SPLAT Baseline Coordinate Definitions

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In this document I summarize the coordinate definitions for the three mirrors in the TMA design filename SPLAT_Base _Fwd.zmx, which can be found in https://github.com/patogallardo/zemax_tools/tree/master/design_analysis/SPLAT_baseline_20210523/SPLAT_Base_Fwd.zmx. For Step files of this design see folder coordinate_definitions/step_files.

Surfaces covered in this document are: Origin, Primary, Secondary, Tertiary and Image surface. These surfaces can be fully defined with a location vector and a rotation angle. Another way of defining these is by using a location vector and a rotation matrix, which is useful for Grasp studies.

1 Surface definitions and rotation angles

Table 1 shows the surface definitions for this design. Angle α refers to the rotation around the X coordinate in degrees.

2 Rotation matrices

The rotation angle can be expressed more generally by a rotation matrix and an offset, which gives the freedom to represent any 3D rotation in space.

In this formalism a vector in the local coordinate system \vec{x}_l can be expressed as a global vector \vec{x}_g via an offset \vec{x}_O and a rotation matrix R as

$$\vec{x}_g = \vec{x}_O + R\vec{x}_l. \tag{1}$$

| surface | X[mm] | Y[mm] | Z[mm] | $\alpha [\mathrm{deg}]$ |
|---------|-------|----------|----------|--------------------------|
| prime | 0.000 | 0.000 | 0.000 | 155.402 |
| second | 0.000 | 5615.000 | 4898.000 | 171.165 |
| tert | 0.000 | 8367.000 | 445.000 | -170.883 |
| Image | 0.000 | 9575.762 | 5024.441 | 168.927 |

Table 1: Surface local coordinate system locations and rotations about the X axis for the TMA.

Note that the columns of R contain the orientation vectors of the local x,y,z directions.

Tables 2, 3, 4 and 5 show the rotation matrices for the origins of the mirror coordinate systems.

| 1.00000 | 0.00000 | 0.00000 | 1.00000 | 0.00000 | 0.00000 |
|---------|----------|----------|---------|----------|----------|
| 0.00000 | -0.90925 | -0.41625 | 0.00000 | -0.98813 | -0.15360 |
| 0.00000 | 0.41625 | -0.90925 | 0.00000 | 0.15360 | -0.98813 |

 $\begin{array}{ll} {\rm Table~2:~Rotation~matrix~for~the~M1~Table~3:~Rotation~matrix~for~the~M2}\\ {\rm local~coordinate~system.} \end{array}$

| 1.00000 | 0.00000 | 0.00000 | 1.00000 | 0.00000 | 0.00000 |
|---------|----------|----------|---------|----------|----------|
| 0.00000 | -0.98737 | 0.15846 | 0.00000 | -0.98138 | -0.19207 |
| 0.00000 | -0.15846 | -0.98737 | 0.00000 | 0.19207 | -0.98138 |

Table 4: Rotation matrix for the M3 Table 5: Rotation matrix for the imlocal coordinate system. age surface local coordinate system.

