

SECTION - A

[Answer-1]

Difference b/w DFA & NDFA

DFA	NDFA
It stand for Deterministic Finite automata.	* It stand for Non-Deterministic Finite automata
DFA require more space.	* NDFA require less space.
The transition takes place from a state to a single particular state for each input symbol.	* for each input symbol, the transition can be to multiple next states.
There are no empty string transition in DFA.	* Empty string transition are also permitted.
Ex- $\delta: Q \times \Sigma \rightarrow Q$	Ex- $\delta: Q \times \Sigma \rightarrow 2^Q$

[Answer-2]

Step-1: Suppose L is regular. Let n be the number of states in FA.

Step 2: Let p be a prime number greater than n .
Let $w = a^p$ by pumping lemma
 $|w| = |a^p|$
 $|w| = p > n$

[Answer -11]

1. Let $w = a^n b^n c^{3n}$

Suppose L be the regular. Let n be the num of states in P.A.

2. Let $w = a^n b^n c^{3n}$

$$|w| = n + n + 3n$$

$$= 5n > n$$

using P.K

$$w = xyz \text{ with } |xy| \leq n \text{ \& } |y| > 0$$

now

$$w = xyz = a^n b^n c^{3n}$$

$$xyz = a^n b^n c^k c^{3n-k} \quad k > 0$$

$$x = a^n b^n$$

$$y = c^k$$

$$z = c^{3n-k}$$

ex-3: Let $i=0$

$$xy^i z = xy^0 z$$

$$= a^n b^n c^{3n-k}$$

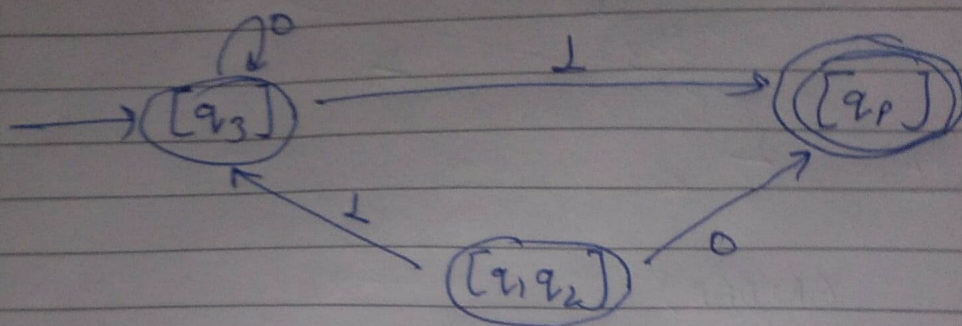
$$|xy^i z| = n + n + 3n - k$$

$$= 5n - k \neq 5n$$

$\therefore xy^i z \notin L$ hence by contradiction

$Z = \{a^i b^i c^k : k > i+j\}$ isn't regular.

The Transition Diagram



Answer - 12(b)

L.H.S -

$$(1+00^*1) + (1+00^*1)(0+10^*1)^*(0+10^*1)$$

using $I_{12} \rightarrow (1+00^*)(\Lambda + (0+10^*1)^*(0+10^*1))$
now,

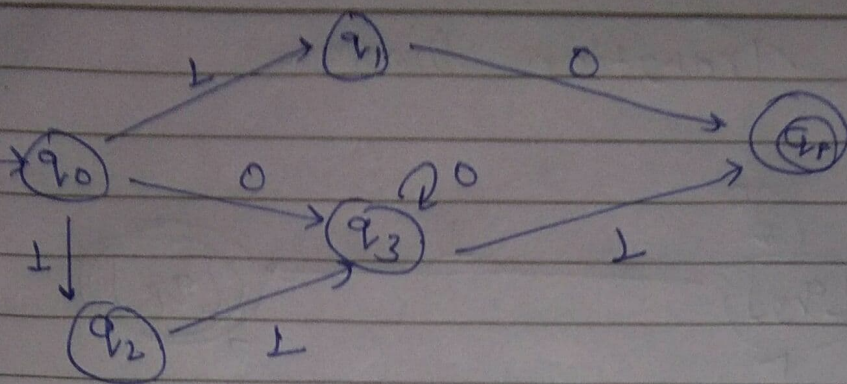
$$\text{using } I_9 \rightarrow (1+00^*1)(0+10^*1)^*$$

$$= (\Lambda + 00^*)(0+10^*1)^* \text{ using } I_{12} \text{ for}$$

$$1+00^*1$$

$$\Rightarrow \boxed{0^*1(0+10^*1)^*} \text{ using } I_9$$

$$\underline{\text{L.H.S} = \text{R.H.S}}$$



(NDPDA)

Transition Table

State	0	1
$\rightarrow q_0$	q_3	q_1, q_2
q_1	q_f	-
q_2	-	q_3
q_3	q_3	q_f
q_f	-	-

$$M' = \{Q', \Sigma', \delta', q_0, F\}$$

where

$$Q' = \{[q_3], [q_1, q_2], [q_f]\}$$

$$\Sigma' = \{0, 1\}$$

$$q_0 = [q_0]$$

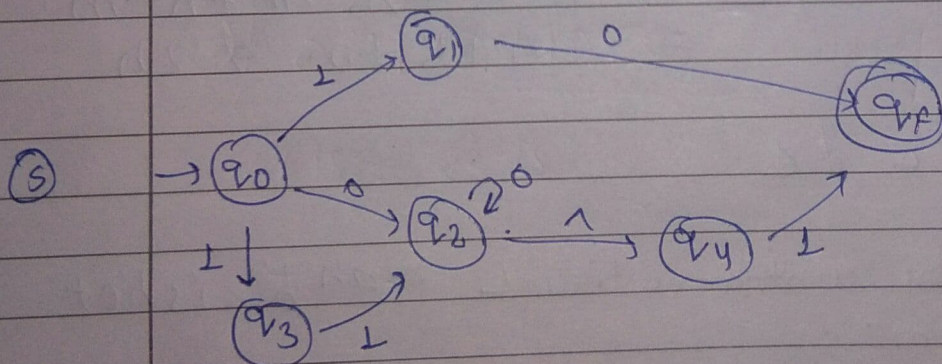
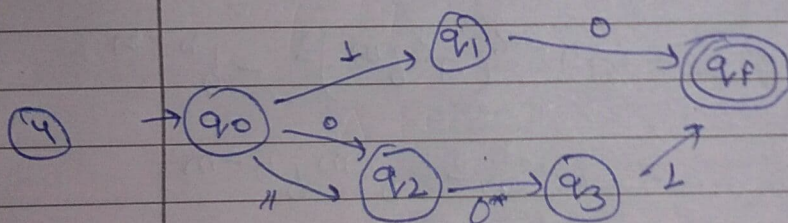
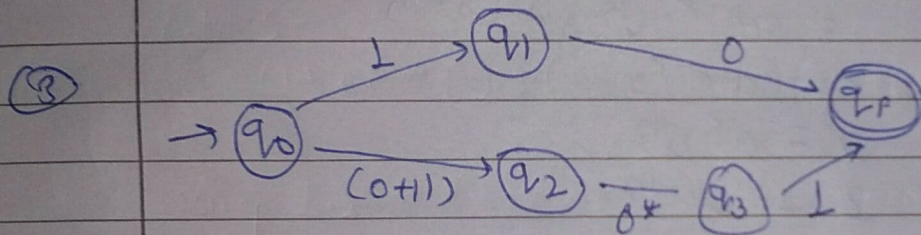
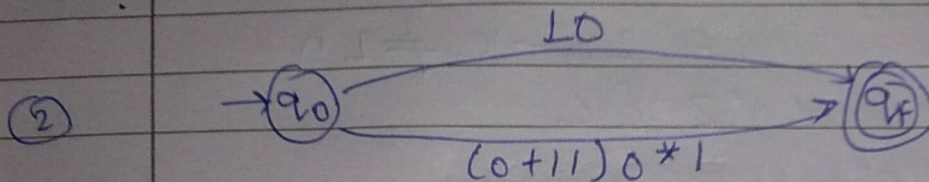
$$F = [q_f]$$

The Transition Table for DPDA

State	0	1
$[q_3]$	$[q_3]$	$[q_f]$
$[q_f]$	$[q_f]$	$[q_3]$
$[q_1, q_2]$		

[Answer - 10]

Construct a DFA for the expression

 $10 + (0+11)^* 0^* 1$ Solution - $\rightarrow q_0 \xrightarrow{10 + (0+11)^* 0^* 1} q_f$ 

6 Remove 1

$$x = a^n$$

$$y^i = b^k$$

$$z = b^{n-k}$$

for $j=0$;

$$xy^0z = xz$$

$$= a^n b^{n-k}$$

$$|xy^0z| = n + n - k$$

$$= 2n - k \neq 2n$$

$$\therefore xy^0z \notin L$$

$$3: xy^i z = a^n b^n$$

$$= a^{n-k} a^k b^m b^{n-m}$$

$$x = a^{n-k}$$

$$y^i = a^k b^m$$

$$z = b^{n-m}$$

for $j=2$

$$xy^2z = a^{n-k} (a^k b^m)^2 b^{n-m}$$

$$= a^{n-k} a^{2k} b^{2m} b^{n-m}$$

$$|xy^2z| = n - k + 2k + 2m + n - m$$

$$= 2n + k + m \neq 2n$$

$$\therefore xy^i z \notin L$$

hence by contradiction $L = a^n b^n$ is not regular.

$b = \{a^n b^n, n \geq 1\}$ isn't a regular.

Section B

(Answer - 6)

Step-1: Suppose L is a regular. Let n be the num of state in the FA.

Step-2: Let $w = a^n b^n$, then
 $|w| = n + n = 2n > n$
 using pumping lemma

$$w = xyz \text{ with } |xy| \leq n \text{ \& } |y| > 0$$

Step-3: find suitable integer
 $xy^iz \notin L$
 Let $xy^iz = a^n b^n$
 here 3 cases arise -

CASE-1: $xy^iz = a^{n-k} a^k b^n$
 $x = a^{n-k}$
 $y = a^k$
 $z = b^n$

for $i=0$

$$xy^0z = xz = a^{n-k} b^n$$

$$\begin{aligned} |xy^0z| &= |a^{n-k} b^n| \\ &= n - k + n \\ &= 2n - k \neq 2n \end{aligned}$$

$$\therefore xy^iz \neq a^n b^n \Rightarrow xy^iz \notin L$$

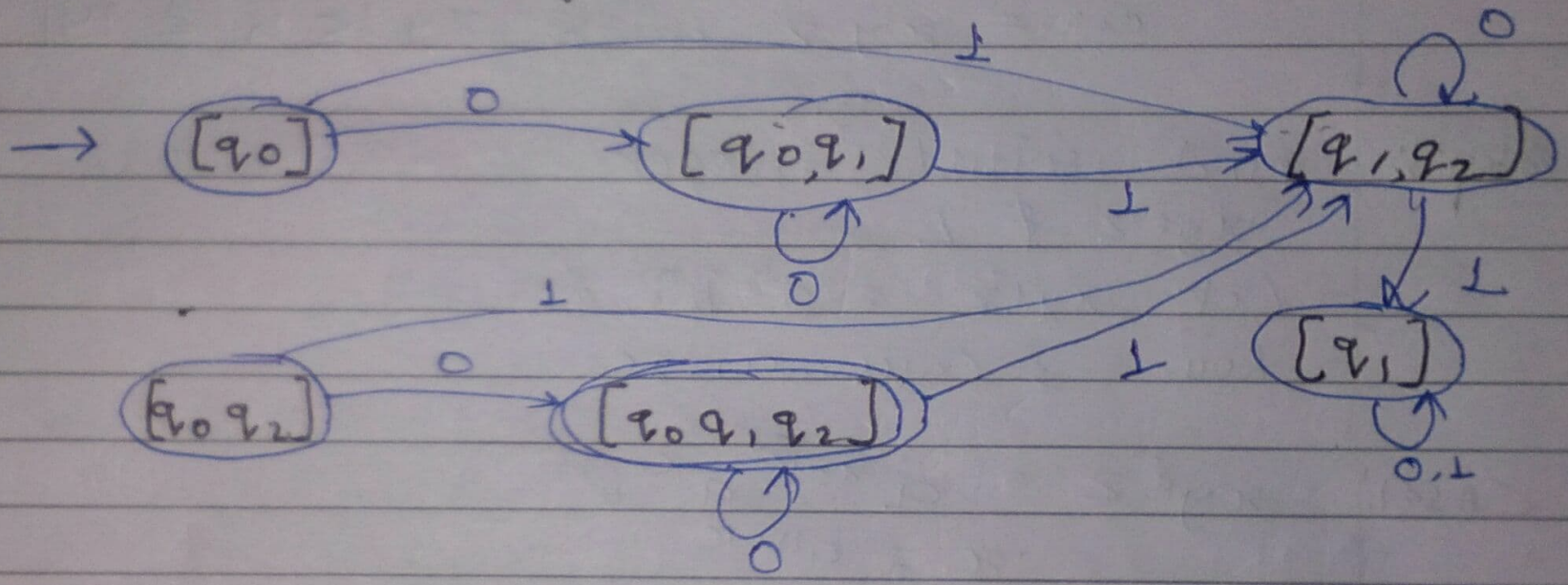
CASE-2: $xy^iz = a^n b^k b^{n-k} \quad n > 0$

$[q_0, q_2]$
 $[q_0 q_1 q_2]$

$[q_0, q_1, q_2]$
 $[q_0 q_1 q_2]$

$[q_1, q_2]$
 $[q_1, q_2]$

Transition Diagram



Comparison Table

States (q, q')	c (q_c, q'_c)	d (q_d, q'_d)
(q_1, q_4)	(q_1, q_4)	(q_2, q_5)
(q_2, q_5)	(q_3, q_1)	(q_1, q_6)

here, q_1 & q_6 are reachable from q_2 & q_5 respectively.

[Answer - 5]

state	0	1
$\rightarrow q_0$	$q_0 q_1$	$q_1 q_2$
q_1	q_1	q_1
(q_2)	q_2	—

Solution - Let $M' = \{Q', \Sigma', \delta', q_0, F'\}$ be the NFA equivalent to DFA.

$$Q' = 2^3 = \{ \phi, [q_1], [q_0], [q_2], [q_1, q_2], [q_0, q_1], [q_0, q_2], [q_1, q_0, q_2] \}$$

$$\Sigma' = \{ 0, 1 \}$$

$$q_0 = [q_0]$$

$$F' = \{ [q_2], [q_1, q_2], [q_0, q_2], [q_0, q_1, q_2] \}$$

δ : Transition Table

$\Rightarrow aabbabS$
 $\Rightarrow aabbabbA$
 $\Rightarrow aabbabba$

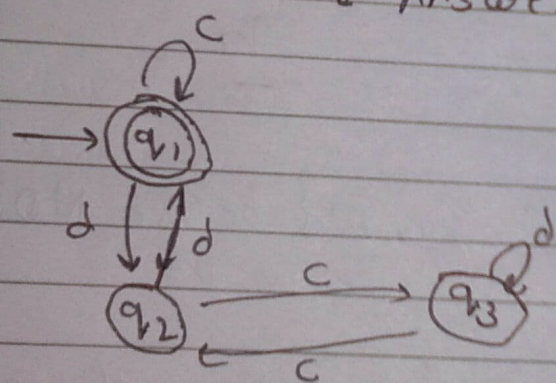
$S \rightarrow bA$
 $A \rightarrow a$

Right most Derivation

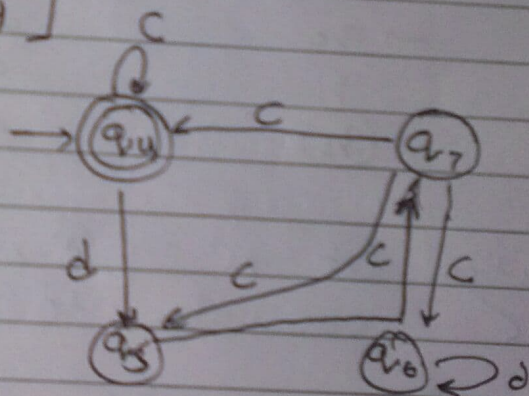
$S \Rightarrow aB$
 $\Rightarrow aabB$
 $\Rightarrow aabBS$
 $\Rightarrow aabbbA$
 $\Rightarrow aabbbba$
 $\Rightarrow aabSbba$
 $\Rightarrow aabbAbba$
 $\Rightarrow aabbabba$

$B \rightarrow aBB$
 $B \rightarrow bS$
 $S \rightarrow bA$
 $A \rightarrow a$
 $B \rightarrow bS$
 $S \rightarrow bA$
 $A \rightarrow a$

[Answer - 4]



(a) M



(b) M'

\Rightarrow The initial states in M & M' are q_1 & q_4 , respectively.

The final state in M & M' are q_1 & q_4 respectively.

The first element of the first column in the comparison table is (q_1, q_4) .

q_2 & q_5 are d-reachable from q_1 & q_4 .

$w = xyz$ with $|xy| \leq n$ & $|y| \geq 1$

hence

$$w = xyz = a^p = a^{p-m-n} a^m a^n$$

$$x = a^{p-n-m}, y = a^m, z = a^n$$

Step-3: Let $j = p + 1$ then

$$xy^jz = xyz * y^{j-1}$$

$$|xy^jz| = |xyz| + |y^{j-1}|$$

$$= |a^p| + |y^{j-1}|$$

$$= p + |(a^m)^{p+1-1}|$$

$$= p + pm$$

$$|xy^jz| = p(1+m)$$

Since p is prime but $p(1+m)$ isn't a prime num.

So $xy^jz \notin L$ hence by contradiction

$L = \{a^p \mid p \text{ is prime}\}$ is not regular.

[Answer - 3]

Consider the CFG

$$S \rightarrow aB \mid bA$$

$$A \rightarrow a \mid aS \mid bAA$$

$$B \rightarrow b \mid bS \mid aBB$$

Solve -

i) Left most Derivation

$$S \Rightarrow aB$$

$$\Rightarrow a a B B$$

$$\Rightarrow a a b B$$

$$\Rightarrow a a b b S$$

$$\Rightarrow a a b b a B$$

$$B \rightarrow a B B$$

$$B \rightarrow b$$

$$B \rightarrow b S$$

$$S \rightarrow a B$$

$$B \rightarrow b S$$