

Offats. Day 4.

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(1)

Continuation of Z-Score

(2)

Central Limit Theorem

(3)

Probability

(4)

Permutation and Combination

(5)

Covariance

(6)

Pearson and Spearman Rank Correlation

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Continuation of Z-Score.

(1)

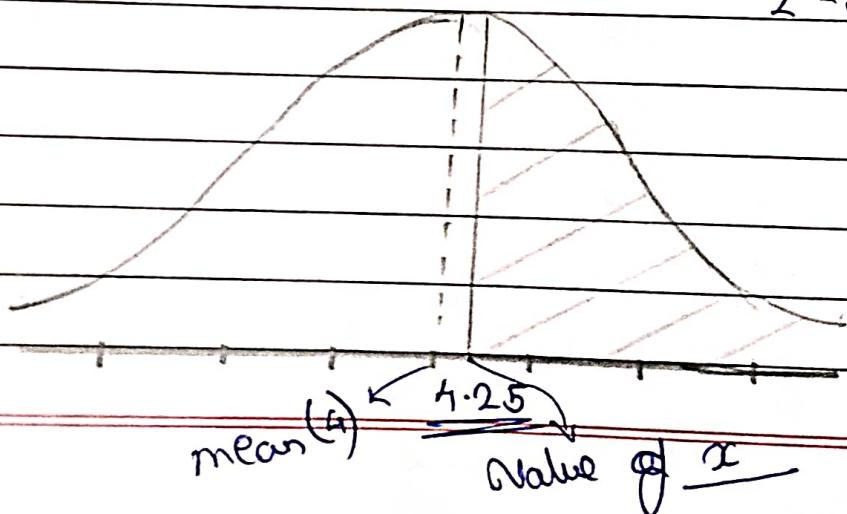
Z-Score

$x = \{1, 2, 3, 4, 5, 6, 7\}$, Let Consider
the mean = 4 and Standard deviation =

$$\bar{x} = 4.25$$

$$Z\text{-Score} = \frac{x_i - \mu}{\sigma / \sqrt{n}}$$

$$= \frac{4.25 - 4}{\sqrt{7}} \\ = 0.25$$



Q. What Percentage of Score falls above 4.25?

Symmetrical

area of the entire curve
= 1 or 100%

Body

Below

4.25

Tail

above.

If we subtract entire area with Tail
It will result, called Body.

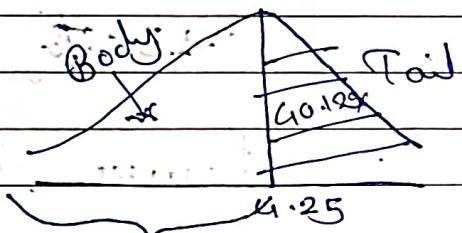
Formula = 1 - area of Body = Area under the Tail

As here our distance between

4 and 4.25 was 0.25, with the help
of Z-Score table we find the value of
0.0.25 is 0.59871.

So with Z-score table

$$1 - 0.59871 = 0.40129$$



So we can say that 40.129%
score fall above 4.25

$$0.59871$$

Normal Distribution is symmetric about the mean

$$0.59871 + 0.59871 = 1.19742$$

Statistics

* Z-Score to know how many Standard deviation away from the mean a specific variable is there.

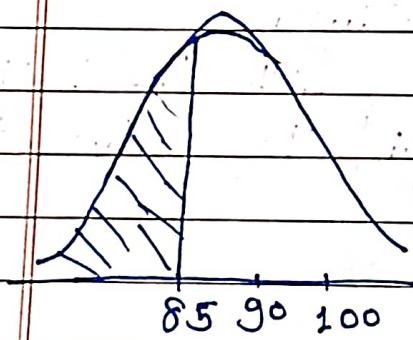
(i) Normal Distribution

(ii) Log normal Distribution

(iii) Power Law

Agenda

(Q.) In India the average IQ is 100, with a standard deviation of 15, what is percentage of population would you expect to have an IQ lower than 85?



$$\mu = 100$$

$$\sigma = 15$$

$$\text{Z-Score} = \frac{85 - 100}{15}$$

$$= -1$$

$$(0.1587)$$

$$= -1$$

$$(1) \text{ Lower than } 85 = 0.1587$$

area of Red

$$(2) \text{ Higher than } 85 = 84.13\%$$

$$0.1587^{-1}$$

$$= 0.8413$$

$$(3) \text{ Between } 85 \text{ to } 100 = 0.3413 (34.13\%)$$

$$0.5 - 0.1587 = 0.8413$$

Find the % of Score between 100 to 125
Standard deviation is 15?

$$m = 100$$

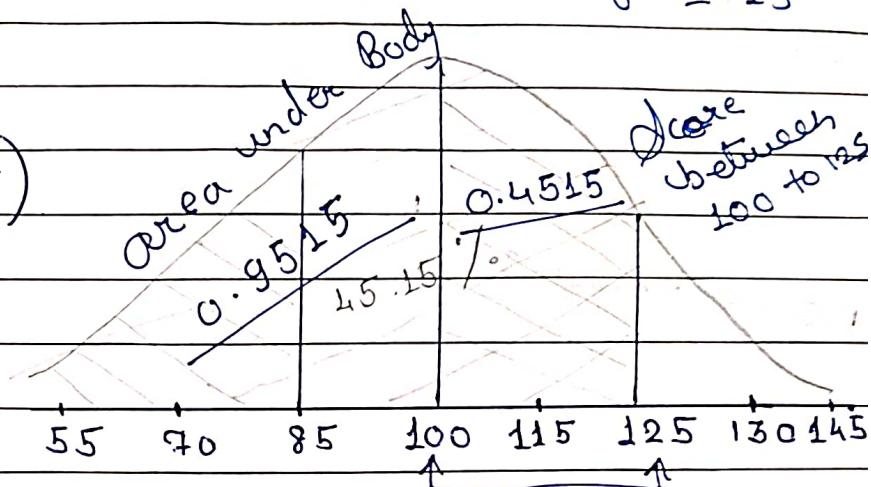
$$\sigma = 15$$

$$z = \frac{125 - 100}{15}$$

$$= 1.66 \quad (.9515)$$

$$\therefore 0.9515 - 0.5$$

$$\therefore \underline{0.4515}$$



Find the % of Score between 85 to 115

$$\text{Z-score} : \frac{85 - 115}{15} = \frac{-30}{15} = -2$$

$$= -2 (0.02275).$$

$$\begin{aligned}\text{Area of Body} &= 0.02275 - 0.5 \\ &= -0.47725 \\ &= \underline{47.725 \%}\end{aligned}$$

Important
Topic

Central Limit Theorem.

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$n > 30$ = Z Table
 $n < 30$ = T Table

Log normal Distribution

Population

Normal Distribution

non - following
Normal Distribution

As from the population we collected
sample where as $n > 30$ and
made the average of sample.

e.g.: $\{x_1, x_2, x_3, \dots, x_n\} \rightarrow \bar{x}_1$

$\{x_1, x_2, x_3, \dots, x_n\} \rightarrow \bar{x}_2$

$\{x_1, x_2, \dots, x_n\} \rightarrow \bar{x}_m$

As $\{\bar{x}_1, \bar{x}_2, \bar{x}_3, \dots, \bar{x}_m\}$

As If we plot all this sample
we can get an Normal distribution

(If we have or not have Normal distribution)

If we take multiple sample mean with $n > 30$ we get the Normal following distribution }.

If is specifically apply for log normal distribution.

Interview Question

Q Tell the size of the sharks of the entire world.

→ By making an assumption and applying multiple sample mean with $n > 30$ we can get a normal following distribution. (Consider)

Statistical
Methodology

* Probability *

Meaning :- Probability is a measure of a likelihood of an event.

Fair

a) Probability (~~measure of~~) Head = 0.5

b) Probability of Tail = 0.5

$$P(H) = 0.5$$

$$P(T) = 0.5$$

when there is an Two Outcomes this
Called an Bernoulli's Distributions

eg :-

$$P(H) = 0.5$$

$$P(T) = 0.5$$

P

q

$$\therefore q = 1 - P$$

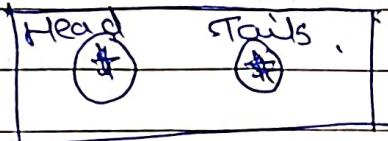
Tosses of Coin and always get outcome
as (H) it is not an *a Fair*
Coin Toss



mutually Exclusive Event

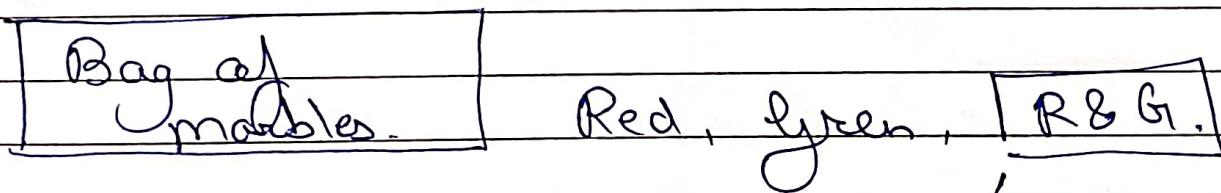
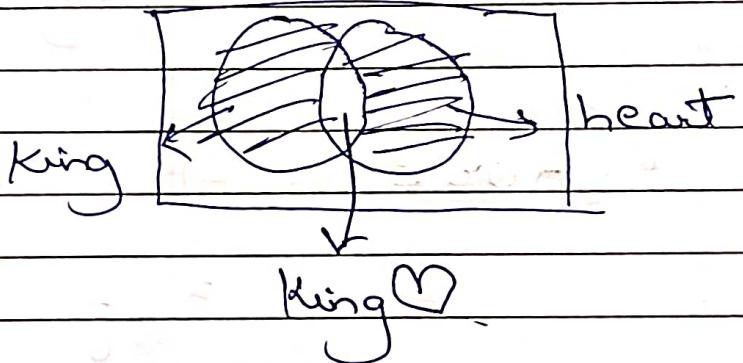
Two events are mutually exclusive
if they cannot occur at the same time.

No overlaps happen in mutual exclusive event.



(ii) Non mutual exclusive Event.

Picking randomly from a deck of cards, two event ("heart") & ("King") are not mutual exclusive event may overlaps in non-mutual exclusive event.



Red or Green

* Mutual exclusive event.

1. What is a probability of coin landing on heads or tails.

→ Rules. (Addition Rule)

$$P(A \text{ or } B) = P(A) + P(B) \text{ formula}$$

$$= \frac{1}{2} + \frac{1}{2} = \underline{\underline{1}}$$

2. What is a probability of getting 1 or 6 or 3 while rolling a dice.

$$P(A \text{ or } B \text{ or } C) = P(A) + P(B) + P(C)$$

$$= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{3}{6} = \underline{\underline{1/2}}$$

Non mutual exclusive event

1. Picking up randomly a marble from bag, what is probability of choosing marbles that is Red or Green.

Bag of marble = R = 10, G = 6, R and G = 3

$$P(R) = \frac{10}{19} \quad P(G) = \frac{6}{19} \quad P(R \text{ and } G) = \frac{3}{19}$$

Addition Rule for non-mutual.

$$\begin{aligned} P(A \text{ or } B) &= P(A) + P(B) - P(A \text{ and } B) \\ &= \frac{10}{19} + \frac{6}{19} - \frac{3}{19} \\ &= \frac{13}{19} \end{aligned}$$

① Independent event

② Non-Independent event

Independent event : Two events are independent if they do not affect one another.

e.g. : Tossing a coin.

$$\begin{aligned} P(H) &= 0.5 && \text{On the} \\ P(T) &= 0.5 && \text{not} \\ &&& \text{impact} \\ &&& \text{another} \\ &&& \text{event} \end{aligned}$$

e.g. : Rolling a "five" and then rolling a "three" in a dice.

$$P(5) = \frac{1}{6} \quad \text{and} \quad P(3) = \frac{1}{6} \quad \text{and} \quad P(4) = \frac{1}{6}$$

Example → Independent Independent Independent

Probability of rolling a "5" and a "3" with a normal six-sided dice?

$$\begin{aligned} P(A \text{ and } B) &= P(A) \times P(B) \\ &= \frac{1}{6} \times \frac{1}{6} \end{aligned}$$

$$= \frac{1}{36}$$

$$A = 5 \\ O = 6. \quad P(A \text{ and } O) = P(A) \times P(O)$$

$$= \frac{5}{11} \times \frac{6}{10} = \frac{30}{110}$$

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$$P(A \text{ and } O) = \frac{3}{11}$$

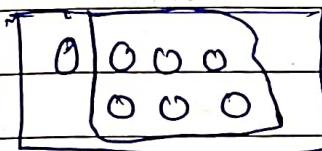
Dependent event : Two events are dependent when they affect one another.

Eg : Bag of colour marbles.

3 Orange } 7. marbles
4 yellow }
7 total

$$P(\text{Orange}) = \frac{3}{7}$$

$$P(\text{Yellow}) = \frac{4}{7}$$



$\frac{3}{6}$ Because 1 marble is already removed.

Probability of drawing a "Orange" and then drawing a "yellow" marble from the bag

$$P(O) = \frac{4}{7}$$

$$P(O \text{ and } Y) = P(O) \times P(Y)$$

$$P(Y) = \frac{3}{6}$$

$$= \frac{4}{7} \times \frac{3}{6}$$

$$= \frac{12}{42} = \frac{6}{21} = \frac{2}{7}$$

$\therefore \frac{2}{7}$. (Probability).

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Permutations and Combinations

e.g. - We went to a Zoo where
the numbers of animals are
presented.

(Tiger, Lion, Zebra)

$$6 \times 5 \times 4 = 120 \text{ way or Possibility}$$

{ Tiger, lion, monkey } Permutation means
 all the possibilities of writing an object.
 { Tiger, lion, Zebra }
 { lion, monkey, Tiger } (Order matters)
 That will be counted.

$$\text{Formula: } n P_r = \frac{n!}{(n-r)!}$$

n (Total number of objects).
 r (Total number of we are picking objects).

$$\frac{6!}{(6-3)!} = \frac{6!}{3!} = \frac{6 \times 5 \times 4 \times 3!}{3!} = 120$$

(1)

{ Krish , youtube channel , Stats , neuron , support , Power BI }.

$$6 \times 5 \times 4 \times 3 \times 2 \quad (R)$$

$$\begin{aligned} n &= 6 \\ R &= 5 \end{aligned}$$

$$P_r = \frac{n!}{P_n} = \frac{6!}{(n-r)!}$$

$$= \frac{6!}{(6-5)!} = 6 \times 5 \times 4 \times 3 \times 2 \times 1!$$

$$= 720$$

(2)

{ Sun , Rain , moon , stars , planet , climate , galaxy }

$$n = 7$$

$$R = 4$$

$$P_r = \frac{n!}{(n-r)!}$$

$$7 \times 6 \times 5 \times 4 \quad (R)$$

$$= P_4 = \frac{7!}{(7-4)!} = 7 \times 6 \times 5 \times 4 \times 3!$$

$$= 840$$

*.

Combination

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(Order not matters)

Lion, Tiger, Zebra

Zebra, Lion, Tiger

Lion, Zebra, Tiger } 1

In Combination Repetition not occurs

$$\textcircled{1} \text{. Formula : } nC_r = \frac{n!}{r!(n-r)!}$$

$n=6$
 $r=5$

$$= \frac{6!}{5!(6-5)!}$$

$$= \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{5 \times 4 \times 3 \times 2 \times 1}$$

$$= 6$$

$$\underline{6 \times 5 \times 4} (r)$$

$$nC_r = \frac{n!}{r!(n-r)!} = 6C_3 = \frac{6!}{3!(3!)!} = \frac{6 \times 5 \times 4}{3 \times 2 \times 1}$$

$$= 120$$

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Co-Variance.

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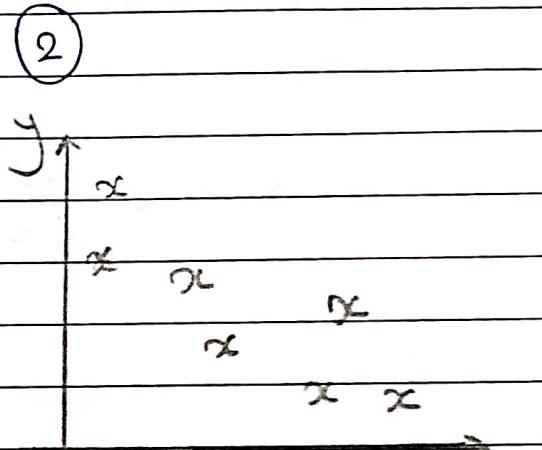
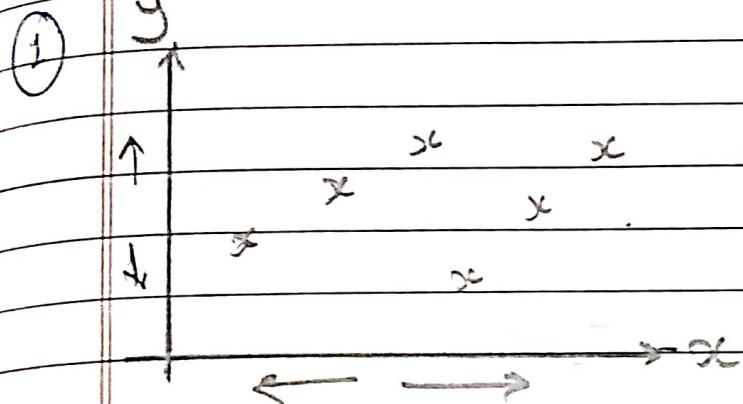
$x \uparrow$ $y \uparrow$
 age weight

12
15
18
19
20

x_i y_i

40
45
50
55
60

① { $x \uparrow y \uparrow$
 $x \downarrow y \downarrow$ }
 ② { $x \downarrow y \uparrow$
 $x \uparrow y \downarrow$ }



Scatterd graph

- mathematical formula to Quantify the relationship between x & y ?

To understand this we have an Co-Variance.

$$\text{Cov}(x, y) = \frac{1}{N-1} \sum (x_i - \bar{x})(y_i - \bar{y})$$

$$\text{Cov}(x, x) = \text{Var}(x) = \frac{1}{N-1} \sum (x_i - \bar{x})^2$$

$$= \frac{\sum (x_i - \bar{x})^2}{N-1} \quad \text{Sample Variance}$$

So the $\text{Cov}(x, x)$ is $\text{Var}(x)$

Just understand the formula.

• Formula of Variance

$$\text{Var}(x) = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1} \quad \text{So,}$$

$$\text{Var}(x) = \frac{\sum_{i=1}^n (x_i - \bar{x})(x_i - \bar{x})}{n-1}$$

\downarrow
 $\text{Cov}(x, x)$.

Such as;

$$\text{Cov}(x, y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n-1}$$

Formula of Co-Variance to understand relationship between x and y.

* Example.

$\text{Cov}(x, y)$

x	y
1	3
2	4
3	5
6	12

$$= \frac{1}{2} (1-2)(3-4) + (2-2)(4-4) + (3-2)(5-4)$$

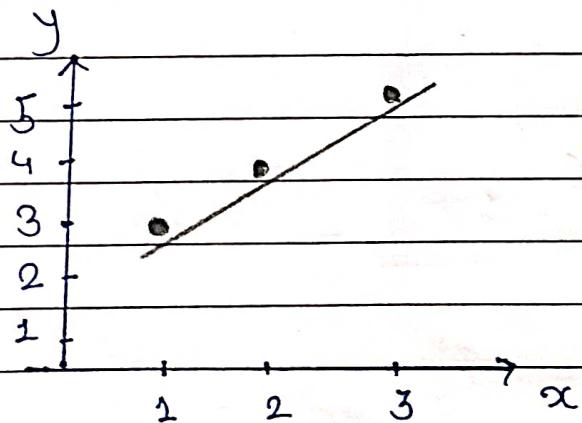
$$\bar{x} : 6 \div 3 \quad \bar{x} : 12 \div 3 \\ \underline{\underline{2}} \qquad \underline{\underline{4}}$$

$\text{Cov}(x, y)$

$$= \frac{1}{2} (1-2)(3-4) + (2-2)(4-4) + (3-2)(5-4)$$

$$= \frac{1+0+2}{2} = \frac{3}{2} = \underline{\underline{1.5}} \quad (\text{Positive value})$$

$$\text{Cov}(x, y) = \underline{\underline{1}}$$



(Perfect Positive relation between x and y)

$x \uparrow y \uparrow$

* Example.

x	y
1	2
2	4
3	6
$\bar{x} = \frac{1+2+3}{3} = 2$	$\bar{y} = \frac{2+4+6}{3} = 4.33$

$\text{Cov}(x, y)$

$$\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$= \frac{[(1-2)(4-3) + (2-2)(4-4.334) + (3-2)(6-4.334)]}{2}$$

$$= \frac{(-1)(-1.334) + 0 + (1)(1.66)}{2}$$

$$= \frac{1.334 + 1.66}{2} = \frac{2.994}{2}$$

$$= 1.497 \quad (\text{Cov } x, y) = 1.497 \quad (\text{Positive Correlated})$$

Disadvantage of Co-Variance

No specific limit define.

No Specific Strength define.

As

$$\begin{array}{c} z = x + y \\ \hline \end{array}$$

$$+1000 \quad +500$$

$$-1000 \quad -500$$

no limit and strength define in Co-variance.

As, $x \uparrow$

$y \uparrow$

(Increases)

$x \uparrow$

$y \downarrow$

(Increases and decreases)

$x \downarrow$

$y \uparrow$

(Decreases and Increases)

$x \downarrow$

$y \downarrow$

(Decreases and decreases)

Covariance is method to quantify the relationship between two data set.