Phaco meta analysis

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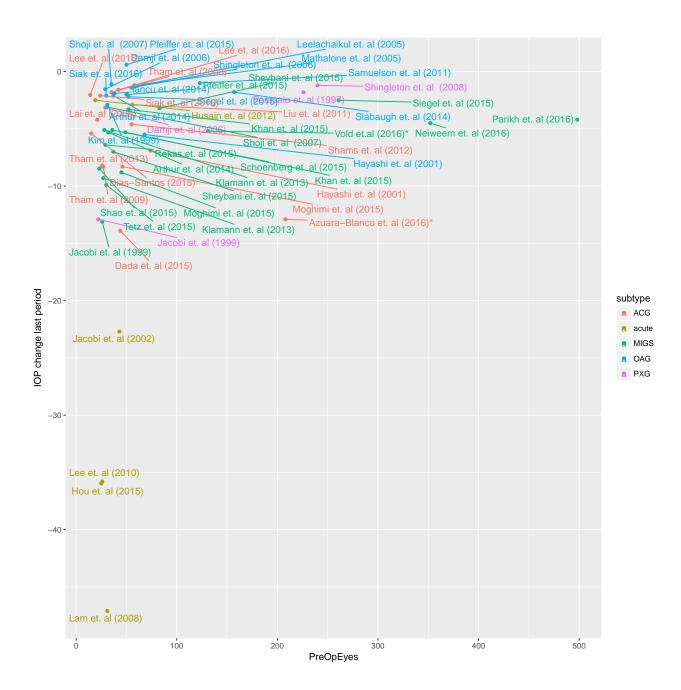
Load data

We load data from a CSV exported from Stata. The Mo variables refer to what happens after 6 months. The letter variables Z, AA etc. refer to what happens after 12 months. That's a bug in how Stata exports names of variables which start with a number - the columns were named 6mo... and 12mo....

```
library(tidyverse)
## Loading tidyverse: ggplot2
## Loading tidyverse: tibble
## Loading tidyverse: tidyr
## Loading tidyverse: readr
## Loading tidyverse: purrr
## Loading tidyverse: dplyr
## Conflicts with tidy packages -----
## filter(): dplyr, stats
## lag():
             dplyr, stats
library(meta)
## Loading 'meta' package (version 4.7-0).
## Type 'help("meta-package")' for a brief overview.
library(ggrepel)
setwd("~/Documents/phaco")
df <- read.csv("phaco.csv", na.strings='-')</pre>
df <- df %>% rename(SixMoEyes = MoEyes,
              SixMoIOPMean = MoIOPMean,
              SixMoIOPStdDev = MoIOPStdDev,
              SixMoAbsIOPChangeMean = MoAbsIOPChangeMean,
              SixMoAbsIOPChangeStdDev = MoAbsIOPChangeStdDev,
              OneYEyes = Y,
              OneYIOPMean = Z,
              OneYIOPStdDev = AA,
              OneYAbsIOPChangeMean = AB,
              OneYAbsIOPChangeStdDev = AC,
              LastPeriodAbsIOPChangeStdDev = LastPeriodAbsIOPChangeStd,
              LastPeriodEyes = LastPeriodofEyes
df <- df %>% mutate(subtype = as.factor(
  ifelse(acuteangleclosure == 'Y', 'acute',
         ifelse(MIGsYorN == 'Y', 'MIGS',
            ifelse(OAG > 50, 'OAG',
              ifelse(ACG > 50, 'ACG'.
                ifelse(PXG > 50, 'PXG', NA))))))
```

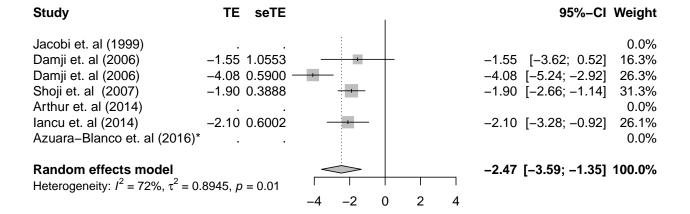
```
df <- df %>% mutate(study.name = paste0(Author, ' (', Year, ')', ifelse(WashOut == 'Y', '*', '')))
df <- df %>% filter(Author != "Mierzejewski et. al") # Exclude Mierzejewski studies, they're abstracts
df <- df %>% dplyr::arrange(Year, study.name)
```

Summary plot



Analysis without imputation

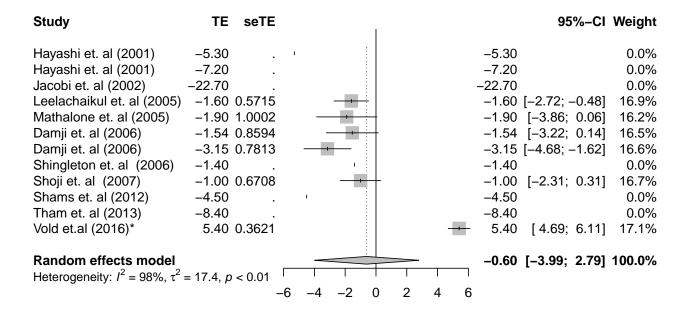
6 month follow-up



12-month follow up

Study	TE s	seTE		ı	95%-CI	Weight
Hayashi et. al (2001) Hayashi et. al (2001) Leelachaikul et. al (2005) Mathalone et. al (2005) Damji et. al (2006) Damji et. al (2006) Shoji et. al (2007) Samuelson et. al (2011) Tham et. al (2013) lancu et. al (2014)	-1.50 0.7 -1.67 0.8 -3.20 0.6 -0.70 0.4	7546 8009 6197 — 4596 3118		-	-4.30 -6.00 -1.40 [-2.38; -0.42] -1.50 [-2.98; -0.02] -1.67 [-3.24; -0.10] -3.20 [-4.41; -1.99] -0.70 [-1.60; 0.20] -1.00 [-1.61; -0.39] -9.60 -1.90 [-3.14; -0.66]	0.0% 0.0% 16.0% 10.3% 9.5% 12.9% 17.1% 21.6% 0.0% 12.7%
Slabaugh et. al (2014) Moghimi et. al (2015) Vold et.al (2016)*	-1.79 -8.30 6.20		ı		-1.79 -8.30 6.20	0.0% 0.0% 0.0%
Random effects model Heterogeneity: $I^2 = 54\%$, τ^2	= 0.3313, <i>j</i>	p = 0.04 -4	-2	0	 -1.53 [-2.12; -0.93]	100.0%

Last period



Subgroup analysis

Study	TE	seTE		1			95%-CI	Weight
subtype = ACG Hayashi et. al (2001) Shams et. al (2012) Tham et. al (2013) Random effects model Heterogeneity: Not applicable	-7.20 -4.50 -8.40		1			-7.20 -4.50 -8.40		0.0% 0.0% 0.0% 0.0%
subtype = acute Jacobi et. al (2002) Random effects model Heterogeneity: Not applicable	-22.70				-	-22.70		0.0% 0.0%
subtype = MIGS Vold et.al (2016)* Random effects model Heterogeneity: Not applicable		0.3621			#	5.40 5.40	[4.69; 6.11] [4.69; 6.11]	17.1% 17.1%
subtype = OAG Hayashi et. al (2001) Leelachaikul et. al (2005) Mathalone et. al (2005) Damji et. al (2006) Shingleton et. al (2006) Shoji et. al (2007) Random effects model Heterogeneity: $l^2 = 0\%$, $\tau^2 =$	-5.30 -1.60 (-1.90 (-1.54 (-1.40 (-1.00 (1.0002 0.8594 0.6708				-1.90 -1.54 -1.40 -1.00	[-2.72; -0.48] [-3.86; 0.06] [-3.22; 0.14] [-2.31; 0.31] [-2.16; -0.74]	0.0% 16.9% 16.2% 16.5% 0.0% 16.7% 66.3%
subtype = PXG Damji et. al (2006) Random effects model Heterogeneity: Not applicable	-3.15 (0.7813					[-4.68; -1.62] [-4.68; -1.62]	16.6% 16.6%
Random effects model Heterogeneity: $I^2 = 98\%$, $\tau^2 =$: 17.4, <i>p</i> ·	< 0.01 -6	-4 -2	0 2	4 6	-0.60	[-3.99; 2.79]	100.0%

There's too much missing data to anything useful with this data.

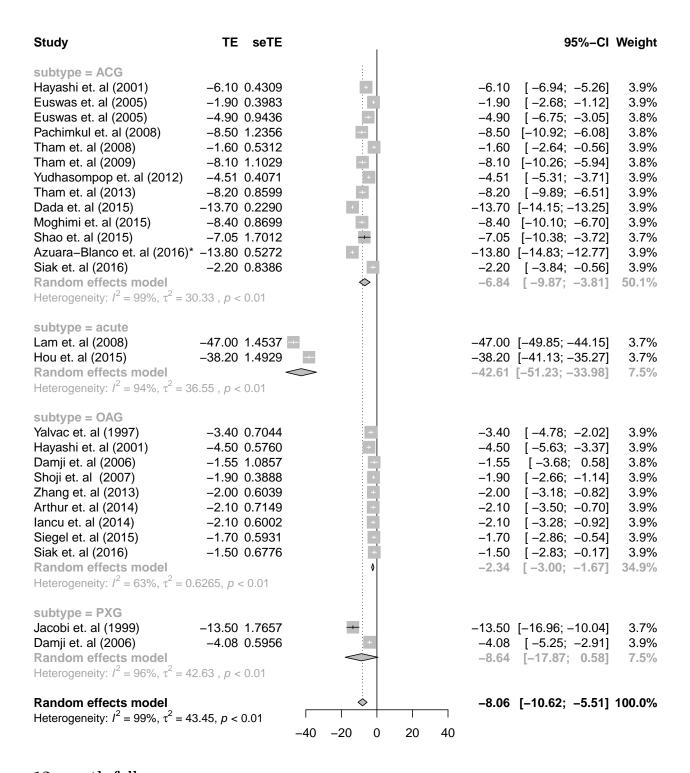
Analyses with imputation

I'm going to start by imputing on the basis of a low loss in follow up, high correlation between pre and post measures, and no change in relative IOP for those patients that were lost in follow up.

```
deltas <- list(lo=c(0, 0, 0), # Same outcome in the unseen arm.
               hi=c(5, 5, 5)) # Worse outcome in the unseen arm.
infer.mean.sem <- function(N.b, m.b, s.b, N.a, m.a, s.a, m.d, s.d, rho, m.delta) {
  # Infer the mean and SEM of the deviation in the metric measured before and after the intervention.
  \# N.b, m.b, s.b: N, mean, S.D. of metric before the intervention
  \# N.a, m.a, s.a: N, mean, S.D. of metric after the intervention
  # m.d, s.d: mean, S.D. of metric after intervention minus the metric before the intervention for
  # the group of survivors (N.a). Can be NA.
  # rho: Assumed correlation between before and after scores. Will be used to infer s.d. if s.d is NA
  # m.delta: the assumed mean delta between the m.b for the non-survivors minus the survivors.
  # Use equations in Section 6.1 of Schwarzer, Carpenter & Rucker (2014), Meta-Analysis with R
  m.d <- ifelse(is.na(m.d), m.a - m.b, m.d)
  s.d \leftarrow ifelse(is.na(s.d), sqrt(s.a ** 2 + s.b ** 2 - 2 * rho * s.a * s.b), s.d)
  # Now generalize the mean difference from the observed subset to the full dataset.
  # pi := unobserved portion
  pi = (N.b - N.a) / N.b
  m.d.full \leftarrow m.d + pi * m.delta
  # Let's assume that delta ~ N(m.delta, s.d)
  sem.d.full <- sqrt(1 + pi ** 2) * s.d / sqrt(N.a)
  return(data.frame(m=m.d.full, sem=sem.d.full))
}
library(testthat)
##
## Attaching package: 'testthat'
## The following object is masked from 'package:dplyr':
##
##
       matches
## The following object is masked from 'package:purrr':
##
##
       is_null
expect_equal(infer.mean.sem(25, 0, 1, 25, 0, 1, NA, NA, 0, 0)$sem, sqrt(2)/sqrt(25))
expect_equal(infer.mean.sem(25, 0, 1, 25, 0, 1, NA, NA, 0.5, 0)$sem, 1/sqrt(25))
expect_equal(infer.mean.sem(25, 0, 1, 25, 0, 1, NA, NA, 0, 0)$m, 0)
expect_equal(infer.mean.sem(25, 0, 1, 16, 0, 1, NA, NA, 0, 0)$sem, sqrt(1 + (9 / 25) ** 2) * sqrt(2)/sq
expect_equal(infer.mean.sem(25, -1, 1, 16, 2, 1, NA, NA, 0, 0)$m, 3)
expect_equal(infer.mean.sem(25, -1, 1, 16, 2, 1, NA, NA, 0, 0)$m, 3)
expect_equal(infer.mean.sem(20, 5, 1, 20, -5, 1, NA, NA, 0, 10)$m, -10)
expect_equal(infer.mean.sem(20, 5, 1, 10, -5, 1, NA, NA, 0, 20)$m, 0)
impute.df <- function(df, loss, corr, delta) {</pre>
  # Impute missing data using the bone-headed method of just assuming the mean effect of
  # - loss of follow-up
  # - correlation between Pre and Post IOP metrics
  # - delta between IOP of eyes that were lost in follow up and eyes that were ok.
  df <- df %>% mutate(imp.SixMoEyes = ifelse(is.na(SixMoEyes), round(loss[1] * PreOpEyes), SixMoEyes),
                      imp.OneYEyes = ifelse(is.na(OneYEyes), round(loss[2] * PreOpEyes), OneYEyes),
                      imp.LastPeriodEyes = ifelse(is.na(LastPeriodEyes), round(loss[3] * PreOpEyes), La
```

```
df_ <- with(df, infer.mean.sem(PreOpEyes, PreOpIOPMean, PreOpIOPStdDev,</pre>
                                   imp.SixMoEyes, SixMoIOPMean, SixMoIOPStdDev,
                                   SixMoAbsIOPChangeMean, SixMoAbsIOPChangeStdDev, corr[1], delta[1]))
  df$imp.SixMoIOPChangeMean <- df_$m</pre>
  df$imp.SixMoIOPChangeSEM <- df_$sem</pre>
  df_ <- with(df, infer.mean.sem(PreOpEyes, PreOpIOPMean, PreOpIOPStdDev,
                                   imp.OneYEyes, OneYIOPMean, OneYIOPStdDev,
                                   OneYAbsIOPChangeMean, OneYAbsIOPChangeStdDev, corr[2], delta[2]))
  df$imp.OneYIOPChangeMean <- df_$m</pre>
  df$imp.OneYIOPChangeSEM <- df_$sem</pre>
  df_ <- with(df, infer.mean.sem(PreOpEyes, PreOpIOPMean, PreOpIOPStdDev,
                                   imp.LastPeriodEyes, LastPeriodIOPMean, LastPeriodIOPStdDev,
                                   LastPeriodAbsIOPChangeMean, LastPeriodAbsIOPChangeStdDev, corr[3], del
  df$imp.LastPeriodIOPChangeMean <- df_$m</pre>
  df$imp.LastPeriodIOPChangeSEM <- df_$sem</pre>
  # Patch up NAs for std dev of medications.
  df$imp.RxPreOpStdDev <- ifelse(is.na(df$RxPreOpStdDev),</pre>
                                   .5* df$RxPreOpMean + .2,
                                   pmax(df$RxPreOpStdDev, .2))
  df$imp.RxPostOpStdDev <- ifelse(is.na(df$RxPostOpStdDev),</pre>
                                   .5* df$RxPostOpMean + .2,
                                   pmax(df$RxPostOpStdDev, .2))
 return(df)
# Q: are we dealing properly with loss of follow-up means?
# Verify where available if the before, after measurements, and changes match up.
df <- impute.df(df, losses[['lo']], corrs[['hi']], deltas[['lo']])</pre>
```

6 month follow-up



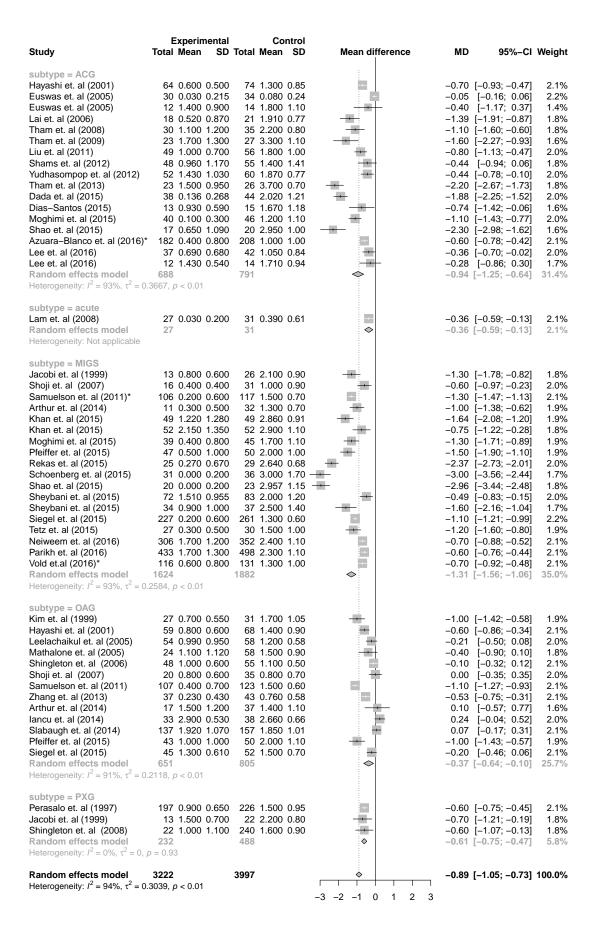
12-month follow up

forest(m, comb.fixed=FALSE) Study TE seTE 95%-CI Weight subtype = ACG Hayashi et. al (2001) -6.00 0.4663-6.00 [-6.91; -5.09] 3.9% Tham et. al (2008) -2.00 0.5492[-3.08; -0.92]3.9% -2.00Tham et. al (2009) -8.90 [-11.05; -6.75] -8.90 1.0963 3.8% Tham et. al (2013) -9.60 1.0032**-9.60** [**-11.57**; **-7.63**] 3.8% Dada et. al (2015) -13.90 0.2298 -13.90 [-14.35; -13.45] 3.9% Moghimi et. al (2015) -8.30 1.0532 -8.30 [-10.36; -6.24] 3.8% Azuara-Blanco et. al (2016)* -13.60 0.5312 **-13.60** [**-14.64**; **-12.56**] 3.9% Siak et. al (2016) -2.10 0.8596 -2.10 [-3.78; -0.42] 3.8% Random effects model -8.06 [-11.89; -4.23] 30.8% Heterogeneity: $I^2 = 99\%$, $\tau^2 = 29.93$, p < 0.01subtype = acute Lam et. al (2008) -47.60 1.4961 --- -47.60 [-50.53; -44.67] 3.7% Hou et. al (2015) -35.96 1.5274 -35.96 [-38.95; -32.97] 3.7% Random effects model -41.78 [-53.19; -30.38] 7.4% Heterogeneity: $I^2 = 97\%$, $\tau^2 = 65.46$, p < 0.01subtype = OAG Hayashi et. al (2001) $-4.30 \ 0.5355$ -4.30[-5.35; -3.25]3.9% Leelachaikul et. al (2005) -1.40 0.4990[-2.38; -0.42]3.9% -1.40Mathalone et. al (2005) -1.50 0.8166 -1.50[-3.10; 0.10]3.8% Damji et. al (2006) -1.67 0.8308-1.67[-3.30; -0.04]3.8% Shoji et. al (2007) -0.70 0.4613 -0.70[-1.60; 0.20] 3.9% Samuelson et. al (2011) -1.00 0.3131-1.00 [-1.61; -0.39] 3.9% Arthur et. al (2014) [-3.95; -1.05]-2.50 0.7378 -2.503.9% lancu et. al (2014) [-3.14; -0.66]-1.90 0.6327-1.903.9% Slabaugh et. al (2014) -1.79 0.2586-1.79 [-2.30; -1.28] 3.9% Pfeiffer et. al (2015) $-1.20 \ 0.5973$ -1.20 [-2.37; -0.03] 3.9% Siegel et. al (2015) -1.50 0.6122 -1.50 [-2.70; -0.30] 3.9% Siak et. al (2016) -2.10 0.7006 -2.10 [-3.47; -0.73] 3.9% Random effects model -1.76 [-2.30; -1.23] 46.5% Heterogeneity: $I^2 = 70\%$, $\tau^2 = 0.5679$, p < 0.01subtype = PXG Perasalo et. al (1997) -1.80 0.3617 -1.80 [-2.51; -1.09] 3.9% Jacobi et. al (1999) -13.60 1.8396 -13.60 [-17.21; -9.99] 3.6% Damji et. al (2006) -3.20 [-4.42; -1.98] 3.9% -3.20 0.6212 Shingleton et. al (2008) -1.60 0.5294-1.60 [-2.64; -0.56] 3.9% Random effects model -4.13 [-6.43; -1.83] 15.3% Heterogeneity: $I^2 = 93\%$, $\tau^2 = 4.722$, p < 0.01Random effects model **-7.16** [**-9.65**; **-4.68**] **100.0%** Heterogeneity: $I^2 = 99\%$, $\tau^2 = 41.09$, p < 0.01-40 -20 0 20 40 ## Last period m <- metagen(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, study.name, data=df %>% filter(!is.na(imp.LastPeriodIOPChangeSEM)), subset=!is.na(imp.LastPeriodIOPChangeSEM), byvar=subtype)

forest(m, comb.fixed=FALSE)

Study TE seTE	:	95%-CI Weight
subtype = ACG Hayashi et. al (2001)		-7.20 [-8.07; -6.33] 2.2% -4.20 [-6.80; -1.60] 2.1% -1.80 [-2.96; -0.64] 2.2% -8.30 [-10.62; -5.98] 2.2% -4.50 [-6.04; -2.96] 2.2% -8.40 [-10.87; -5.93] 2.1% -5.40 [-9.64; -1.16] 2.0% -12.90 [-13.97; -11.83] 2.2% -1.59 [-2.99; -0.19] 2.2% -2.04 [-4.24; 0.16] 2.2% -5.64 [-8.37; -2.91] 21.7%
subtype = acute Jacobi et. al (2002) -22.70 0.5312 Lam et. al (2008) -47.10 1.5576 Lee et. al (2010) -35.80 1.9890 Husain et. al (2012) -2.50 1.6276 Random effects model Heterogeneity: $I^2 = 99\%$, $\tau^2 = 245$, $\rho < 0.01$	5 🖽	-22.70 [-23.74; -21.66] 2.2% -47.10 [-50.15; -44.05] 2.1% -35.80 [-39.70; -31.90] 2.0% -2.50 [-5.69; 0.69] 2.1% -27.01 [-42.42; -11.60] 8.4%
Subtype = MIGS Jacobi et. al (1999) Shoji et. al (2007) Klamann et. al (2013) Arthur et. al (2014) Khan et. al (2015) Moghimi et. al (2015) Rekas et. al (2015) Schoenberg et. al (2015) Shao et. al (2015) Sheybani et. al (2015) Sheybani et. al (2015) Sheybani et. al (2015) Tetz et. al (2015) Parikh et. al (2015) Parikh et. al (2015) Parikh et. al (2015) Parikh et. al (2016) Parikh et. al (2016) Parikh et. al (2016) Random effects model Heterogeneity: I² = 98%, τ² = 13.58, p < 0.01		-13.10 [-17.49; -8.71] 2.0% -3.10 [-3.99; -2.21] 2.2% -5.10 [-7.43; -2.77] 2.2% -9.30 [-11.47; -7.13] 2.2% -5.30 [-8.69; -1.91] 2.1% -5.30 [-6.62; -3.98] 2.2% -3.30 [-5.20; -1.40] 2.2% -8.80 [-10.88; -6.72] 2.2% -2.00 [-2.99; -1.01] 2.2% -6.40 [-8.84; -3.96] 2.2% -5.10 [-7.02; -3.18] 2.2% -5.10 [-7.02; -3.18] 2.2% -3.20 [-5.08; -1.32] 2.2% -7.00 [-8.32; -5.68] 2.2% -7.00 [-8.32; -5.68] 2.2% -2.50 [-3.08; -1.92] 2.2% -9.90 [-11.75; -8.05] 2.2% -4.50 [-5.10; -3.90] 2.2% -4.20 [-4.70; -3.70] 2.2% 5.40 [4.69; 6.11] 2.2% -5.16 [-6.88; -3.44] 41.5%
subtype = OAG Kim et. al (1999) $-2.90 \ 0.6114$ Hayashi et. al (2001) $-5.30 \ 0.6304$ Leelachaikul et. al (2005) $-1.60 \ 0.5725$ Mathalone et. al (2006) $-1.54 \ 0.8726$ Shingleton et. al (2006) $-1.40 \ 0.4802$ Shoji et. al (2007) $-1.00 \ 0.7298$ Arthur et. al (2014) $-2.10 \ 1.2513$ Pfeiffer et. al (2015) $0.60 \ 0.6968$ Siegel et. al (2015) $-2.20 \ 0.6393$ Random effects model Heterogeneity: $I^2 = 81\%$, $\tau^2 = 2.045$, $p < 0.01$	+ 	-2.90 [-4.10; -1.70] 2.2% -5.30 [-6.54; -4.06] 2.2% -1.60 [-2.72; -0.48] 2.2% -1.90 [-4.17; 0.37] 2.2% -1.54 [-3.25; 0.17] 2.2% -1.40 [-2.34; -0.46] 2.2% -1.00 [-2.43; 0.43] 2.2% -2.10 [-4.55; 0.35] 2.2% 0.60 [-0.77; 1.97] 2.2% -2.20 [-3.45; -0.95] 2.2% -1.95 [-2.95; -0.94] 22.1%
subtype = PXG Jacobi et. al (1999) -12.90 2.1133 Damji et. al (2006) -3.15 0.7833 Shingleton et. al (2008) -1.20 1.7363 Random effects model Heterogeneity: $I^2 = 91\%$, $\tau^2 = 21.71$, $p < 0.01$ Random effects model Heterogeneity: $I^2 = 99\%$, $\tau^2 = 33.73$, $p < 0.01$	-	-12.90 [-17.04; -8.76] 2.0% -3.15 [-4.69; -1.61] 2.2% -1.20 [-4.60; 2.20] 2.1% -5.53 [-11.11; 0.05] 6.3% -6.45 [-8.16; -4.74] 100.0%

Meds



Multivariate model to integrate across time

Correlation between meds and drop in IOP

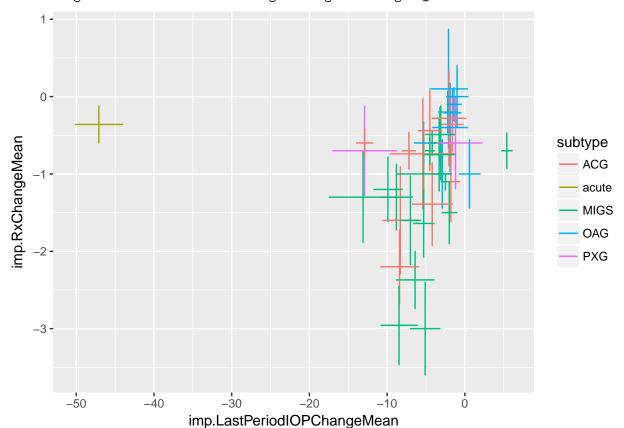
How is IOP drop related to change in meds? Two hypotheses:

- Those studies that see the largest IOP drops also have drop in meds, as doctors see that can use the newfound slack to decrease the number of meds people take
- The studies that see the largest IOP drops are those that don't change meds, because dropping meds would also increase IOP

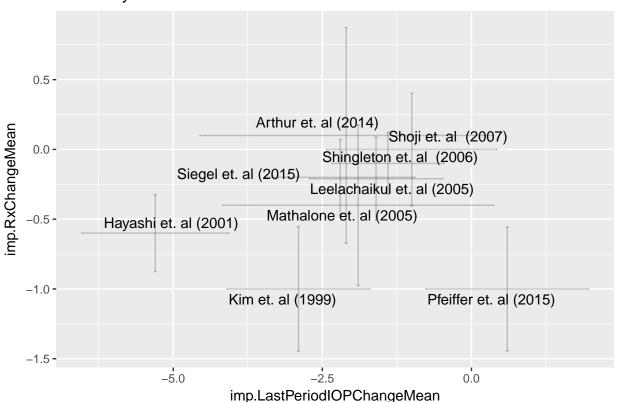
So which is it?

Warning: Removed 25 rows containing missing values (geom_errorbar).

Warning: Removed 25 rows containing missing values (geom_errorbarh).



OAG only



In fact, apart from the Pfeiffer et al. (2015) study, there is an apparent positive correlation between the two effect sizes: studies with larger drops in IOP also tend to see larger drops in Rx.

Mean +- SE correlation, without Pfeiffer et al

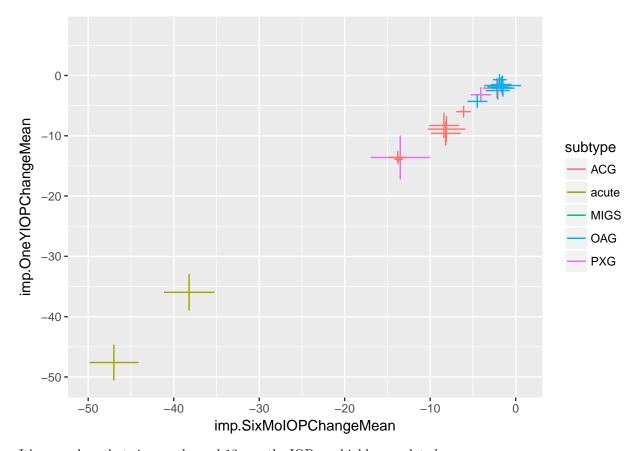
```
df_ <- df %>% filter(!(study.name %in% c("Pfeiffer et. al (2015)")), subtype=='OAG')
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                                                                                                                                                            draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, imp.LastPeriod
mean(drawn.corrs)
## [1] 0.4414706
sd(drawn.corrs)
## [1] 0.2087896
cat("Mean +- SE correlation, with Pfeiffer et al\n")
## Mean +- SE correlation, with Pfeiffer et al
df_ <- df %>% filter(subtype=='OAG')
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                                                                                                                                                        draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, im
mean(drawn.corrs)
## [1] 0.03711403
sd(drawn.corrs)
## [1] 0.2077679
```

Joint inferences

Measure the correlation between different outcomes (IOP at 6 months vs. 12 months).

```
## Warning: Removed 45 rows containing missing values (geom_errorbar).
```

^{##} Warning: Removed 45 rows containing missing values (geom_errorbarh).



It's very clear that six months and 12 months IOP are highly correlated.

```
df_ <- df %>% filter(subtype=='OAG')
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                                     draw.corr(imp.SixMoIOPChangeMean, imp.SixMoIOPChangeSEM, imp.OneYIOP
cat("Mean +- SE correlation, OAG only\n")
## Mean +- SE correlation, OAG only
print(mean(drawn.corrs))
## [1] 0.6212267
print(sd(drawn.corrs))
## [1] 0.2047245
df_{-} \leftarrow df
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                                     draw.corr(imp.SixMoIOPChangeMean, imp.SixMoIOPChangeSEM, imp.OneYIOP
cat("Mean +- SE correlation, All subtypes\n")
## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))
## [1] 0.9935905
print(sd(drawn.corrs))
## [1] 0.00318292
```

```
Let's repeat the same analysis, this time for 12 months vs. last period
df_ <- df %>% filter(subtype=='OAG')
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                          draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, imp.OneYIOP
cat("Mean +- SE correlation, OAG only\n")
## Mean +- SE correlation, OAG only
print(mean(drawn.corrs))
## [1] 0.6635031
print(sd(drawn.corrs))
## [1] 0.1582084
df <- df
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                          draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, imp.OneYIOP
cat("Mean +- SE correlation, All subtypes\n")
## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))
## [1] 0.9913575
print(sd(drawn.corrs))
## [1] 0.00297567
That's also really high! Finally, 6 months vs. last period
df_ <- df %>% filter(subtype=='OAG')
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                          draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, imp.SixMoIO
cat("Mean +- SE correlation, OAG only\n")
## Mean +- SE correlation, OAG only
print(mean(drawn.corrs))
## [1] 0.7329639
print(sd(drawn.corrs))
## [1] 0.1858193
df <- df
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                          draw.corr(imp.LastPeriodIOPChangeMean, imp.LastPeriodIOPChangeSEM, imp.SixMoIO
cat("Mean +- SE correlation, All subtypes\n")
## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))
## [1] 0.9932244
print(sd(drawn.corrs))
```

[1] 0.003924695

6 months is also highly correlated with the last period. Let's use mymeta to infer the effect size for both 6 months and 12 months together.

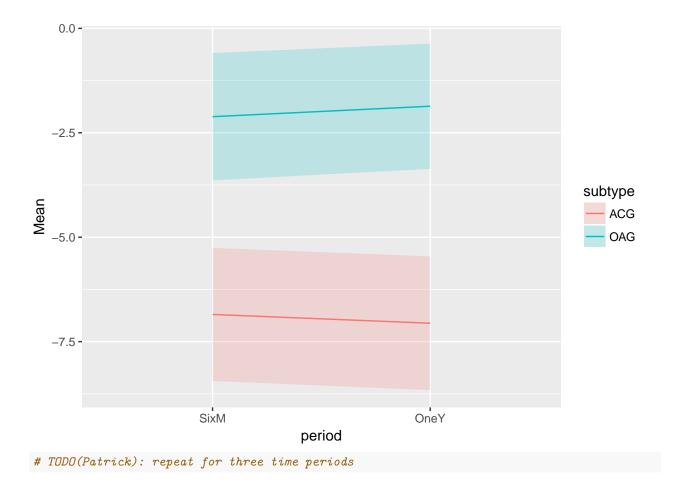
```
library(mvmeta)
## This is mvmeta 0.4.7. For an overview type: help('mvmeta-package').
get.correlation.matrices.bi <- function(x, y, assumed.rho) {</pre>
  S <- list()
  for(i in 1:length(x)) {
   x[i] <- ifelse(is.na(x[i]), y[i], x[i])
   y[i] <- ifelse(is.na(y[i]), x[i], y[i])</pre>
   S[[i]] \leftarrow matrix(c(x[i] ** 2, x[i] * y[i] * assumed.rho,
                       x[i] * y[i] * assumed.rho, y[i] ** 2), ncol=2)
 }
 S
}
df_ <- df %>% filter(!is.na(imp.SixMoIOPChangeSEM) | !is.na(imp.OneYIOPChangeSEM), subtype %in% c('OAG'
thefit <- mvmeta(cbind(imp.SixMoIOPChangeMean, imp.OneYIOPChangeMean) ~ subtype,
       S=get.correlation.matrices.bi(df_$imp.SixMoIOPChangeSEM, df_$imp.OneYIOPChangeSEM, .7),
       data=df_,
       method="reml")
summary(thefit)
## Call: mvmeta(formula = cbind(imp.SixMoIOPChangeMean, imp.OneYIOPChangeMean) ~
##
       subtype, S = get.correlation.matrices.bi(df_$imp.SixMoIOPChangeSEM,
       df_$imp.OneYIOPChangeSEM, 0.7), data = df_, method = "reml")
##
##
## Multivariate random-effects meta-regression
## Dimension: 2
## Estimation method: REML
##
## Fixed-effects coefficients
## imp.SixMoIOPChangeMean :
                                             z Pr(>|z|)
##
                Estimate Std. Error
                                                          95%ci.lb
                                                                    95%ci.ub
## (Intercept)
                 -6.8486
                                                  0.0000
                                                           -8.4406
                                                                      -5.2567
                              0.8122 - 8.4319
## subtypeOAG
                  4.7346
                              1.1244
                                       4.2108
                                                  0.0000
                                                            2.5308
                                                                      6.9384
##
## (Intercept)
## subtypeOAG
## imp.OneYIOPChangeMean :
##
                Estimate Std. Error
                                             z Pr(>|z|)
                                                          95%ci.lb
                                                                    95%ci.ub
## (Intercept)
                 -7.0589
                              0.8161 -8.6494
                                                  0.0000
                                                           -8.6584
                                                                      -5.4594
## subtypeOAG
                  5.1950
                              1.1184
                                       4.6452
                                                  0.0000
                                                            3.0031
                                                                      7.3870
##
## (Intercept)
## subtypeOAG
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Between-study random-effects (co)variance components
##
   Structure: General positive-definite
```

Corr

Std. Dev

##

```
## imp.SixMoIOPChangeMean
                              2.8086 imp.SixMoIOPChangeMean
## imp.OneYIOPChangeMean
                              2.7854
                                                       0.9946
## Multivariate Cochran Q-test for residual heterogeneity:
## Q = 1418.0961 (df = 38), p-value = 0.0000
## I-square statistic = 97.3%
## 27 studies, 42 observations, 4 fixed and 3 random-effects parameters
##
     logLik
                  AIC
                             BIC
## -77.5246 169.0491 180.5123
newdata <- data.frame(subtype=c('OAG', 'ACG'))</pre>
pred <- predict(thefit, newdata, se=TRUE)</pre>
newdata$SixMoIOPChangeMean <- pred$fit[,1]</pre>
newdata$OneYIOPChangeMean <- pred$fit[,2]</pre>
newdata$SixMoIOPChangeSEM <- pred$se[,1]</pre>
newdata$OneYIOPChangeSEM <- pred$se[,2]</pre>
library(reshape2)
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
       smiths
nd <- melt(newdata)</pre>
## Using subtype as id variables
nd$period <- substr(nd$variable, 0, 4)
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable))</pre>
nd
##
     subtype
                        variable
                                      value period metric
## 1
         OAG SixMoIOPChangeMean -2.1140397
                                              SixM
                                                      Mean
## 2
         ACG SixMoIOPChangeMean -6.8486463
                                              SixM
                                                      Mean
## 3
         OAG OneYIOPChangeMean -1.8638527
                                              OneY
                                                      Mean
## 4
         ACG OneYIOPChangeMean -7.0588996
                                              OneY
                                                      Mean
## 5
         OAG SixMoIOPChangeSEM 0.7775207
                                              SixM
                                                      eSEM
## 6
         ACG SixMoIOPChangeSEM 0.8122344
                                               SixM
                                                      eSEM
## 7
         OAG
               OneYIOPChangeSEM 0.7646785
                                               OneY
                                                      eSEM
## 8
         ACG
               OneYIOPChangeSEM 0.8161110
                                               OneY
                                                      eSEM
df_ <- dcast(nd, formula = subtype + period ~ metric)</pre>
df_$period <- relevel(as.factor(df_$period), ref='SixM')</pre>
ggplot(df_, aes(x=period,
                y=Mean,
                ymin=Mean - 1.96*eSEM,
                ymax=Mean + 1.96*eSEM,
                group=subtype,
                fill=subtype)) + geom_ribbon(alpha=.2) + geom_line(aes(color=subtype))
```



Impute under every scenario

Look at what happens depending on how we impute the data.

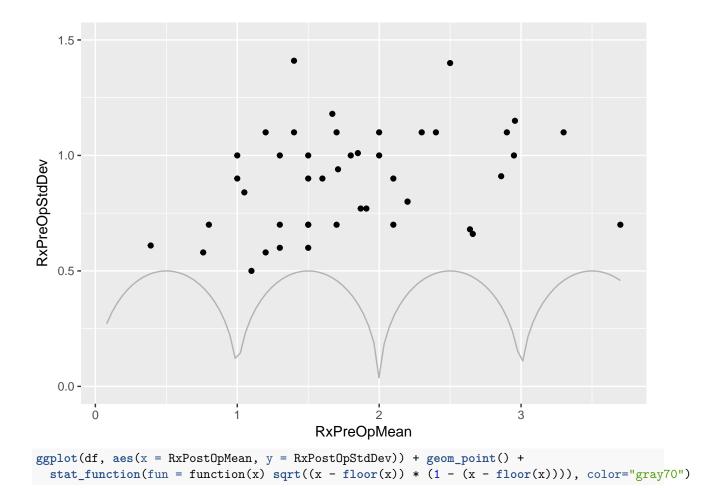
```
# TODO(Patrick): Fix this.
results <- list()
for(loss in c('lo', 'hi')) {
         for(corr in c('lo', 'hi')) {
                  for(delta in c('lo', 'hi')) {
                           df <- impute.df(df, losses[[loss]], corrs[[corr]], deltas[[delta]])</pre>
                            s <- (metagen(imp.SixMoIOPChangeMean,</pre>
                                                                                       imp.SixMoIOPChangeSEM,
                                                                                       study.name,
                                                                                       data=df,
                                                                                       subset=!is.na(imp.SixMoIOPChangeSEM) & MIGsYorN == 'N',
                                                                                      byvar=subtype))
                           row <- data.frame(loss=loss, corr=corr, delta=delta, m=s$TE.random.w, ci.lo=s$upper.random.w, ci.lo=s$
                           results[[length(results) + 1]] <- row</pre>
                            s <- (metagen(imp.OneYIOPChangeMean,</pre>
                                                                                       imp.OneYIOPChangeSEM,
                                                                                       study.name,
                                                                                       data=df,
```

```
subset=!is.na(imp.OneYIOPChangeSEM) & MIGsYorN == 'N',
                                                                                             byvar=subtype))
                             row <- data.frame(loss=loss, corr=corr, delta=delta, m=s$TE.random.w, ci.lo=s$upper.random.w, ci.lo=s$
                            results[[length(results) + 1]] <- row
                             s <- (metagen(imp.LastPeriodIOPChangeMean,</pre>
                                                                                             imp.LastPeriodIOPChangeSEM,
                                                                                             study.name,
                                                                                             data=df,
                                                                                             subset=!is.na(imp.LastPeriodIOPChangeSEM) & MIGsYorN == 'N',
                                                                                             byvar=subtype))
                            row <- data.frame(loss=loss, corr=corr, delta=delta, m=s$TE.random.w, ci.lo=s$upper.random.w, ci.lo=s$
                            results[[length(results) + 1]] <- row</pre>
         }
}
all.df <- do.call(rbind, results)</pre>
p <- position_dodge(width=1)</pre>
ggplot(all.df, aes(x=period, y = m, ymin=ci.lo, ymax=ci.hi, color=subtype)) + geom_pointrange(position=
summary(metagen(imp.LastPeriodIOPChangeMean,
                                                               imp.LastPeriodIOPChangeSEM,
                                                               study.name,
                                                               data=df,
                                                               subset=!is.na(imp.LastPeriodIOPChangeSEM) & MIGsYorN == 'N',
                                                               byvar=subtype))
summary(metagen(imp.LastPeriodIOPChangeMean,
                                                               imp.LastPeriodIOPChangeSEM,
                                                               study.name,
                                                               data=df,
                                                               subset=!is.na(imp.LastPeriodIOPChangeSEM) & MIGsYorN == 'N',
                                                               byvar=subtype))
```

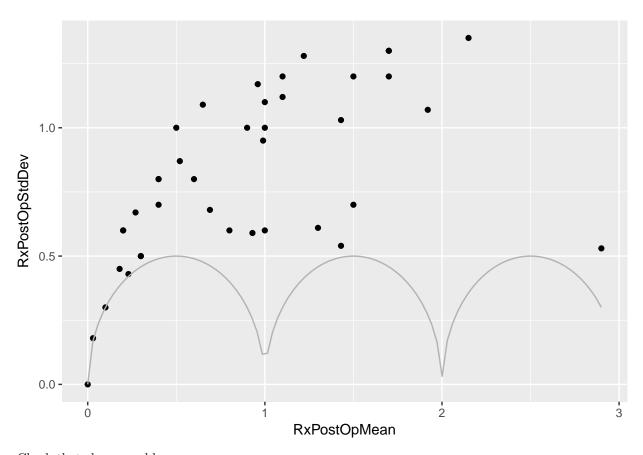
Sanity check data graphically

Check the relationship between RxPreOpMean and s.d.

```
ggplot(df, aes(x = RxPreOpMean, y = RxPreOpStdDev)) +
  geom_point() +
  coord_cartesian(y=c(0, 1.5)) +
  stat_function(fun = function(x) sqrt((x - floor(x)) * (1 - (x - floor(x)))), color="gray70")
## Warning: Removed 19 rows containing missing values (geom_point).
```



Warning: Removed 24 rows containing missing values (geom_point).



Check that changes add up.

```
ggplot(df, aes(x = SixMoIOPMean - PreOpIOPMean, y = SixMoAbsIOPChangeMean, label = study.name)) +
geom_point() +
coord_cartesian(xlim=c(-10, 0)) +
geom_abline() +
geom_text_repel()
```

- ## Warning: Removed 58 rows containing missing values (geom_point).
- ## Warning: Removed 58 rows containing missing values (geom_text_repel).

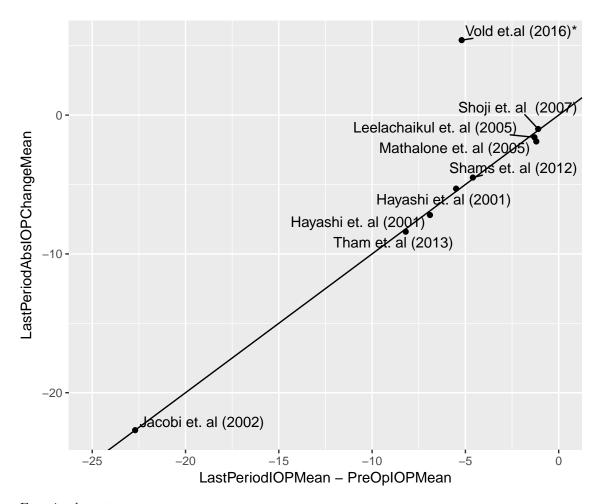
```
-2 -
                                                    lancu et. al (2014)
                                                   Yalvac et. al (1997)
SixMoAbsIOPChangeMean
                                     Hayashi et. al (2001)
                                       Yudhasompop et. al (2012)
                               Hayashi et. al (2001)
    -6 -
    −8 -
                           -7.5
        -10.0
                                              -5.0
                                                                -2.5
                                                                                   0.0
                              SixMolOPMean - PreOplOPMean
ggplot(df, aes(x = OneYIOPMean - PreOpIOPMean, y = OneYAbsIOPChangeMean, label = study.name)) +
  geom_point() +
  coord_cartesian(xlim=c(-10, 0)) +
  geom_abline() +
  geom_text_repel()
## Warning: Removed 55 rows containing missing values (geom_point).
```

Warning: Removed 55 rows containing missing values (geom_text_repel).

```
Vold et.al (2016)*
      5 -
OneYAbsIOPChangeMean
      0 -
                                                                          Shoji et. al (2007)
                                                        Leelachaikul et. al (2005)
                                          Mathalone et. al (2005)
                                                lancu et. al (2014)
                                                                       Stabaugh et. al (2014)
                                           Hayashi et. al (2001)
     -5 -
                                  Hayashi et al (2001)
            Moghimi et. al (2015)
                              -7.5
          -10.0
                                                  -5.0
                                                                      -2.5
                                                                                          0.0
                                 OneYIOPMean - PreOpIOPMean
```

```
ggplot(df, aes(x = LastPeriodIOPMean - PreOpIOPMean, y = LastPeriodAbsIOPChangeMean, label = study.name
  geom_point() +
  coord_cartesian(xlim=c(-25, 0)) +
  geom_abline() +
  geom_text_repel()
```

- ## Warning: Removed 55 rows containing missing values (geom_point).
- ## Warning: Removed 55 rows containing missing values (geom_text_repel).

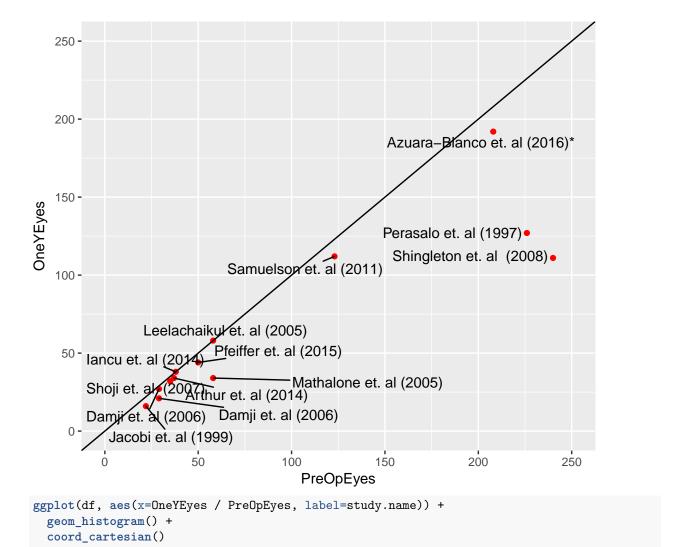


Examine loss at one year.

```
ggplot(df, aes(x=PreOpEyes, y=OneYEyes, label=study.name)) +
  geom_point(color="red") +
  geom_abline() +
  geom_text_repel() + coord_cartesian(xlim=c(0, 250), ylim=c(0, 250))
```

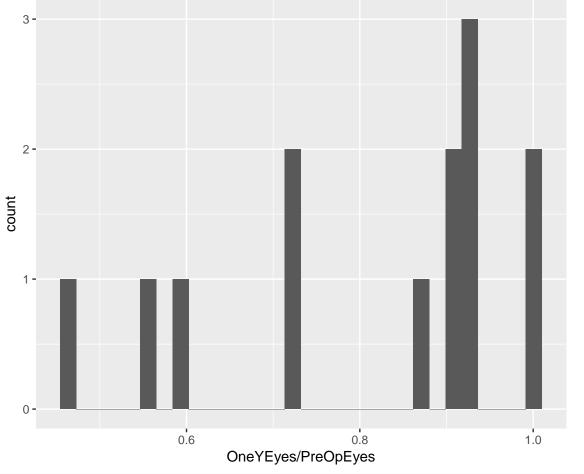
```
## Warning: Removed 51 rows containing missing values (geom_point).
```

Warning: Removed 51 rows containing missing values (geom_text_repel).



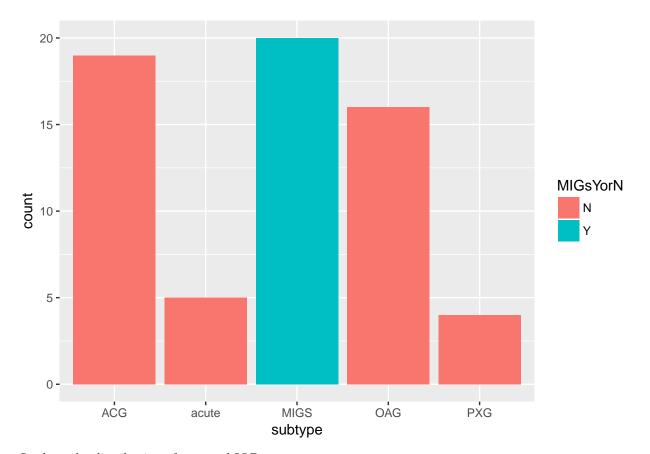
```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

^{##} Warning: Removed 51 rows containing non-finite values (stat_bin).



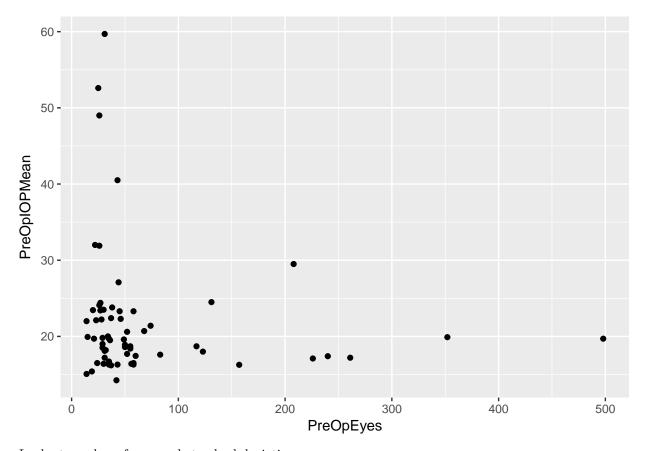
ggplot(df, aes(x=subtype, fill=MIGsYorN)) + geom_histogram(stat="count", position = 'dodge')

Warning: Ignoring unknown parameters: binwidth, bins, pad



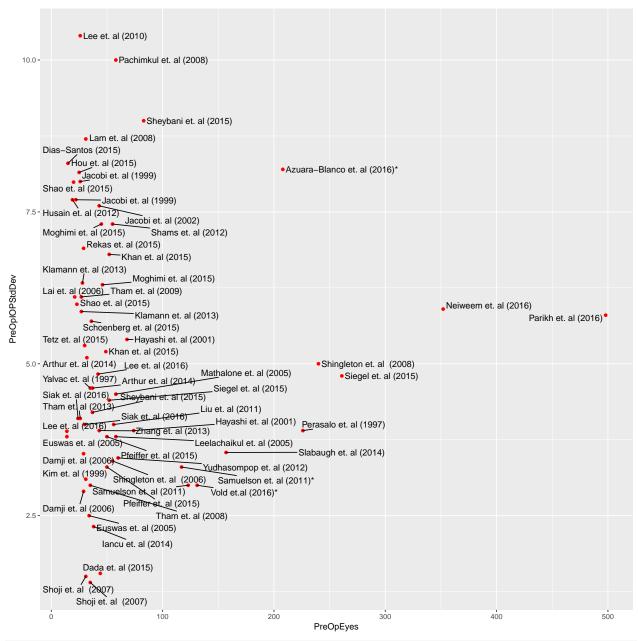
Look at the distribution of eyes and IOP means.

ggplot(df, aes(x=PreOpEyes, y=PreOpIOPMean)) + geom_point()



Look at number of eyes and standard deviation.

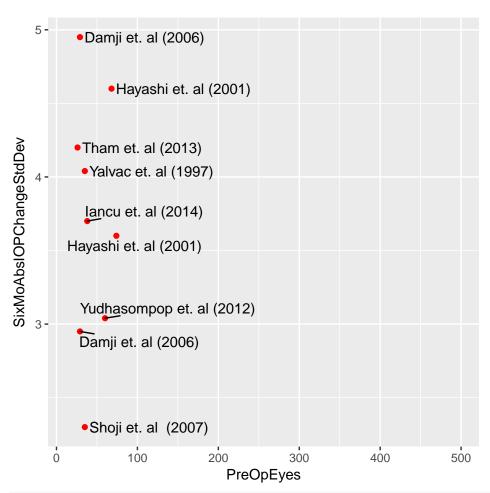
ggplot(df, aes(x=PreOpEyes, y=PreOpIOPStdDev, label=study.name)) + geom_point(color="red") + geom_text_



ggplot(df, aes(x=PreOpEyes, y=SixMoAbsIOPChangeStdDev, label=study.name)) + geom_point(color="red") + g

Warning: Removed 55 rows containing missing values (geom_point).

Warning: Removed 55 rows containing missing values (geom_text_repel).



```
ggplot(df, aes(x=PreOpEyes, y=SixMoIOPStdDev, label=study.name)) + geom_point(color="red") + geom_text_:
## Warning: Removed 41 rows containing missing values (geom_point).
```

Warning: Removed 41 rows containing missing values (geom_text_repel).

```
Pachimkul et. al (2008)
  6 -
        •Shao et. al (2015)
  5 -
SixMolOPStdDev
      Hayashi et. al (2001)
                                Azuara-Blanco et. al (2016)*
        Moghimi et. al (2015)
               al (2009) Siegel et. al (2015)
           Siak et. al (2016) rthur et. al (2014)
              Lam et. al (2008)Zhang et. al (2013)
        Hou et. al (2018) Ivac et. al (1997)
     Tham et. al (2008) Hayashi et. al (2001)
                  Shoji et. al (2012)
          Hancu et. al (2014)
        Siak et. al (2016) uswas et. al (2005)
     Jacobi et. al (1999)
                          Euswas et. al (2005)
             Dada et. al (2015)
                              200
                 100
                                                        400
                                                                     500
                                 PreOpEyes
```

```
ggplot(df, aes(x=PreOpEyes, y=OneYAbsIOPChangeStdDev, label=study.name)) + geom_point(color="red") + geom_
## Warning: Removed 51 rows containing missing values (geom_point).
```

```
7 -
             •Moghimi et. al (2015)
    6 -
OneYAbsIOPChangeStdDev
          •Tham et. al (2013)
        Mathalone et. al (2005)
                Hayashi et. al (2001)
       lancu et. al (2014)
                          Leelachaikul et. al (2005)
           Hayashi et. al (2001)/old et.al (2016)*
       Damji et. al (2006)
                           -Samuelson et. al (2011)
    3 - Damji et. al (2006)
                             Slabaugh et. al (2014)

    Shoji et. al (2007)

                   100
       0
                                 200
                                               300
                                                             400
                                                                           500
                                    PreOpEyes
```

```
ggplot(df, aes(x=PreOpEyes, y=OneYIOPStdDev, label=study.name)) + geom_point(color="red") + geom_text_r
## Warning: Removed 41 rows containing missing values (geom_point).
## Warning: Removed 41 rows containing missing values (geom_text_repel).
```

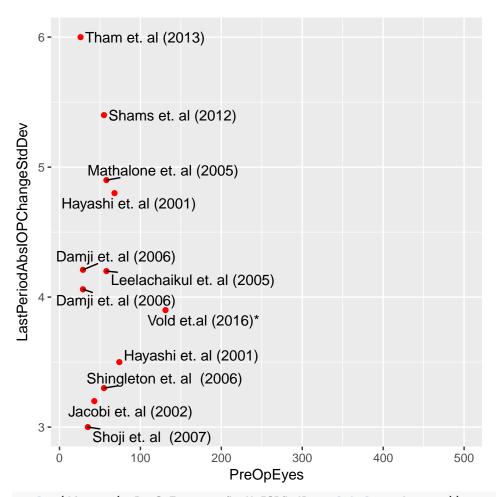
```
Shingleton et. al (2008)
                ·Hayashi et. al (2001)
            Moghimi et. al (2015)
      Pfeiffer et al (2015)
                    Hayashi et. al (2001)
                                Slabaugh et. al (2014)
      Siak et. al (2016)
      Siegel et. al (2015) Azuara-Blanco et. al (2016)*
Arthur et. al (2016)*
OneYIOPStdDev
     Hou et. al (2015) et. al (2009) Perasalo et. al (1997)
                               Shoji et. al (2007)
          Lam et. al (2008)
Wathalone et. al (2005)
              et. al (2016) eelachaikul et. al (2005)
       lancu et. al (2014)
   2 -
         •Jacobi et. al (1999)

    Dada et. al (2015)

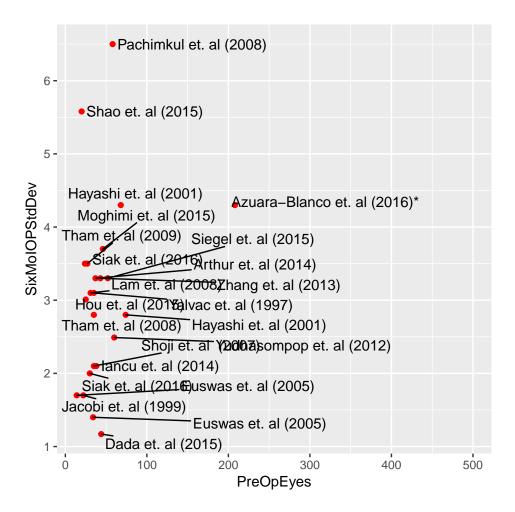
                                 200
                   100
                                               300
                                                             400
                                                                            500
                                    PreOpEyes
```

ggplot(df, aes(x=PreOpEyes, y=LastPeriodAbsIOPChangeStdDev, label=study.name)) + geom_point(color="red"
Warning: Removed 52 rows containing missing values (geom_point).

Warning: Removed 52 rows containing missing values (geom_text_repel).



```
ggplot(df, aes(x=PreOpEyes, y=SixMoIOPStdDev, label=study.name)) + geom_point(color="red") + geom_text_
## Warning: Removed 41 rows containing missing values (geom_point).
```



Some notes on the analysis and the studies

- None of the studies are randomized, except the EAGLE one (2016) Azuara-Bianco et al., Lancet
- There's no control arm in any of the studies
- Main outcome is IOP drop
 - The older studies are phaco + glaucoma surgery
 - The new ones are phaco + MIGS minimally invasive glaucoma surgery

Slicings to look at

- MIGS
 - Don't look at MIGS
- Type of glaucoma:
 - OAG -> open angle glaucoma ** ~2-3mm **
 - NTG -> normal tension glaucoma?
 - ACG -> angle closure glaucoma ** known to be effective **
 - PXG: pseudo-exfoliation?

Dimensions to look at - meta-regression

- Initial severity (IOP before)
- Size of study (number of eyes)
- Year

Different outcomes

- Primary is IOP drop
 - time points 6 mo, 12 mo, (last time point)
 - most important is 12 months
- Number of meds
 - Huge confound, because it's controlled by the doctor
 - Meds themselves decrease the IOP
 - A handful of studies use washout pre and post (measuring the IOP without meds) to undo the confounding
 - * EAGLE, Samuelson studies have washout
 - * Lack of washout will have a tendency to decrease the apparent effectiveness of the studies
 - One med $\sim = 20\%$ decrease in IOP
 - One med := decrease in quality of life
 - RxPostOpMean is at the same time as LastPeriod
- (visual acuity but it's kind of obvious)

Additional analyses to perform

- Funnel plot for small / medium large studies
- Deal appropriately with multiple arms of same study, e.g. Damji et al., Merz...
- Deal with three forms of lossiness:
 - Absolutes reported, relatives needed
 - Can patch up using estimate of rho sqrt(s_1 ** 2 + s 2 ** 2 2 * rho * s 1 * s 2)
 - Try rho = 0, rho = 0.5
 - Loss of follow-up
 - Can deal with by assuming that follow up is either MCAR or worse than MCAR
 - Try mean_delta = 0, mean_delta = -3, mean_delta = -5
 - Not all metrics reported for every study
 - Use mvmeta