

Let  $n$  be the input that is being checked for primality.

If  $n$  is composite (not prime),  
then it will be of the form

$$n = a \times b$$

$$1 < a, b < n$$

$$77 = 7 \times 11$$

$$77 \% 7 = 0$$

$$n \% a \stackrel{?}{=} 0$$

$$n = 2 \times b$$

$$n = 3 \times b$$

$$n = 5 \times b$$

$\vdots$

$$n = \sqrt{n} \times \sqrt{n}$$

$$49 = 7 \times 7$$

$$\begin{array}{r}
 2 \overline{) 48} \\
 2 \overline{) 24} \\
 2 \overline{) 12} \\
 2 \overline{) 6} \\
 3 \overline{) 3} \\
 \underline{1}
 \end{array}$$

$$48 = 2^4 \times 3^1$$

$$28 = 2^2 \times 7^1$$

$$\text{LCM}(48, 28) = 2^4 \times 3^1 \times 7^1$$

$$\text{GCD}(48, 28) = 2^2 \times 3^0 \times 7^0$$

$$\begin{array}{r}
 2 \overline{) 28} \\
 2 \overline{) 14} \\
 7 \overline{) 7} \\
 \underline{1}
 \end{array}$$

$$28 = 2^2 \times 7^1$$

$$= 2^2 \times 3^0 \times 5^0 \times 7^1$$