

Day 3.

Page No.

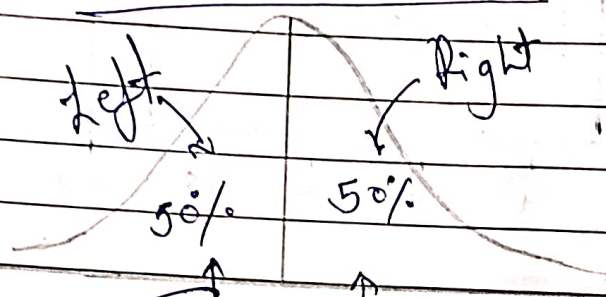
Date

- (i) Normal Distribution / Gaussian Distribution
- (ii) Standard Normal Distribution
- (iii) Z-score

Empirical Rule (Property of Gaussian Distribution)

\* Normal Distribution / Gaussian Distribution

Symmetrical



mirror reflection of data.

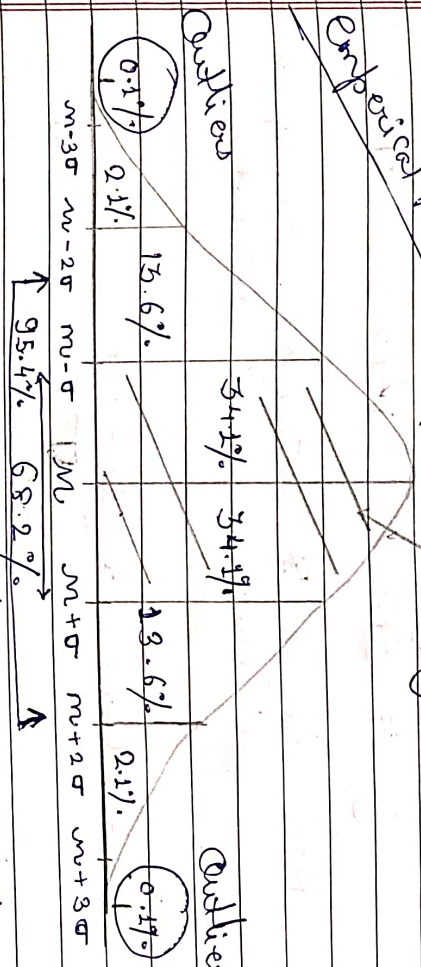
Identical to each others.

eg: ~~Weight~~ of people in the City?  
Height of people in the City

As here This data was collected by an domain expert (Doctor)  
As here we can say that the height and weight of people in the City was identical to each others.

As example of Normal Distribution  
lets understand the concept.

Empirical Rule Area of distribution



As here I have data, dataset of  $x$  with 100 numbers.

$x = \{1, 2, 4, 8, 10, 12, \dots, 68.2\% \dots 100\}$

As By adding the both numbers  $34.1\% + 34.1\%$  output is  $68.2\%$

It consider that the  $68.2\%$  of distribution is available in 1st Area (just standard distribution).

As also By adding on 2nd standard distribution ( $13.6\%$ ) output is on  $95.4\%$  which indicates that  $95.4\%$  of distributio available in this Area of distribution.

# \* Standard Normal Distribution

$X \approx$  Gaussian Distribution ( $m, \sigma$ )

$Y \approx$  SMD ( $m=0, \sigma=1$ )

Here from  $X$  distribution trying to convert in  $Y$  distribution.

Formula

$$Z\text{-score} = \frac{X_i - m}{\sigma}$$

$$= \frac{X_i - m}{\frac{\sigma}{\sqrt{n}}}$$

$$\frac{X_i - m}{\frac{\sigma}{\sqrt{n}}} = \frac{X_i - m}{\sqrt{\frac{\sigma^2}{n}}}$$

$\{1, 2, 3, 4, 5\}$   
 $n = 5$

$\sigma = 1$

$\{1, 2, 3, 4, 5\}$   
 $X_i - m = 1.3$

$\frac{1.3}{1} = 1.3$

$Z\text{-score}$

$\{-2, -1, 0, 1\}$

1	2	3	4	5
-2	-1	0	1	2



## Assignment (Z-Score)

$$\mu = 0, \sigma = 1$$

$$X = \{2, 3, 4, 5, 8\} \Rightarrow Y = \{9\}$$

$$\mu = 9$$

$$\sigma = 9$$

$$\mu = 4.4$$

$$\sigma = 2.05 \text{ (Assumed)}$$

Formula : Z-Score =  $\frac{X_i - \mu}{\sigma}$

$$2 = -1.17$$

$$3 = -0.68$$

$$4 = -4.09$$

$$5 = 0.29$$

$$8 = 1.75$$

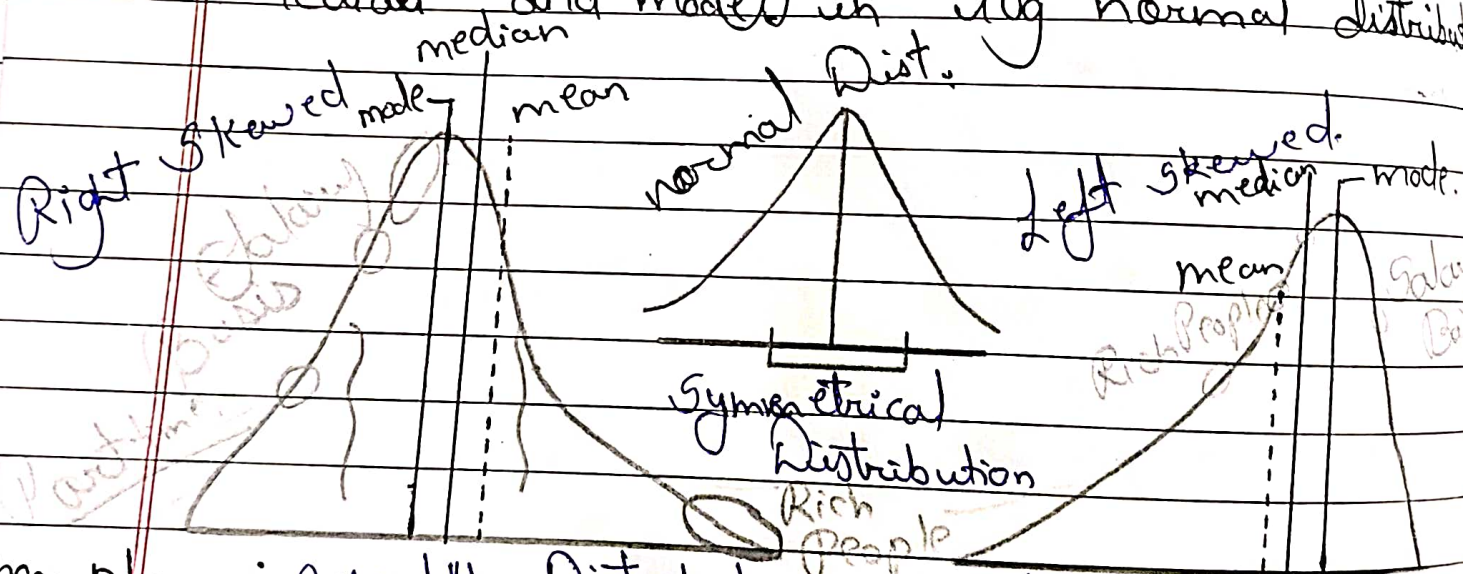
Q. Why we learn Standard Normal Distribution?  
 → Standard Normal Distribution, scale data into same scale.  
 eg:  $\mu = 0$ ,  $\sigma = 1$ .

Q. Z-score?

If we have an data set  $x$  ~ Normal Distribution ( $\mu, \sigma$ ) and trying to convert in  $y$  ~ SNO condition of ( $\mu = 0, \sigma = 1$ ) with formula of Z-score  $\left( \frac{x_i - \mu}{\sigma} \right)$  it is also called Standardization

### \* Assignment

Define the difference between mean, median and mode in log normal distribution.



Examples: Wealth Distribution, Length of Comment, Life span of Human Being.

As the relationship between mean, median and mode.

- (1) Positive Skewed :  $\text{mean} > \text{median} > \text{mode}$
- (2) Symmetrical Dist :  $\text{mean} \approx \text{median} \approx \text{mode}$
- (3) Negative Skewed :  $\text{mode} > \text{median} > \text{mean}$ .