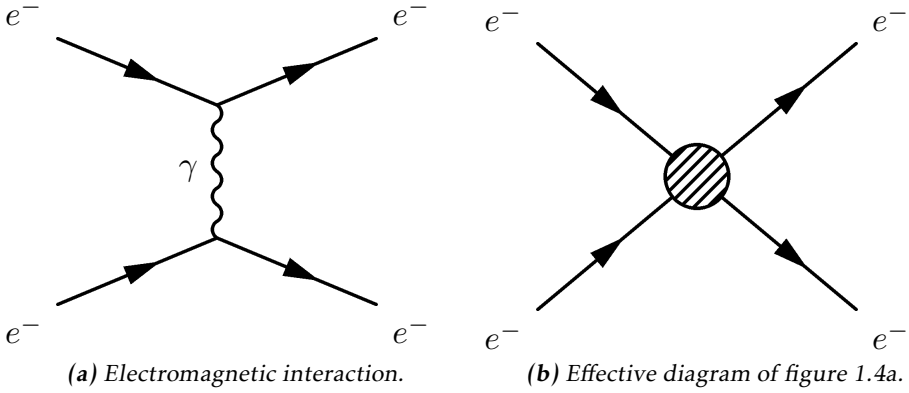
ruled out. There are several different ideas for how dark matter can be detected, [9]

- Ordinary matter interacting with ordinary matter can produce dark matter, known as production.
- Dark matter interacting with ordinary matter can produce dark matter, known as direct detection.
- Dark matter interacting with dark matter can produce ordinary matter, known as indirect detection.

In this thesis the focus lies with production. There are several theories how to detect dark matter in proton-proton collisions such that occur at CERN this is covered more in subsection 1.2.6.

## 1.2.5 Effective field theory

In quantum field theory the objective is usually to find the part of the Lagrangian which explains a type of interaction, known as the operator of the interaction and also to find the probability amplitude (cross-section) for a certain interaction. For complicated processes it is easier to employ certain conditions so that the small scale phenomena are simplified and the whole picture understood. This is called using an effective field theory and the idea can be seen in figure 1.4. The operator can be found through assuming the possible interactions and using the effective field theory [4]. The cross-sections can be found through the Feynman diagrams as described in subsection 1.2.1.



**Figure 1.4:** Feynman diagram of an electron-electron scattering, both as an ordinary diagram and as its effective version, where the details are hidden in the blob.

In this thesis the same effective field theory as in [12, 14] will be considered. The WIMP (usually denoted  $\chi$ ) is assumed as the only particle in addition to the standard model fields.  $\chi$  will be assumed odd under some  $Z_2$  symmetry. This means that an even number of  $\chi$  must be in every coupling. It is assumed that the whatever mediator exists is heavier than the WIMPs, meaning that their interactions are in higher order terms of the effective field theory and thus not included in the operators. For simplicity, the WIMPs are assumed to be SM singlets, thus invariant under SM gauge transformations, and the coupling to the Higgs boson is neglected.

The focus for the operators will be quark bilinear operators on the form  $\bar{q}\Gamma q$  where  $\Gamma$  is a  $4 \times 4$  matrix of the complete set,

$$\Gamma = \{1, \gamma^5, \gamma^\mu, \gamma^\mu \gamma^5, \sigma^{\mu\nu}\} \quad (1.3)$$

This will dictate how the operators are written, more of why this is done can be found in [4, 12, 14].

This, together with the coupling with the strong force defines an effective field theory of the interaction of singlet WIMPs with hadronic matter. It is a non-renormalizable field theory which will break down when the mediator mass is close to the mass of the WIMP. The condition for this is derived in [14] and gives:

$$M > 2m_\chi \quad (1.4)$$

where  $m_\chi$  is the mass of the WIMP and  $M$  is the mass of the mediator. There is also the requirement that:

$$M \lesssim 4\pi M_* \quad (1.5)$$

where  $M_*$  is the energy scale where the effective theory is no longer a good ap-

proximation.

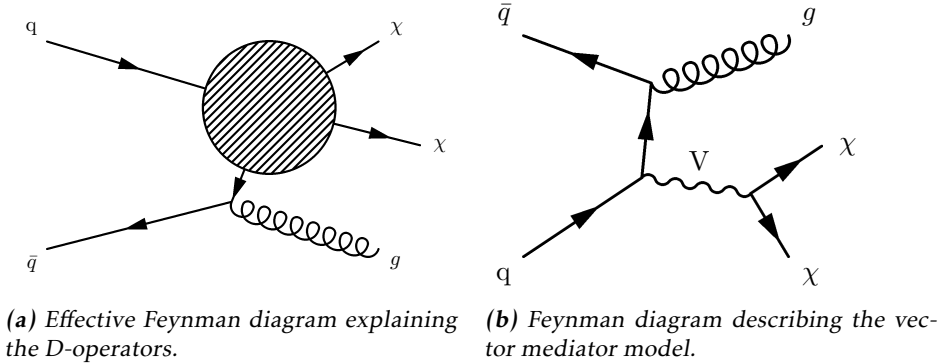
In this work, WIMPS are assumed to be Dirac fermions (half integer spin and is not its own antiparticle).

In table 1.1 the operators which are integrated out via the effective field theory and are of interest in this thesis are given.

Name	Initial state	Type	Operator
D1	qq	scalar	$\frac{m_q}{M_*^3} \bar{\chi} \chi \bar{q} q$
D5	qq	vector	$\frac{1}{M_*^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q$
D8	qq	axial-vector	$\frac{1}{M_*^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q$
D9	qq	tensor	$\frac{1}{M_*^2} \bar{\chi} \sigma^{\mu\nu} \chi \bar{q} \sigma_{\mu\nu} q$
D11	gg	scalar	$\frac{1}{4M_*^3} \bar{\chi} \chi \alpha_s (G_{\mu\nu}^a)^2$

**Table 1.1:** Table based on discussion in [13]

Where D denotes that the WIMPS are assumed to be Dirac fermions. These can all be described using figure 1.5a



**Figure 1.5:** Feynman diagrams describing the used signal models.

Another model which is considered is when the WIMP mass is close to the mediator mass. Then the effective theory fails and the process is assumed to be described by figure 1.5b.

## 1.2.6 Search for WIMPS

The search of WIMPS is based on a mono-jet analysis which is described in subsection 1.3.6. This method revolves around looking at all energy before and after

a collision and making sure energy conservation exists. If it does not, then something has happened which the detectors can not detect. If it is so that the models from subsectionrefsec:tb:subsec:eft can explain the missing energy, then a model for WIMPS has been found.

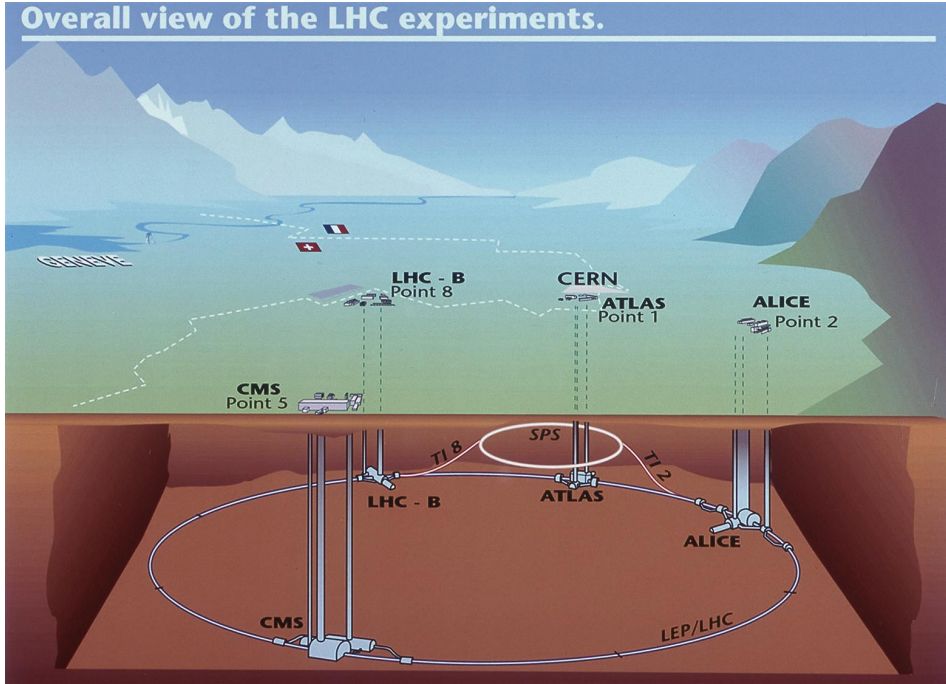
Since the search for WIMPS at the LHC is based on looking at the missing energy, not actual detection, the experiment can not establish if a WIMP is stable on a cosmological time scale and thus if it is a dark matter candidate [13]. This means that if a candidate is found, it may still not be the dark matter that is needed to explain the cosmological observations.

The different theories discussed in subsection 1.2.5 requires some process in which quarks and anti-quarks are produced. This process happens in a lot of different accelerators. The main problem is that nothing has been found low energy levels. This is why it is very interesting that the LHC is undergoing a upgrade that will allow higher energy levels, see subsection 1.3.7. With this the processes can be given higher energy and thus the produced particles can be comprised of higher mass.

## 1.3 Experimental overview

### 1.3.1 LHC

The Large hadron collider (LHC) is a particle accelerator located at CERN near Geneva in Switzerland, see figure 1.6. The accelerator was built to explore physics beyond the standard model and to make more accurate measurements of standard model physics. Before it was shut down for an upgrade in 2012 it was able to accelerate two proton beams to such a velocity that they had an energy of 4 TeV which gives a center of mass energy,  $\sqrt{s} = 8$  TeV. It should be noted that the proton beam is not homogeneous, it is comprised of bunches of protons with enough spacing that bunch collisions can happen independent of each other. Apart from the energy, the ability for an accelerator to produce interactions can be calculated through the instantaneous luminosity of the LHC was  $10^{34} \text{ cm}^{-2}\text{s}^{-1}$  or  $10\text{nb}^{-1}\text{s}^{-1}$  where 1 barn(b)=  $10^{-24} \text{ cm}^2$ . All values taken from [15].



**Figure 1.6:** Figure showing the LHC and the different detector sites[16]

The instantaneous luminosity, often just denoted luminosity, can be defined in different ways depending on how the collision takes place. For two collinear intersecting particle beams it is defined as:

$$\mathcal{L} = \frac{fkN_1N_2}{4\pi\sigma_x\sigma_y} \quad (1.6)$$



where  $N_i$  are the number of particles in each of the bunches,  $f$  is the frequency at which the bunches collide,  $k$  the number of colliding bunches in each beam, and  $\sigma_x$  ( $\sigma_y$ ) is the horizontal (vertical) beam size at the interaction point. Since the instantaneous luminosity increases quadratically with more particles in each bunch this would be a good strategy. However aside from the difficulties to create and maintain a beam with more particles, a large  $N_i$  increases the probability for multiple collisions per bunch crossing, referred to as pile-up. Pile up will be a key aspect which is described more in subsection 1.3.5.

The expected number of events can be calculated by using the instantaneous luminosity through the following:

$$N = \sigma \int \mathcal{L} dt := \sigma \mathcal{L} \quad (1.7)$$

where  $\mathcal{L}$  is the integrated luminosity and  $\sigma$  is the cross section which is often measured in barn. The integrated luminosity is a measurement of total number of interactions that have occurred over time. Before the LHC was shut down this values was  $20.8 \text{ fb}^{-1}$ .

The cross section is defined through the integral of the differential cross section, as explained in subsection 1.2.1, over the whole solid angle:

$$\sigma = \oint d\Omega \frac{d\sigma}{d\Omega} \quad (1.8)$$

The cross section is therefore a measure of the effective surface area seen by the impinging particles, and as such is expressed in units of area. The cross section is proportional to the probability that an interaction will occur. It also provides a measure of the strength of the interaction between the scattered particle and the scattering center. Further details can be found in reference [17]

### 1.3.2 ATLAS

As seen in figure 1.6, there are several detectors at CERN. One of these is a large toroidal LHC apparatus (ATLAS) which is a general purpose detector that uses a toroid magnet. Its goal is to observe several different production and decay channels. The detector is composed of three concentric sub-detectors, the Inner detector, the Calorimeters and the Muon spectrometer [18].

The Inner detectors main job is to detect the tracks of the particles and their interaction with the material in the detector.

The Calorimeters, the electromagnetic and hadronic, are used to calculate the energy contained in the different particles (electromagnetic get this and that, hadronic get this and that).

The Muon spectrometer is used to detect signs of muons, which will simply pass through the other detectors without leaving a trace.

From this, it is known that neutrinos, and as assumed in this thesis WIMPS pass through all the detectors without leaving a trace.

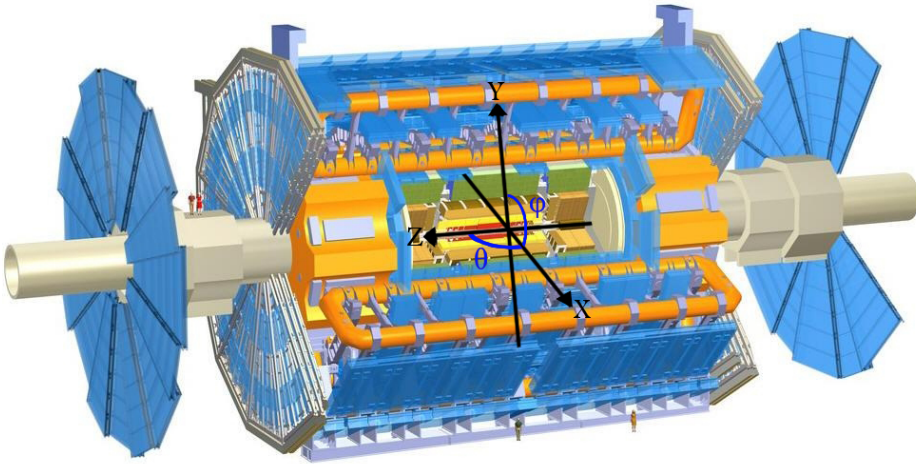
### 1.3.3 Coordinate system

The coordinate system of ATLAS, seen in figure 1.7 is a right-handed coordinate system with the x-axis pointing towards the centre of the LHC tunnel, and the z-axis along the tunnel/beam (counter clockwise) seen from above. The y-axis points upward. The origin is define as the interaction point. A cylindrical coordinate system is also used for the transversal plane.  $(R, \phi, Z)$ . For simplicity the pseudorapidity of particles from the primary vertex is defined as:

$$\eta = -\ln\left(\tan \frac{\theta}{2}\right) \quad (1.9)$$

where  $\theta$  is the polar angle (xz-plane) of the particle direction measured from the positive z-axis.  $\eta$  is through this definition invariant under boosts in the z-direction.

It is quite common to calculate the distance between particles and jets in the  $(\eta, \phi)$  plane,  $d = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$



**Figure 1.7:** Figure showing the ATLAS detector and the definition of the orthogonal Cartesian coordinate system. Image altered from[19]

### 1.3.4 Reconstructing data

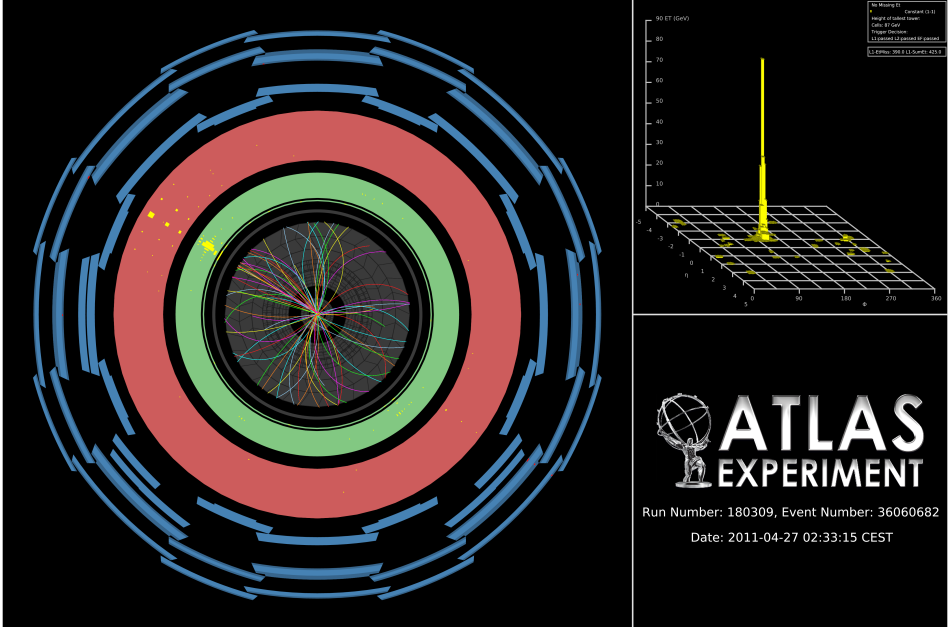
To be able to compare the emulated data to measurable data it is important to include effects of the detectors. This is done using so called smearing functions which try to emulate the reconstruction of data.

The reconstruction process of data [18], is based on what response is given from the detectors. It is affected by pile-up and the energy of that which is detected. The reconstruction process is not specifically used in the thesis, however the smearing functions are discussed in section 2.1.

### 1.3.5 Pile-up

Pile-up is defined as the average number of proton-proton collisions that occur per bunch crossing per second. It is denoted as  $\langle\mu\rangle$ .  $\mu$  can be calculated by adjusting a Poisson distribution to fit the curve created by the number of interactions per bunch crossing at a given luminosity. When this is done  $\mu$  will be the mean value of the Poisson distribution.

### 1.3.6 Mono-jet analysis



*Figure 1.8: Image of a mono-jet event [20].*

Transversal energy since it is known that it is almost zero before the collision and that it is unknown the amount of energy before and after in the z-direction. (Hard to create a detector that does not block the beam.)

When measuring the transversal energy one can in some interactions find inconsistencies, such as jets that are in excess in one direction. In figure 1.8 one can see a high energetic jet which gives an excess of transversal energy in one direction after the collision. Since there is no balancing jet there must be transversal energy that is not detected, denoted  $E_T^{Miss}$ , since it was close to zero before the collision. This gives an indication that there energy to balance this that simply can not be detected. This could for instance be neutrinos or the sign of a new particle.

Jets are showers of particles that are produced at collisions. They are composed of highly energetic quarks and/or gluons. Since the gluons have self interaction, they split into even more gluons which then results in shower of particles mov-

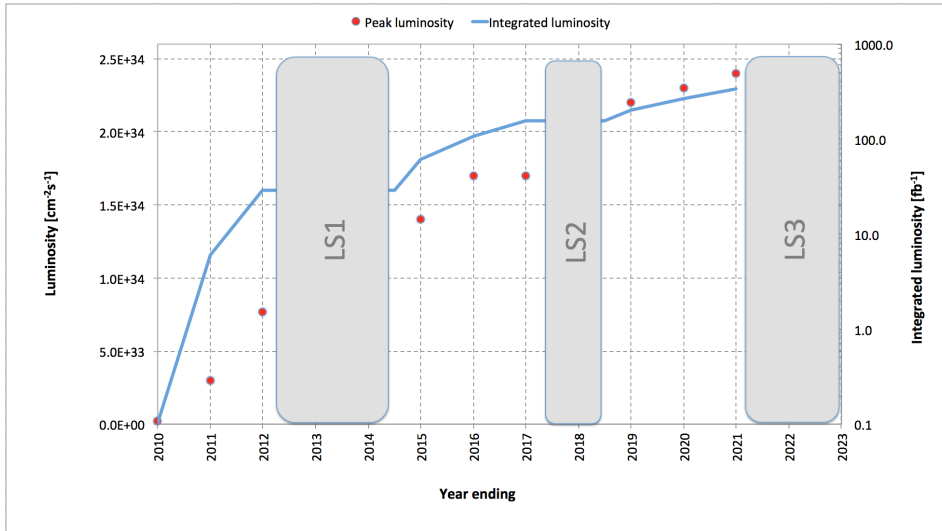
ing in the same direction. In the final stages the quarks and gluons can combine to form larger particles. It is by measuring these end products that one can gain more information about the collision which created the jet.

There are two main concepts to the analysis, signal and background. The signal is what theoretically should be detected by a assumed process. In this thesis the different dark matter processes, from subsection 1.2.5, will constitute different signals. However to know that the missing energy is sign of the signal then one must understand all the other components that could contribute to the missing energy.

The background comprises of all the background processes that occur and that could contribute to the missing energy. By finding so called Control regions, where background process are in excess, one can model the missing energy by how many neutrinos come from the processes.

### 1.3.7 Phase II high luminosity upgrade

At the moment, the whole LHC is undergoing a huge upgrade program which be finalized around 2022-2023, denoted the high luminosity upgrade, or HL-upgrade. The upgrade contains of different stages, meaning that the upgrade will halt for periods so that experiments can take place. In figure 1.9 one can see the three



**Figure 1.9:** A graph showing the upgrading timetable with the instantaneous luminosity, denoted luminosity, and integrated luminosity expected in the different stages.

proposed upgrades. LS1 is denoted phase 0, LS2 phase I and LS3 phase II.

LS1 is the upgrade which will take the LHC to its designed performance.

LS2 will take the LHC to the ultimate designed instantaneous luminosity.

LS3 which is the upgrade which is of focus in this thesis, will increase the instantaneous luminosity yet again. Though for this to happen a modification of the whole LHC must be done, instead of just an upgrade and maintenance as before.

The following is expected for the experiments done after phase II:

Entity	Expected	Last run (2012)
Instantaneous luminosity	$\mathcal{L} \sim 50 \text{ nb}^{-1} \text{ s}^{-1}$	$\mathcal{L} \sim 10 \text{ nb}^{-1} \text{ s}^{-1}$
Integrated luminosity	$\mathcal{L} = 1000 - 3000 \text{ fb}^{-1}$	$\mathcal{L} = 20 \text{ fb}^{-1}$
Pile-up	$\langle \mu \rangle = 140$	$\langle \mu \rangle = 20$
Center of mass energy	$\sqrt{s} = 14 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$

**Table 1.2:** Expected running values for the Phase II HL-upgraded LHC with older values for comparison [21].

Where it should be noted that the integrated luminosity indicates the total amount of data which will be collected after the upgrade is completed before the next upgrade takes place.

### 1.3.8 Monte Carlo simulation

As mentioned before, in this thesis only emulated data has been used. This data is created by using a Monte Carlo simulation of the background processes and the expected signal. To do this a program called MadGraph is used.

MadGraph [22] starts with Feynman diagrams and then generates simulated events based on lots of different parameters. To create correct simulations for this analysis PYTHIA has been used.

PYTHIA [23] is a package which adds the correct description of jets and missing energy to MadGraph. PYHIA also adds the correct description of pile-up.

The tool to access all this data and analyse it a tool called ROOT was used. ROOT is used for programming high energy physics related tools [24]



# 2

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## Validation of smearing functions

One might assume that using a Monte Carlo simulation it would be easy to model and emulate the whole process, from collision to detection and reconstruction in the upgraded LHC. It is possible, but it requires a lot of computing power. Instead one can use one simulation and a mathematical model to calculate the estimated response in the detector. This was validated and used in this thesis to be able to create the data needed for further analysis.

This was done by using a Monte Carlo simulation of a proton-proton collision and applying the official Truth to reco code, also known as the smearing functions, that was developed using previous studies [1, 25]. to simulate how the detector and the reconstruction is affected by the increased luminosity and the pile-up that comes with this.

The code uses the experimental data from the previous studies to smear the reconstructed energy and momenta, it is from this that the name smearing functions comes. The key feature of those studies were that the direction of the momenta does not alter direction and also that only jets and  $E_T^{miss}$  are effected by pile-up, more in subsection 2.3.

## 2.1 Smearing functions

**Put in introduction?** The particles that are directly detectable in ATLAS are: electron, photon, muon, tau. Aside from this jets can be detected, and from this  $E_T^{Miss}$  can be calculated. This means that the all detectable entities must have their own smearing functions.

Somehow explain the entities used.

The electron and photon have the same smearing since they are both detected in a similar way. Perhaps add more to the introduction about each part of the detector. or simply write that here?

The smearing takes a lot into account, efficiency etc...

## 2.2 Validation

To validate the smearing functions a comparison with [25] was made where the standard deviation, depending on the energy of momentum value of an entity, was given, see subsection 2.3.4. To calculate this some simulated processes were needed to extract data, see table 2.1.

**Table 2.1:** Different processes from where data has been taken. Each sample is a simulation of a physical process, the simulation names can be found in appendix A

Data	Process
Electron	$W \rightarrow e \nu$
Muon	$W \rightarrow \mu \nu$
Tau	$W \rightarrow \tau \nu$
$\gamma$	$\gamma$ + Jet sample
Jets	Jet sample
$E_T^{Miss}$	$Z \rightarrow \nu \nu$ + Jet sample

By plotting the data for each data point before and after the smearing function, denoted truth and reco, for that data point had been used, one could verify the functions. It was done looking at the reco data for a given truth energy or momentum value. The reco data will be spread out, since there should be effects **explain more about efficiency, why spread?!**.

Trying to fit a Gaussian curve to this data will then result in the mean value, and the standard deviation. The mean value is not of interest for the purposes of the thesis, though it is this standard deviation which is compared.



## 2.3 Results

### 2.3.1 Leptons and photon

### 2.3.2 Jets

### 2.3.3 Missing Energy

### 2.3.4 Expected results

The expected response has been calculated and taken from: ATL-PHYS-PUB-2013-004 Find more information in my presentation. also mention no pile-up dependence of leptons.

That this is true can be shown from **figures and references from nonpileupdep.txt presentation!**. The smearing functions should be given!

To validate the smearing code comparisons were made with [25] which gave the following formulation for the expected rms:

Process	Absolute rms
Electron & photon	$\sigma = 0.3 \oplus 0.1 \sqrt{E(\text{GeV})} \oplus 0.01 E(\text{GeV}),  \eta  < 1.4$ $\sigma = 0.3 \oplus 0.15 \sqrt{E(\text{GeV})} \oplus 0.015 E(\text{GeV}), 1.4 <  \eta  < 2.47$
Muon	$\sigma = \frac{\sigma_{id} \sigma_{ms}}{\sigma_{id} \oplus \sigma_{ms}}$ $\sigma_{id} = P_T(a_1 \oplus a_2 P_T)$ $\sigma_{ms} = P_T(\frac{b_0}{P_T} \oplus b_1 \oplus b_2 P_T)$
Tau	$\sigma = (0.03 \oplus \frac{0.76}{\sqrt{E(\text{GeV})}}) E(\text{GeV})$
Jet	$\sigma = P_T(\text{GeV})(\frac{N}{P_T} \oplus \frac{S}{\sqrt{P_T}} \oplus C)$
$E_T^{miss}$	$\sigma = (0.4 + 0.09 \sqrt{\mu}) \sqrt{\sum E(\text{GeV})} + 20 \mu$

- For muon: Where  $a_i$  and  $b_i$  are dependent on  $\eta$ .
- For tau: Fixed at 3 prong. 1 prong exists though was not used in this thesis. Where prong refers to the different amount of tracks that were from which they were reconstructed.
- For Jet: Where  $N$ ,  $S$ , and  $C$  depend on  $\eta$ .  $N$  is also dependent on the pile-up that is simulated.  
Where  $\eta$  is the same as discussed in subsection 1.3.3
- All parameters can be found in [25].

Remember for the discussion to mention different types of rms, relative or absolute. and the problem which occurred with this and the papers faults.

WHAT IS 3prong! must be explained.

## **2.4 Discussion**

## **2.5 Conclusion**

### **2.5.1 Validation**

### **2.5.2 Some smearing independent on pile-up**

# 3

---

## Evaluating dark matter signals

The main goal of the thesis is to investigate if certain dark matter signals can be detected after the high luminosity upgrade. One immediate worry is that the background will be large in comparison to the signal, thus making it undetectable.

The following signals models have been used: **Here only the operators should be explained, or different models. The names and the MC here or in appendix?** They are explained somewhat in the introduction. Each of these has been evaluated in different signal regions and the detectability has been evaluated using a statistical P-value. This process has been performed at different pile-up values.

**What background existed? How was it simulated in MC? Should that be here or in appendix?**

Dont mention, but good to know. Used METpt in all histograms, with the weight as in main.C and mainclass.C.

### 3.1 Signal to background ratio

What I am doing now, looking at what signal? What are the different background processes? What and why was the weight used?

Signals should be explained somewhat in the introduction.

Look at presentation, is it worth bringing up the first signal regions when the data has already been filtered? Should that be here?

### 3.1.1 Selection criteria

What criteria were used and more importantly why? It is quite important that you can explain why this was used.

## 3.2 Comparing with published papers

To verify that the background data was correct it was compared with [26], in which the luminosity is  $10 \text{ fb}^{-1}$  and thus the expected values from the paper scaled up with a factor 100. **Also, somewhat unexpectedly is that the difference in center of mass energy required the cross-sections to be lowered than compared with the upgrade.** The signal region used in the article were the following:

- Jet veto, require no more than 2 jets with  $p_T > 30 \text{ GeV}$  and  $|\eta| < 4.5$
- Lepton veto, no electron or muon, leading jet with  $|\eta| < 2.0$  and  $\Delta\phi(\text{jet}, E_T^{\text{miss}}) > 0.5$  (second-leading jet)
- Leading jet with  $p_T > 500 \text{ GeV}$  and  $E_T^{\text{miss}} > 500 \text{ GeV}$

The article has several different signal regions, the difference is the last item, unfortunately since the simulated events are already filtered before the analysis only one of the regions could be used.

Process	Simulated events	Expected events (Scaled to $1000 \text{ fb}^{-1}$ )
$Z \rightarrow \nu\nu$	27675.1	27000
$W \rightarrow \tau\nu$	6506.09	3900
$W \rightarrow e\nu$	1660.06	1600
$W \rightarrow \mu\nu$	2048.77	4200
Total background	37890	36700

**Table 3.1:** Comparison of the simulated and expected events from [26].

The scaling is done by multiplying by a factor 100. In table 3.1 a comparison has been made. It can be seen that the simulated events and expected events coincide on all accounts apart from  $W \rightarrow \tau\nu$ ,  $W \rightarrow \mu\nu$  and thus the total as well. **This can be explained by better separation of  $\mu, \tau$  and missing energy.**

## 3.3 Figures of merit

P-value, see more in Majas phd thesis when completed.

The percentage value of the probability that the signal is "covered" by the fluctuations in the background. Try matching two Gaussians.

### 3.4 D5 operators

Discuss  $M^*$ , and the difference in mDM. From presentation given, 3-4 April.

### 3.5 Light vector mediator models

Discuss  $M_m$ , width, and the difference in mDM. From presentation given, 3-4 April.

### 3.6 Other selection criteria and observables

New signal regions.

Selection Criteria					
Jet veto, require no more than 2 jets with $p_T > 30\text{GeV}$ and $ \eta  < 4.5$					
Lepton veto, no electron or muon					
Leading jet with $ \eta  < 2.0$ and $\Delta\phi(\text{jet}, E_T^{\text{miss}}) > 0.5$ (second-leading jet)					
signal region	SR0	SR1	SR2	SR3	SR4
minimum leading jet $p_T$ (GeV)	120	350	600	800	1000
minimum $E_T^{\text{Miss}}$ (GeV)	120	350	600	800	1000
signal region	SR0	SRa	SRb	SRc	SRd
minimum leading jet $p_T$ (GeV)	350	350	350	350	350
minimum $E_T^{\text{Miss}}$ (GeV)	120	350	600	800	1000

### 3.7 Mitigating the effect of the high luminosity

### 3.8 Results

#### 3.8.1 Limit on $M^*$

Give both at 10fb-1 and 1000fb-1.

#### 3.8.2 Previous results

Valerios paper for instance.

#### 3.8.3 Limit on mediator mass

Are there previous results?

### 3.9 Discussion

### 3.10 Conclusion



# 4

---

## Results and Conclusions

### 4.1 Validation of smearing functions

Have some discussion.

### 4.2 Signal to background ratio

### 4.3 Other selection criteria and observables

### 4.4 Mitigating the effect of the high luminosity

### 4.5 Recommendations to mitigate the effect of the high luminosity

### 4.6 Suggestions for future research

Sätt av ett kort kapitel sist i rapporten till att avrunda och föreslå rikningar för framtida utveckling av arbetet.

Saving as reference. test citing as: Here we cite Duck [27] [27].

If the above works, remember to edit myreferences.





# Appendix



# A

---

## Datasets

- A.1 Background processes**
- A.2 D5 signal processes**
- A.3 Light vector mediator processes**



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