

$$z(r) = \frac{a^2}{1 + \sqrt{1 - (1 + k)c^2 r^2}} + \sqrt[8]{\frac{8}{2j - 1}} a^2 r^2$$