

**Regression Inference and Forecasting**  
COR1-GB.1305 – Statistics and Data Analysis

## Inference

- Here are the least squares estimates from the fitting the model

$$\text{Price} = \beta_0 + \beta_1 \text{Size} + \varepsilon_1$$

for  $n = 18$  apartments in Greenwich Village. Price is measured in units of \$1000 and size is measured in units of 100 ft<sup>2</sup>.

### Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
101.375	86.87%	86.05%	81.13%

### Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	182.3	62.4	2.92	0.010	
Size(100sqft)	44.95	4.37	10.29	0.000	1.00

### Regression Equation

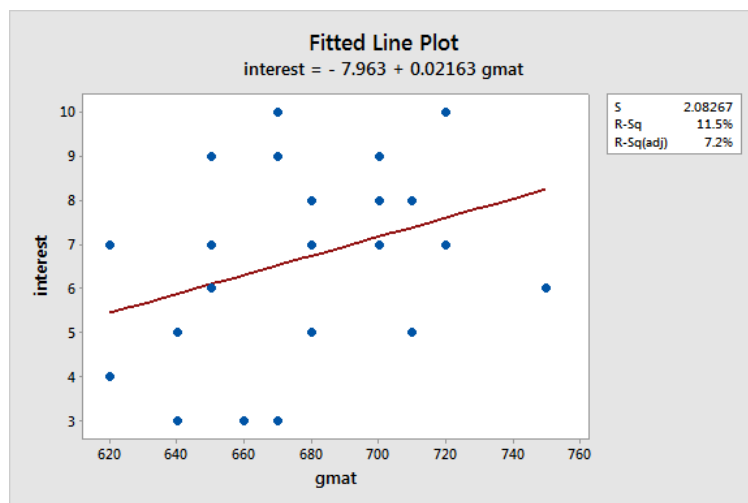
Price(\$1000) = 182.3 + 44.95 Size(100sqft)

- Construct a 95% confidence interval for  $\beta_1$ .
- What is the meaning of the confidence interval for  $\beta_1$ ?
- What is the meaning of a 95% confidence interval for  $\beta_0$ ? In the context of the housing data, is this useful?
- Perform a hypothesis test at level 5% of whether or not there is a linear relationship between Size and mean Price.

2. 23 students reported their GMAT scores and their interest levels in the course material (1–10). We will use this data to examine the relationship between these two variables. We fit the model

$$\text{Interest} = \beta_0 + \beta_1 \text{GMAT} + \varepsilon$$

using least-squares. The scatterplot at Minitab regression output follow.



#### Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
2.08267	11.45%	7.24%	0.00%

#### Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	-7.96	8.90	-0.89	0.381	
gmat	0.0216	0.0131	1.65	0.114	1.00

#### Regression Equation

$\text{interest} = -7.96 + 0.0216 \text{ gmat}$

- Quantify the relationship between GMAT score and interest using a 95% confidence interval. (You will need the value  $t_{.025,21} = 2.080$ .)
- Perform a hypothesis test to determine if there is a significant linear relationship between GMAT score and expected interest in the course.

## Forecasting

3. We used the regression model fit to the housing data to predict price at size 2000 ft<sup>2</sup>:

Regression Equation

$$\text{Price}(\$1000) = 182.3 + 44.95 \text{ Size}(100\text{sqft})$$

Variable	Setting
Size(100sqft)	20

Fit	SE Fit	95% CI	95% PI
1081.27	38.1287	(1000.44, 1162.10)	(851.667, 1310.88)

- (a) Find a 95% confidence interval for the mean price of all apartments with size 2000 ft<sup>2</sup>.
- (b) Find a 95% prediction interval for the price of a particular apartments with size 2000 ft<sup>2</sup>.
- (c) Make a statement about the prices of 95% of all apartments with size 2000 ft<sup>2</sup>.
- (d) What is the difference between the confidence interval and the prediction interval?

4. We fit a regression model to the 294 restaurants from the 2003 Zagat data. Our predictor variable is food quality (1–30), and our response variable is price (\$). Here is the result of using the fitted model to predict the price when the food quality is 25.

Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
12.5559	27.93%	27.68%	26.86%

Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	-4.74	3.95	-1.20	0.232	
Food	2.129	0.200	10.64	0.000	1.00

Regression Equation

Price = -4.74 + 2.129 Food

Variable	Setting
Food	25

Fit	SE Fit	95% CI	95% PI
48.4832	1.33906	(45.8478, 51.1187)	(23.6315, 73.3349)

(a) What is the interpretation of the 95% confidence interval?

(b) What is the interpretation of the 95% prediction interval?

(c) Explain how the confidence interval is related to Fit, SE Fit, and S.

(d) Explain how the prediction interval is related to Fit, SE Fit, and S.