
Tests from Proofs

Patrice Godefroid

Microsoft Research

Part 1:

Tests from Satisfiability Proofs

(Whitebox Fuzzing for Security Testing)

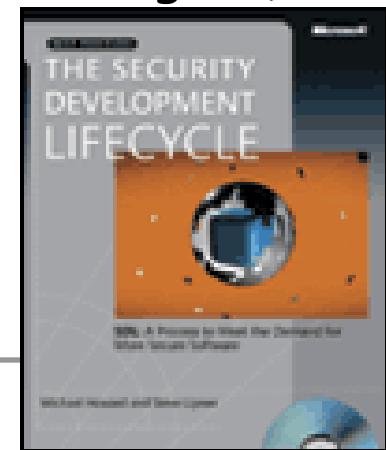
Security is Critical (to Microsoft)

- Software security bugs can be very expensive:
 - Cost of each Microsoft Security Bulletin: \$Millions
 - Cost due to worms (Slammer, CodeRed, Blaster, etc.): \$Billions
- Many security exploits are initiated via files or packets
 - Ex: MS Windows includes parsers for hundreds of file formats
- Security testing: “hunting for million-dollar bugs”
 - Write A/V (always exploitable), Read A/V (sometimes exploitable), NULL-pointer dereference, division-by-zero (harder to exploit but still DOS attacks), etc.

I am from
Belgium too!

Hunting for Security Bugs

- Main techniques used by “black hats”:
 - Code inspection (of binaries) and
 - Blackbox fuzz testing
- Blackbox fuzz testing:
 - A form of blackbox random testing [Miller+90]
 - Randomly **fuzz** (=modify) a well-formed input
 - Grammar-based fuzzing: rules that encode “well-formed”ness + heuristics about how to fuzz (e.g., using probabilistic weights)
- Heavily used in security testing
 - Simple yet effective: many bugs found this way...
 - At Microsoft, fuzzing is mandated by the SDL →



Introducing Whitebox Fuzzing

- Idea: mix fuzz testing with dynamic test generation
 - Dynamic symbolic execution
 - Collect constraints on inputs
 - Negate those, solve with constraint solver, generate new inputs
 - → do "systematic dynamic test generation" (=DART)
- Whitebox Fuzzing = "DART meets Fuzz"
Two Parts:
 1. Foundation: DART (Directed Automated Random Testing)
 2. Key extensions ("Whitebox Fuzzing"), implemented in SAGE

Automatic Code-Driven Test Generation

Problem:

Given a sequential program with a set of input parameters,
generate a set of inputs that maximizes code coverage

= “automate test generation using program analysis”

This is **not** “model-based testing”
(= generate tests from an FSM spec)

How? (1) Static Test Generation

- Static analysis to partition the program's input space
[King76,...]
- Ineffective whenever symbolic reasoning is not possible
 - which is frequent in practice... (pointer manipulations, complex arithmetic, calls to complex OS or library functions, etc.)

Example:

```
int obscure(int x, int y) {  
    if (x==hash(y)) error();  
    return 0;  
}
```

Can't statically generate
values for x and y
that satisfy "x==hash(y)" !

How? (2) Dynamic Test Generation

- Run the program (starting with some random inputs), gather constraints on inputs at conditional statements, use a constraint solver to generate new test inputs
- Repeat until a specific program statement is reached [Korel90,...]
- Or repeat to try to cover **ALL** feasible program paths:
DART = Directed Automated Random Testing
= systematic dynamic test generation [PLDI'05,...]
 - detect crashes, assertion violations, use runtime checkers (Purify,...)

DART = Directed Automated Random Testing

Example:

```
int obscure(int x, int y) {  
    if (x==hash(y)) error();  
    return 0;  
}
```

Run 1 :- start with (random) $x=33, y=42$
- execute concretely and symbolically:
if ($33 \neq 567$) | if $(x \neq \text{hash}(y))$
constraint too complex
→ simplify it: $x \neq 567$
- solve: $x \neq 567 \rightarrow \text{solution: } x=567$
- new test input: $x=567, y=42$

Run 2 : the other branch is executed
All program paths are now covered !

- Observations:

- Dynamic test generation extends static test generation with additional runtime information: it is more powerful
- The number of program paths can be infinite: may not terminate!
- Still, DART works well for small programs (1,000s LOC)
- Significantly improves code coverage vs. random testing

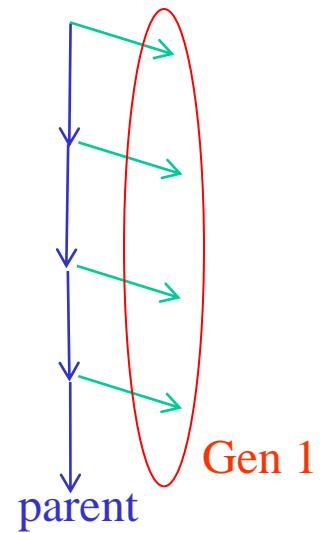
DART Implementations

- Defined by symbolic execution, constraint generation and solving
 - Languages: C, Java, x86, .NET,...
 - Theories: linear arith., bit-vectors, arrays, uninterpreted functions,...
 - Solvers: lp_solve, CVCLite, STP, Disolver, Z3,...
- Examples of tools/systems implementing DART:
 - EXE/EGT (Stanford): independent ['05-'06] closely related work
 - CUTE = same as first DART implementation done at Bell Labs
 - SAGE (CSE/MSR) for x86 binaries and merges it with "fuzz" testing for finding security bugs (*more later*)
 - PEX (MSR) for .NET binaries in conjunction with "parameterized-unit tests" for unit testing of .NET programs
 - YOGI (MSR) for checking the feasibility of program paths generated statically using a SLAM-like tool
 - Vigilante (MSR) for generating worm filters
 - BitScope (CMU/Berkeley) for malware analysis
 - CatchConv (Berkeley) focus on integer overflows
 - Splat (UCLA) focus on fast detection of buffer overflows
 - Apollo (MIT/IBM) for testing web applications

...and more!

Whitebox Fuzzing [NDSS'08]

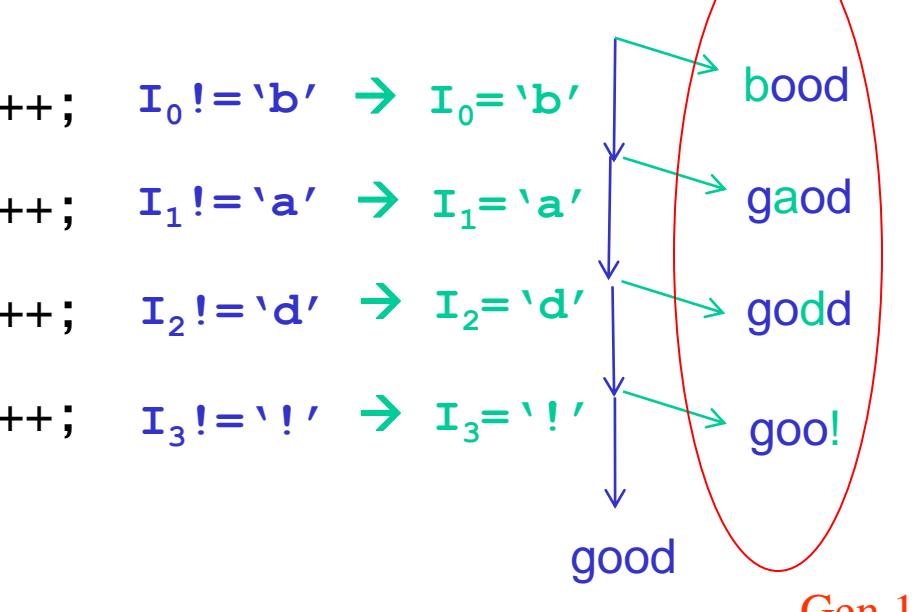
- Whitebox Fuzzing = "DART meets Fuzz"
- Apply DART to large applications (not unit)
- Start with a well-formed input (not random)
- Combine with a generational search (not DFS)
 - Negate 1-by-1 each constraint in a path constraint
 - Generate many children for each parent run
 - Challenge all the layers of the application sooner
 - Leverage expensive symbolic execution
- Search spaces are huge, the search is partial... yet effective at finding bugs !



Example

```
void top(char input[4])  
{  
    int cnt = 0;  
  
    if (input[0] == 'b') cnt++; I0 != 'b' → I0 = 'b'  
    if (input[1] == 'a') cnt++; I1 != 'a' → I1 = 'a'  
    if (input[2] == 'd') cnt++; I2 != 'd' → I2 = 'd'  
    if (input[3] == '!') cnt++; I3 != '!' → I3 = '!'  
  
    if (cnt >= 3) crash();  
}
```

Path constraint:

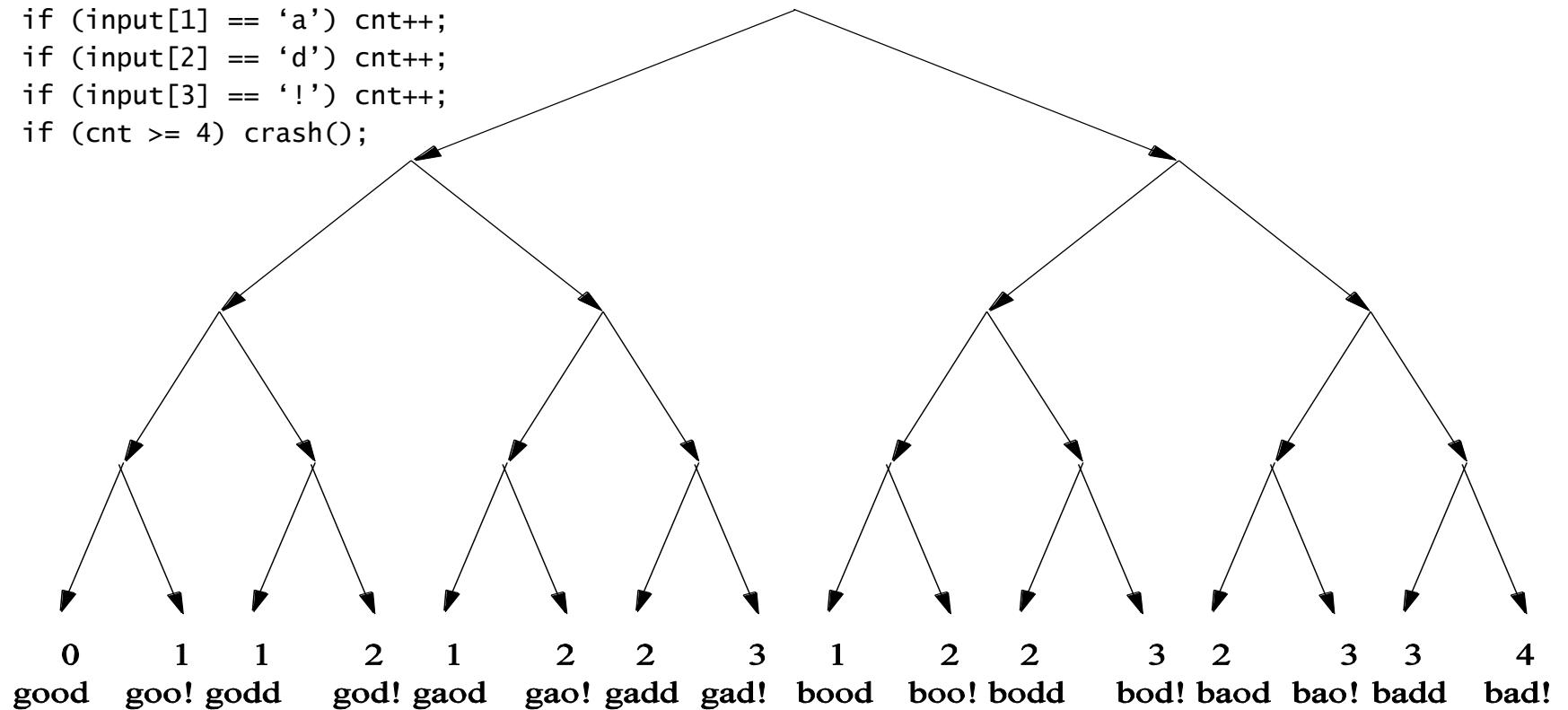


Negate each constraint in path constraint
Solve new constraint → new input

The Search Space

```
void top(char input[4])
{
    int cnt = 0;
    if (input[0] == 'b') cnt++;
    if (input[1] == 'a') cnt++;
    if (input[2] == 'd') cnt++;
    if (input[3] == '!') cnt++;
    if (cnt >= 4) crash();
}
```

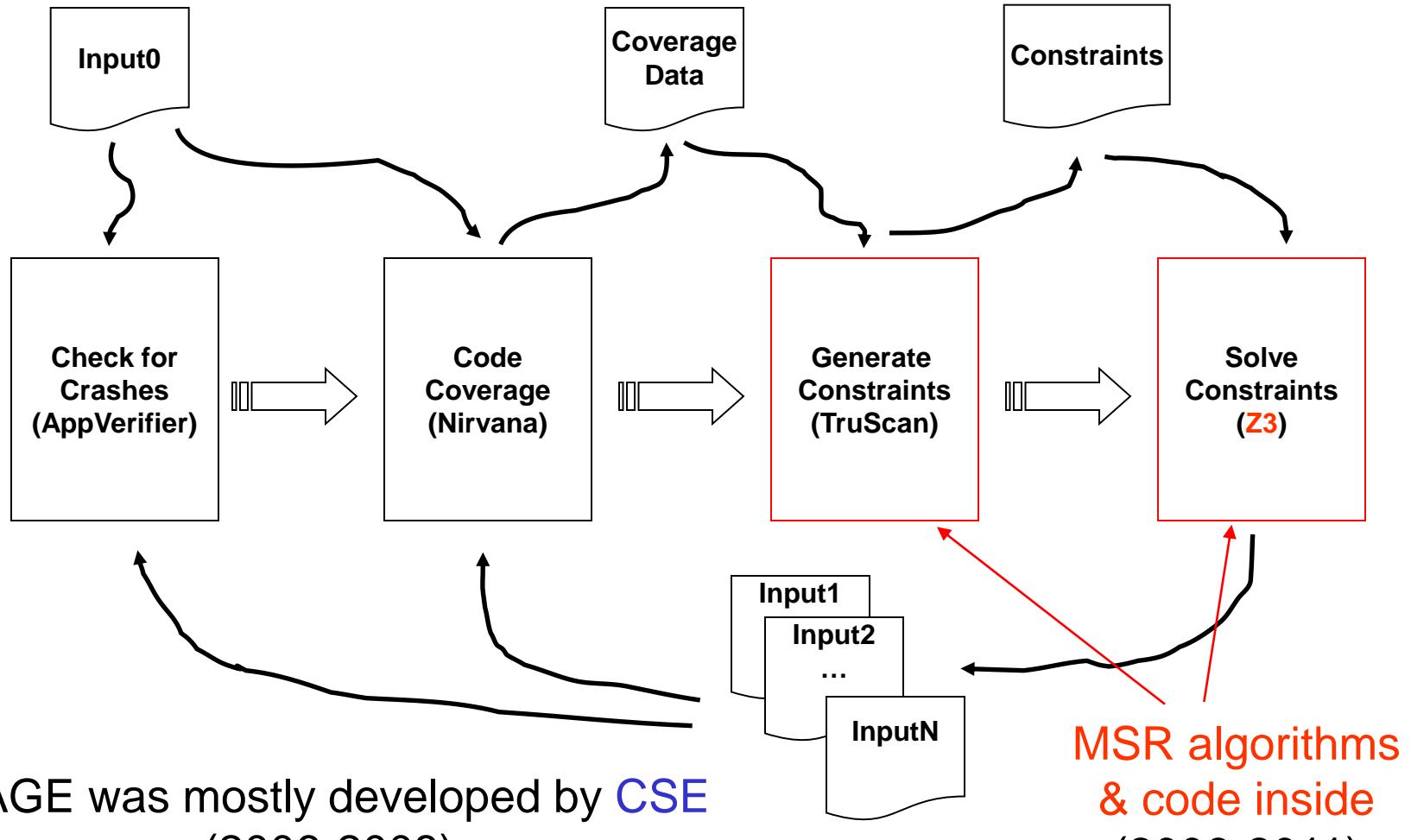
If symbolic execution is perfect
and search space is small,
this is **verification** !



SAGE (**Scalable** Automated Guided Execution)

- Generational search introduced in SAGE
- Performs symbolic execution of *x86* execution traces
 - Builds on Nirvana, iDNA and TruScan for *x86* analysis
 - Don't care about language or build process
 - Easy to test new applications, no interference possible
- Can analyse any *file*-reading Windows applications
- Several optimizations to handle *huge* execution traces
 - Constraint caching and common subexpression elimination
 - Unrelated constraint optimization
 - Constraint subsumption for constraints from input-bound loops
 - "Flip-count" limit (to prevent endless loop expansions)

SAGE Architecture



SAGE was mostly developed by CSE
(2006-2008)

MSR algorithms
& code inside
(2006-2011)

Some Experiments

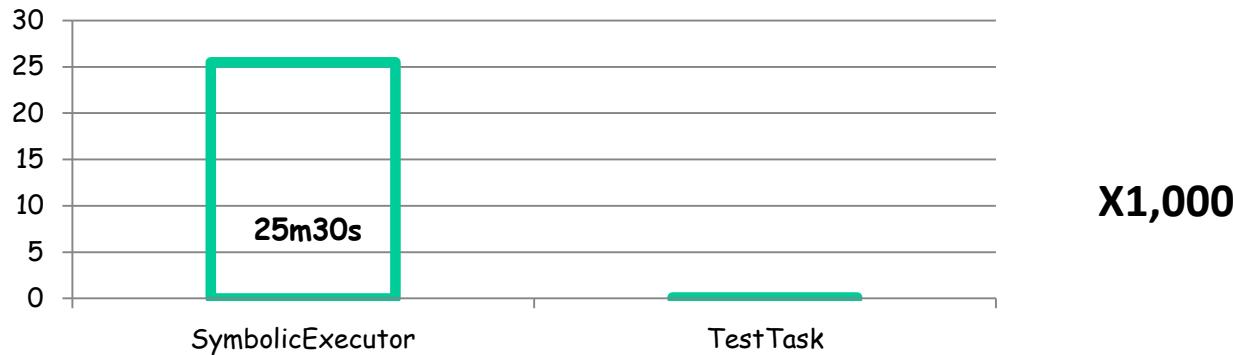
Most much (100x) bigger than ever tried before!

- Seven applications - 10 hours search each

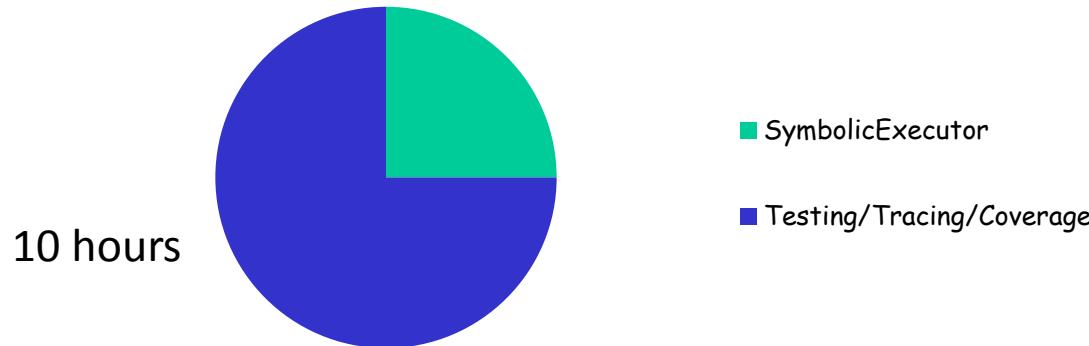
App Tested	#Tests	Mean Depth	Mean #Instr.	Mean Input Size
ANI	11468	178	2,066,087	5,400
Media1	6890	73	3,409,376	65,536
Media2	1045	1100	271,432,489	27,335
Media3	2266	608	54,644,652	30,833
Media4	909	883	133,685,240	22,209
Compressed File Format	1527	65	480,435	634
OfficeApp	3008	6502	923,731,248	45,064

Generational Search Leverages Symbolic Execution

- Each symbolic execution is expensive



- Yet, symbolic execution does not dominate search time



SAGE Results

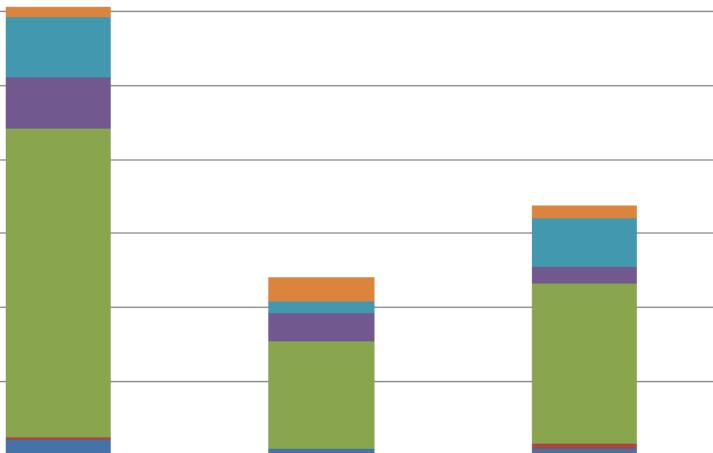
Since April'07 1st release: many new security bugs found
(missed by blackbox fuzzers, static analysis)

- Apps: image processors, media players, file decoders,...
- Bugs: Write A/Vs, Read A/Vs, Crashes,...
- Many triaged as "security critical, severity 1, priority 1"
(would trigger Microsoft security bulletin if known outside MS)
- Example: WEX Security team for Win7
 - Dedicated fuzzing lab with 100s machines →
 - 100s apps (deployed on 1billion+ computers)
 - ~1/3 of all fuzzing bugs found by SAGE !
- SAGE = gold medal at Fuzzing Olympics
organized by SWI at BlueHat'08 (Oct'08)
- Credit due to entire SAGE team + users !



WEX Fuzzing Lab Bug Yield for Win7

How fuzzing bugs found (2006-2009) :



Default
Blackbox
Fuzzer
+ Regression

SAGE is running 24/7 on 100s machines:
“the largest usage ever of any SMT solver”
N. Bjorner + L. de Moura (MSR, Z3 authors)

- 100s of apps, total number of fuzzing bugs is confidential
- But SAGE didn't exist in 2006
- Since 2007 (SAGE 1st release), ~1/3 bugs found by SAGE
- But SAGE currently deployed on only ~2/3 of those apps
- Normalizing the data by 2/3, SAGE found ~1/2 bugs
- SAGE was run last in the lab, so all SAGE bugs were missed by everything else!

SAGE Summary

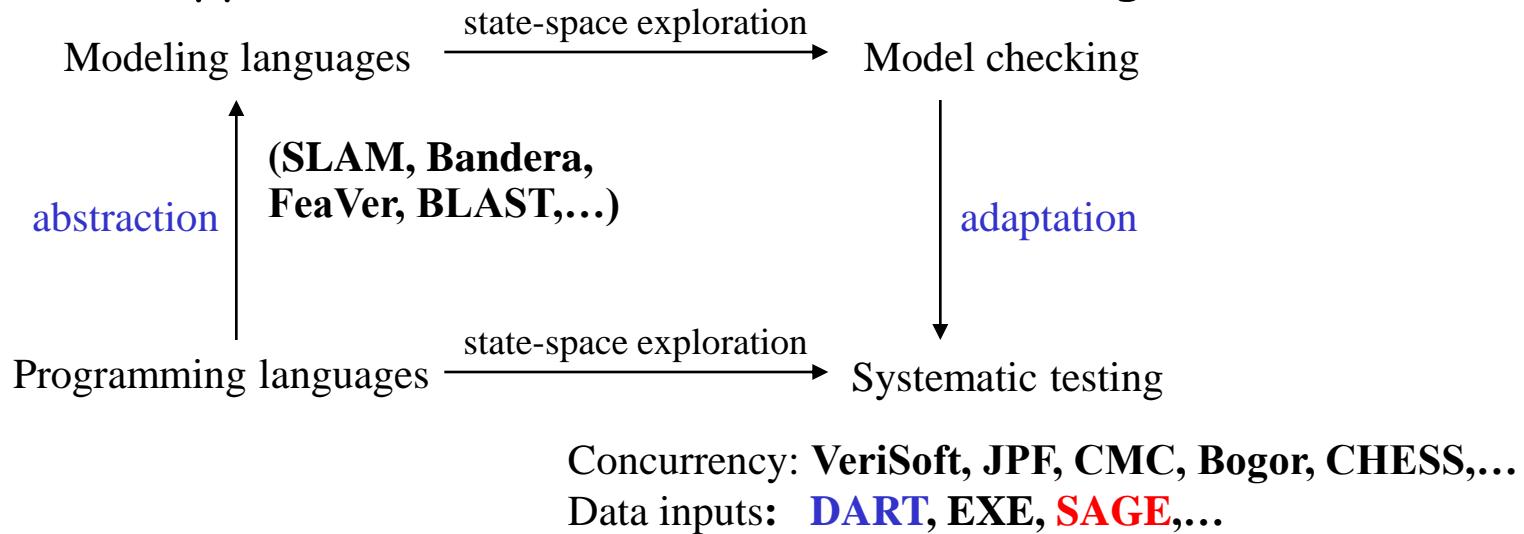
- SAGE is so effective at finding bugs that, for the first time, we face “bug triage” issues with dynamic test generation
- What makes it so effective?
 - Works on large applications (not unit test, like DART, EXE, etc.)
 - Can detect bugs due to problems across components
 - Fully automated (focus on file fuzzing)
 - Easy to deploy ($x86$ analysis - any language or build process !)
 - 1st tool for whole-program dynamic symbolic execution at $x86$ level
 - Now, used daily in various groups at Microsoft

More On the Research Behind SAGE

- How to recover from **imprecision** in symbolic exec.? PLDI'05, PLDI'11
 - Must under-approximations (**more later**)
 - How to **scale** symbolic exec. to billions of instructions? NDSS'08
 - Techniques to deal with large path constraints
 - How to check efficiently **many properties** together? EMSOFT'08
 - Active property checking
 - How to leverage **grammars** for **complex input formats**? PLDI'08
 - Lift input constraints to the level of symbolic terminals in an input grammar
 - How to deal with **path explosion**? POPL'07, TACAS'08, POPL'10, SAS'11
 - Symbolic test summaries (**more later**)
 - How to reason precisely about **pointers**? ISSTA'09
 - New memory models leveraging concrete memory addresses and regions
 - How to deal with **floating-point** instructions? ISSTA'10
 - Prove "non-interference" with memory accesses
 - How to deal with **input-dependent loops**? ISSTA'11
 - Automatic dynamic loop-invariant generation and summarization
- + research on **constraint solvers**

What Next? Towards “Verification”

- When can we safely stop testing?
 - When we know that there are no more bugs ! = “Verification”
 - “Testing can only prove the existence of bugs, not their absence.” [Dijkstra]
 - Unless it is exhaustive! This is the “model checking thesis”
 - “Model Checking” = exhaustive testing (state-space exploration)
 - Two main approaches to software model checking:



Exhaustive Testing ?

- Model checking is always “up to some bound”
 - Limited (often finite) input domain, for specific properties, under some environment assumptions
 - Ex: exhaustive testing of Win7 JPEG parser up to 1,000 input bytes
 - 8000 bits → 2^{8000} possibilities → if 1 test per sec, 2^{8000} secs
 - FYI, 15 billion years = 4730400000000000000 secs = 2^{60} secs!
 - MUST be “symbolic” ! ☺ How far can we go?
- Practical goals: (easier?)
 - Eradicate **all** remaining buffer overflows in **all** Windows parsers
 - Reduce costs & risks for Microsoft: when to stop fuzzing?
 - Increase costs & risks for Black Hats !
 - Many have probably moved to greener pastures already... (Ex: Adobe)
 - Ex: <5 security bulletins in all the SAGE-cleaned Win7 parsers
 - If noone can find bugs in P, P is observationally equivalent to “verified”!

How to Get There?

1. Identify and patch holes in symbolic execution + constraint solving
2. Tackle “path explosion” with compositional testing and symbolic test summaries [POPL’07, TACAS’08, POPL’10]

→ Fuzzing in the (Virtual) Cloud (Sagan)

- New centralized server collecting stats from **all** SAGE runs !
- Track results (bugs, concrete & symbolic test coverage), incompleteness (unhandled tainted x86 instructions, Z3 timeouts, divergences, etc.)
- Help troubleshooting (SAGE has 100+ options...)
- Tell us what works and what does not

Summaries Cure Search Redundancy

- Across different program paths



- Across different program versions
 - “Incremental Compositional Dynamic Test Generation” [SAS’11]
- Across different applications →
- Summaries avoid unnecessary work
- What if central server of summaries for **all** code?...

DLL	JPEG	GIF	ANI	All instr.
advapi32	✓	✓	✓	156442
clbeatq	✓	✓	✓	114240
comctl32		✓	✓	376620
gdi32	✓	✓	✓	81834
GdiPlus		✓	✓	476642
imm32	✓	✓	✓	26178
kernel32	✓	✓	✓	15958
lpk	✓	✓	✓	5389
msctf	✓	✓	✓	159228
msvert	✓	✓	✓	147640
ntdll	✓	✓	✓	207815
ole32	✓	✓		367226
oleaut32	✓	✓		148777
rpcrt4	✓	✓	✓	240231
shell32		✓	✓	-
shlwapi		✓	✓	73092
user32	✓	✓	✓	121223
usp10	✓	✓	✓	79990
uxtheme	✓	✓	✓	62276
WindowsCodecs	✓		✓	193415
JPEG (Total)				2127862
GIF (Total)				2860801
ANI (Total)				1753916

Part 2:

Tests from Validity Proofs

(Higher-Order Test Generation)

[PLDI'2011]

Why Dynamic Test Gen.? Most Precise !

Example:

```
int obscure(int x, int y) {  
    if (x==hash(y)) error();  
    return 0;  
}
```

Run 1 :- start with (random) $x=33, y=42$
- execute concretely and symbolically:
if ($33 \neq 567$) | if $(x \neq \text{hash}(y))$
constraint too complex
→ simplify it: $x \neq 567$
- solve: $x \neq 567 \rightarrow \text{solution: } x=567$
- new test input: $x=567, y=42$

Run 2 : the other branch is executed
All program paths are now covered !

Observations:

- “Unknown/complex symbolic expressions can be simplified using concrete runtime values” [DART, PLDI’05]
- Let’s call this step “concretization” (ex: $\text{hash}(y) \rightarrow 567$)
- Dynamic test generation extends static test generation with additional runtime information: it is more powerful

How often? When exactly? Why? → this work!

Unsound and Sound Concretization

- Concretization is not always sound

```
int foo(int x, int y) {  
    if (x==hash(y)) {  
        if (y==10) error();  
    } ...  
}
```

Run: $x=567, y=42$

pc: $x==567$ and $y!=10$

New pc: $x==567$ and $y==10$

New inputs: $x=567, y=10$

Divergence!

pc and new pc are unsound !

- Definition: A path constraint pc for a path w is **sound** if every input satisfying pc defines an execution following w

- Sound concretization: add **concretization constraints**

pc: $y==42$ and $x==567$ and $y!=10$ (sound)

New pc: $y==42$ and $x==567$ and $y==10$ (sound)

- Theorem: path constraint is now always sound. Is this better? No
 - Forces us to detect **all** sources of imprecision (expensive/impossible...)
 - Can prevent test generation and "good" divergences

Idea: Using Uninterpreted Functions

- Modeling imprecision with uninterpreted functions

```
int obscure(int x, int y) {      Run: x=33, y=42
    if (x==hash(y)) error();
    return 0;                      pc:      x != h(y)
}
New pc: x == h(y)
```

- How to generate tests?

- Is $(\exists x,y,h:) x=h(y)$ SAT? Yes, but so what? (ex: $x=y=0, h(0)=0$)
- Need universal quantification!

$(\forall h:) \exists x,y: x=h(y)$ is this first-order logic formula valid?

Yes. Solution (**strategy**): "fix y , set x to the value of $h(y)$ "

- Test generation from **validity proofs**! (not SAT models)
 - Necessary but not sufficient: what "value of $h(y)$?"

Need for Uninterpreted Function Samples

- Record I/O UF samples

```
int obscure(int x, int y) {  
    if (x==hash(y)) error();  
    return 0;  
}
```

Run: x=33, y=42

Record: 567 == h(42)

pc: x!=h(y)

- Use UF samples to interpret a validity proof/strategy

- "fix y, set x to the value of h(y)" → set y=42, x=567

- Or new pc: $(\forall h:) \exists x,y: (567=h(42)) \Rightarrow (x=h(y))$ is valid?

- Higher-order test generation =

- models imprecision using Uninterpreted Functions
- records UF samples as concrete input/output value pairs
- generates tests from validity proofs of FOL formulas

Key: a "higher-order" logic representation of path constraints

Higher-Order Test Generation is Powerful

- Theorem: HOTG is as powerful as sound concretization
 - Can simulate it (both UFs and UF samples are needed for this)
- Higher-Order Test Generation is more powerful

Ex 1: $(\forall h:) \exists x,y: h(x)=h(y)$ is valid (solution: set $x=y$)

Ex 2: $(\forall h:) \exists x,y: h(x)=h(y)+1$ is invalid

But $(\forall h:) \exists x,y: (h(0)=0 \wedge h(1)=1) \Rightarrow h(x)=h(y)+1$ is valid
(solution: set $x=1, y=0$)

Ex 3: Run: $x=567, y=42$

```
int foo(int x, int y) { pc: x==h(y) and y!=10
    if (x==hash(y)) {
        if (y==10) error();
    }
}
```

New pc: $(\forall h:) \exists x,y: (h(42)=567) \Rightarrow x=h(y) \wedge y=10$
is valid. Solution: set $y=10$, set $x=h(10)$

2-step test generation:

- run1 with $y=10, x=567$ to learn $h(10)=66$
- run2 with $y=10, x=66$!

Implementability Issues

- Tracking **all** sources of imprecision is problematic
 - Excel on a 45K input bytes executes 1 billion x86 instructions
 - Imprecision cannot always be represented by UFs
 - Unknown input/output signatures, nondeterminism,...
 - Capturing all input/output pairs can be very expensive
 - Limited support from current SMT solvers
 - $\exists X:\Phi(F,X)$ is valid iff $\forall X:\neg\Phi(F,X)$ is UNSAT
 - little support for generating+parsing UNSAT 'saturation' proofs
 - In practice, HOTG can be used for **targeted** reasoning about specific user-defined complex/unknown functions
-

Application: Lexers with Hash Functions

- Parsers with input lexers using hash functions for fast keyword recognition

Initially, for all language keywords: `addsym(keyword, hashtable)`
when parsing the input:

```
x=findsym(inputChunk, hashtable); // is inputChunk in hashtable?  
if (x==52) ... // how to get here?
```

- With higher-order test generation:

- Represent hashfunct by one UF h
- Capture all pairs $(\text{hashvalue}, h(\text{keyword}))$
- If " $h(\text{inputChunk}) == 52$ " and " $(52, h(\text{'while'}))$ " $\rightarrow \text{inputChunk} = \text{'while'}$
- This effectively **inverses** hashfunct **only for all keywords**
- Sufficient to drive executions through the lexer !
- See [PLDI'2011] for details

Conclusion: Impact of SAGE (In Numbers)

- 200+ machine-years
 - Runs in the largest dedicated fuzzing lab in the world
- 1 Billion+ constraints (lots of **tests from proofs !**)
 - Largest computational usage ever for any SMT solver
- 100s of apps, 100s of bugs (missed by everything else)
- Bug fixes shipped quietly (no MSRCs) to 1 Billion+ PCs
- Millions of dollars saved
 - for Microsoft + time/energy savings for the world
- DART, Whitebox fuzzing now adopted by (many) others (10s tools, 100s citations)

What Next? Towards Verification

- Tracking all(?) sources of incompleteness
 - Possibly using UFs and Higher-Order Test Generation
- Summaries (on-demand...) against path explosion
- How far can we go?
 - Reduce costs & risks for Microsoft: when to stop fuzzing?
 - Increase costs & risks for Black Hats (goal already achieved?)
- For history books !?



Acknowledgments

- SAGE is joint work with:
 - MSR: Ella Bounimova, David Molnar, ...
 - CSE: Michael Levin, Chris Marsh, Lei Fang, Stuart de Jong, ...
 - Interns Dennis Jeffries (06), David Molnar (07), Adam Kiezun (07), Bassem Elkarablieh (08), Marius Nita (08), Cindy Rubio-Gonzalez (08,09), Johannes Kinder (09), Daniel Luchaup (10), Nathan Rittenhouse (10), Mehdi Bouaziz (11), ...
- Thanks to the entire SAGE team and users !
 - Z3 (MSR): Nikolaj Bjorner, Leonardo de Moura, ...
 - Windows: Nick Bartmon, Eric Douglas, Dustin Duran, Elmar Langholz, Isaac Sheldon, Dave Weston, ...
 - TruScan support: Evan Tice, David Grant, ...
 - Office: Tom Gallagher, Eric Jarvi, Octavian Timofte, ...
 - SAGE users all across Microsoft!
- References: see <http://research.microsoft.com/users/pg>