

## Multiple Regression 2

COR1-GB.1305 – Statistics and Data Analysis

### Multiple Regression (Review)

- Consider the dataset of 147 movies from 2013. Here is the result of fitting a linear regression model to predict the base-10 logarithm of the total gross (**Log10Gross**) using Rotten Tomatoes audience and critics scores, along with the base-10 logarithm of the budget (**Log10Budget**) as predictors:

#### Analysis of Variance

Source	DF	Adj SS	Adj MS	F-Value	P-Value
Regression	3	18.8920	6.2973	55.70	0.000
Rotten Tomatoes Audience Score	1	3.3973	3.3973	30.05	0.000
Rotten Tomatoes Critics Score	1	0.1526	0.1526	1.35	0.247
Log10Budget	1	9.5855	9.5855	84.78	0.000
Error	143	16.1676	0.1131		
Total	146	35.0595			

#### Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
0.336244	53.89%	52.92%	51.28%

#### Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	3.175	0.397	8.00	0.000	
Rotten Tomatoes Audience Score	0.01388	0.00253	5.48	0.000	2.53
Rotten Tomatoes Critics Score	-0.00191	0.00164	-1.16	0.247	2.50
Log10Budget	0.4934	0.0536	9.21	0.000	1.07

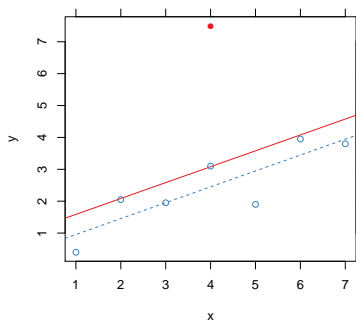
#### Regression Equation

Log10Gross = 3.175 + 0.01388 Rotten Tomatoes Audience Score  
 - 0.00191 Rotten Tomatoes Critics Score + 0.4934 Log10Budget

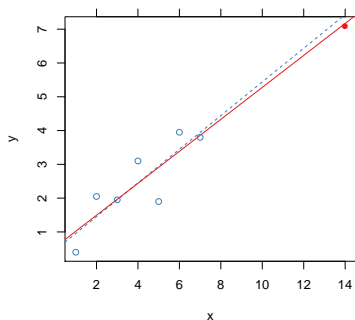
- Based on the ANOVA  $F$  test, is there evidence that the model is useful?
- What is the interpretation of the  $R^2$ ?
- In the fitted model, what is the interpretation of  $s$ ?
- In the fitted model, what is the interpretation of the coefficient of “Rotten Tomatoes Audience Score”?
- Based on the coefficient  $t$  tests, which predictor(s) would you remove from the model? What is the interpretation of the  $p$ -value for this predictor?

## Extreme Points

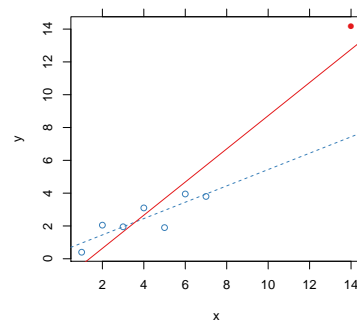
2. Each of the following scatterplots show two regression lines: the solid line is fitted to all of the points, and the dashed line is fitted to just the hollow points.



(a)



(b)



(c)

- (a) For each of the three cases, when the solid point is added to the dataset, is its residual from the least squares line large or small?

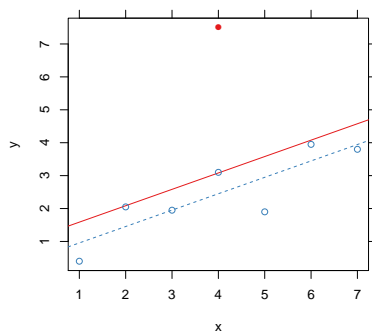
- (b) Is the  $x$  value of the solid point close to  $\bar{x}$  or far away from  $\bar{x}$ ?

- (c) What affect does adding the solid point have on  $\hat{\beta}_0$ ,  $\hat{\beta}_1$ , and  $R^2$ ?

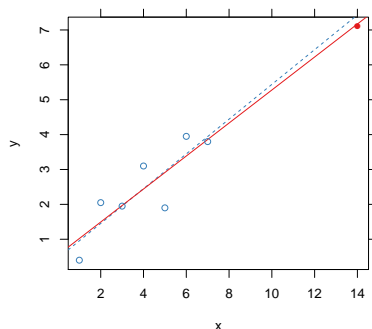
- (d) Should we include the solid point in the regression analysis? If not, what should we do with it?

## Outliers, leverage, and influence

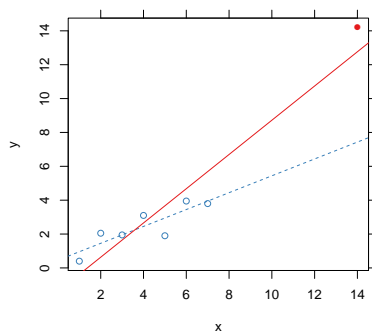
3. The following tables gives the observation number ( $i$ ), the standardized residual ( $r_i$ ), the leverage ( $h_i$ ), and Cook's distance ( $C_i$ ) for each data point. The solid point is observation 8.



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	-0.78	0.45	$2 \times 10^{-1}$
2	-0.02	0.27	$7 \times 10^{-5}$
3	-0.34	0.16	$1 \times 10^{-2}$
4	0.01	0.12	$7 \times 10^{-6}$
5	-0.90	0.16	$8 \times 10^{-2}$
6	-0.07	0.27	$1 \times 10^{-3}$
7	-0.51	0.45	$1 \times 10^{-1}$
8	2.32	0.12	$4 \times 10^{-1}$



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	-1.14	0.28	$3 \times 10^{-1}$
2	0.98	0.22	$1 \times 10^{-1}$
3	-0.03	0.17	$8 \times 10^{-5}$
4	1.11	0.14	$1 \times 10^{-1}$
5	-1.68	0.13	$2 \times 10^{-1}$
6	0.94	0.13	$7 \times 10^{-2}$
7	-0.10	0.15	$9 \times 10^{-4}$
8	-0.24	0.79	$1 \times 10^{-1}$



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	0.64	0.28	0.081
2	1.12	0.22	0.174
3	0.24	0.17	0.006
4	0.34	0.14	0.009
5	-1.33	0.13	0.126
6	-0.55	0.13	0.022
7	-1.44	0.15	0.185
8	2.19	0.79	8.892

In each of the three cases are any of the standardized residual, leverage, or Cook's distance large for observation 8? What counts as "large" for these diagnostics?

## Summary

4. Should an outlier or a point with high leverage always be removed from a regression analysis?
5. If we decide to remove a point from an analysis, what should we do with the point?
6. Does a leverage point always have a high Cook's Distance?
7. Can a point have low leverage and high Cook's Distance?