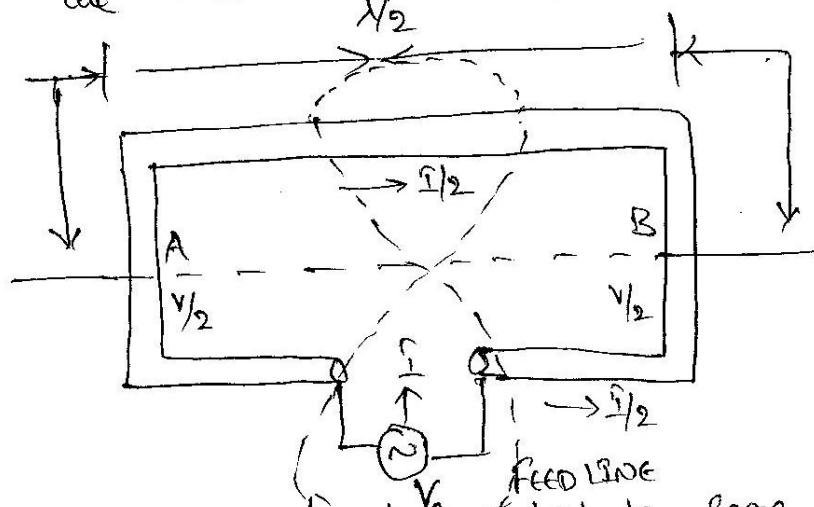


(2)

1) Folded Dipole Antenna :- (used at VHF & Yagi-Uda Antenna).

Conventional half wave dipole is the folded dipole in which two half wave dipoles - one continuous and other split at the centre - have been folded and joined together in parallel at the ends. The split dipole is fed at the centre by a transmission line with a voltage source hence the voltages in both the dipoles are same and currents are also divided equally.



- The radiation pattern of folded dipole is same as half wave dipole but differs from directivity & beam width.
- The η_{IP} impedance of folded dipole is very high.
- The radius (r_0) radii of two dipoles are same as the current flowing through the two half wave dipoles.
- The folded dipole has impedance transformer property means that η_{IP} impedance can be changed by choosing different diameters of the half wave dipoles.
- The η_{IP} impedance of folded dipole antenna is equal to the product of square of ratio of conductors and radiation resistance of half wave dipole 73Ω .

(3)

For equation of impedance for 2-wire dipole is

$$Z_{in} = n^2 * R_{rad} \left(\frac{1}{2}\right)$$

$$= (2)^2 * 73\Omega$$

$$= 4 * 73\Omega$$

$$Z_{in} = 292\Omega$$

(i) Equation for impedance of 2-wire folded dipole:

Let V be the applied volts to the two wide folded dipole

Since the diameter of 2-half wave dipoles are same so the currents flowing through 2-dipoles are same and volts is divided equally i.e $V/2$

$$I_1 = I_2$$

The diameters of 2-dipoles is same

by Z-parameters

$$V_i = Z_{11}I_1 + Z_{12}I_2$$

\therefore the volt is divided equally for 2-dipoles

$$\begin{aligned} \frac{V}{2} &= Z_{11}I_1 + Z_{12}I_2 \\ &= I_1 [Z_{11} + Z_{12}] \quad (\because Z_{11} = Z_{12}) \end{aligned}$$

spacing b/w the dipoles are same

$$\frac{V}{2} = I_1 [Z_{11} + Z_{11}]$$

$$\frac{V}{2} = 2I_1 Z_{11}$$

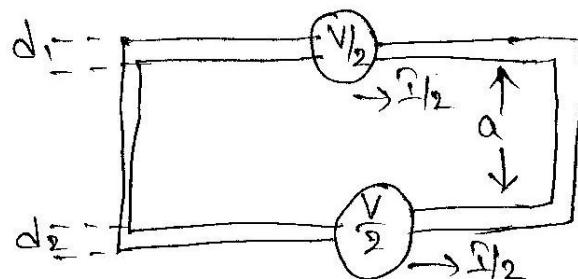
$$V = 4I_1 Z_{11}$$

$$4Z_{11} = \frac{V}{I_1}$$

$$\Rightarrow \frac{V}{I_1} = 4 \times 73 \quad (\because Z_{11} = 73\Omega)$$

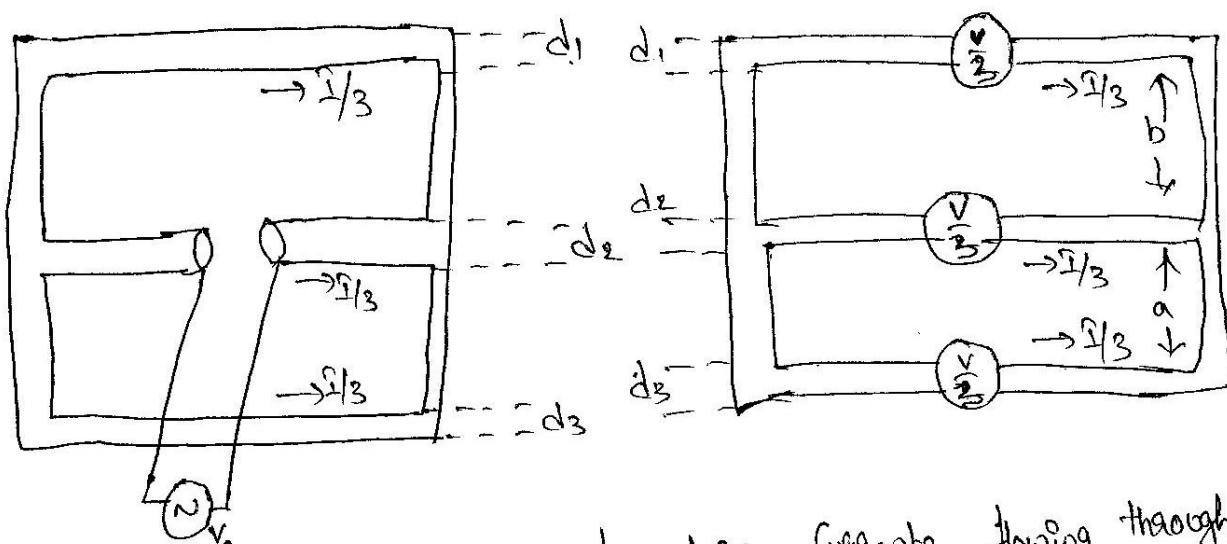
$$= 292\Omega$$

Z_{11} = radiation resistance of halfwave dipole.



(ii) Equation for dipole (iii) 3-wire folded dipole :-

41



Since 3-dipoles have same diameters currents flowing through them is same and voltages are divided equally and assume spacing b/w the dipole is less (a, b).

$$Z_{11} = Z_{12} = Z_{13} \text{ (spacing)}$$

$$\underline{I}_1 = \underline{I}_2 = \underline{I}_3 \text{ (diameter)}$$

From Z -parameters

$$V = Z_{11}\underline{I}_1 + Z_{12}\underline{I}_2 + Z_{13}\underline{I}_3$$

$$\frac{V}{3} = Z_{11}\underline{I}_1 + Z_{12}\underline{I}_2 + Z_{13}\underline{I}_3$$

$$\frac{V}{3} = Z_{11}\underline{I}_1 + Z_{11}\underline{I}_1 + Z_{11}\underline{I}_1$$

$$\frac{V}{3} = 3Z_{11}\underline{I}_1$$

$$V = 9Z_{11}\underline{I}_1$$

$$\frac{V}{\underline{I}_1} = 9Z_{11}$$

$$= 9 \times 73$$

$$\frac{V}{\underline{I}_1} = 657 \Omega$$

In general the imp impedance of folded dipole is given by -

$$\text{Two wire } \frac{V}{2} = 2Z_{11}\underline{I}_1$$

$$\text{Three wire } \frac{V}{3} = 3Z_{11}\underline{I}_1$$

(5)

n-wire

$$\frac{V}{n} = n Z_{\parallel} \quad \text{Fig}$$

$$V = n^2 Z_{\parallel} I$$

$$Z_{in} = \frac{V}{I} = n^2 Z_{\parallel}$$

 $n = \text{no of half wave dipole}$ $Z_{\parallel} = \text{radiation resistance of half wave dipole}$

We know that G.P impedance depends on spacing b/w the half wave dipoles so it is given by

$$Z_{in} = \left[1 + \frac{\log \frac{a}{\delta_1}}{\log \frac{a}{\delta_2}} \right] \cdot Z_{\parallel}$$

 $\delta_1 \rightarrow \text{radius of first half wave dipole}$ $\delta_2 \rightarrow \text{radius of second half wave "}$

H.W dipole depends of diameter if it is given by

$$Z_{in} = \left[1 + \frac{\delta_2}{\delta_1} \right]^2 Z_{\parallel}$$

Advantages of folded dipole:-

* It has high impedance

* Act as a impedance transformer

* Directivity is very high since 2-dipoles arranged in parallel.

Applications:-

→ Used as a driven element in Yagi-Uda Antenna

→ Used in wide band applications i.e. TV Applications.

Q) Yagi-Uda Antenna :-

It is a high gain Antenna used in television applications. This antenna is otherwise called as Yagi-Uda array. It contains

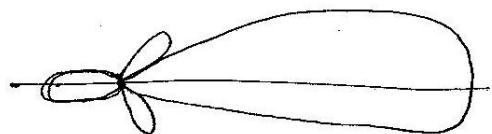
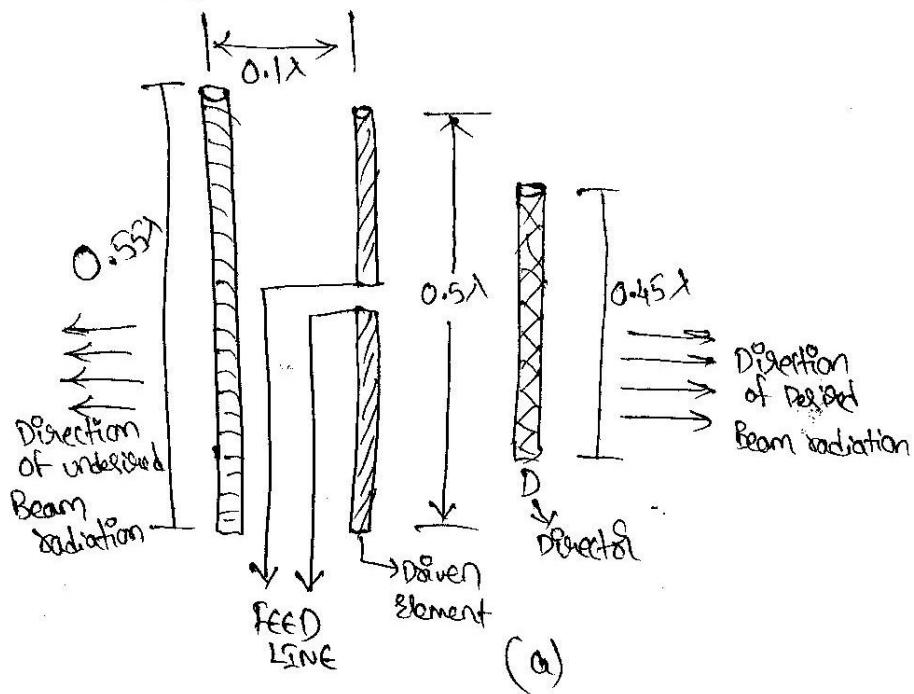
3-Elements

- (i) Driver Element
- (ii) Reflector
- (iii) Director

The Driver element is connected to the transmission line through which signal source connected and it is a resonant half wave dipole. Reflector and director elements are parasitic elements because they are not connected directly to the source but they are connected to the driver element through the magnetic coupling.

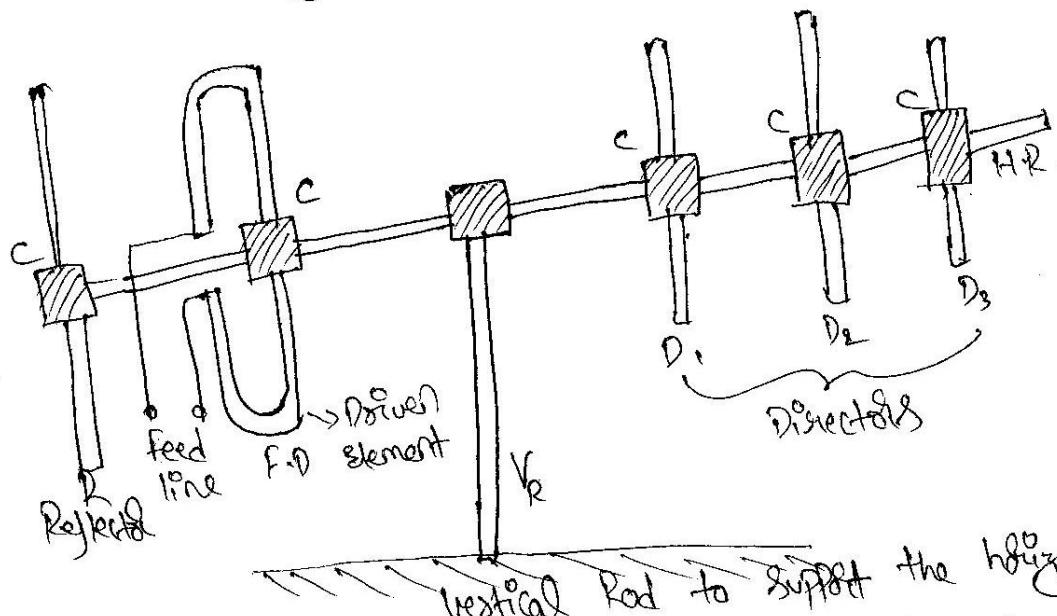
The parasitic element in front of the driver element is called as the director. It directs the signal towards the desired directions.

The parasitic element behind & back to the driver element is called as Reflector. It reflects the signal from driver element to towards the desired directions.



(b) Radiation Pattern

The length of the driven element is 0.5λ & director length is 5λ & driven element and also the reflector length is 5λ . The spacing b/w elements is 0.1λ .



Vertical Rod to support the horizontal rod.

The parasitic elements reflector and directors are clamped on a metallic rod parallel to the driven element either to reflect or direct the radiated energy.

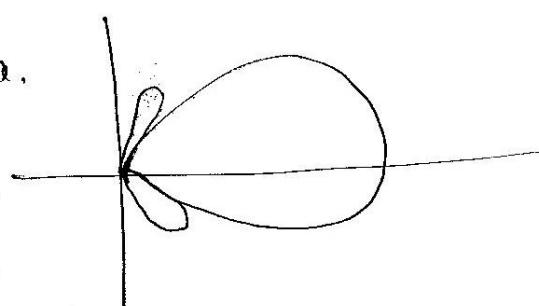
The parasitic elements of equal or $\approx \frac{\lambda}{2}$ will be inductive in nature (lagging phase).

The parasitic elements of equal or $\approx \frac{\lambda}{2}$ will be capacitive ie leading in phase.

The additional gain will be achieved by increasing the no. of directors.

② Radiation Pattern:-

It is a fixed frequency Antenna.



(3)

(b) Design Parameters :-

- (i) Reflector length $l_R = \frac{500}{f(\text{MHz})}$
- (ii) Driver element length $l_{DR} = \frac{475}{f(\text{MHz})}$
- (iii) Director length $l_D = \frac{455}{f(\text{MHz})}$

(c) General Characteristics of Yagi-Uda Antenna :-

- This Antenna contains three elements i.e., Driver element, director, and reflector such an Antenna is called as Beam Antenna.
- This Antenna is otherwise called as Uni-directional Antenna, which moderate directivity, light weight and low cost.
- The gain & directivity are high so the Antenna is called as Super gain (SI) Super directive antenna.
- It is a fixed freq device the band width is about 3% and is sufficient for the reception of T.V. signals.
- It provides a gain of 8dB and front to back ratio of 20dB.

(d) Voltage and Current Relations in Parasitic Antennas :-

Voltage and Current relations in Parasitic Antennas:-
 One or more passive elements coupled magnetically to driven element is known as Parasitic antenna. The presence of parasitic elements effect the directional pattern. The effect on the directional pattern produced depends upon the magnitude and phase of the induced current in parasitic elements i.e. on spacing of antenna and tuning of the parasitic antenna.

The relations b/w currents and voltages of Yagi-Uda's array is obtained by the Z-parameter.

$$V_1 = Z_{11} I_1 + Z_{12} I_2 \rightarrow ①$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 \rightarrow ②$$

$$V_n = Z_{n1} I_1 + Z_{n2} I_2 + \dots + Z_{nn} I_n \rightarrow ③$$

$V_1, V_2, V_n \dots \rightarrow$ Voltage applied to antenna no. 1, 2, 3 ... n (9)

$I_1, I_2, \dots, I_n \rightarrow$ Current flowing in antenna 1, 2, 3 ... n

$Z_{11}, Z_{22}, Z_{33} \dots Z_{nn} \rightarrow$ Self Impedance of Antenna no. 1, 2, 3 ... n

$Z_{12}, Z_{21}, Z_{32} \dots Z_{23} \rightarrow$ Mutual Impedance b/w Antenna of subscripts

V_1 is driven Volt ; V_2 is induced Volt

$$V_2 = 0$$

Now: $\therefore V_1 = I_1 Z_{11} + I_2 Z_{12}$

$$0 = I_1 Z_{21} + I_2 Z_{22}$$

$$Z_{21} I_1 = -Z_{22} I_2$$

$$I_1 = \left(\frac{-Z_{22}}{Z_{21}} \right) I_2 \rightarrow (3)$$

$$\Rightarrow I_2 = \left(\frac{-Z_{21}}{Z_{22}} \right) I_1 \rightarrow (4)$$

Substitute eq (3) in eq (1)

$$V_1 = Z_{11} \left(-\frac{Z_{22}}{Z_{21}} \right) I_2 + Z_{12} I_2$$

$$V_1 = I_2 \left(Z_{11} - \frac{Z_{12} \cdot Z_{22}}{Z_{21}} \right)$$

Impedance of Parasitic Elements

$$\boxed{\frac{V_1}{I_2} = Z_{12} - \frac{Z_{11} Z_{22}}{Z_{21}}}$$

By Reciprocity theorem $Z_{12} = Z_{21}$

Substituting eq (4) in (1)

$$V_1 = Z_{11} I_1 + Z_{12} \left[\frac{-Z_{21}}{Z_{22}} \right] I_1$$

$$V_1 = I_1 \left[Z_{11} - \frac{Z_{12} \cdot Z_{21}}{Z_{22}} \right]$$

$$\boxed{\frac{V_1}{I_1} = Z_{11} - \frac{Z_{12} \cdot Z_{21}}{Z_{22}}}$$

③ Horn Antenna :-

- It is a flared wave guide to transmit the FM waves into free space. It is a micro waves antenna.
- A microwave is capable of radiating radiation into open space provided the same is excited at one end and opened at other end.
- In a wave guide a small amount of energy incident at one end results a large amount of energy reflected back if it is open circuited to improper impedance matching.
- To overcome this drawback waveguide is terminated with a poof of horn (flared end) which is wired. So that entire energy is transmitted towards the forward direction.

There are 2-types of horn Antennas

- (i) Rectangular horn Antenna
- (ii) Circular horn Antenna.

As compared with radiation through transmission line, the radiation through the waveguide is larger.

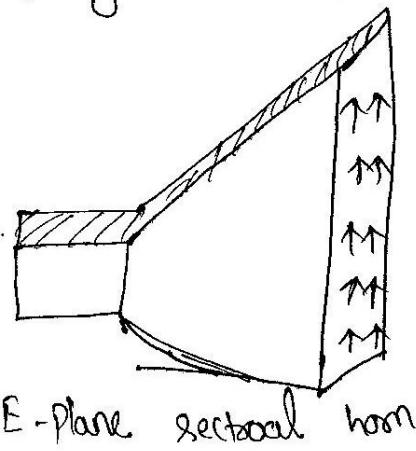
Depending upon the direction of flaring(widening), the rectangular are further classified as Sectoral horn and Pyramidal horn.

A Sectoral horn is obtained if the flaring(tapering) is done in one direction.

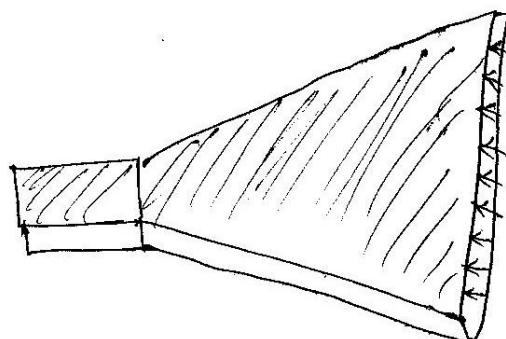
further classified as

- (i) E-Plane sectoral horn
- (ii) H-Plane sectoral horn
- (iii) Pyramidal horn

- * The E-plane sectoral horn is obtained when the flaring is done in the direction of electric field vectors.
- * The H-plane sectoral horn is obtained if the flaring is done in the direction of magnetic field vectors.
- * In both E & H-Plane sectoral horn the flaring is done along a single wall of the rectangular waveguide in one direction.

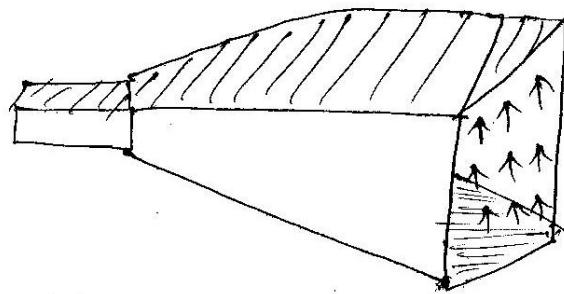


E-Plane sectoral horn



H-Plane sectoral horn

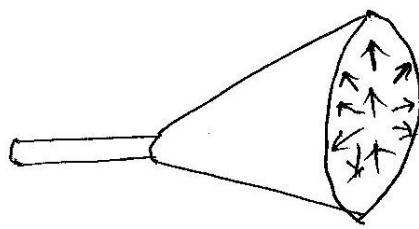
→ Pyramidal horn:- The flaring is done along both the walls of the rectangular waveguide in the direction of both the electric and magnetic field vectors the horn is obtained Pyramidal horn.



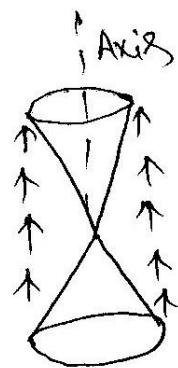
(ii) Circular horn Antenna:-

2 - types

- a) Conical horn Antenna
- b) Biconical horn Antenna



(a) Conical horn



(b) Bi-conical horn

By providing feeder impedance matching we can avoid the standing wave ratio and we get maximum directivity.

Design Equations:-

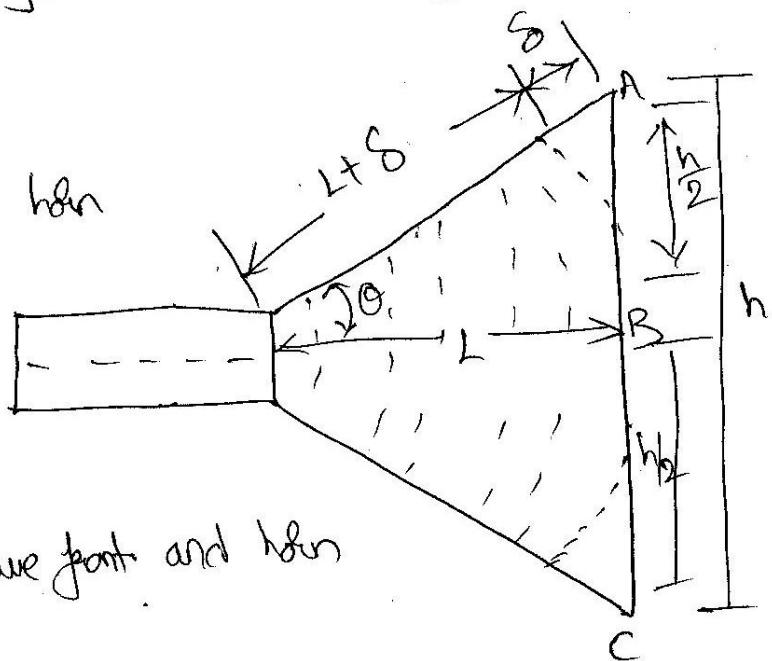
Consider a E-plane sectorial horn

where θ is flare angle

L - is axial length

h - is height of the mouth

s - is path difference b/w wave front and horn



$$\cos \theta = \frac{L}{L+s}$$

$$\tan \theta = \frac{h/2}{L} = \frac{h}{2L}$$

$$\theta = \cos^{-1} \left(\frac{L}{L+s} \right) \approx \tan^{-1} \left(\frac{h}{2L} \right)$$

From right angled triangle

$$(L+s)^2 = L^2 + \left(\frac{h}{2}\right)^2$$

$$L^2 + s^2 + 2sL = L^2 + \frac{h^2}{4}$$

Let s as small so s^2 is negligible

$$L^2 + 2sL = L^2 + \frac{h^2}{4}$$

$$2sL = \frac{h^2}{4} \Rightarrow$$

$$L = \frac{h^2}{8s}$$

$$h = \sqrt{8sL}$$

Here S-Variety values for E-plane horn $S_E = 0.21$ (13)

For H-plane horn $S_H = 0.41$

For Co-axial horn $S_{Coaxial} = 0.31$

The approximate formulae for half power beamwidth of optimum horn antenna is

$$\theta_E = \frac{57.1}{R} \text{ deg}$$

$$\theta_H = \frac{57.1}{W} \text{ deg}$$

Area = height \times width

$$\text{Directivity } (D) = \frac{7.5 \text{ hw}}{\lambda^2} = \frac{7.5 A}{\lambda^2}$$

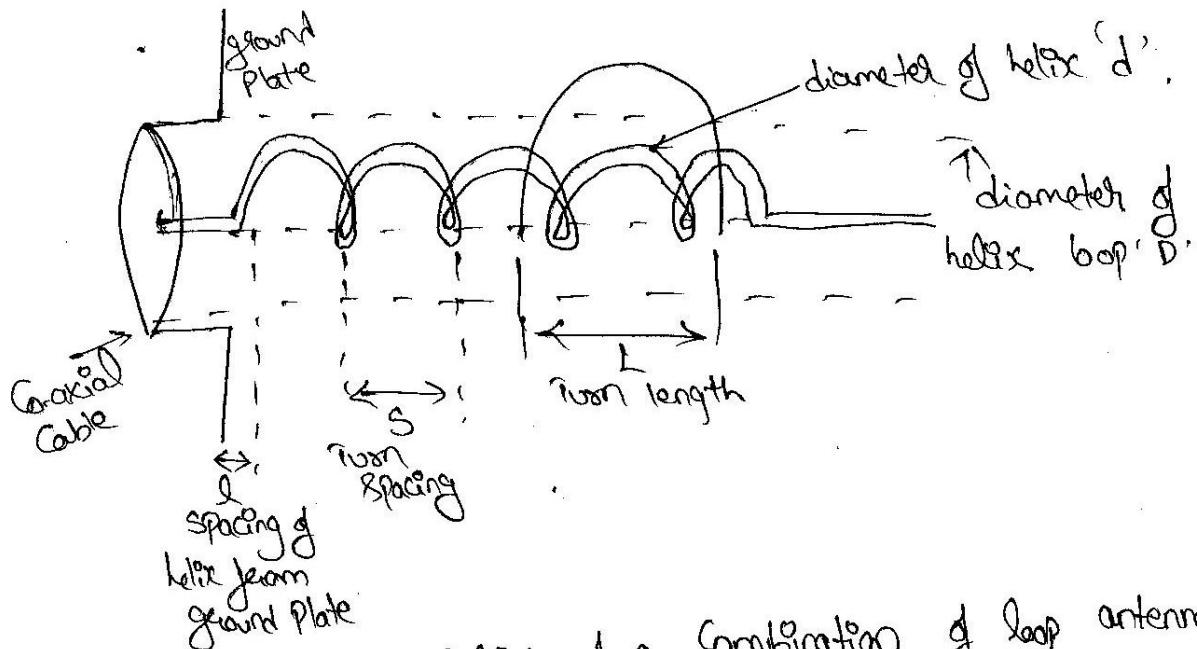
$$\text{Directive gain } G_d = \frac{4.5 \text{ hw}}{\lambda^2} = \frac{4.5 A}{\lambda^2} \quad \text{hw - half width}$$

small flare angle represents small aperture and also less directivity. For optimum operation flare angle varied from $40-15^\circ$ and beam width of $66^\circ //$

4) Helical Antenna:-

Helical Antenna is a very high frequency antenna used to generate a circularly polarised wave and is used in communication system (Satellite Communication). The Antenna is a helix of thick copper wire & tubing wound and shape is like a screw thread used as an antenna or has a flat metal plate called as ground plate.

→ The helix is fed from a Co-axial cable with its helix one end is connected to inner conductor of the Co-axial cable and other conductor is connected to ground plate.



→ This antenna is a series of a combination of loop antennas and dipole antennas.

→ The radiation pattern of helical antenna depends on a diameter of the helices (d), the turn spacing (s) and also axial length ($A = \pi s$) and also the circumference of helices.

→ There is a relation b/w circumference $C = \pi D$ and turn spacing (s) and pitch angle (α).

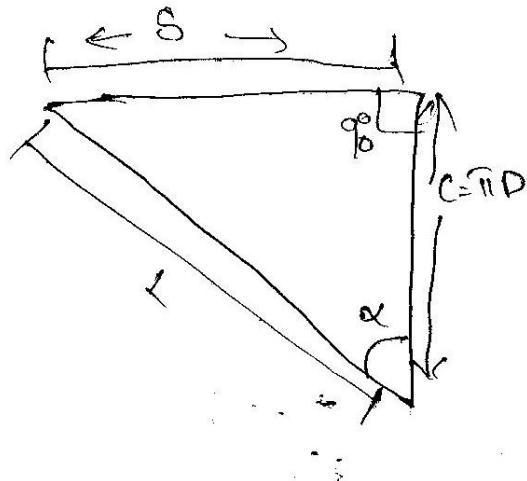
(a) Pitch angle :-

pitch angle is defined as the angle b/w a line tangent to the helix and a plane normal to the axis and it is calculated from the triangle.

$$\tan \alpha = \frac{s}{C}$$

$$\alpha = \tan^{-1} \left(\frac{s}{C} \right)$$

$$\alpha = \tan^{-1} \left(\frac{s}{\pi D} \right) \quad (\because C = \pi D)$$



(15)

→ For one turn helix the relation bw spacing s ,
Pitch angle α , Circumference is given by

$$L^2 = S^2 + C^2$$

$$L = \sqrt{S^2 + C^2}$$

In helical antenna in two ways radiation takes place based on the parameters like N, C, S , they are

N = No. of turns

D = Diameter of helix (Centre to Centre).

C = Circumference of helix = πD

S = Spacing bw two turn measured Centre to Centre

A = Axial length

x = Length of one turn

α = Pitch angle

d = Diameter of conductor.

In general, a helical antenna can radiate in many modes. But the most important modes of radiation

- (i) Normal (d) Perpendicular mode of radiation
- (ii) Axial (d) End fire (d) Beam mode of radiation.



(a) Normal mode



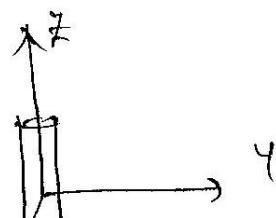
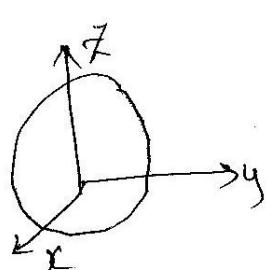
(b) Axial mode



(c) Conical mode

(i) Normal mode (d) Perpendicular mode of radiation:-

- Normal mode can be set by considering N.L $\ll \lambda$
- In this mode the maximum radiation is \perp to the axis.
- This mode gives narrow beamwidth and less efficiency
- Based on the pitch angle if $\alpha = 0^\circ$ then antenna becomes loop
- If $\alpha = 90^\circ$ then Antenna becomes a wide (d) dipole



- The radiation pattern is same for both antenna (loop & dipole) and is either circularly polarised or linearly polarised
- In general α is small then loop Polarization dominated

(ii) Axial ratio :-

$$(A_x) \text{ Axial ratio} = \frac{E_\theta}{E_\phi}$$

$$\therefore E_\phi = \frac{120 \pi^2 I \sin\theta}{\delta} A^{1/2} ; E_\theta = \frac{j 60 \pi I \sin\theta}{\delta} s/\lambda$$

where I is retarded current ; A is area of helix $= \frac{\pi D^2}{4}$
 δ is distance ; s → spacing (d) length of the dipole

$$A_x = \frac{E_\theta}{E_\phi} = \frac{\frac{j 60 \pi I \sin\theta}{\delta} s/\lambda}{\frac{120 \pi^2 I \sin\theta}{\delta} A^{1/2}}$$

$$A_x = \frac{j 60 \pi I \sin\theta}{\delta} s/\lambda \times \frac{\delta}{120 \pi^2 I \sin\theta} \cdot \frac{A^{1/2}}{2} / A$$

$$A_x = \frac{JS\lambda}{2\pi A}$$

(17)

$$(A_x) = \frac{S\lambda}{2\pi A} = \frac{S\lambda}{2\pi \times \frac{\pi D^2}{4r_2}}$$

$$(A_x) = \frac{2S\lambda}{\pi^2 D^2} = \frac{2S\lambda}{c^2} (\because c = \pi D)$$

From above A_x when $A_x = 0$, then Pnch horizontal
Polarization takes place.

→ when $A_x = \infty$ Pnch vertical Polarization takes place

→ when $A_x = 1$ then we get circular Polarization.

$$A_x = \frac{2S\lambda}{\pi^2 D^2}$$

$$\frac{2S\lambda}{\pi^2 D^2} = 1 \Rightarrow 2S\lambda = \frac{\pi^2 D^2}{c^2}$$

$$S = \frac{\pi^2 D^2}{2\lambda} > \frac{c^2}{2\lambda}$$

∴ Pitch Angle :-

$$\alpha = \tan^{-1} \left(\frac{S}{c} \right)$$

$$= \tan^{-1} \left(\frac{S}{\pi D} \right) = \tan^{-1} \left(\frac{\pi^2 D^2}{2\lambda \cdot \pi D} \right)$$

$$\Rightarrow \tan^{-1} \left(\frac{\pi D}{2\lambda} \right)$$

$$\boxed{\alpha = \tan^{-1} \left(\frac{c}{2\lambda} \right)}$$

(18)

(iii) Axial Mode operation:-

In this mode we get maximum radiation along the axis and is used in practical applications. This mode is also called as End fire mode. Because radiation is along the axis.

This mode is set by considering spacing and circumference ω of the spiral of wavelength. The gain is high in this mode and also we get wide bandwidth. The pitch angle for axial mode of operation is varies from 12° to 18° for optimum operation it should be 14° .

The terminal impedance varies from 100 to 200Ω

$$R_{terminal} = \frac{140 C}{\lambda} \Omega$$

Half Power beam width is

$$\theta_{HPBW} = \frac{52}{C} \sqrt{\frac{\lambda^3}{N}} \text{ degrees}$$

Beam width b/w the first nulls is given by

$$\theta_{BWN} = \frac{115}{C} \sqrt{\frac{\lambda^3}{N}} \text{ deg}$$

Max. directive gain is represented by

$$G_d = \frac{15 N S c^2}{\lambda}$$

Axial ratio is

$$A_r = 1 + \frac{1}{2N}$$

