

**Regression Inference and Forecasting**  
COR1-GB.1305 – Statistics and Data Analysis

## Inference

- Here are the least squares estimates from the fitting the model

$$\text{Price} = \beta_0 + \beta_1 \text{Size} + \varepsilon_1$$

for  $n = 18$  apartments in Greenwich Village. Price is measured in units of \$1000 and size is measured in units of 100 ft<sup>2</sup>.

### Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
101.375	86.87%	86.05%	81.13%

### Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	182.3	62.4	2.92	0.010	
Size(100sqft)	44.95	4.37	10.29	0.000	1.00

### Regression Equation

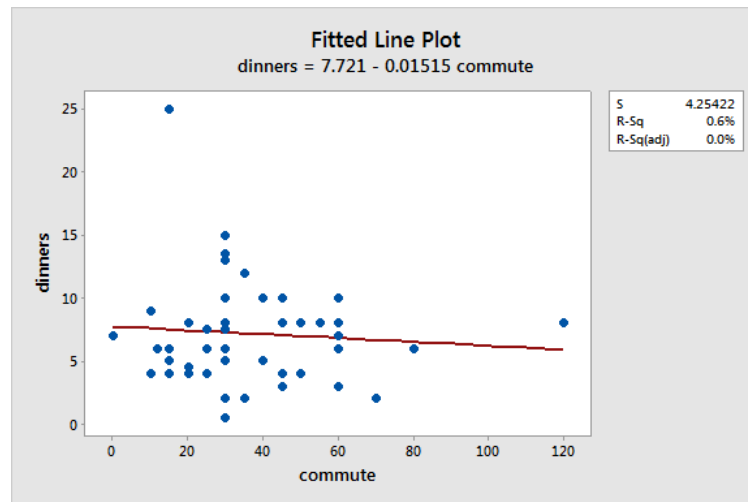
Price(\$1000) = 182.3 + 44.95 Size(100sqft)

- Construct a 95% confidence interval for  $\beta_1$ .
- What is the meaning of the confidence interval for  $\beta_1$ ?
- What is the meaning of a 95% confidence interval for  $\beta_0$ ? In the context of the housing data, is this useful?
- Perform a hypothesis test at level 5% of whether or not there is a linear relationship between Size and mean Price.

2. 51 students reported their commute times (in minutes) and the number of times they go out to dinner in a typical month. We will use this data to examine the relationship between these two variables. We fit the model

$$\text{Dinners} = \beta_0 + \beta_1 \text{Commute} + \varepsilon$$

using least-squares. The scatterplot at Minitab regression output follow.



#### Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
4.25422	0.56%	0.00%	0.00%

#### Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	7.72	1.21	6.38	0.000	
commute	-0.0152	0.0288	-0.53	0.601	1.00

#### Regression Equation

dinners = 7.72 - 0.0152 commute

- (a) Quantify the relationship between dinners and commute time using a 95% confidence interval. (You will need the value  $t_{.025,49} \approx 2.021$ .)
- (b) Perform a hypothesis test to determine if there is a significant linear relationship between dinners and commute time.

## Forecasting

3. We used the regression model fit to the housing data to predict price at size 2000 ft<sup>2</sup>:

Regression Equation

$$\text{Price}(\$1000) = 182.3 + 44.95 \text{ Size}(100\text{sqft})$$

Variable	Setting
Size(100sqft)	20

Fit	SE Fit	95% CI	95% PI
1081.27	38.1287	(1000.44, 1162.10)	(851.667, 1310.88)

- (a) Find a 95% confidence interval for the mean price of all apartments with size 2000 ft<sup>2</sup>.
- (b) Find a 95% prediction interval for the price of a particular apartments with size 2000 ft<sup>2</sup>.
- (c) Make a statement about the prices of 95% of all apartments with size 2000 ft<sup>2</sup>.
- (d) What is the difference between the confidence interval and the prediction interval?

4. We fit a regression model to the 294 restaurants from the 2003 Zagat data. Our predictor variable is food quality (1–30), and our response variable is price (\$). Here is the result of using the fitted model to predict the price when the food quality is 25.

Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
12.5559	27.93%	27.68%	26.86%

Coefficients

Term	Coef	SE Coef	T-Value	P-Value	VIF
Constant	-4.74	3.95	-1.20	0.232	
Food	2.129	0.200	10.64	0.000	1.00

Regression Equation

Price = -4.74 + 2.129 Food

Variable	Setting
Food	25

Fit	SE Fit	95% CI	95% PI
48.4832	1.33906	(45.8478, 51.1187)	(23.6315, 73.3349)

(a) What is the interpretation of the 95% confidence interval?

(b) What is the interpretation of the 95% prediction interval?

(c) Explain how the confidence interval is related to Fit, SE Fit, and S.

(d) Explain how the prediction interval is related to Fit, SE Fit, and S.