

Compound Events and the Additive Rule

1. Suppose that two customers give ratings (1–5 stars) to the same restaurant on Yelp.
 - (a) Express the event “at least one customer gives a 1 star rating” as a union of two other events.

 - (b) Suppose that both customers randomly assign their ratings, giving equal probabilities to all possible star ratings. In this case, all 25 sample points have equal probability. Compute the probability of the event in part (a).

2. Suppose that two customers give ratings to the same restaurant on Yelp.
 - (a) Express the event “the average of their ratings is 3.5 or 4” as a union of two other events.
Hint: this is the same event as “the sum of their ratings is 7 or 8.”

 - (b) As in problem 1(b), suppose that both customers randomly assign their ratings with equal probability for all possible star ratings, so that all 25 sample points have equal probability. Compute the probability of the event in part (a).

Complementary Events and the Complement Rule

3. Here are the tabulated undergraduate major and gender frequencies from the class survey.

Undergrad Major	Gender		Total
	Female	Male	
Business	5	5	10
Hum./Soc. Sci.	7	16	23
Sci./Eng.	4	8	12
Total	16	29	45

Use the data and the complement rule to answer the following questions:

- (a) If you pick a random survey respondent, what is the probability that the undergraduate major will not be Business?
- (b) What proportion of survey respondents have an undergraduate major that is not listed as “Sci./Eng.”?
4. Suppose you flip five coins. What is the probability of getting at least one head?
Hint: what is the complement of this event?

Conditional Probability

5. Here is a table of the tabulated frequencies for the political parties and presidential votes of the respondents to the class survey.

Party	Vote			Total
	Clinton	Trump	Other	
Democrat	34	1	1	36
Republican	1	2	2	5
Other	2	1	2	5
Total	37	4	5	46

- (a) Express the following statements as conditional probabilities:

- $\frac{34}{36} \approx 94\%$ of the Democrats vote Clinton.
- $\frac{1}{4} \approx 25\%$ of the Trump votes come from Democrats.

- (b) Compute $P(\text{Trump} \mid \text{Republican})$ and $P(\text{Republican} \mid \text{Trump})$. Explain the difference between these two quantities.

6. The following table lists the pick-up and drop-off locations of approximately 170 million yellow cab taxi trips made in New York City in 2013. Numbers are reported in thousands.

Pick-up	Drop-off					Total
	Bronx	Brooklyn	Manhattan	Queens	Staten Is.	
Bronx	53	1	37	4	0	95
Brooklyn	8	2,707	1,598	273	2	4,588
Manhattan	638	5,458	143,656	5,906	22	155,680
Queens	122	1,022	5,058	2,281	8	8,491
Staten Is.	0	0	0	0	3	3
Total	821	9,188	150,349	8,464	35	168,857

- (a) Find $P(\text{drop-off Brooklyn} \mid \text{pick-up Manhattan})$ and $P(\text{pick-up Manhattan} \mid \text{drop-off Brooklyn})$. Explain the difference between these two quantities.

- (b) Express the following statement as a conditional probability: “29% of the trips with drop-off locations in Brooklyn originated in the same borough.”

The Multiplicative Rule

7. Out of the 51 students enrolled in the class, 18 are female (35%) and 33 are male (65%). Suppose that we randomly select two different students.
- (a) What is the probability that both students are male?
 - (b) What is the probability that both students are female?
 - (c) What is the probability that one of the students is male and one of the students is female?
8. Of the 47 students who filled out the survey, 36 indicated that they drink at least one cup of coffee per day, while 11 indicated that they do not drink coffee on a typical day. Suppose that we randomly select two different survey respondents.
- (a) What is the probability that both students regularly drink coffee?
 - (b) What is the probability that neither student regularly drinks coffee?
 - (c) What is the probability that exactly one student regularly drinks coffee?