

Consider the system with 5 processes $\langle P_0, P_1, P_2, P_3, P_4 \rangle$
 & 3 Resources (A, B, C) ⑥

A	B	C
11	7	8

Total

- a) find Need Matrix $\{ \text{Need} = (\text{Max} - \text{allocation}) \}$
 b) Is the system in a safe state, if yes find safe sequence.

	Allocation			Max			Need			Available.		
	A	B	C	A	B	C	A	B	C	A	B	C
P ₀	1	0	1	7	5	3	6	5	2	4	4	5
P ₁	2	1	0	3	2	2	1	1	2			
P ₂	2	0	2	9	0	2	7	0	0			
P ₃	1	2	0	2	2	2	1	0	2			
P ₄	1	0	0	4	3	2	3	3	2			
	7	3	3									

$$\text{Available} = \text{Total} - \text{allocation}$$

$$= \begin{bmatrix} 11 & 7 & 8 \end{bmatrix} - \begin{bmatrix} 7 & 3 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 4 & 5 \end{bmatrix}$$

Safety algo.

True $\left\{ \begin{array}{l} \text{if } \text{Need} \leq \text{available.} \\ \text{execute } P_i. \end{array} \right.$ $\langle P_1, P_3, P_4, P_0 \rangle$
 false $\left\{ \begin{array}{l} \text{else.} \\ \text{forward.} \end{array} \right.$
 N. available. = old available + allocation.

$P_0 \Rightarrow$

Need. available.
 $\boxed{6|5|2} \not\leq \boxed{4|4|5}$

forward.

$P_1 \Rightarrow$

Need. available.
 $\boxed{1|1|2} \leq \boxed{4|4|5}$
 execute P_1

$$\begin{array}{r} 445 \\ - 112 \\ \hline \text{av } 333 \end{array}$$

$$\begin{array}{r} 210 \\ P_1 + 112 \\ \hline 322 \end{array} \text{ Release.}$$

$$\begin{array}{r} 333 \\ + 322 \\ \hline 655 \end{array}$$

New available = Old. available + allocation

$$= \boxed{4|4|5} + \boxed{2|1|0}$$

$$= \boxed{6|5|5}$$

$P_2 \Rightarrow$

Need. available.
 $\boxed{7|0|0} \not\leq \boxed{6|5|5}$
 forward.

$P_3 \Rightarrow$

Need available
 $\boxed{1|0|2} \leq \boxed{6|5|5}$
 execute P_3

New available = $\boxed{6|5|5} + \boxed{1|2|0} = \boxed{7|7|5}$

$$P_4 \Rightarrow \begin{array}{c} \text{Need.} \\ \boxed{3|3|2} \end{array} \leq \begin{array}{c} \text{available} \\ \boxed{7|7|5} \end{array}$$

execute P_4

$$\begin{aligned} \text{N. available} &= \boxed{7|7|5} + \boxed{1|0|0} \\ &= \boxed{8|7|5} \end{aligned}$$

$$P_0 \Rightarrow \begin{array}{c} \text{Need.} \\ \boxed{6|5|2} \end{array} \leq \begin{array}{c} \text{available} \\ \boxed{8|7|5} \end{array}$$

execute P_0

$$\begin{aligned} \text{N. available} &= \boxed{8|7|5} + \boxed{1|0|1} \\ &= \boxed{9|7|6} \end{aligned}$$

$$P_2 \Rightarrow \begin{array}{c} \text{Need.} \\ \boxed{7|0|0} \end{array} \leq \begin{array}{c} \text{available} \\ \boxed{9|7|6} \end{array}$$

execute P_2 .

$$\text{N. available} = \boxed{9|7|6} + \boxed{2|0|2}$$

$$= \boxed{11|7|8} = \text{Total Resources}$$

Yes System is in Safe State. { Safe State!

Safe Sequence. $\langle P_1 P_3 P_4 P_0 P_2 \rangle$

Q.

5. $\langle P_0, P_1, P_2, P_3, P_4 \rangle$ processes
3 Resources.

(5)

A	B	C
10	5	7

	Allocation			MAX	Need	Available
	A	B	C	A B C	A B C	A B C
P ₀	0	1	0	7 5 3	7 4 3	3 3 2
P ₁	2	0	0	3 2 2	1 2 2	
P ₂	3	0	2	9 0 2	6 0 0	
P ₃	2	1	1	2 2 2	0 1 1	
P ₄	0	0	2	4 3 2	4 3 0	
	7	2	5			

- (a) find Need Matrix.
- (b) is the system in safe state, if yes then find safe sequence.
- (c) P_1 request for $[1|0|2]$, is it will be fullfill immediately or not.
if then
then find safe sequence.

Solution
Part c

P_1 request $[1|0|2]$

Resource
allocation
algorithm.

Test.

if request \leq Need.

if request \leq available

else.

not fullfill request

if. P_1 Request

Need.

$\begin{bmatrix} 1 & 0 & 2 \end{bmatrix}$

\leq

$\begin{bmatrix} 1 & 2 & 2 \end{bmatrix}$

} True.

if

Request

available.

$\begin{bmatrix} 1 & 0 & 2 \end{bmatrix}$

\leq

$\begin{bmatrix} 3 & 3 & 2 \end{bmatrix}$

Request will fulfill immediately.

available = available - Request.

P_1 allocation = allocation + Request.

Need = Need - Request

available = $\begin{bmatrix} 3 & 3 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 0 & 2 \end{bmatrix}$
= $\begin{bmatrix} 2 & 3 & 0 \end{bmatrix}$

P_1 allocation = $\begin{bmatrix} 2 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 2 \end{bmatrix}$
= $\begin{bmatrix} 3 & 0 & 2 \end{bmatrix}$

Need = $\begin{bmatrix} 1 & 2 & 2 \end{bmatrix} - \begin{bmatrix} 0 & 1 & 0 & 2 \end{bmatrix}$
= $\begin{bmatrix} 0 & 2 & 0 \end{bmatrix}$

updated
Table.

(7)

	Allocation			MAX			Need			Available.		
	A	B	C	A	B	C	A	B	C	A	B	C
P ₀	0	1	0	7	5	3	7	4	3	2	3	0
P ₁	3	0	2	3	2	2	0	2	0			
P ₂	3	0	2	9	0	2	6	0	0			
P ₃	2	1	1	2	3	2	0	1	1			
P ₄	0	0	2	4	3	2	4	3	0			

P₀ = $\begin{array}{|c|c|c|} \hline \text{Need} & & \\ \hline 7 & 4 & 3 \\ \hline \end{array} \not\leq \begin{array}{|c|c|c|} \hline \text{available} & & \\ \hline 2 & 3 & 0 \\ \hline \end{array} < P_1$
forward.

P₁ = $\begin{array}{|c|c|c|} \hline \text{Need} & & \\ \hline 0 & 2 & 0 \\ \hline \end{array} \leq \begin{array}{|c|c|c|} \hline \text{available} & & \\ \hline 2 & 3 & 0 \\ \hline \end{array}$
executes P₁

N. available = Old available. + allocation
 $= \begin{array}{|c|c|c|} \hline 2 & 3 & 0 \\ \hline \end{array} + \begin{array}{|c|c|c|} \hline 3 & 0 & 2 \\ \hline \end{array}$
 $= \begin{array}{|c|c|c|} \hline 5 & 3 & 2 \\ \hline \end{array}$

P₂ = $\begin{array}{|c|c|c|} \hline \text{Need} & & \\ \hline 6 & 0 & 0 \\ \hline \end{array} \not\leq \begin{array}{|c|c|c|} \hline \text{available} & & \\ \hline 2 & 3 & 0 \\ \hline \end{array}$
forward.

(8)

 $P_3 \Rightarrow$

Need		
0	1	1

 \neq

Available		
2	3	0

~~cannot~~ \rightarrow forward
 $P_4 \Rightarrow$

Need		
4	3	0

 \neq

available		
2	3	0

forward.
 $P_0 \Rightarrow$

Need		
7	4	3

 \neq

available		
2	3	0

forward.
 $P_2 \Rightarrow$

Need		
6	0	0

 \neq

available		
2	3	0

forward.
 $P_3 \Rightarrow$

Need		
0	1	1

 \neq

available		
2	3	0

Now, System is not in Safe state.
 So there will be not safe sequence.

⇒ Resource allocation
Algorithm.

{ if Request \leq Need.
if Request \leq available.

Then. Request approved
else.
decline.

changes { available = available - Request
Need = Need - Request.
allocation = allocation + Request.