# Reinforcement Learning

Al Systems Implementation

#### Overview

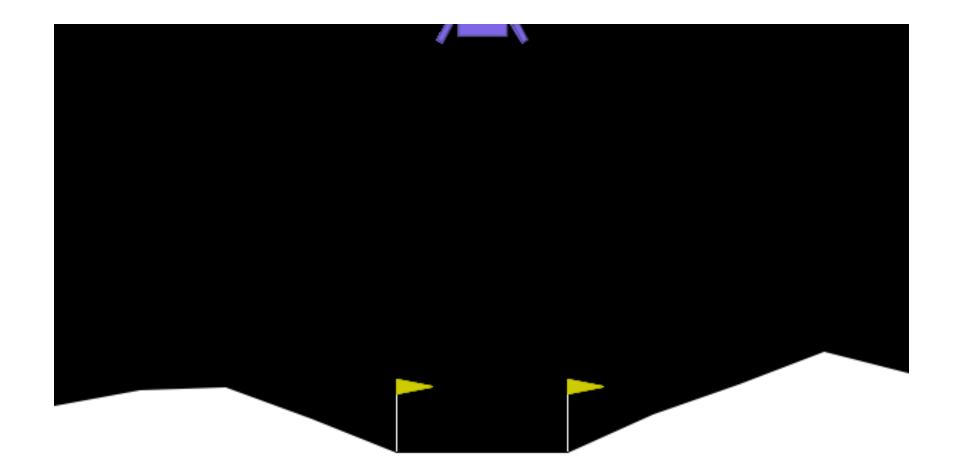
- What is the In-Class Test?
- What is Reinforcement Learning
- The OpenAl Gym / Farama Foundation Gymnasium
- Basic Policies
- Neural Network based Policy
- Q-Learning

#### In-Class Test

- Examination Conditions
- You will be provided a Jupyter Notebook
- Each section will have a task, and a cell to enter your answer into
- You may not look at your previous classwork, but you can look at the documentation for relevant libraries
- 90 minutes
- COMP5850 Different class time to usual, double check your timetable!

## What is Reinforcement Learning?

- Algorithms capable of learning behaviours
- Each system typically has 5 elements:
  - Environments
  - States
  - Agents
  - Actions
  - Rewards



## Farama Gymnasium

#### **Environments**

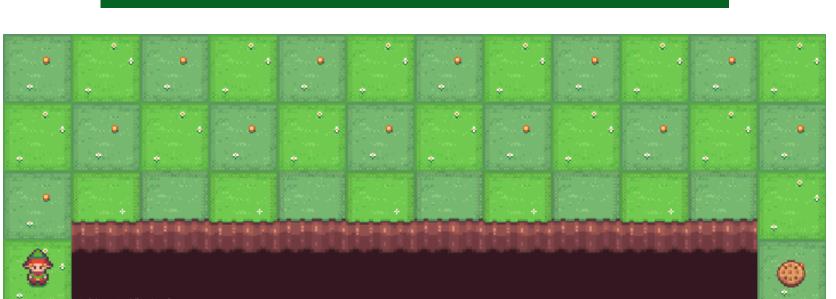
- Formerly OpenAl Gym
- A collection of simulations and environments
- Each environment allows you to simulate step-by-step whilst connecting to an agent
- Huge variety of environments available

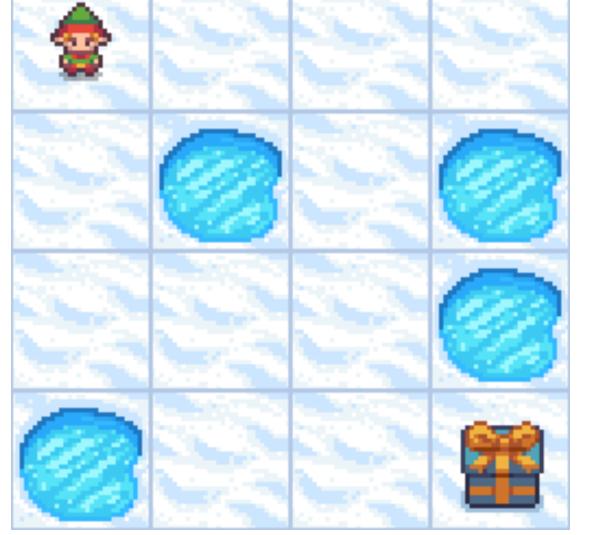
# Farama Gymnasium Toy Text

- Very basic environments
- Very limited states and action spaces
- Designed for basic testing, and designing new models









## Farama Gymnasium

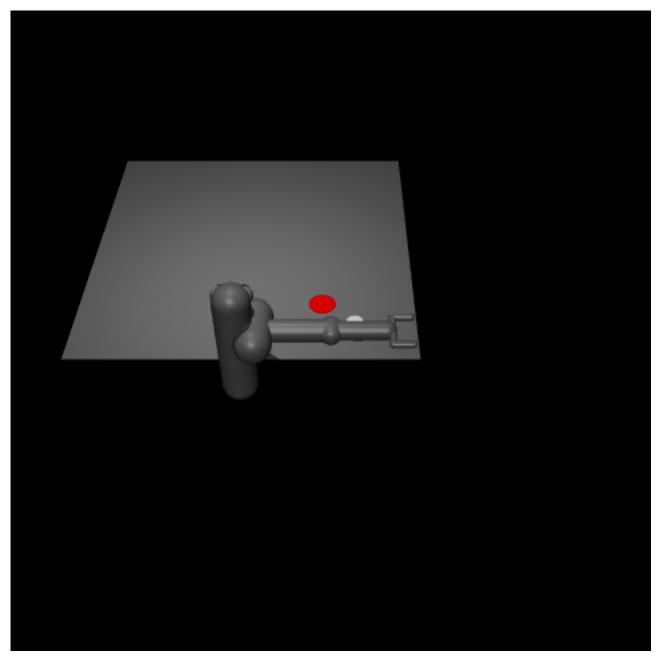
#### **Classic Control**

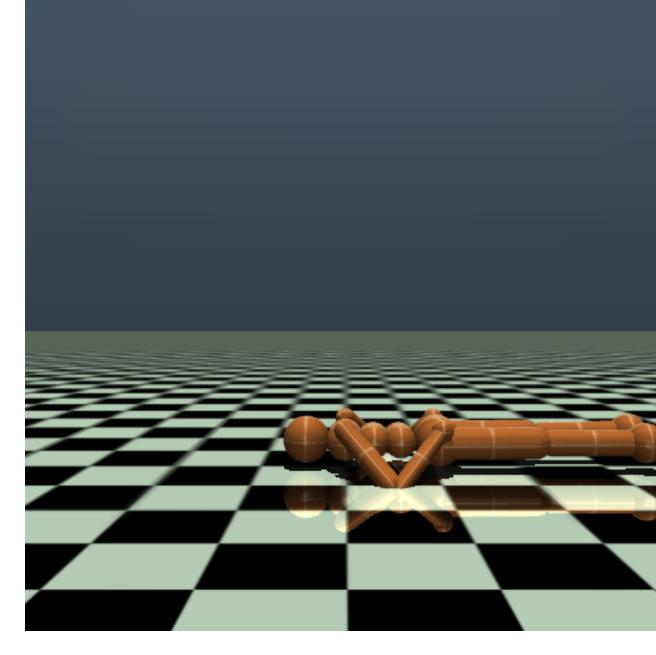
- A set of "classic" environments
- Typically simple environments, with basic "states"
- Great for early experimentation

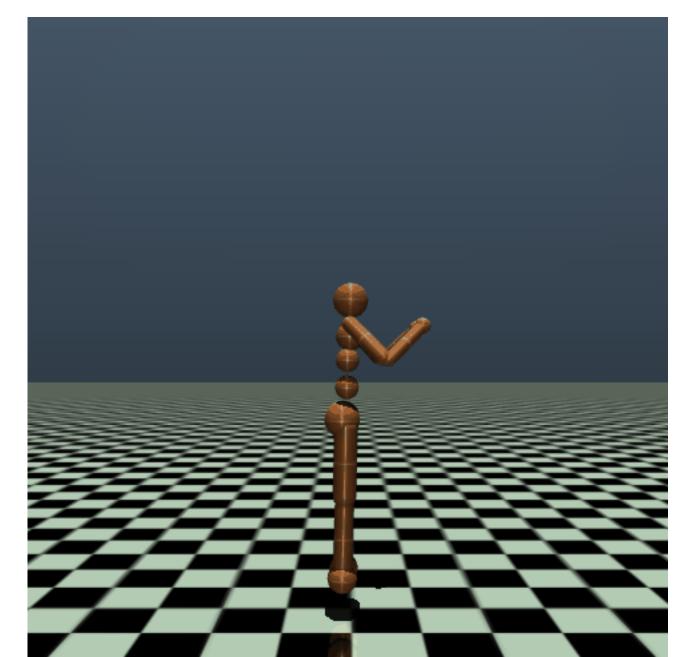


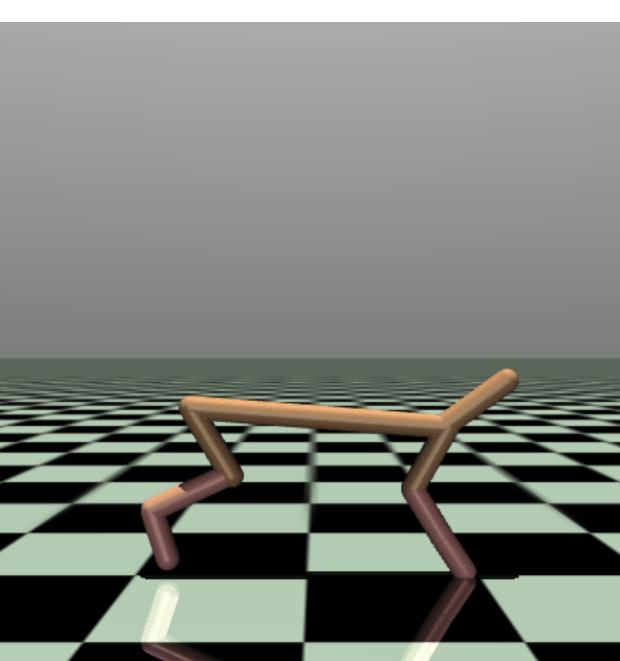
# Farama Gymnasium MuJoCo

- Advanced simulations utilising MuJoCo physics
- Much more complex scenarios, with more open states and environments
- More advanced experiments



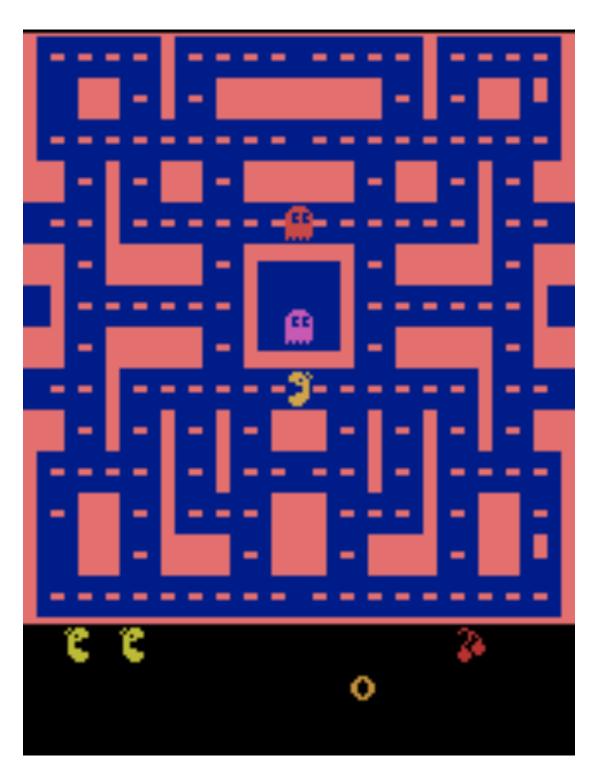


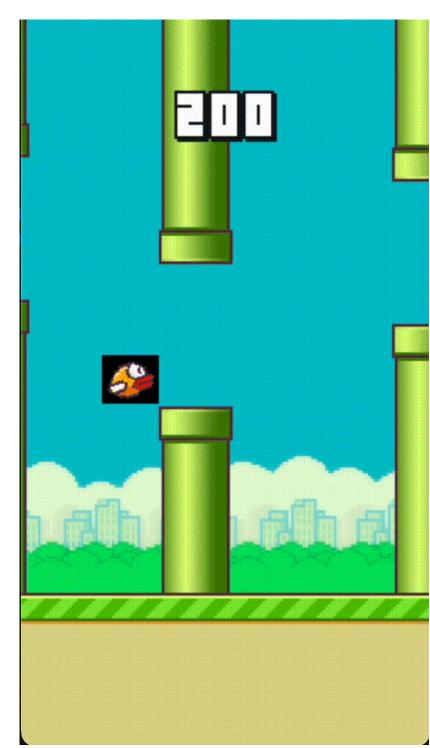


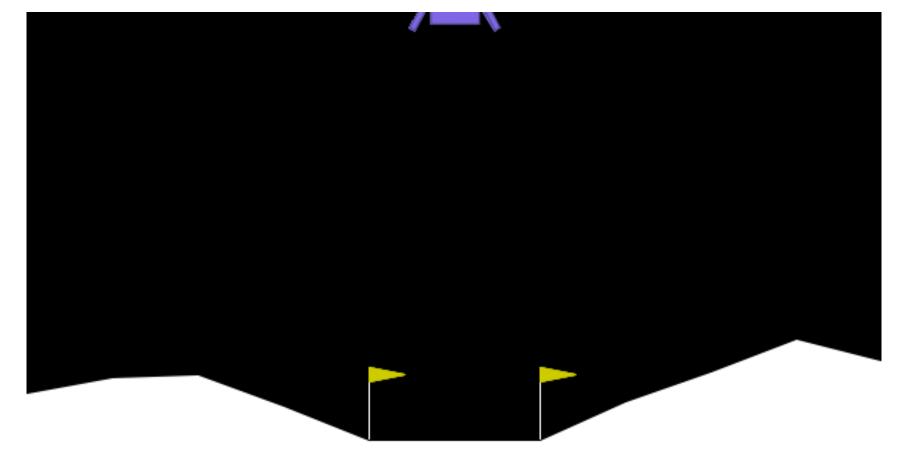


# Farama Gymnasium Others

- Box2D
  - Simply physics environments
- Atari
  - Literal Atari 2600 games
- Third Party
  - Pretty much anything!







### Some more definitions

- States  $(S_t)$ 
  - Represent the current state of the scenario. Could be an array of values
- Actions  $(A_t)$ 
  - An array representing some forces to be applied in the Simulation.
- Rewards  $(R_t)$ 
  - A value representing how the system performed
- Agents
  - The system that reads the states, provides the actions by following it's *policy*, and receives the rewards
- Every system can be represented as  $(S_t, A_t, R_t)$ , i.e.  $S_0, A_0, R_0, S_1, A_1, R_1, S_2 \dots$

### Policies

- Imagine we want the elf to reach the present, but avoid the frozen lakes
- Observation space: 16
  - One for each possible square, telling us it's current content
- Action space: 4
  - One for each direction we can move
- Reward
  - 1 for reaching the present, 0 for lakes



#### **Bacis Neural Network**

```
import tensorflow as tf
from tensorflow import keras

n_inputs = env.observation_space.shape[0] # 4, 1 for each State value

model = keras.models.Sequential([
    keras.layers.Dense(5, activation="relu", input_shape=[n_inputs]),
    keras.layers.Dense(1, activation="sigmoid")
])
```

- We could define a very simple network!
  - 4 input neurons, a 5 neuron hidden layer, and a 1 neuron output
  - But wait... how do we train this?

## Credit assignment

- If a model is responsible for a single action on a single step, how do we know what steps were successful?
  - Surely it won't be just the last step that caused the system to fail?
- Instead of evaluating with the reward, lets add a reduction ( $\gamma$ ) and evaluate with the sum of all the last reward steps

## Credit assignment

Lets say the last few steps look like this:

$$10 \rightarrow 0 \rightarrow -50$$

- So without a penalty, our reward would be 10 + 0 + -50 = -40
- Lets say also say  $\gamma = 0.8$ , then our reward would be

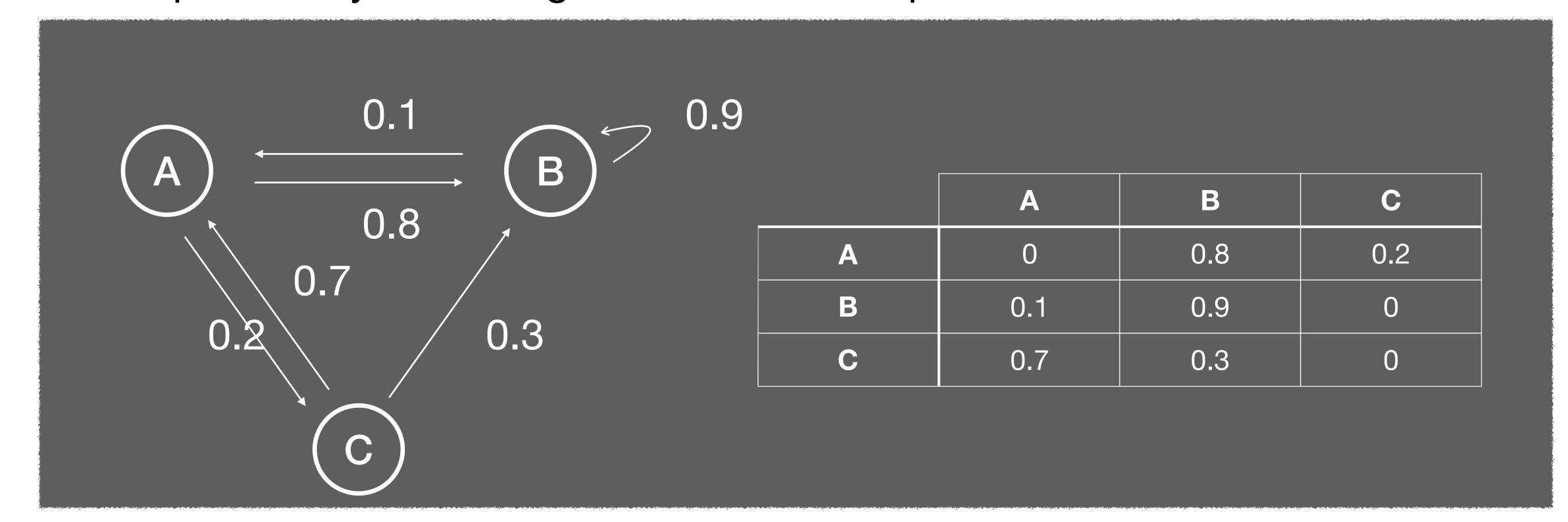
$$10 + \gamma \times 0 + \gamma^2 \times (-50) = -22$$

$$10 + 0.8 \times 0 + 0.8^2 \times (-50) = -22$$

• That way, future rewards are weighted less than current rewards

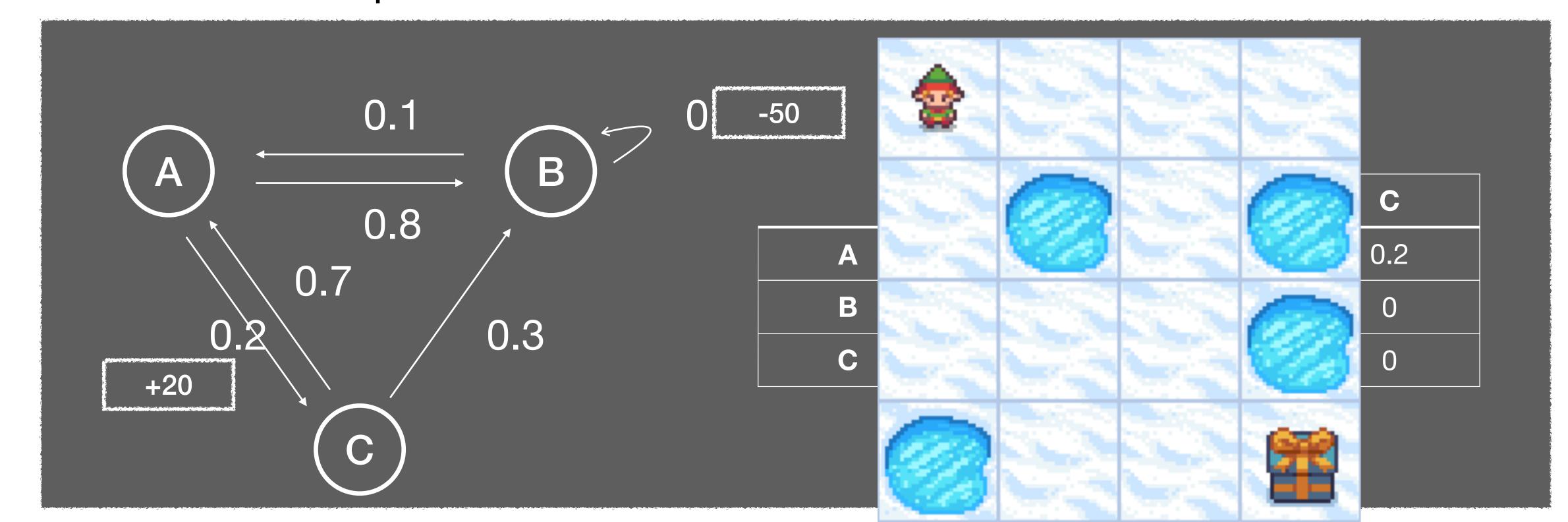
#### Markov Models

- A Markov Model is a probabilistic model of states
  - The probability of moving to a new state depends on the current state



#### Markov Decision Process

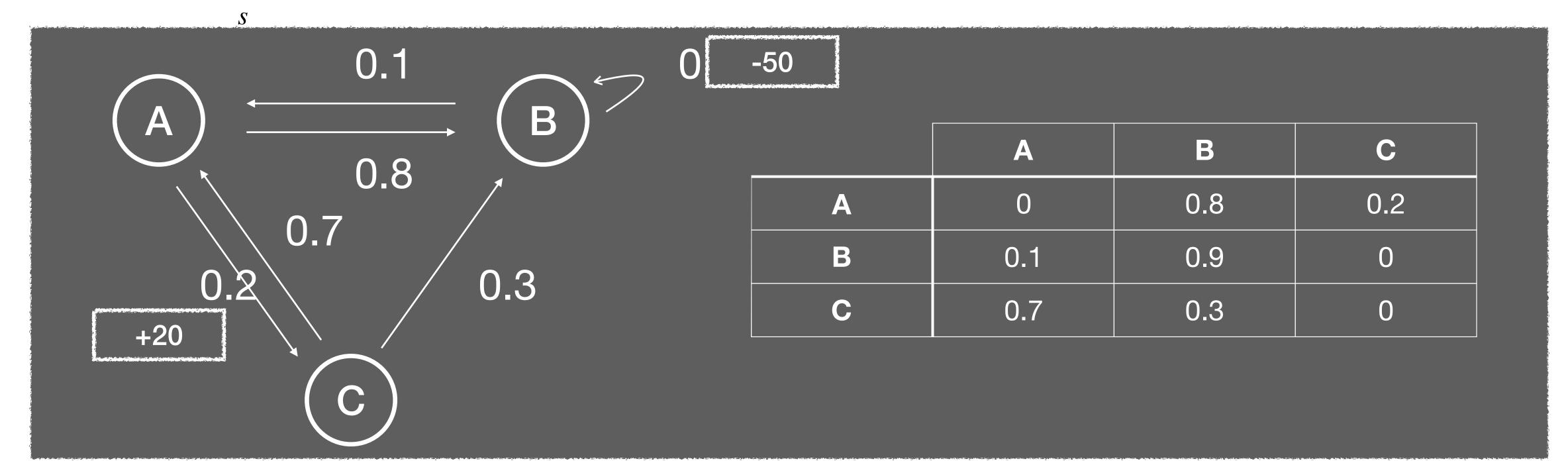
- Now imagine we also model rewards as a part of this model
  - Now we can represent the states of our environment!



#### Markov Decision Process

- Is there an optimal way to traverse this scene to maximise the reward?
  - Yes! Bellman's Optimality Equation:

$$V^*(s) = max_a \sum T(s, a, s')[R(s, a, s') + \gamma \cdot V^*(s')]$$
 for all  $s$ 



- Models a MDP
- Maintains a Q-Table of shape Q(s, a)
  - Ever row represents a current state  $S_t$
  - Each row contains a list for each possible action  $\boldsymbol{A}_t$
  - Each Q-Value shows what the algorithm thinks would be the best decision



State	Q-Values
1	[0.735, 0.773, 0.773, 0.735]
2	[0.735, 0, 0.814, 0.773]
3	[0.773, 0.857, 0.773, 0.814]
4	[0.814, 0, 0.773, 0.773]
5	[0.773, 0.814, 0, 0.735]
6	[0, 0, 0, 0]
7	[0, 0.902, 0.902, 0]
	•••

#### **Update Formula**

$$Q(s,a) \leftarrow Q(s,a) + \alpha \cdot [r + \gamma \cdot max_{a'}Q(s',a') - Q(s,a)]$$

- Q(s, a): The current Q-value for s and a
- r: The immediate reward for taking action a in state s
- $\alpha$ : The learning rate
- s': The next state after taking action a in state s
- a': The next action chosen in s'
- $max_{a'}Q(s',a')$ : the maximum possible Q-Value from all possible actions in the next state s



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4	[0.814, 0, 0.773, 0.773]
5	[0.773, 0.814, 0, 0.735]
6	[0, 0, 0, 0]
7	[0, 0.902, 0.902, 0]

- Train thousands of times, and test as many state/ action combinations as possible, then adjust values based on outcomes
- During training, each step is either stochastic or greedy ( $\epsilon$ -greedy)
  - $\epsilon$  probability to be random,  $1-\epsilon$  chance to be Greedy
- Why? Why not just be Greedy?



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	•••

### SARSA

#### State-Action-Reward-State-Action

- Similarly to Q-Learning, SARSA maintains a Q-Table
- Initialise a Q-Table with arbitrary values
- Utilise  $\epsilon$ -greedy search

• 
$$Q(s,a) \leftarrow Q(s,a) + \alpha \cdot [r + \gamma \cdot Q(s',a') - Q(s,a)]$$

- How is that different than Q-Learning?
- Q(s', a'), not  $max_{a'}Q(s', a')$
- SARSA values the current action over possible future actions



State	Q-Values
1	[0.735, 0.773, 0.773, 0.735]
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7	[0, 0.902, 0.902, 0]

- So far so good, so why don't we always use Q-Learning or SARSA?
- Well, what if you weren't trying to play a basic game, but wanted to teach something how to walk?
  - How many states are there?
  - How do we model that as a table?
    - How big will the table be?!



State	Q-Values
1	[0.735, 0.773, 0.773, 0.735]
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	•••

## Deep Q-Learning

- Now, imagine populating that Q-Table for a more complex situation...
  - Suddenly, the table becomes so large it's impossible to model!
- Instead of modelling every possible state, we can fin a function that approximates  $Q_{\theta}(s,a)$ 
  - Instead, we can use a Deep Neural Network (DNN) to estimate Q-Values
    - This is called a "Deep Q-Network" (DQN)
- OK, but how do we use it?
  - The TF-Agents package!