$$z(r) = \frac{cr^2}{1 + \sqrt{1 - (1+k)c^2r^2}}$$