# Phaco meta analysis

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# Analysis of full dataset

# Main analysis: $\geq 12$ month follow up

Study	ΔΙΟΡ	SE	eyes	I	95%-CI
subtype = ACG Hayashi et al. (2001) Lai et al. (2006) Mierzejewski et al. (2008) Tham et al. (2008) Tham et al. (2009) Liu et al. (2011) Tham et al. (2013) Dada et al. (2015) Dias-Santos (2015) Moghimi et al. (2015) Azuara-Blanco et al. (2016)** Lee et al. (2016) Siak et al. (2016) Random effects model Heterogeneity: I² = 99%, τ² = 3	-1.8 -8.3 -3.8 -8.4 -13.9 -5.4 -8.3 -12.9 -1.7 -2.1	1.31 0.97 0.59 1.16 0.70 1.18 0.24 2.04 0.90 0.57 0.60 0.89	72 21 25 35 27 30 26 44 15 46 182 56 24		-7.2 [-8.0; -6.4] -4.2 [-6.8; -1.6] -5.1 [-7.0; -3.2] -1.8 [-3.0; -0.6] -8.3 [-10.6; -6.0] -3.8 [-5.2; -2.4] -8.4 [-10.7; -6.1] -13.9 [-14.4; -13.4] -5.4 [-9.4; -1.4] -8.3 [-10.1; -6.5] -12.9 [-14.0; -11.8] -1.7 [-2.9; -0.5] -2.1 [-3.8; -0.4] -6.4 [-9.4; -3.4]
subtype = OAG  Kim et al. (1999)  Hayashi et al. (2001)  Leelachaikul et al. (2005)  Mathalone et al. (2006)  Shingleton et al. (2006)  Shoji et al. (2007)  Mierzejewski et al. (2008)  Fea et. al (2010)  Samuelson et al. (2011)  Arthur et al. (2014)  lancu et al. (2014)  Pfeiffer et al. (2015)*  Siegel et al. (2015)  Siak et al. (2016)  Vold et al. (2016)  Random effects model  Heterogeneity: I <sup>2</sup> = 91%, τ <sup>2</sup> = 3	-1.0 -4.0 -1.6 -1.0 -2.1 -1.9 -7.4 -2.2 -2.1 -5.4	0.68 0.57 1.00 0.86 0.44 0.67 0.56 0.70 0.30 1.20 0.63 0.74 0.64 0.71 0.36	31 50 54 24 25 20 52 21 123 17 38 47 52 30 116		-2.9 [-4.1; -1.7] -5.3 [-6.6; -4.0] -1.6 [-2.7; -0.5] -1.9 [-3.9; 0.1] -1.5 [-3.2; 0.1] -1.4 [-2.3; -0.5] -1.0 [-2.3; 0.3] -4.0 [-5.1; -2.9] -1.6 [-3.0; -0.2] -1.0 [-1.6; -0.4] -2.1 [-4.4; 0.2] -1.9 [-3.1; -0.7] -7.4 [-8.9; -5.9] -2.2 [-3.5; -0.9] -2.1 [-3.5; -0.7] -5.4 [-6.1; -4.7] -2.7 [-3.7; -1.7]
subtype = PXG Jacobi et al. (1999) Damji et al. (2006) Mierzejewski et al. (2008) Shingleton et al. (2008) Random effects model Heterogeneity: $I^2 = 95\%$ , $\tau^2 = 1$	-14.0 -3.1 -6.6 -1.1	0.78 0.81 0.59	13 27 23 51	-15 -10 -5 0	-14.0 [-18.0; -10.0] -3.1 [-4.7; -1.6] -6.6 [-8.2; -5.0] -1.1 [-2.3; 0.1] -5.8 [-9.5; -2.0]

### Acute

```
df <- df %>%
 filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "acute", MIGsYorN == 'N') %%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(Year)
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             n.e=LastPeriodEyes, comb.fixed = FALSE)
print(m)
##
                                               95%-CI %W(random)
## Jacobi et al. (2002) -22.7000 [-23.6565; -21.7435]
                                                            20.5
                                                            20.3
## Lam et al. (2008)
                       -47.1000 [-50.0449; -44.1551]
## Lee et al. (2010)
                        -35.8000 [-39.5586; -32.0414]
                                                            20.1
## Husain et al. (2012) -44.5000 [-51.8668; -37.1332]
                                                            18.9
## Hou et al. (2015)
                        -35.9600 [-38.9540; -32.9660]
                                                            20.3
## Number of studies combined: k = 5
##
##
                                              95%-CI
                                                         z p-value
## Random effects model -37.076 [-48.2779; -25.8742] -6.49 < 0.0001
##
## Quantifying heterogeneity:
## tau^2 = 158.9410; H = 9.13 [7.57; 11.00]; I^2 = 98.8% [98.3%; 99.2%];
## Rb = 97.3\% [92.7\%; 100.0\%]
##
## Test of heterogeneity:
##
         Q d.f. p-value
## 333.21
             4 < 0.0001
##
## Details on meta-analytical method:
## - Inverse variance method
## - DerSimonian-Laird estimator for tau^2
```

### Meds

```
overall=FALSE,
leftcols=c("studlab", "TE", "seTE", "n.e"),
leftlabs=c("Study", "ΔΙΟΡ", "SE", "eyes"))
```

Study	ΔIOP SE	eyes	1	95%-CI
subtype = ACG Hayashi et al. (2001) Lai et al. (2006) Mierzejewski et al. (2008) Tham et al. (2008) Tham et al. (2009) Liu et al. (2011) Tham et al. (2013) Dada et al. (2015) Dias-Santos (2015) Moghimi et al. (2015) Azuara-Blanco et al. (2016)** Lee et al. (2016) Siak et al. (2016) Random effects model Heterogeneity: I² = 94%, τ² = 0	-0.4 0.14 	56 24		-0.7 -1.4 [-1.9; -0.9] -0.3 [-0.6; 0.1] -1.1 [-1.6; -0.6] -1.6 [-2.2; -1.0] -0.8 -2.2 -1.9 [-2.1; -1.7] -0.7 [-1.4; -0.1] -1.1 [-1.4; -0.8] -0.6 [-0.8; -0.4] -0.4 [-0.6; -0.1]
subtype = OAG  Kim et al. (1999)  Hayashi et al. (2001)  Leelachaikul et al. (2005)  Mathalone et al. (2006)  Shingleton et al. (2006)  Shoji et al. (2007)  Mierzejewski et al. (2008)  Fea et. al (2010)  Samuelson et al. (2011)  Arthur et al. (2014)  lancu et al. (2014)  Pfeiffer et al. (2015)*  Siegel et al. (2015)  Siak et al. (2016)  Vold et al. (2016)*  Random effects model  Heterogeneity: I² = 92%, τ² = 0	-1.00.60.2 0.15 -0.4 0.29			-1.0 -0.6 -0.2 [-0.5; 0.1] -0.4 [-1.0; 0.2]  -0.1 [-0.3; 0.1] 0.0 -0.2 [-0.4; 0.1] -0.6 [-1.1; -0.1] -1.1 [-1.3; -0.9] 0.1 [-0.7; 0.9] 0.2 [0.0; 0.5] -1.0 [-1.4; -0.6] -0.2 [-0.5; 0.1]  -0.7 [-0.9; -0.5] -0.4 [-0.7; -0.1]
subtype = PXG Jacobi et al. (1999) Damji et al. (2006) Mierzejewski et al. (2008) Shingleton et al. (2008) Random effects model Heterogeneity: $I^2 = 7\%$ , $\tau^2 = 0.0$	-1.1 0.31 	51	-2 -1 0 1	-1.1 [-1.7; -0.5] -0.6 [-1.0; -0.1] -0.6 [-1.0; -0.2] -0.7 [-1.0; -0.4]

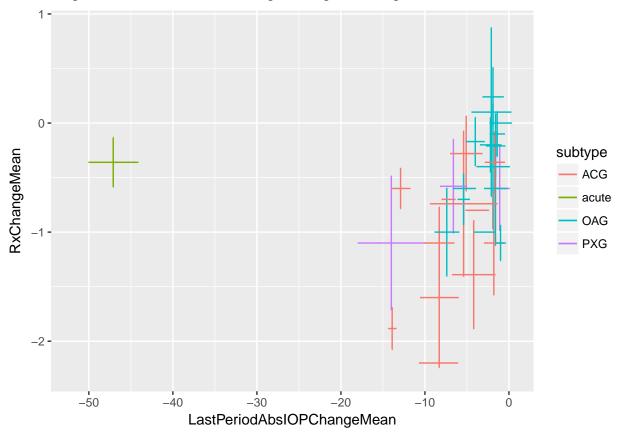
# Correlation between meds and drop in IOP

How is IOP drop related to change in meds? Two hypotheses:

- Those studies that see the largest IOP drops also have drop in meds, as doctors see that can use the newfound *slack* to decrease the number of meds people take
- The studies that see the largest IOP drops are those that don't change meds, because dropping meds would also increase IOP

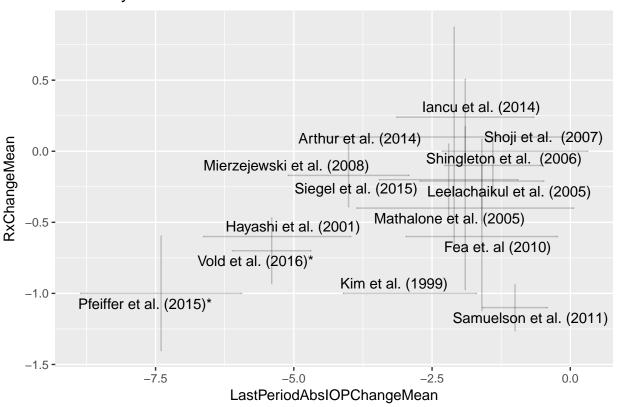
```
So which is it?
```

## Warning: Removed 15 rows containing missing values (geom\_errorbarh).



```
xmin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeSEM,
xmax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeSEM,
y =RxChangeMean,
ymin=RxChangeMean - 1.96*RxChangeSEM,
ymax=RxChangeMean + 1.96*RxChangeSEM,
label=study.name
)) + geom_errorbar(alpha=.2) + geom_errorbarh(alpha=.2) + ggtitle('OAG only') + geom_text_re
```

### OAG only



There is an apparent positive correlation between the two effect sizes: studies with larger drops in IOP also tend to see larger drops in Rx.

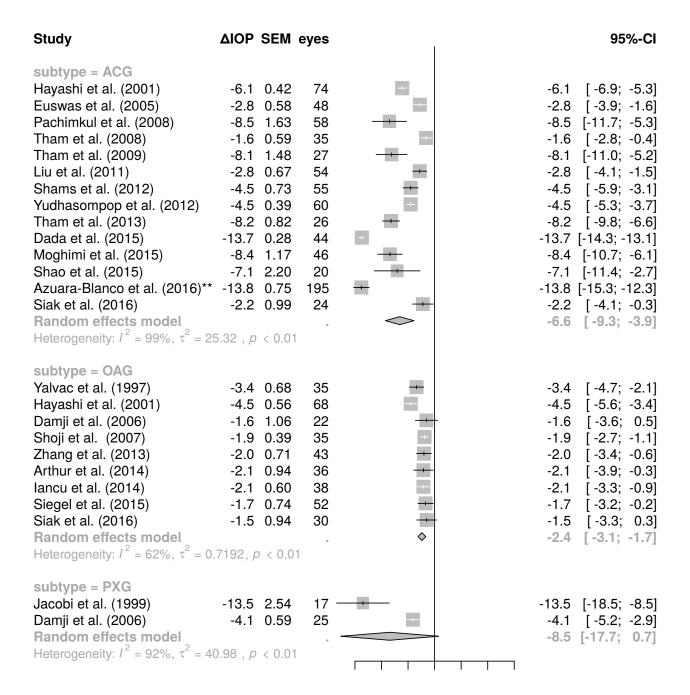
However, this effect goes away when we focus on the studies which don't have washout.

# Separate meta-analysis for each time period

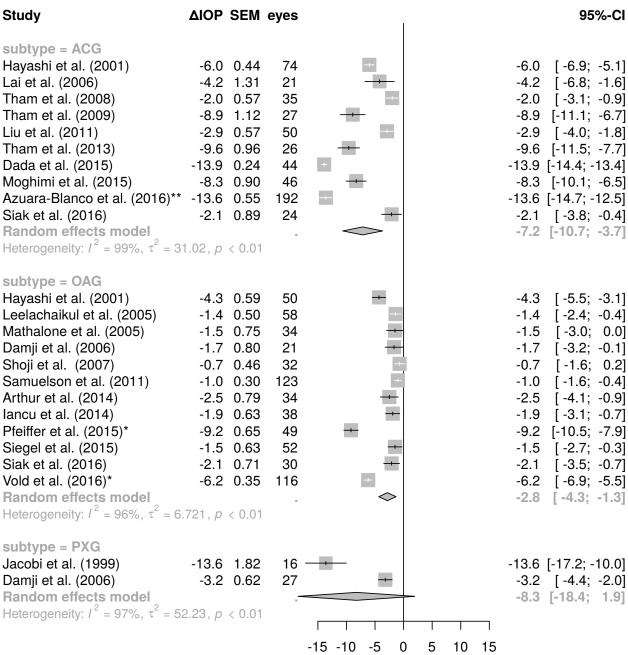
```
df <- read.data(fill.last = FALSE)</pre>
```

### 6 month follow-up

```
df_ <- df %>%
 filter(!is.na(SixMoAbsIOPChangeMean), subtype != "acute") %>%
 mutate(subtype=factor(subtype))
m <- metagen(SixMoAbsIOPChangeMean,
             SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=SixMoEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"),
       leftlabs=c("Study", "AIOP", "SEM", "eyes"))
```

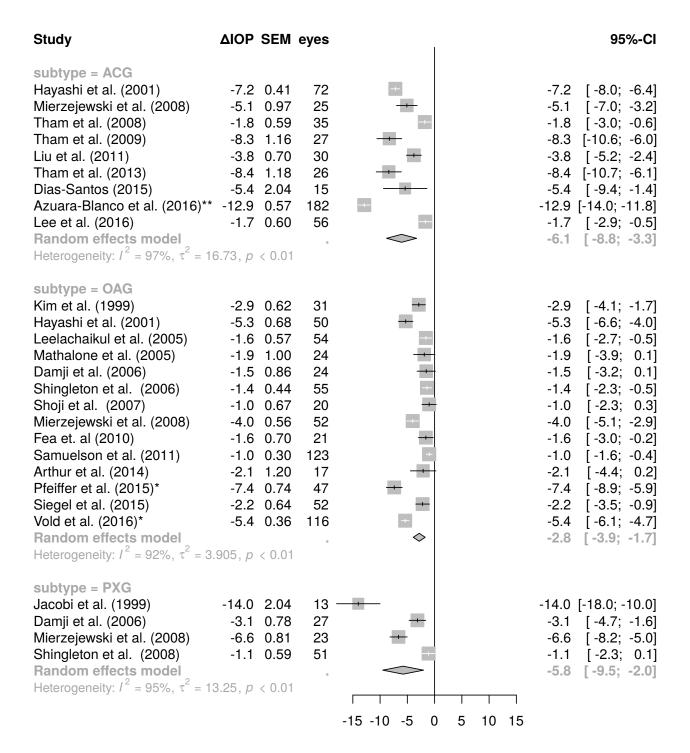


### 12-month follow up



# Last period

```
df_ <- df %>%
 filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(LastPeriodAbsIOPChangeMean,</pre>
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"),
       leftlabs=c("Study", "AIOP", "SEM", "eyes"))
```

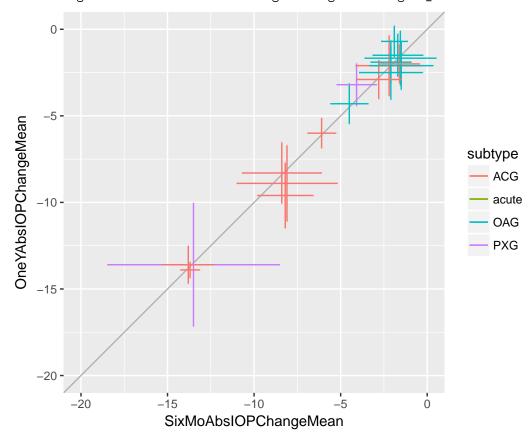


### Correlation among time points

Measure the correlation between different outcomes (IOP at 6 months vs. 12 months).

## Warning: Removed 25 rows containing missing values (geom\_errorbar).

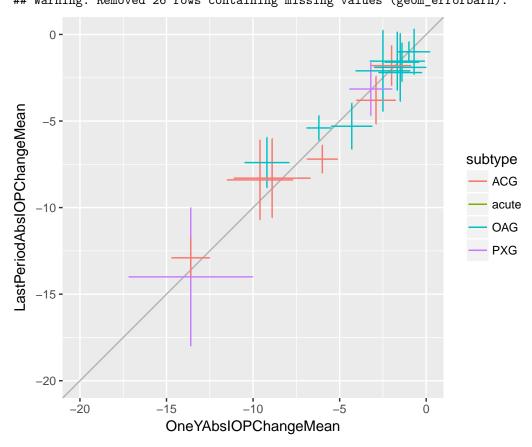
## Warning: Removed 25 rows containing missing values (geom\_errorbarh).



It's very clear that six months and 12 months IOP are highly correlated.

Similarly for one-year vs. last period:

```
## Warning: Removed 26 rows containing missing values (geom_errorbar).
## Warning: Removed 26 rows containing missing values (geom_errorbarh).
```



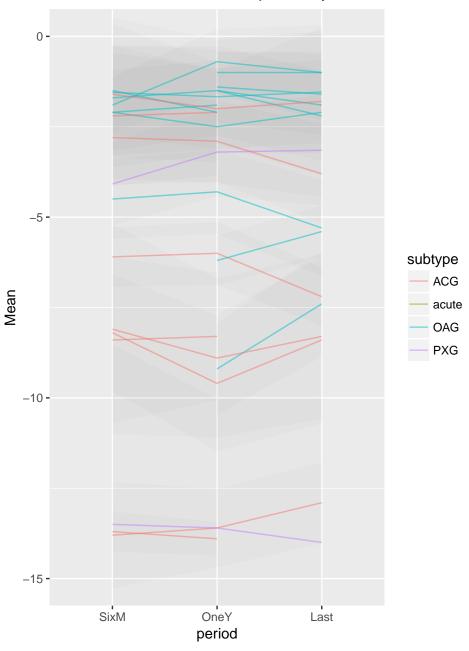
Again, correlations are very high. Present this in another way.

```
library(reshape2)
```

```
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
       smiths
nd <- melt(df %>%
             filter(MIGsYorN == 'N',
                    1*is.na(SixMoAbsIOPChangeMean) +
                    1*is.na(OneYAbsIOPChangeMean) +
                    1*is.na(LastPeriodAbsIOPChangeMean) < 2) %>%
             mutate(SixMoChangeSEM = SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
                    OneYChangeSEM = OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
                    LastPeriodChangeSEM = LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes)) %%
             select(study.name, subtype,
                    SixMoAbsIOPChangeMean,
                    OneYAbsIOPChangeMean,
                    LastPeriodAbsIOPChangeMean,
                    SixMoChangeSEM,
                    OneYChangeSEM,
```

```
LastPeriodChangeSEM), id.vars=c("study.name", "subtype"))
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable))</pre>
nd$period <- substr(nd$variable, 0, 4)</pre>
df_ <- dcast(nd, formula = study.name + subtype + period ~ metric)</pre>
df_ <- df_ %>% mutate(period = factor(period, c('SixM', 'OneY', 'Last')),
                      g = paste(study.name, as.character(subtype))) %>% filter(!is.na(Mean))
ggplot(df_, aes(y
                    =Mean,
               ymin=Mean - 1.96*eSEM,
               ymax=Mean + 1.96*eSEM,
               x = period,
               label=study.name,
               group=g)) +
  geom_ribbon(alpha=.02) +
  geom_line(alpha=.5, aes(color=subtype)) +
  coord_cartesian(y=c(-15, 0)) + ggtitle('Time course of IOP per study') + theme(plot.title = element_t
```

# Time course of IOP per study



It's remarkable how consistent measurements are between time periods. At most, we find a change of +- 2.5 mm Hg between the first and last period.

## Mean +- SE correlation, OAG only

```
print(mean(drawn.corrs))
## [1] 0.6202973
print(sd(drawn.corrs))
## [1] 0.2077722
df_<-df
drawn.corrs <- with(df_, replicate(n = 100,</pre>
                                    draw.corr(SixMoAbsIOPChangeMean,
                                              SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
                                              OneYAbsIOPChangeMean,
                                              OneYAbsIOPChangeStdDev / sqrt(OneYEyes))))
cat("Mean +- SE correlation, All subtypes\n")
## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))
## [1] 0.9925379
print(sd(drawn.corrs))
```

## [1] 0.003406047

library(mvmeta)

}

This is also reflected in the correlations - even accounting for noise, the correlations are > .9 between month 6 and month 12.

### Multivariate inference

 $yy \leftarrow fill.na(y[i], x[i], z[i])$ zz <- fill.na(z[i], x[i], y[i])</pre>

Let's use mymeta to infer the effect size for all periods together.

```
## This is mvmeta 0.4.7. For an overview type: help('mvmeta-package').
fill.na <- function(x, y, z) {
  return(ifelse(!is.na(x),
                    х,
                    ifelse(is.na(y),
                           z,
                           ifelse(is.na(z),
                             sqrt((y**2 + z**2) / 2 )))))
}
get.correlation.matrices.tri <- function(x, y, z, assumed.rho) {</pre>
 S <- list()
  for(i in 1:length(x)) {
    xx <- fill.na(x[i], y[i], z[i])</pre>
```

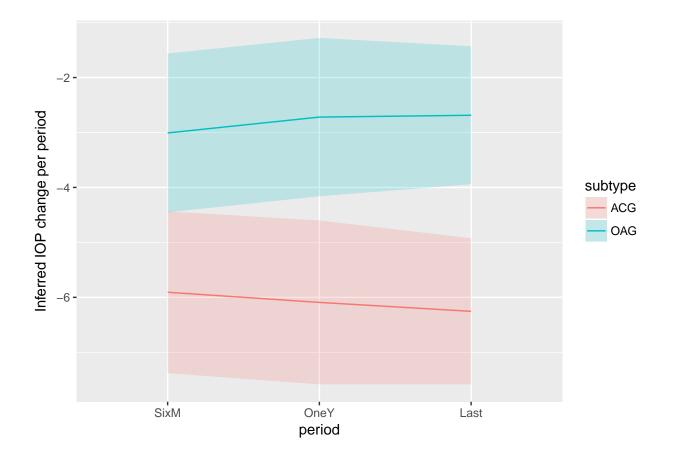
xx \* yy \* assumed.rho, yy \*\* 2, zz \* yy\* assumed.rho,

xx \* zz \* assumed.rho \*\* 2, zz \* yy \* assumed.rho, zz \* zz), ncol=3)

 $S[[i]] \leftarrow matrix(c(xx ** 2, xx * yy * assumed.rho, xx * zz * assumed.rho ** 2,$ 

```
S
}
df_ <- df %>% filter(!is.na(LastPeriodAbsIOPChangeStdDev) |
                                                                     !is.na(SixMoAbsIOPChangeStdDev) |
                                                                     !is.na(OneYAbsIOPChangeStdDev), subtype %in% c('OAG', 'ACG'), MIGsYorN == 'N')
thefit <- mvmeta(cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean, LastPeriodAbsIOPChangeMean) ~ subty
                       S=get.correlation.matrices.tri(df_$SixMoAbsIOPChangeStdDev / sqrt(df_$SixMoEyes),
                                                                                                                          df_$OneYAbsIOPChangeStdDev / sqrt(df_$OneYEyes),
                                                                                                                          df_$LastPeriodAbsIOPChangeStdDev / sqrt(df_$LastPeriodEyes), .7),
                       data=df_,
                       method="reml")
summary(thefit)
## Call: mvmeta(formula = cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean,
##
                 Last Period Abs IOP Change Mean) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \verb|matrices.tri| (df_\$SixMoAbsIOP Change StdDev/location) ~ subtype, S = get.correlation. \| subtype = get.correlation ~ subtype = get.correlation ~ subtype = get.correlation) ~ subtype = get.correlation ~ sub
                 {\tt df\_\$OneYAbsIOPChangeStdDev/sqrt(df\_\$OneYEyes),\ df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbsIOPChangeStdDev/sqrt(df\_\$LastPeriodAbs
##
##
                       0.7), data = df_, method = "reml")
##
## Multivariate random-effects meta-regression
## Dimension: 3
## Estimation method: REML
##
## Fixed-effects coefficients
## SixMoAbsIOPChangeMean :
##
                                                   Estimate Std. Error
                                                                                                                                             z Pr(>|z|)
                                                                                                                                                                                       95%ci.lb
                                                                                                                                                                                                                        95%ci.ub
## (Intercept)
                                                       -5.9077
                                                                                                 0.7511
                                                                                                                         -7.8657
                                                                                                                                                              0.0000
                                                                                                                                                                                           -7.3797
                                                                                                                                                                                                                            -4.4356
## subtypeOAG
                                                          2.8997
                                                                                                 1.0525
                                                                                                                             2.7551
                                                                                                                                                              0.0059
                                                                                                                                                                                              0.8368
                                                                                                                                                                                                                              4.9625
##
## (Intercept)
## subtypeOAG
## OneYAbsIOPChangeMean :
##
                                                   Estimate Std. Error
                                                                                                                                                       Pr(>|z|)
                                                                                                                                                                                       95%ci.lb
                                                                                                                                                                                                                        95%ci.ub
                                                       -6.0920
                                                                                                                                                                                           -7.5828
                                                                                                                                                                                                                            -4.6011
## (Intercept)
                                                                                                 0.7607
                                                                                                                          -8.0089
                                                                                                                                                              0.0000
## subtypeOAG
                                                          3.3725
                                                                                                 1.0576
                                                                                                                             3.1888
                                                                                                                                                               0.0014
                                                                                                                                                                                               1.2996
                                                                                                                                                                                                                              5.4454
##
## (Intercept)
## subtypeOAG
                                                       **
## LastPeriodAbsIOPChangeMean :
                                                                                                                                              z Pr(>|z|) 95%ci.lb
##
                                                   Estimate Std. Error
                                                                                                                                                                                                                        95%ci.ub
                                                       -6.2546
                                                                                                                                                                                           -7.5842
                                                                                                                                                                                                                            -4.9250
## (Intercept)
                                                                                                0.6784
                                                                                                                          -9.2199
                                                                                                                                                              0.0000
## subtypeOAG
                                                          3.5680
                                                                                                 0.9329
                                                                                                                             3.8246
                                                                                                                                                              0.0001
                                                                                                                                                                                              1.7396
                                                                                                                                                                                                                              5.3965
##
## (Intercept)
## subtypeOAG
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Between-study random-effects (co)variance components
            Structure: General positive-definite
##
                                                                                                    Std. Dev
                                                                                                                                                                                           Corr
## SixMoAbsIOPChangeMean
                                                                                                          2.9877 SixMoAbsIOPChangeMean
```

```
## OneYAbsIOPChangeMean
                                   3.0236
                                                            0.9981
## LastPeriodAbsIOPChangeMean
                                   2.6030
                                                            0.9919
## SixMoAbsIOPChangeMean
                                 OneYAbsIOPChangeMean
## OneYAbsIOPChangeMean
## LastPeriodAbsIOPChangeMean
                                                0.9821
## Multivariate Cochran Q-test for residual heterogeneity:
## Q = 1625.2906 (df = 62), p-value = 0.0000
## I-square statistic = 96.2%
## 36 studies, 68 observations, 6 fixed and 6 random-effects parameters
      logLik
                     AIC
                                 BIC
## -118.5856
                261.1712
                           286.6968
newdata <- data.frame(subtype=c('OAG', 'ACG'))</pre>
pred <- predict(thefit, newdata, se=TRUE)</pre>
newdata$SixMoAbsIOPChangeMean <- pred$fit[,1]</pre>
newdata$OneYAbsIOPChangeMean <- pred$fit[,2]</pre>
newdata$LastPeriodAbsIOPChangeMean <- pred$fit[,3]</pre>
newdata$SixMoAbsIOPChangeSEM <- pred$se[,1]</pre>
newdata$OneYAbsIOPChangeSEM <- pred$se[,2]</pre>
newdata$LastPeriodAbsIOPChangeSEM <- pred$se[,3]</pre>
library(reshape2)
nd <- melt(newdata)</pre>
## Using subtype as id variables
nd$period <- substr(nd$variable, 0, 4)</pre>
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable))
df_ <- dcast(nd, formula = subtype + period ~ metric)</pre>
df_$period <- factor(df_$period, c('SixM', 'OneY', 'Last'))</pre>
ggplot(df_, aes(x=period,
                 y=Mean,
                 ymin=Mean - 1.96*eSEM,
                 ymax=Mean + 1.96*eSEM,
                 group=subtype,
                 fill=subtype)) + geom_ribbon(alpha=.2) + geom_line(aes(color=subtype)) + ylab("Inferred
```



# Meta-regression

Consider relationships between different covariates and outcomes. Focus on the IOP drop at one year and its correlation with different factors.

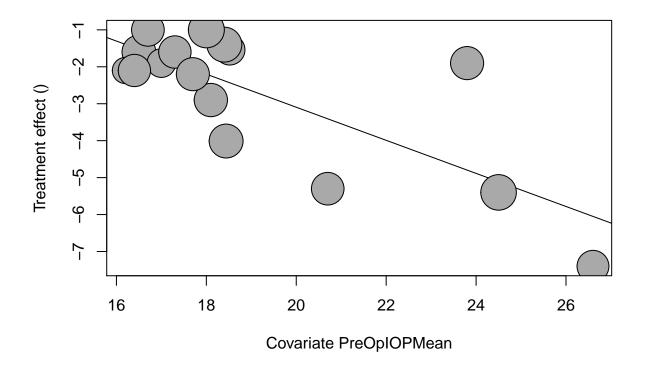
```
df <- read.data()</pre>
## These retrospective studies are losing eyes per period - not impossible, but unusual:
## Mathalone et al. (2005)
## Leelachaikul et al. (2005)
## Shoji et al. (2007)
## Liu et al. (2011)
## Arthur et al. (2014)
## Tetz et al. (2015)
## These retrospective studies are gaining eyes as the study goes
## Samuelson et al. (2011)
df_ <- df %>% filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
 mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen(LastPeriodAbsIOPChangeMean,</pre>
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=OneYEyes)
```

```
print(metareg(~ LastPeriodEyes, x=m))
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
## tau^2 (estimated amount of residual heterogeneity):
                                                           26.2513 (SE = 9.6875)
## tau (square root of estimated tau^2 value):
                                                           5.1236
## I^2 (residual heterogeneity / unaccounted variability): 98.62%
## H^2 (unaccounted variability / sampling variability):
                                                           72.73
## R^2 (amount of heterogeneity accounted for):
                                                           0.00%
## Test for Residual Heterogeneity:
## QE(df = 31) = 2254.5144, p-val < .0001
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.8360, p-val = 0.3605
##
## Model Results:
##
##
                   estimate
                                       zval
                                               pval
                                                       ci.lb
                                se
## intrcpt
                   -3.4752 1.4802 -2.3478 0.0189 -6.3764
                                                              -0.5740 *
                   -0.0238 0.0260 -0.9144 0.3605 -0.0747
## LastPeriodEyes
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
print(metareg(~ LastPeriodEyes * subtype, x=m))
##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
## tau^2 (estimated amount of residual heterogeneity):
                                                           15.5304 (SE = 5.8744)
## tau (square root of estimated tau^2 value):
                                                           3.9409
## I^2 (residual heterogeneity / unaccounted variability): 97.52%
## H^2 (unaccounted variability / sampling variability):
                                                           40.31
## R^2 (amount of heterogeneity accounted for):
                                                           36.43%
##
## Test for Residual Heterogeneity:
## QE(df = 27) = 1088.3177, p-val < .0001
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 13.5909, p-val = 0.0184
## Model Results:
##
##
                              estimate
                                                                   ci.lb
                                            se
                                                  zval
                                                           pval
                              -2.0693 1.8525 -1.1171 0.2640
                                                                 -5.7002
## intrcpt
## LastPeriodEyes
                              -0.0135 0.0328 -0.4125 0.6800
                                                                 -0.0778
## subtypeACG
                              -2.1400 2.5047 -0.8544 0.3929
                                                                 -7.0492
## subtypePXG
                              -12.1575 5.1350 -2.3676 0.0179
                                                               -22.2219
## LastPeriodEyes:subtypeACG
                              -0.0332 0.0422 -0.7882 0.4306
                                                                 -0.1159
## LastPeriodEyes:subtypePXG
                               0.2999 0.1512
                                               1.9839 0.0473
                                                                   0.0036
##
                               ci.ub
                               1.5615
## intrcpt
```

```
## LastPeriodEyes
                              0.0508
## subtypeACG
                              2.7691
## subtypePXG
                              -2.0932 *
## LastPeriodEyes:subtypeACG
                               0.0494
## LastPeriodEyes:subtypePXG
                               0.5962 *
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
print(metareg(~ Year, x=m))
##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):
                                                           22.3228 (SE = 8.2207)
## tau (square root of estimated tau^2 value):
                                                           4.7247
## I^2 (residual heterogeneity / unaccounted variability): 98.40%
## H^2 (unaccounted variability / sampling variability):
                                                           62.34
## R^2 (amount of heterogeneity accounted for):
                                                           8.63%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 1932.3895, p-val < .0001
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.0830, p-val = 0.7732
## Model Results:
##
##
           estimate
                                           pval
                                                     ci.lb
                                                               ci.ub
                            se
                                   zval
## intrcpt 89.0966 324.9770
                                0.2742 0.7840
                                                -547.8466
                                                           726.0397
                       0.1617 -0.2881 0.7732
## Year
            -0.0466
                                                   -0.3635
                                                              0.2703
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
print(metareg(~ Year * subtype, x=m))
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
## tau^2 (estimated amount of residual heterogeneity):
                                                           13.5115 (SE = 4.9389)
## tau (square root of estimated tau^2 value):
                                                           3.6758
## I^2 (residual heterogeneity / unaccounted variability): 97.20%
## H^2 (unaccounted variability / sampling variability):
                                                           35.67
## R^2 (amount of heterogeneity accounted for):
                                                           44.70%
## Test for Residual Heterogeneity:
## QE(df = 27) = 963.1148, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 12.4364, p-val = 0.0293
## Model Results:
##
##
                      estimate
                                       se
                                              zval
                                                      pval
                                                                 ci.lb
```

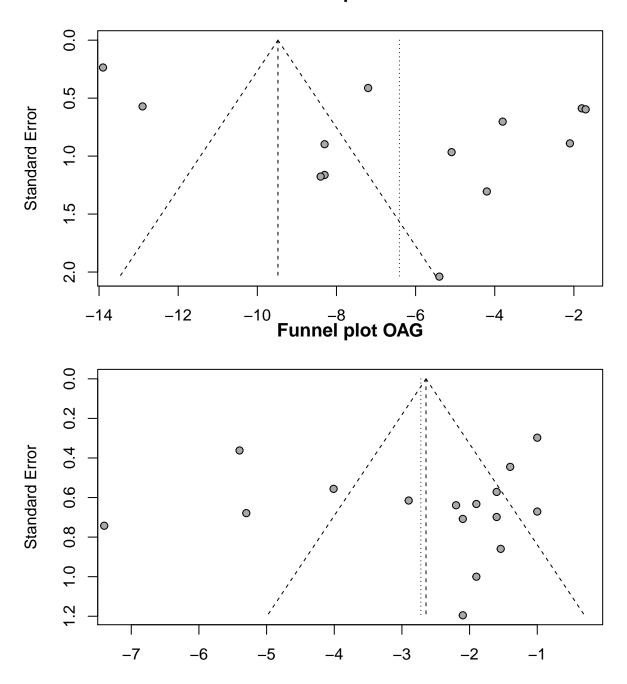
```
## intrcpt
                     101.1568
                                 356.9373
                                          0.2834 0.7769
                                                             -598.4274
## Year
                      -0.0517
                                  0.1776 -0.2910 0.7710
                                                              -0.3999
                                          0.3700 0.7114
## subtypeACG
                     215.3198
                                 581.9158
                                                             -925.2142
## subtypePXG
                   -2425.5387 1160.3658 -2.0903 0.0366 -4699.8138
## Year:subtypeACG
                      -0.1088
                                  0.2894 -0.3761 0.7069
                                                              -0.6761
## Year:subtypePXG
                       1.2078
                                   0.5785
                                          2.0879 0.0368
                                                               0.0740
                        ci.ub
## intrcpt
                    800.7410
## Year
                       0.2965
## subtypeACG
                   1355.8538
## subtypePXG
                   -151.2635 *
## Year:subtypeACG
                       0.4584
## Year:subtypePXG
                      2.3415 *
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
print(metareg(~ PreOpIOPMean, x=m))
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):
                                                           5.0095 (SE = 1.8023)
## tau (square root of estimated tau^2 value):
                                                           2.2382
## I^2 (residual heterogeneity / unaccounted variability): 92.99%
## H^2 (unaccounted variability / sampling variability):
                                                           14.27
## R^2 (amount of heterogeneity accounted for):
                                                           79.50%
## Test for Residual Heterogeneity:
## QE(df = 31) = 442.4039, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 57.5862, p-val < .0001
## Model Results:
##
##
                 estimate
                               se
                                      zval
                                             pval
                                                     ci.lb
                                                               ci.ub
## intrcpt
                 11.3336 2.1216
                                   5.3421
                                           <.0001
                                                     7.1754
                                                            15.4918 ***
## PreOpIOPMean
                 -0.7859 0.1036 -7.5886 <.0001 -0.9888 -0.5829
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
print(metareg(~ PreOpIOPMean * subtype, x=m))
##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
                                                          1.3374 \text{ (SE = } 0.5549)
## tau^2 (estimated amount of residual heterogeneity):
## tau (square root of estimated tau^2 value):
                                                           1.1564
## I^2 (residual heterogeneity / unaccounted variability): 77.18%
## H^2 (unaccounted variability / sampling variability):
                                                           4.38
## R^2 (amount of heterogeneity accounted for):
                                                           94.53%
## Test for Residual Heterogeneity:
```

```
## QE(df = 27) = 118.3200, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 202.7962, p-val < .0001
## Model Results:
##
##
                           estimate
                                         se
                                                zval
                                                        pval
                                                                ci.lb
## intrcpt
                            5.8521 2.1063
                                              2.7784 0.0055
                                                               1.7238
## PreOpIOPMean
                            -0.4475 0.1085 -4.1251 <.0001 -0.6601
## subtypeACG
                             5.5905 2.7842
                                             2.0079 0.0447
                                                               0.1336
## subtypePXG
                             8.8300 4.5191
                                             1.9539 0.0507 -0.0272
                           -0.4137 0.1375 -3.0091 0.0026 -0.6832
## PreOpIOPMean:subtypeACG
## PreOpIOPMean:subtypePXG
                            -0.4777 0.2179 -2.1928 0.0283 -0.9047
##
                             ci.ub
## intrcpt
                            9.9803
## PreOpIOPMean
                           -0.2349
                                   ***
## subtypeACG
                           11.0475
## subtypePXG
                           17.6873
## PreOpIOPMean:subtypeACG
                          -0.1443
                                     **
## PreOpIOPMean:subtypePXG -0.0507
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Same, restricted to OAG only
df_ <- df %>% filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "OAG", MIGsYorN == 'N') %>%
 mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen(LastPeriodAbsIOPChangeMean,</pre>
            LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
            study.name,
            data=df ,
            byvar=subtype,
            n.e=LastPeriodEyes)
bubble(metareg(~ PreOpIOPMean, x=m))
```

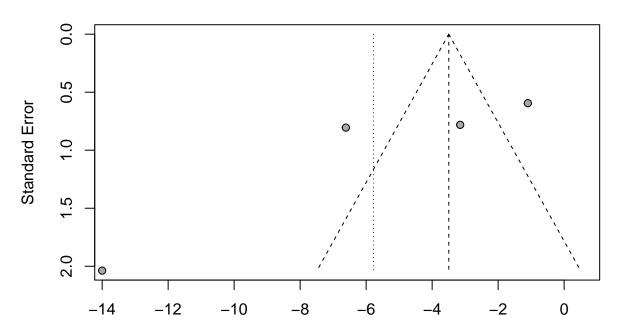


# Small study bias

# Funnel plot ACG

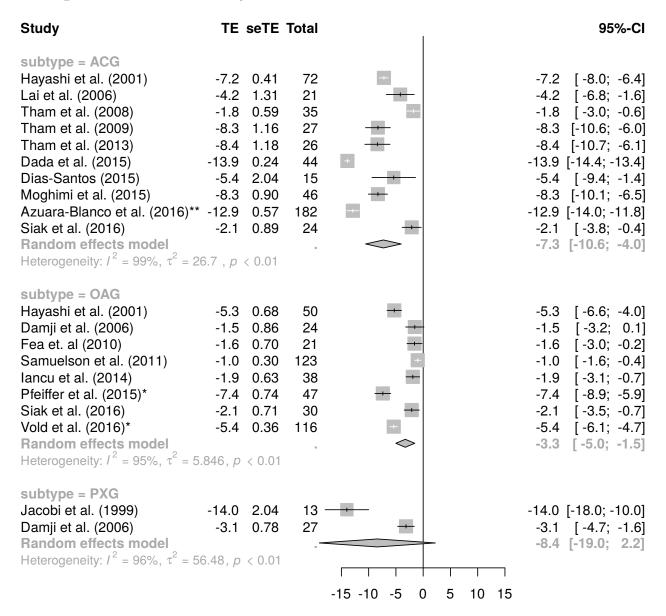


# Funnel plot PXG

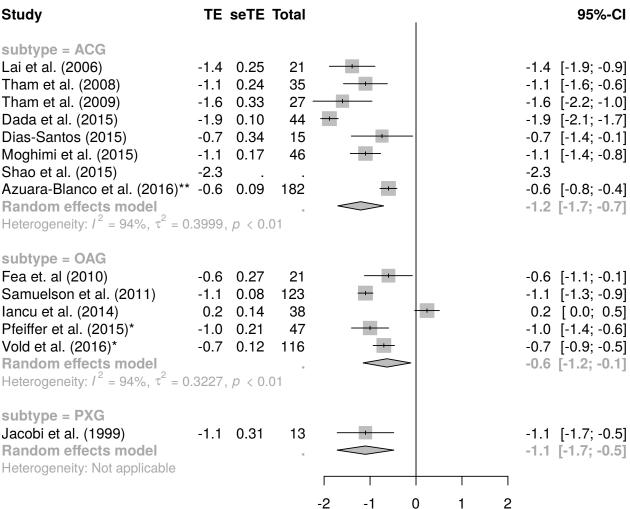


# Alternative filterings of the data

# Prospective studies only



### Meds



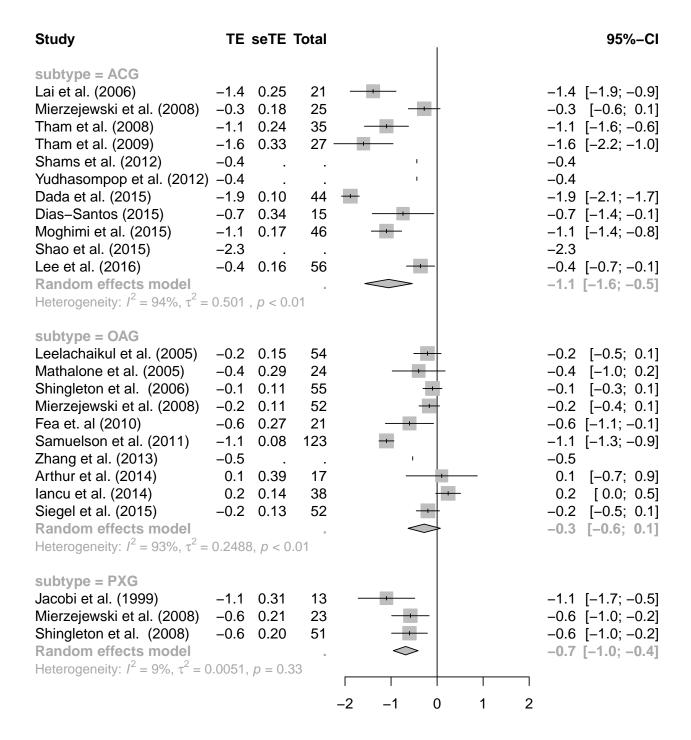
# Excluding washout studies

### Last period

Study	TE	seTE	Total	1	95%-CI
subtype = ACG Hayashi et al. (2001) Lai et al. (2006) Mierzejewski et al. (2008) Tham et al. (2008) Tham et al. (2009) Liu et al. (2011) Tham et al. (2013) Dada et al. (2015) Dias-Santos (2015) Moghimi et al. (2015) Lee et al. (2016) Siak et al. (2016) Random effects model Heterogeneity: I <sup>2</sup> = 99%, τ <sup>2</sup>	-5.1 -1.8 -8.3 -3.8 -8.4 -13.9 -5.4 -8.3 -1.7 -2.1	1.31 0.97 0.59 1.16 0.70 1.18 0.24 2.04 0.90 0.60 0.89	72 21 25 35 27 30 26 44 15 46 56 24		-7.2 [-8.0; -6.4] -4.2 [-6.8; -1.6] -5.1 [-7.0; -3.2] -1.8 [-3.0; -0.6] -8.3 [-10.6; -6.0] -3.8 [-5.2; -2.4] -8.4 [-10.7; -6.1] -13.9 [-14.4; -13.4] -5.4 [-9.4; -1.4] -8.3 [-10.1; -6.5] -1.7 [-2.9; -0.5] -2.1 [-3.8; -0.4] -5.9 [-9.1; -2.6]
subtype = OAG Kim et al. (1999) Hayashi et al. (2001) Leelachaikul et al. (2005) Mathalone et al. (2005) Damji et al. (2006) Shingleton et al. (2006) Shoji et al. (2007) Mierzejewski et al. (2008) Fea et. al (2010) Samuelson et al. (2011) Arthur et al. (2014) lancu et al. (2014) Siegel et al. (2015) Siak et al. (2016) Random effects model Heterogeneity: I <sup>2</sup> = 76%, τ <sup>2</sup>	-1.0 -4.0 -1.6 -1.0 -2.1 -1.9 -2.2 -2.1	0.62 0.68 0.57 1.00 0.86 0.44 0.67 0.56 0.70 0.30 1.20 0.63 0.64 0.71	31 50 54 24 25 20 52 21 123 17 38 52 30		-2.9 [-4.1; -1.7] -5.3 [-6.6; -4.0] -1.6 [-2.7; -0.5] -1.9 [-3.9; 0.1] -1.5 [-3.2; 0.1] -1.4 [-2.3; -0.5] -1.0 [-2.3; 0.3] -4.0 [-5.1; -2.9] -1.6 [-3.0; -0.2] -1.0 [-1.6; -0.4] -2.1 [-4.4; 0.2] -1.9 [-3.1; -0.7] -2.2 [-3.5; -0.9] -2.1 [-3.5; -0.7] -2.2 [-2.8; -1.5]
subtype = PXG Jacobi et al. (1999) Damji et al. (2006) Mierzejewski et al. (2008) Shingleton et al. (2008) Random effects model Heterogeneity: I <sup>2</sup> = 95%, τ <sup>2</sup>	-1.1	0.78 0.81 0.59	13 - 27 23 51	*	-14.0 [-18.0; -10.0] -3.1 [-4.7; -1.6] -6.6 [-8.2; -5.0] -1.1 [-2.3; 0.1] -5.8 [-9.5; -2.0]

# Meds

```
df_ <- df %>%
  filter(!is.na(RxChangeMean), !is.na(RxChangeStdDev),
```



# Sensitivity to missingness

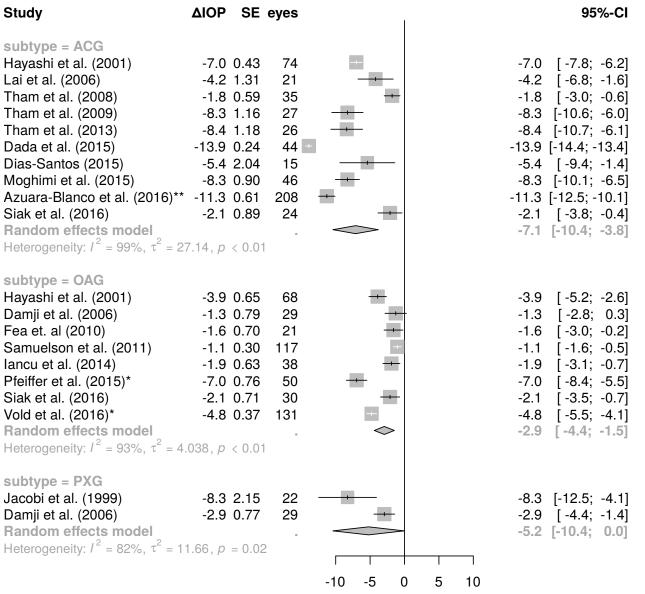
Simulate what the results would look like if there was no effect in the eyes lost to follow up  $(\Delta IOP = 0)$ .

```
meta.analysis.with.sensitivity <- function(missingness='zero') {
   df <- read.data()
   df <- filter.data(df, 'prospective')

   df_ <- df %>%
```

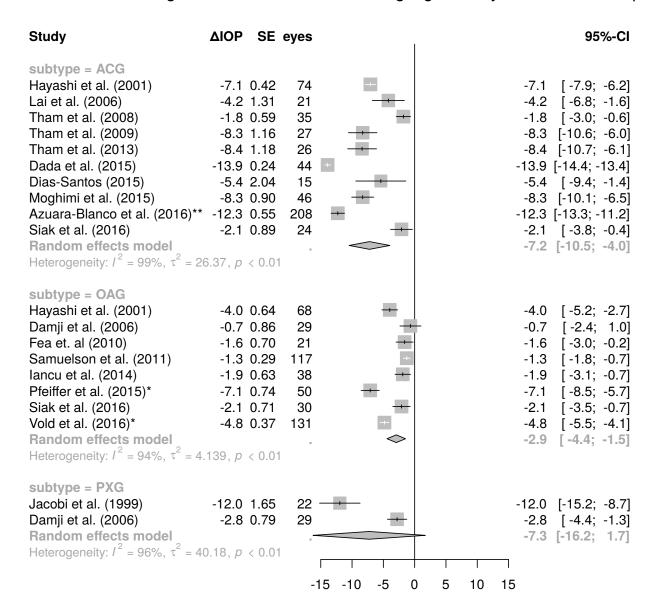
```
filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute") %>%
    mutate(subtype=factor(subtype))
  # Simulate a O effect in the unobserved fraction.
  df.missing <- df_</pre>
  if(missingness == 'zero') {
    # Zero out.
    df.missing <- df.missing %>% mutate(LastPeriodEyes = PreOpEyes - LastPeriodEyes,
                           LastPeriodAbsIOPChangeMean = 0)
  } else {
    # Add 5 mm Hg to each missing eye.
    df.missing <- df.missing %>% mutate(LastPeriodEyes = PreOpEyes - LastPeriodEyes,
                           LastPeriodAbsIOPChangeMean = LastPeriodAbsIOPChangeMean + 5)
 }
  df_ <- rbind(df_, df.missing)</pre>
  # Aggregate two by two
  for(i in seq(nrow(df.missing), 1)) {
   idx <- rep(FALSE, nrow(df_))</pre>
    idx[i] <- TRUE</pre>
   idx[i*2] <- TRUE</pre>
    df_ <- agg.arms(df_, idx)</pre>
 df_ <- df_ %>% dplyr::arrange(Year, study.name)
 m <- metagen(LastPeriodAbsIOPChangeMean,</pre>
               LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
               study.name,
               data=df_,
               byvar=subtype,
               n.e=LastPeriodEyes)
  forest(m,
         comb.fixed=FALSE,
         digits=1,
         digits.se = 2,
         overall=FALSE,
         leftcols=c("studlab", "TE", "seTE", "n.e"),
         leftlabs=c("Study", "AIOP", "SE", "eyes"))
}
meta.analysis.with.sensitivity()
grid.text(paste0("Simulated net change IOP when AIOP = 0 in eyes lost to follow up"), .5, .97, gp=gpar(
```

### Simulated net change IOP when $\triangle IOP = 0$ in eyes lost to follow up



meta.analysis.with.sensitivity('five')
grid.text(paste0("Simulated net change IOP when ΔΙΟΡ = 5 mm Hg higher in eyes lost to follow up"), .5,

### Simulated net change IOP when $\triangle IOP = 5$ mm Hg higher in eyes lost to follow up



### **MIGS**

We don't report these results because it's a bit misleading – the studies aren't very similar to each other, and we don't use the information in their control arms. We can do a much better job through, for example, network meta-analysis, which we plan to do in a future paper.

```
df <- read.data(drop.migs = FALSE)

## These retrospective studies are losing eyes per period - not impossible, but unusual:

## Mathalone et al. (2005)

## Leelachaikul et al. (2005)

## Shoji et al. (2007)

## Liu et al. (2011)</pre>
```

```
## Arthur et al. (2014)
## Tetz et al. (2015)
## These retrospective studies are gaining eyes as the study goes
## Samuelson et al. (2011)
df <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'Y') %>%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(TypesofMIGSifany, Year)
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df ,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=TRUE,
       leftcols=c("studlab", "TE", "seTE", "n.e", "TypesofMIGSifany"),
       leftlabs=c("Study", "TE", "seTE", "Total", "Type"))
```

