

## **DESIGN AND ANALYSIS OF ALGORITHMS**

### **Sorting Algorithms**

Sorting algorithms arrange data in a particular order (usually ascending or descending).

- **Selection Sort:** Repeatedly selects the smallest (or largest) element and places it in the correct position. Simple but inefficient for large datasets ( $O(n^2)$ ).
- **Insertion Sort:** Builds the final sorted array one element at a time by comparing and inserting elements into their correct position. Efficient for small or partially sorted arrays ( $O(n^2)$ ).
- **Merge Sort:** Divides the array into halves, recursively sorts them, and merges the sorted halves. More efficient than selection and insertion sorts ( $O(n \log n)$ ).
- **Quick Sort:** A divide-and-conquer algorithm that selects a "pivot" and partitions the array around it, then sorts each partition. Average case  $O(n \log n)$ , worst case  $O(n^2)$ , but practical and fast.

### **Searching Algorithms**

Searching algorithms are used to find elements in a dataset or validate the existence of an element.

- **Binary Search:** Efficiently searches a sorted array by repeatedly dividing the search interval in half. Time complexity is  $O(\log n)$ .

### **Data Structures**

Efficient data management is key to effective algorithms. Some important data structures introduced:

- **Stacks:** A last-in, first-out (LIFO) data structure. Used in algorithms like depth-first search (DFS) and function call management.
- **Queues:** A first-in, first-out (FIFO) data structure. Useful in breadth-first search (BFS) and task scheduling.
- **Priority Queues:** A queue where elements are dequeued based on priority rather than arrival order. Used in Dijkstra's and Prim's algorithms.

### **Divide and Conquer**

This technique splits a problem into smaller subproblems, solves each subproblem independently, and combines the results. Both **merge sort** and **quick sort** fall into this category.

### **Union-Find (Dynamic Connectivity)**

Union-Find is a data structure used to manage a set of elements that are partitioned into disjoint subsets. It supports two main operations:

- **Union:** Merge two sets.
- **Find:** Determine which set an element belongs to. Efficient for solving connectivity problems (e.g., determining if two nodes in a graph are connected).