

CSC 3315 Languages & Compilers

Lab: Designing a Simple Interpreter for Arithmetic Expressions (C)

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An arithmetic expression is a set of operands connected by operators. The usual notation of arithmetic expressions is called infix notation. Here, we focus on fully parenthesized infix expressions, such as:

$(((3 + 4) * 8) - 6)$ OR $(3 + (4 * (8 - 6)))$

Evaluating an infix notation expression can be done in two steps:

1. Conversion to postfix notation.
2. Evaluation of the postfix expression.

Conversion to Postfix Notation

An expression can be represented by a string of characters:

Example: The expression $(3 + (4 * (8 - 6)))$ is represented as follows:

(3	+	(4	*	(8	-	6)))	\0
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We consider a string of characters **expInf** representing an expression. The conversion of this expression to postfix notation is done using a stack of operators according to the following steps:

1. Create an empty string **expPost** to store the postfix expression.
2. Create a stack of character elements.
3. Traverse the expression **expInf**:
 - If an opening parenthesis '(' is encountered, do nothing.
 - If it is an operand, it is directly copied into the string **expPost**.
 - If it is an operator (+, -, *, / or %), it is pushed onto the stack.
 - For each closing parenthesis ')' read, an operator is popped from the stack and copied into **expPost**. At the end of the traversal, the string **expPost** contains the postfix notation of the expression **expInf**.
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Example: If **expInf** = $(3+(4*(8-6)))$, then **expPost** = 3 4 8 6 - * +.

Evaluation of the Postfix Expression

For simplicity, we limit to integer operands between **0** and **9**. To avoid arithmetic problems, we will only use the operators **+**, **-**, *****, and **/**.

Postfix notation is evaluated very simply using a stack of operands:

- Operands are pushed onto the stack as they are read.
- Operators are applied immediately by popping the top two operands from the stack and pushing the result back onto the stack.
- The final result is the only value left in the stack.

Example: Evaluating "**3 4 8 6 - * +**" results in **11**.

The expression	3	4	8	6	-	*	+
Stack state			8	6	2		
		4	4	4	4	8	
	3	3	3	3	3	3	11

And the evaluation of "**3 4 + 8 * 6 -**" (in infix notation **((3+4)*8)-6**)) results in **50**.

Tasks to Complete:

1. Define the structure of an operand stack **StackOpd**.
2. Write the function **void initStackOpd(StackOpd * adrP)** to initialize an empty operand stack at address **adrP**.
3. Write the function **void empilerOpd(StackOpd *adrP, int x)** to add an element **x** to the stack at address **adrP**.
4. Write the function **int depilerOpd(StackOpd *adrP)** to remove and return the top of the stack.
5. Redo the previous tasks with an operator stack **StackOpr** (make sure to change the function names).
6. Write the function **char *convertirInf2Post(char *expInf)** that takes an infix notation expression as a parameter and returns its conversion to postfix notation.

7. Write the function **int calculate(int x, int y, char op)** that takes two operands **x** and **y** and an operator **op** as parameters to compute the expression **x op y**. Example: the call **calculate(3, 7, '+')** should return **10**.
8. Write the function **int evaluator(char *exp)** that takes a postfix expression as a parameter and returns an integer which is the result of evaluating **exp**. To do this:
 - Convert **exp** to a postfix notation **expPost**.
 - Create an empty integer stack to push/pop operands.
 - Traverse **expPost** and evaluate it following the procedure described above.
 - Return the result.
9. Write the main function **main()** to:
 - Declare and read a fully parenthesized infix expression **expInf**.
 - Evaluate **expInf**.

Note:

- **int isdigit(int c)**: Returns a non-zero value if **c** is a decimal digit (**ctype.h**).
- **int atoi(const char *str)**: Returns the numeric value represented by **str** as an **int** (**stdlib.h**).