

IFES Report

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ABSTRACT

1 Chapter 1

Structures and Cell Dimensions of Some Elements and Compounds

Element or compound	Structure	a , Å	c , Å
Al	fcc	4.04	
Be	hcp	2.27	3.59
Ca	fcc	5.56	

Figure 1

Unit Cell

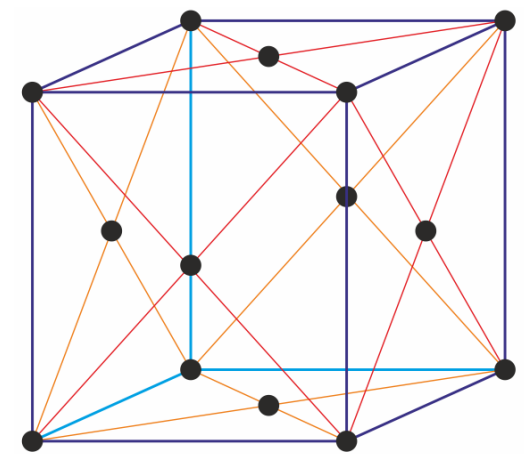


Figure 2: FCC-Lattice

Primitive Vectors

The three primitive vectors are

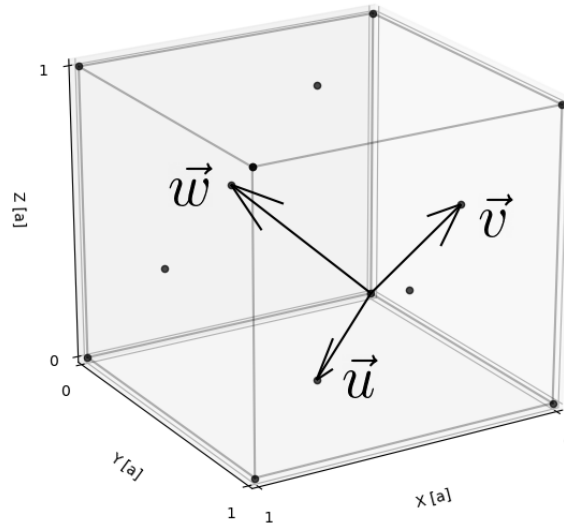


Figure 3: Primitive Vectors in a FCC-Lattice

$$\vec{u} = \frac{a}{2} \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \quad \vec{v} = \frac{a}{2} \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} \quad \vec{w} = \frac{a}{2} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$$

The volume can be calculated with the following formula

$$V_{PC} = |(\vec{u} \times \vec{v}) \cdot \vec{w}|$$

which equals (with $a = 5.56 \text{ \AA}$)

$$V_{PC} = \frac{a^3}{4} = 4.297 \cdot 10^{-30} m^3 = 4.297 \cdot 10^{-24} cm^3$$

Packaging Factor

The Packaging Factor can be calculated as the ratio between the volume of the atoms in the unit cell to the volume of the unit cell.

The volume of the unit cell can be calculated as:

$$V_{UC} = a^3$$

The unit cell contains 4 whole atoms

The relationship between the parameter a and the radius of the atomic sphere is given as:

$$r = \frac{\sqrt{2}}{4} a$$

$$APF = \frac{\pi}{3 \cdot \sqrt{2}} \approx 74\%$$

Density

The atomic mass of calcium is given as:

$$M_{Ca} = 40.078 \frac{g}{mol}$$

$$\rho = \frac{4}{N_A} \cdot \frac{M_{Ca}}{V_{UC}} = 1.55 \frac{g}{cm^3}$$

Planes

In the following the planes $P1 : (0\bar{3}2)$ and $P2 : (\bar{1}21)$ are drawn inside the unit cell. The Miller-Indices of the planes correspond to the following plane equations:

$$P1 : -\frac{1}{3}y + \frac{1}{2}z = 1$$

$$P2 : -x + \frac{1}{2}y + z = 1$$

With respect of the fact that all parallel planes have the same Miller-Indices the planes which were drawn are:

$$P1 : z = \frac{2}{3}y$$

$$P2 : z = x - \frac{1}{2}y$$

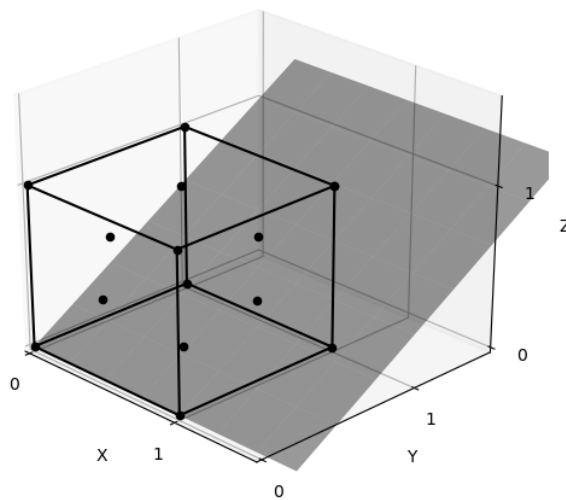


Figure 4: $(0\bar{3}2)$ -Plane in a FCC-Lattice

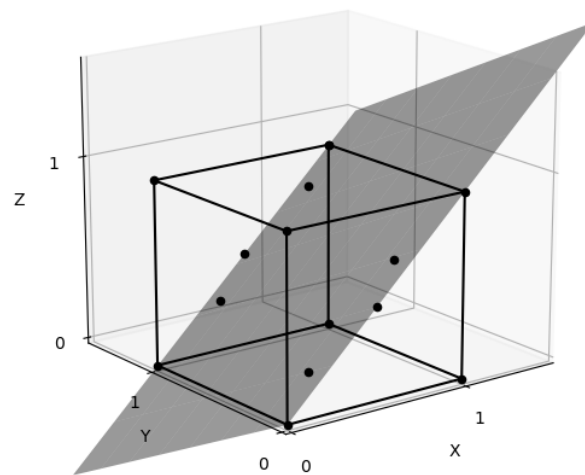


Figure 5: $(\bar{1}21)$ -Plane in a FCC-Lattice

Linear Density $[110]$

$$\lambda = \frac{2 \cdot m_{Ca}}{\sqrt{2}a}$$

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