

GOVERNMENT COLLEGE OF ENGINEERING, AMRAVATI

(An Autonomous Institute of Govt. of Maharashtra)

CT-II W-2018

SHU101 ENGG. MATHS-I

Marks :15

Date: 15/11/18

TIME- 1 HOUR

Q 1) If $z^3 = i(z - 1)^3$ then prove that $z = \frac{1}{2} - \frac{i}{2} \cot \frac{\theta}{2}$.

(03)

Q 2) Solve any Four:

(12)

(i) If n be the positive integer, prove that $(1 + i)^n + (1 - i)^n = 2^{\frac{n+2}{2}} \cos \frac{n\pi}{4}$

(ii) Show that n^{th} roots of unity form a G.P. with the common ratio

$(\cos \frac{2\pi}{n} + i \sin \frac{2\pi}{n})$ and show that continued product of roots is $(-1)^{n+1}$.

(iii) Prove that $\operatorname{sech}^{-1}(\sin \theta) = \log \cot \frac{\theta}{2}$

(iv) Prove that $\log \left[\frac{\cos(x-iy)}{\cos(x+iy)} \right] = 2i \tan^{-1}(\tan x \cdot \tanh y)$

(v) If $\frac{(1+i)^{x+iy}}{(1-i)^{x-iy}} = \alpha + i\beta$, then show that $\tan^{-1} \frac{\beta}{\alpha} = \frac{\pi x}{2} + y \log 2$.