

QUESTÃO 2 a)

$$u(x) = \sigma_0 e^{\sigma_1 x + \sigma_2 x^2}$$

$$v(x) = \ln(u(x))$$

Aplicando as propriedades de log:

$$\ln(u(x)) = \ln(\sigma_0 e^{\sigma_1 x + \sigma_2 x^2})$$

$$\boxed{\log_a(b \cdot c) = \log_a b + \log_a c}$$

$$\Rightarrow \ln(\sigma_0) + \ln(e^{\sigma_1 x + \sigma_2 x^2})$$

$$\boxed{\log_a b^c = c \cdot \log_a b}$$

$$\Rightarrow \ln(\sigma_0) + \sigma_1 x + \sigma_2 x^2 \cdot \overbrace{\ln(e)}^1$$

$$\Rightarrow \ln(\sigma_0) + \sigma_1 x + \sigma_2 x^2$$

Sobremos que $(x_i, y_i) \neq (x_i, \ln(y_i))$

Logo, podemos interpolar por Newton:

$$v(x) = \ln(y_0) + f[x_0, x_1](x - x_0) + f[x_0, x_1, x_2](x - x_0)(x - x_1)$$

$$\text{como } v(x) = \ln(u(x)) \Rightarrow$$

$$u(x) = e^{v(x)} = e^{\ln(y_0) + f[x_0, x_1](x - x_0) + f[x_0, x_1, x_2](x - x_0)(x - x_1)}$$

$$\boxed{u(x) = e}$$