

Date. 7/4/2017

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Government College of Engineering, Amravati
(An Autonomous Institute of Government of Maharashtra)

Sixth Semester B. Tech. (CS / IT)

Summer – 2017

Course Code: ITU601

Course Name: Design and Analysis of Algorithms

Time: 2 Hrs. 30 Min.

Max. Marks: 60

Instructions to Candidate

- 1) All questions are compulsory.
- 2) Assume suitable data wherever necessary and clearly state the assumptions made.
- 3) Diagrams/sketches should be given wherever necessary.
- 4) Use of logarithmic table, drawing instruments and non-programmable calculators is permitted.
- 5) Figures to the right indicate full marks.

1. Solve any two:

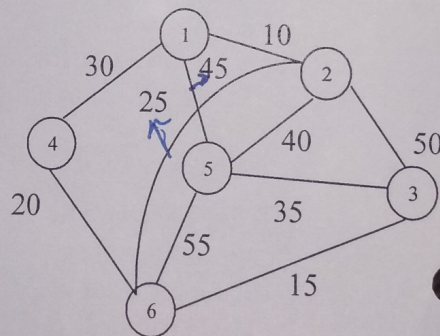
- a) Give Asymptotic upper bound for $T(n)$. Make your upper bound as tight as possible. You may assume that n is power of 2. 6
 - 1) $T(1) = 1$
 $T(n) = T(n/2) + 1 \quad \text{if } n > 1$
 - 2) $T(1) = 1$
 $T(n) = 2.T(n/2) + n \quad \text{if } n > 1$
- b) Let $f(n)$ and $g(n)$ be asymptotically nonnegative functions. Using the basic definition of Θ notation, prove that $\max(f(n), g(n)) = \Theta(f(n) + g(n))$. 6

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- c) What is empirical analysis & theoretical Analysis of an algorithm? Explain pros and cons of the empirical & theoretical analysis of an algorithm

2. **Solve any two**

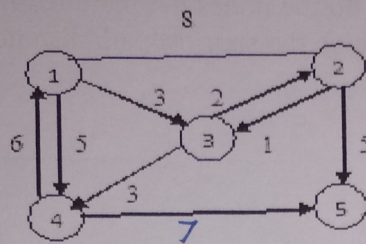
- a) Solve the recurrence : $T(n) = 4T\left(\frac{n}{2}\right) + n^2$
When n is a power of 2, $n \geq 2$.
- b) What is binomial heap? Explain following operations on binomial heap H & Also find the time taken for these operations:
i) Deleting the largest item of a binomial heap H
ii) Inserting a new item into a binomial heap H
- c) Find the minimum spanning tree for the given graph using Prim's algorithm & draw the corresponding weight matrix which shows the updating of weights after each iteration.



3. **Solve any two**

- a) Write algorithm for greedy strategies for the knapsack problem & find optimal solution to the knapsack instance $n=3, m=20$
 $(p_1, p_2, p_3) = (25, 24, 15)$
 $(w_1, w_2, w_3) = (18, 15, 10)$.

- b) Explain the Floyd's algorithm for computing all pairs shortest path. Also find the matrix D that gives 6



- c) Prove that Quick sort takes a time in $O(n \log n)$ to sort n elements on the average. 6

4. Solve the following

- a) Multiple Choice question(Each Carry Two Marks) 6

1) Assume that the algorithms considered here sort the input sequences in ascending order. If the input is already in ascending order, which of the following are TRUE ?

- I. Quicksort runs in $\Theta(n^2)$ time
- II. Bubblesort runs in $\Theta(n^2)$ time
- III. Mergesort runs in $\Theta(n)$ time
- IV. Insertion sort runs in $\Theta(n)$ time

- a) I and II only b) I and III only
c) II and IV only d) I and IV only

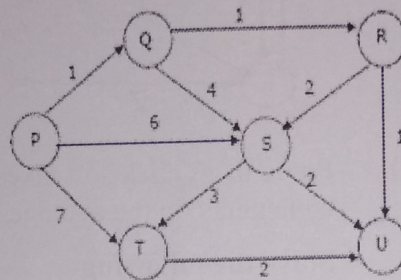
2) Let A_1 , A_2 , A_3 , and A_4 be four matrices of dimensions 10×5 , 5×20 , 20×10 , and 10×5 , respectively. The minimum number of scalar multiplications required to find the product $A_1A_2A_3A_4$ using the basic matrix multiplication method is

- a) 1500 b) 2000 c) 500 d) 100

3) Suppose we run Dijkstra's single source shortest-

Contd..

path algorithm on the following edge weighted directed graph with vertex P as the source. In what order do the nodes get included into the set of vertices for which the shortest path distances are finalized?



a) P, Q, R, S, T, U

b) P, Q, R, U, S, T

c) P, Q, R, U, T, S d) P, Q, T, R, U, S

b) **Multiple Choice question(Each Carry one Marks)**

1) Given an unsorted array. The array has this property that every element in array is at most k distance from its position in sorted array where k is a positive integer smaller than size of array. Which sorting algorithm can be easily modified for sorting this array and what is the obtainable time complexity?

- (A) Insertion Sort with time complexity $O(kn)$
- (B) Heap Sort with time complexity $O(n \log k)$
- (C) Quick Sort with time complexity $O(k \log k)$
- (D) Merge Sort with time complexity $O(k \log k)$

2) If every square of the board is visited, then the total number of knight moves of 8-queen problem is

- (A) 64
- (B) 62
- (C) 61
- (D) 63

3) The total running time of knapsack problem for a simple approach

Contd..

5.

a)

Ag
Tas
A
B
C
D

b) Give

- (A) $O(n)$ (B) $O(\log n)$
 (C) $O(2^n \log n)$ (D) $O(2^n)$

4) Which of the following method is computing total cost of an algorithm in amortized analysis?

- (A) Aggregate method
 (B) accounting method
 (C) potential method
 (D) both (C) and (B)

5) The running time of merge sort can be recursively represented by

- (A) $T(n) = 2T(n/2) + n$
 (B) $T(n) = 3T(n/2) + n$
 (C) $T(n) = 4T(n/2) + n$
 (D) $T(n) = 2T(n/4) + n$

6) If a problem Q is known as NP-hard, then which of the following is true?

- (A) if Q is NP then Q is NP Complete
 (B) Q is not NP complete
 (C) Q is not in NP
 (D) Not all problems in NP reduce to Q

5.

Solve the following

- a) What is branch and bound technique? Using branch and bound solve the following assignment problem. Also draw the completely explored tree.

6

Agent/ Task	1	2	3	4
A	11	12	18	40
B	14	15	13	22
C	11	17	19	23
D	17	14	20	28

- b) Give the relation between P, NP and NP complete.

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