

Phaco meta analysis

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14/02/2017

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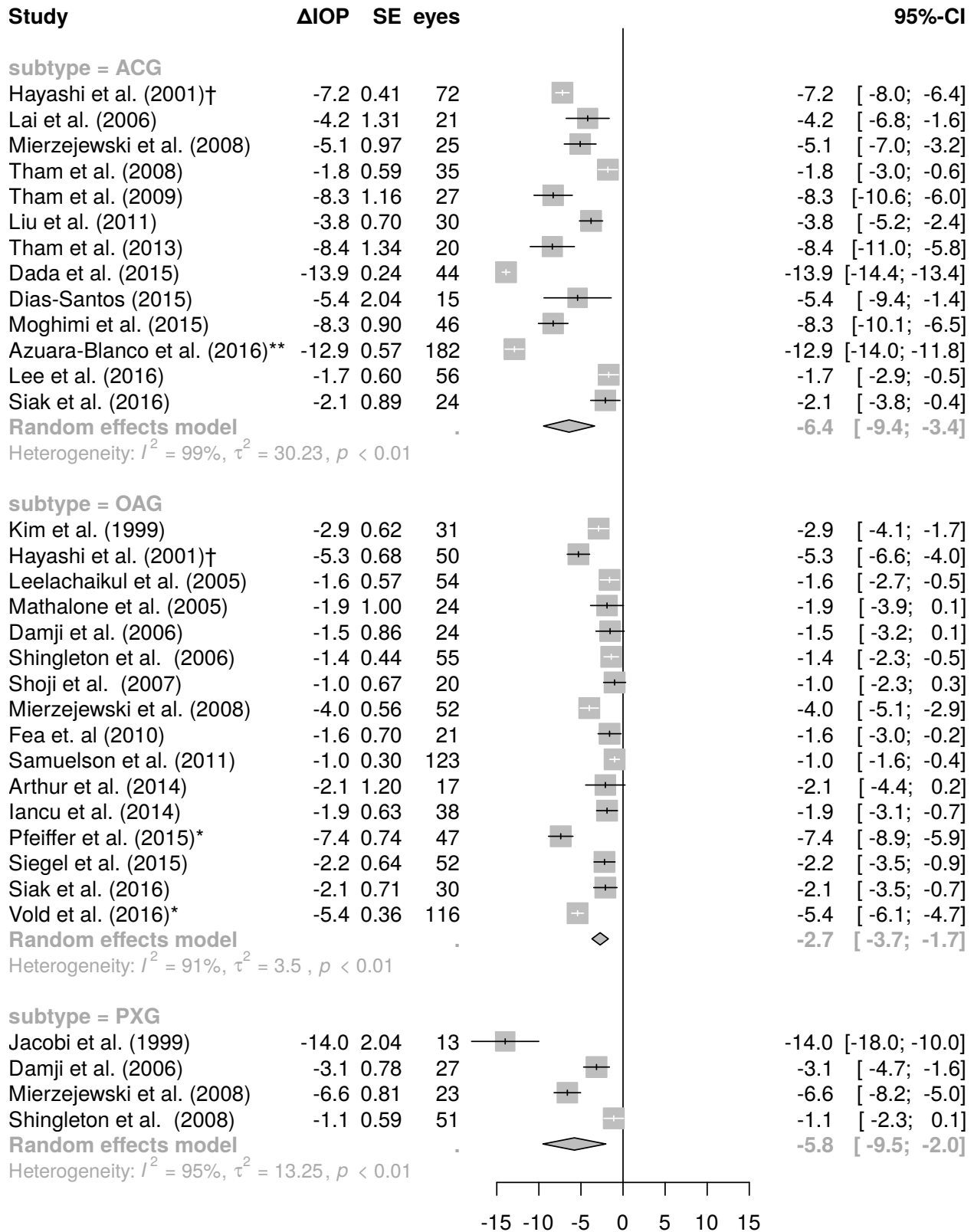
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Analysis of full dataset

Main analysis: 12-month+ follow up

```
df_ <- df %>%
  filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen>LastPeriodAbsIOPChangeMean,
      LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
      study.name,
      data=df_,
      byvar=subtype,
```

```
        n.e=LastPeriodEyes)
forest(m,
      comb.fixed=FALSE,
      digits=1,
      digits.se = 2,
      overall=FALSE,
      leftcols=c("studlab", "TE", "seTE", "n.e"),
      leftlabs=c("Study", "ΔIOP", "SE", "eyes"))
```



Acute

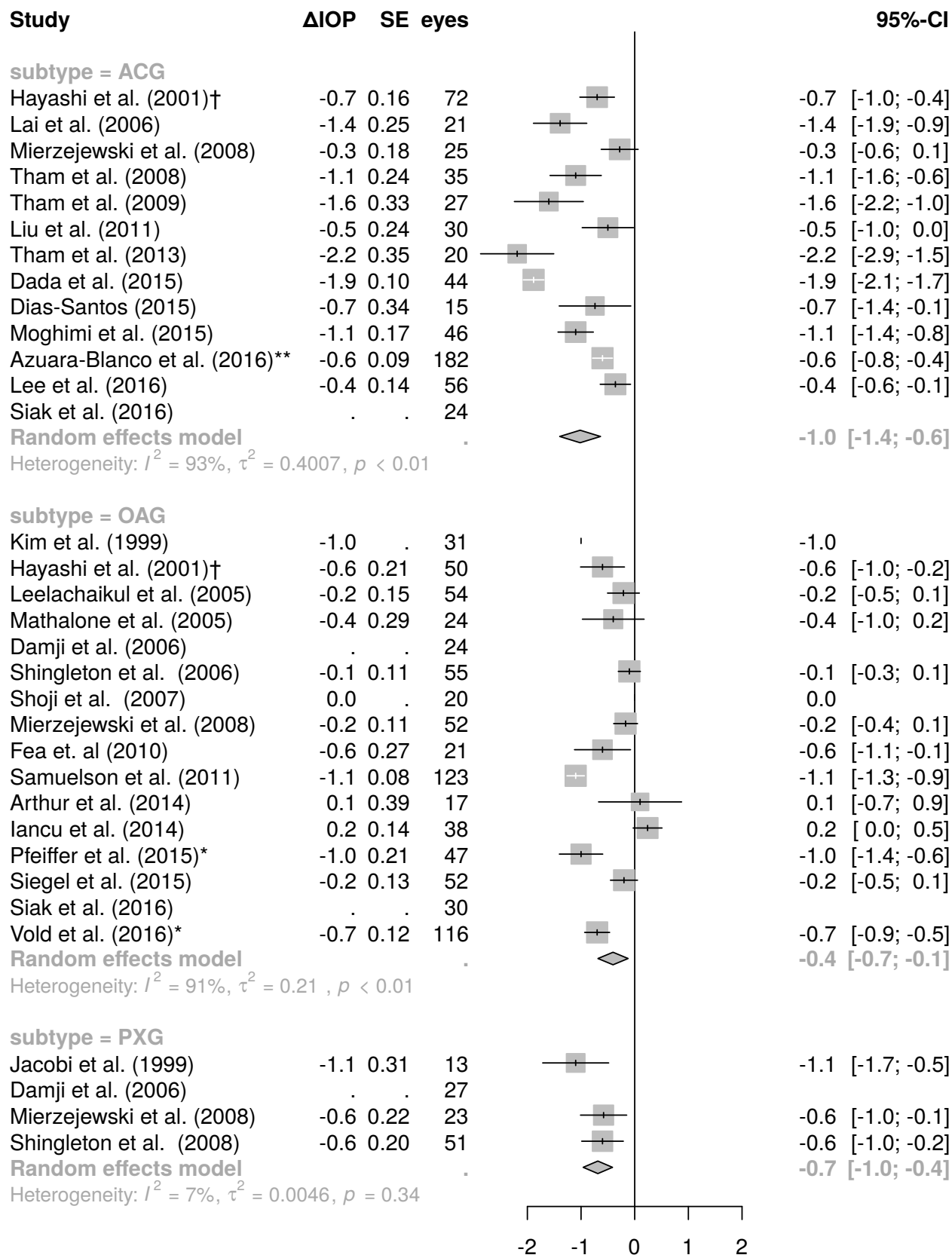
```
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(Year)
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             n.e=LastPeriodEyes, comb.fixed = FALSE)
print(m)
```

```
##                               95%-CI %W(random)
## Jacobi et al. (2002) -22.7000 [-23.6565; -21.7435]      20.5
## Lam et al. (2008)   -47.1000 [-50.0449; -44.1551]      20.3
## Lee et al. (2010)   -35.8000 [-39.5586; -32.0414]      20.1
## Husain et al. (2012) -44.5000 [-51.8668; -37.1332]     18.9
## Hou et al. (2015)   -35.9600 [-38.9540; -32.9660]      20.3
##
## Number of studies combined: k = 5
##
##                               95%-CI      z  p-value
## Random effects model -37.076 [-48.2779; -25.8742] -6.49 < 0.0001
##
## Quantifying heterogeneity:
## tau^2 = 158.9410; H = 9.13 [7.57; 11.00]; I^2 = 98.8% [98.3%; 99.2%];
## Rb = 97.3% [92.7%; 100.0%]
##
## Test of heterogeneity:
##      Q d.f.  p-value
## 333.21    4 < 0.0001
##
## Details on meta-analytical method:
## - Inverse variance method
## - DerSimonian-Laird estimator for tau^2
```

Meds

```
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean),
         df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             RxChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
```

```
overall=FALSE,  
leftcols=c("studlab", "TE", "seTE", "n.e"),  
leftlabs=c("Study", "ΔIOP", "SE", "eyes"))
```



Correlation between meds and drop in IOP

How is IOP drop related to change in meds? Two hypotheses:

- Those studies that see the largest IOP drops also have drop in meds, as doctors see that can use the newfound *slack* to decrease the number of meds people take
- The studies that see the largest IOP drops are those that don't change meds, because dropping meds would also increase IOP

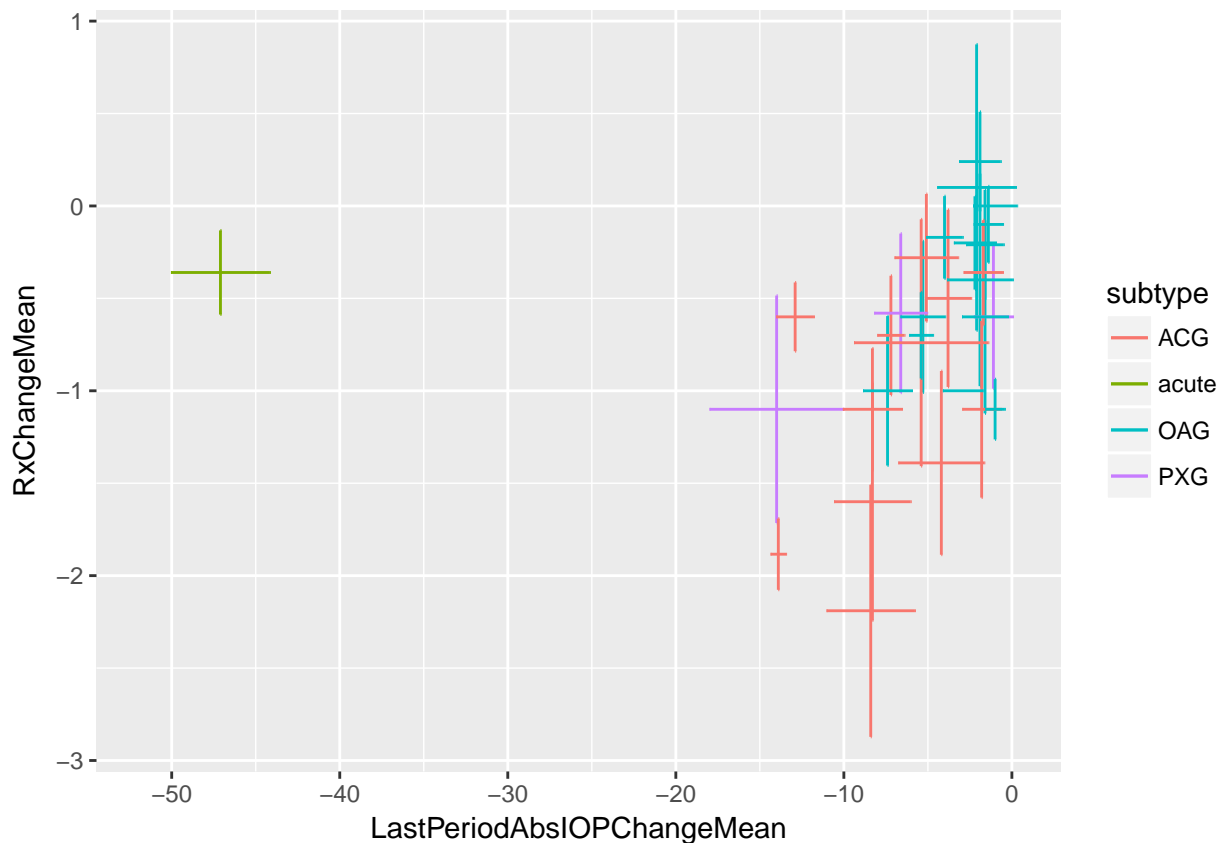
So which is it?

```
df_ <- df %>% mutate(RxChangeSEM = RxChangeStdDev / sqrt>LastPeriodEyes),
                    LastPeriodAbsIOPChangeSEM = LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes))

ggplot(df_, aes(x =LastPeriodAbsIOPChangeMean,
                xmin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeSEM,
                xmax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeSEM,
                y =RxChangeMean,
                ymin=RxChangeMean - 1.96*RxChangeSEM,
                ymax=RxChangeMean + 1.96*RxChangeSEM,
                color=subtype
            )) + geom_errorbar() + geom_errorbarh()
```

Warning: Removed 17 rows containing missing values (geom_errorbar).

Warning: Removed 15 rows containing missing values (geom_errorbarh).



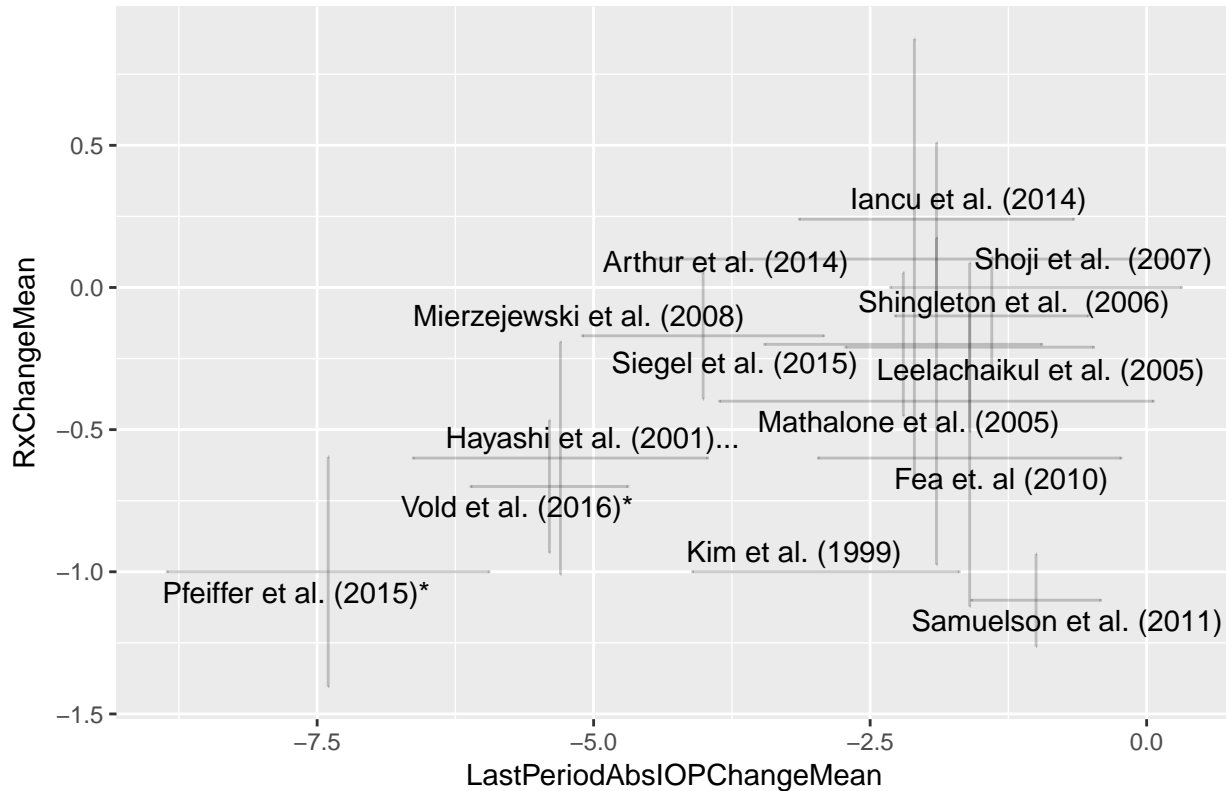
```
ggplot(df_ %>% filter(subtype=='OAG' & MIGsYorN == 'N'),
        aes(x =LastPeriodAbsIOPChangeMean,
```

```

xmin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeSEM,
xmax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeSEM,
y =RxChangeMean,
ymin=RxChangeMean - 1.96*RxChangeSEM,
ymax=RxChangeMean + 1.96*RxChangeSEM,
label=study.name
)) + geom_errorbar(alpha=.2) + geom_errorbarh(alpha=.2) + ggtitle('OAG only') + geom_text_rep

```

OAG only



There is an apparent positive correlation between the two effect sizes: studies with larger drops in IOP also tend to see larger drops in Rx.

```

draw.corr <- function(x.mean, x.sem, y.mean, y.sem) {
  d_ <- data.frame(x = rnorm(n = length(x.mean), mean=x.mean, sd = x.sem),
                    y = rnorm(n = length(x.mean), mean=y.mean, sd = y.sem))
  with(d_ %>% filter(!is.na(x) & !is.na(y)), cor(x, y))
}

cat("Mean +- SE correlation, all studies\n")

## Mean +- SE correlation, all studies

df_ <- df %>% filter(subtype=='OAG', MIGsYorN == 'N')
drawn.corr <- with(df_, replicate(n = 100,
  draw.corr(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             RxChangeMean,
             RxChangeStdDev / sqrt(LastPeriodEyes))))
mean(drawn.corr)

```



```
## [1] 0.3816005
sd(drawn.corrs)

## [1] 0.1337711
cat("Mean +- SE correlation, no washout\n")

## Mean +- SE correlation, no washout
df_ <- filter.data(df, 'nowashout') %>% filter(subtype=='OAG', MIGsYorN == 'N')
drawn.corrs <- with(df_, replicate(n = 100,
                                   draw.corr(LastPeriodAbsIOPChangeMean,
                                              LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
                                              RxChangeMean,
                                              RxChangeStdDev / sqrt(LastPeriodEyes))))
mean(drawn.corrs)

## [1] -0.02245687
sd(drawn.corrs)

## [1] 0.1921681
```

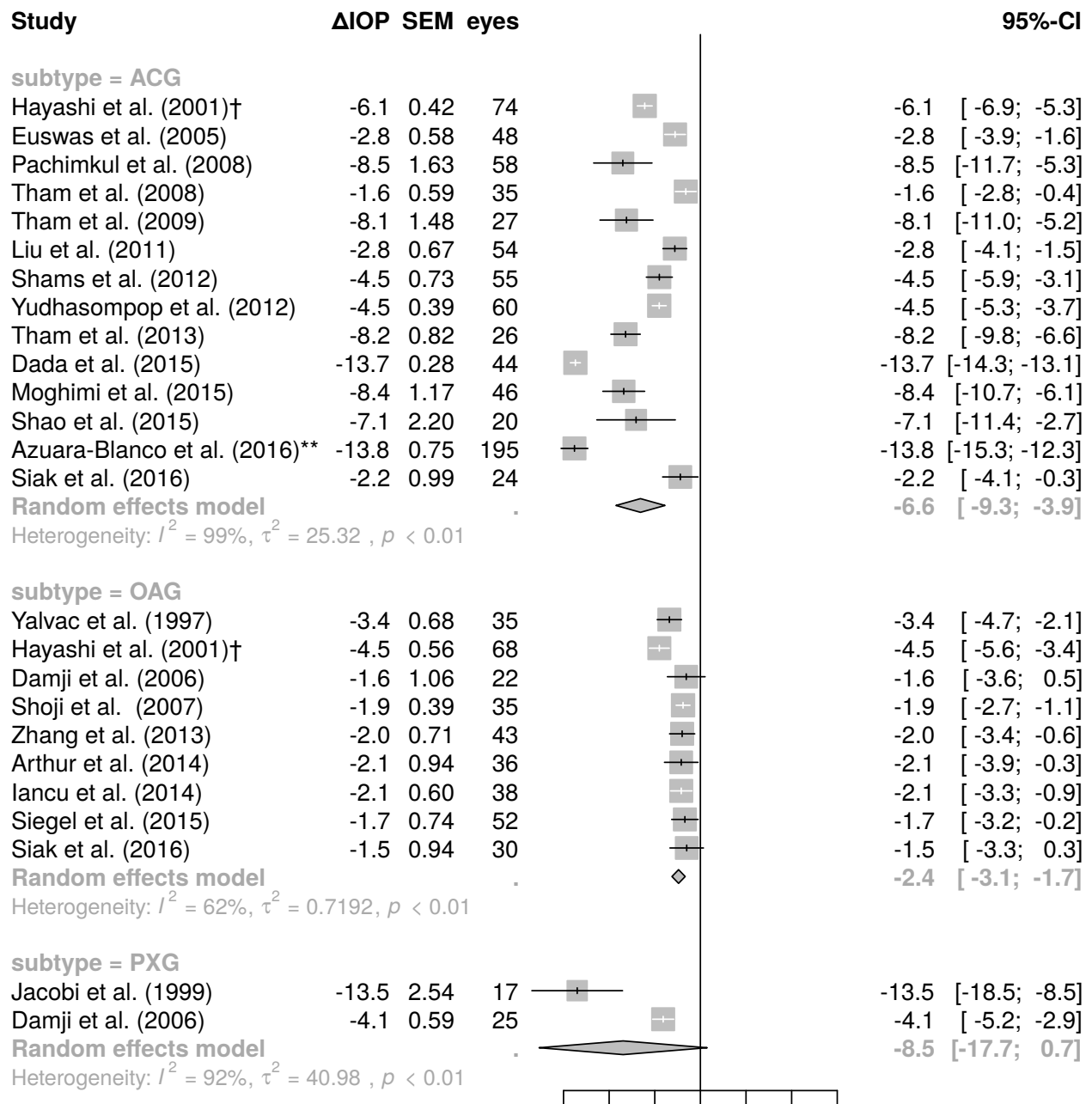
However, this effect goes away when we focus on the studies which don't have washout.

Separate meta-analysis for each time period

```
df <- read.data(fill.last = FALSE)
```

6 month follow-up

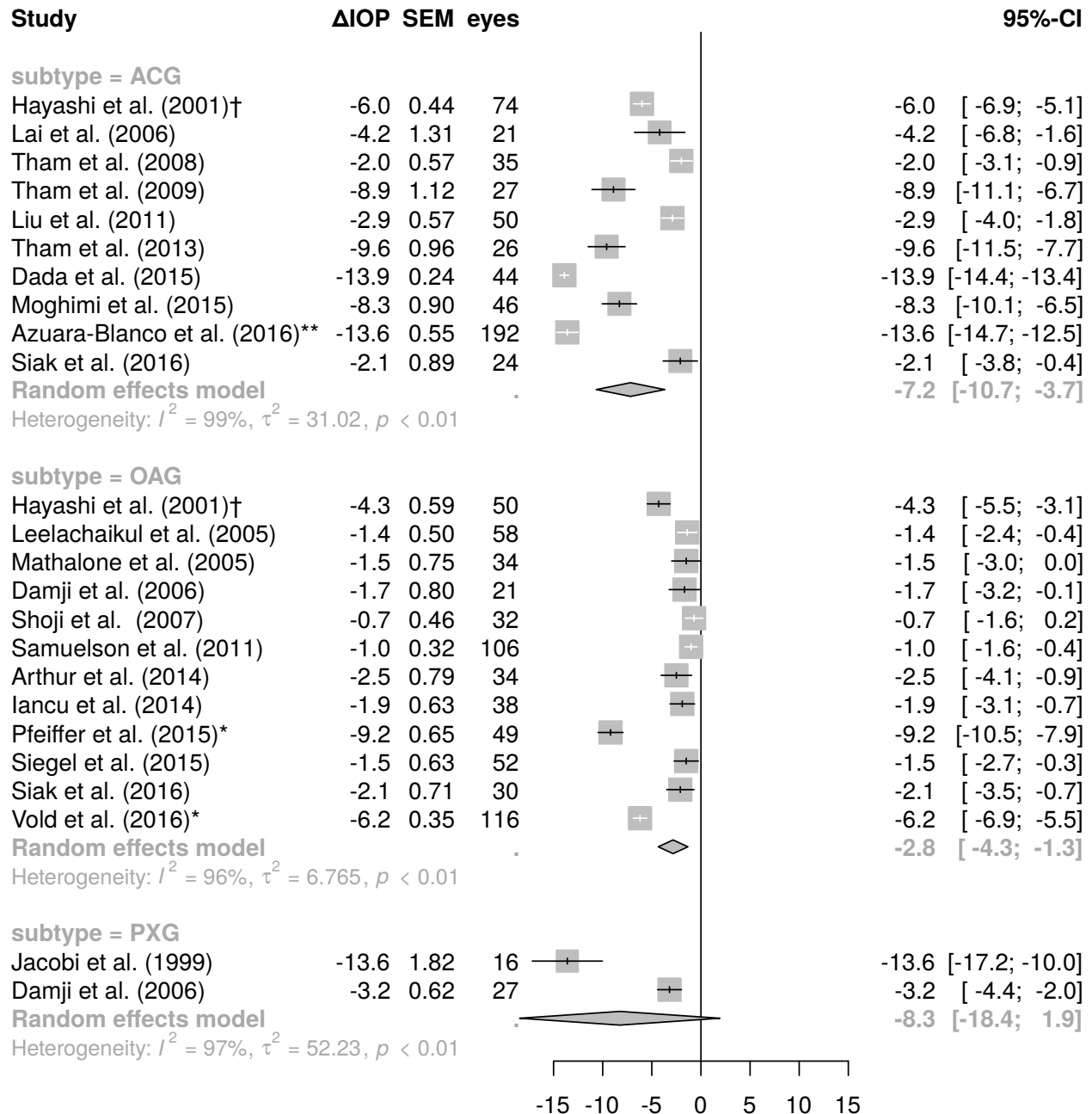
```
df_ <- df %>%
  filter(!is.na(SixMoAbsIOPChangeMean), subtype != "acute") %>%
  mutate(subtype=factor(subtype))
m <- metagen(SixMoAbsIOPChangeMean,
             SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=SixMoEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"),
       leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



12-month follow up

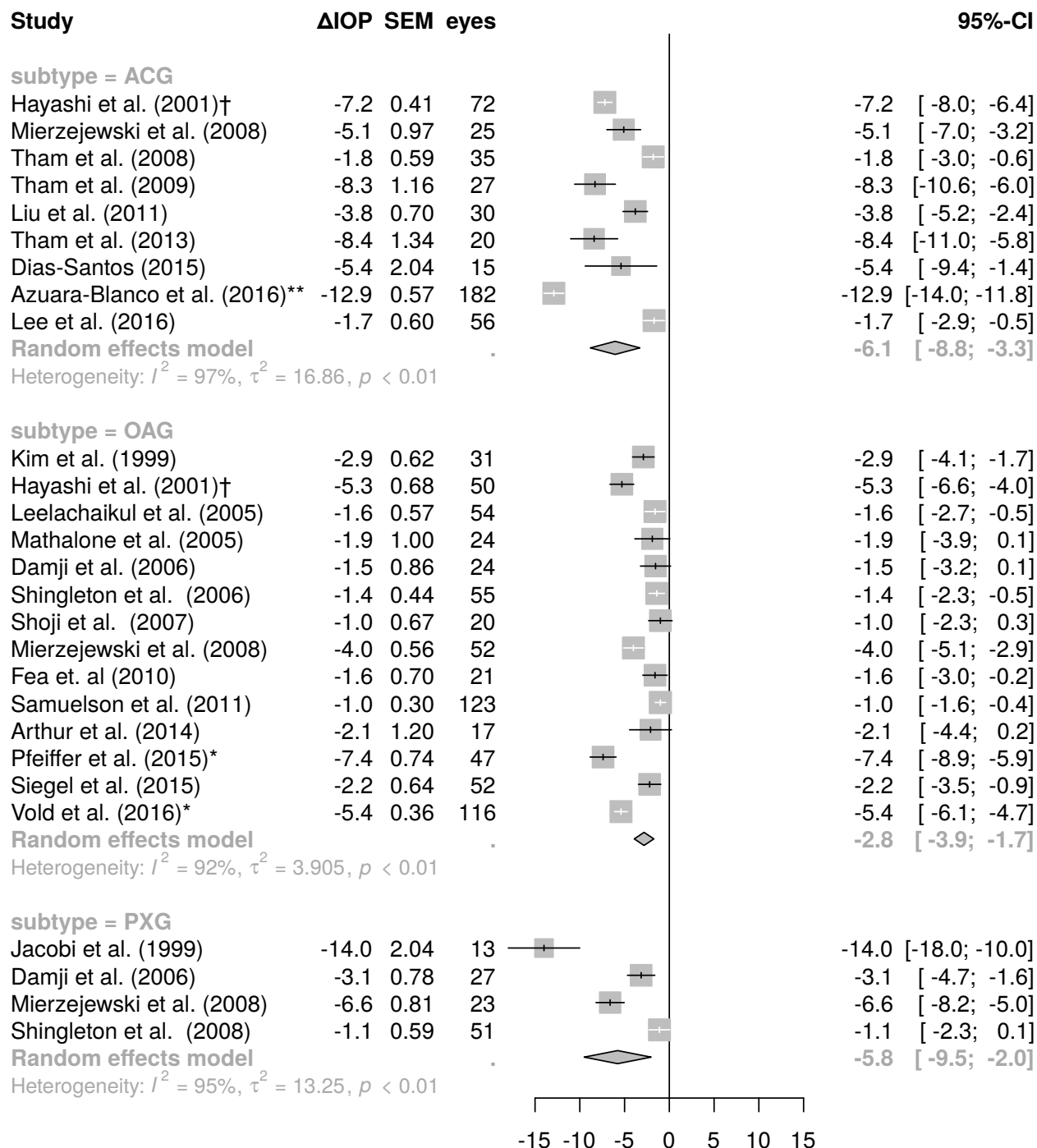
```
df_ <- df %>%
  filter(!is.na(OneYAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(OneYAbsIOPChangeMean,
  OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  study.name,
  data=df_,
  byvar=subtype,
  n.e=OneYEyes)
```

```
forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=FALSE,
  leftcols=c("studlab", "TE", "seTE", "n.e"),
  leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



Last period

```
df_ <- df %>%
  filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen>LastPeriodAbsIOPChangeMean,
      LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
      study.name,
      data=df_,
      byvar=subtype,
      n.e>LastPeriodEyes)
forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=FALSE,
  leftcols=c("studlab", "TE", "seTE", "n.e"),
  leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



Correlation among time points

Measure the correlation between different outcomes (IOP at 6 months vs. 12 months).

```
ggplot(df %>% filter(subtype != 'acute') %>% mutate(subtype = factor(subtype)),
  aes(x = SixMoAbsIOPChangeMean,
      xmin=SixMoAbsIOPChangeMean - 1.96*SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
      xmax=SixMoAbsIOPChangeMean + 1.96*SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
      y = OneYAbsIOPChangeMean,
```

```

      ymin= OneYAbsIOPChangeMean - 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
      ymax= OneYAbsIOPChangeMean + 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
      label=study.name,
      color=subtype
    )) +
  geom_abline(slope = 1, color="gray70") +
  geom_errorbar() +
  geom_errorbarh() +
  xlab('ΔIOP at 6 months') +
  ylab('ΔIOP at one year') +
  coord_fixed(xlim=c(-18, 0), ylim=c(-18,0))

```

```

## Warning: Removed 22 rows containing missing values (geom_errorbar).
## Warning: Removed 22 rows containing missing values (geom_errorbarh).
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted for <ce>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted for <94>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted for <ce>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :

```

```

## conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot
## substituted for <ce>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot
## substituted for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

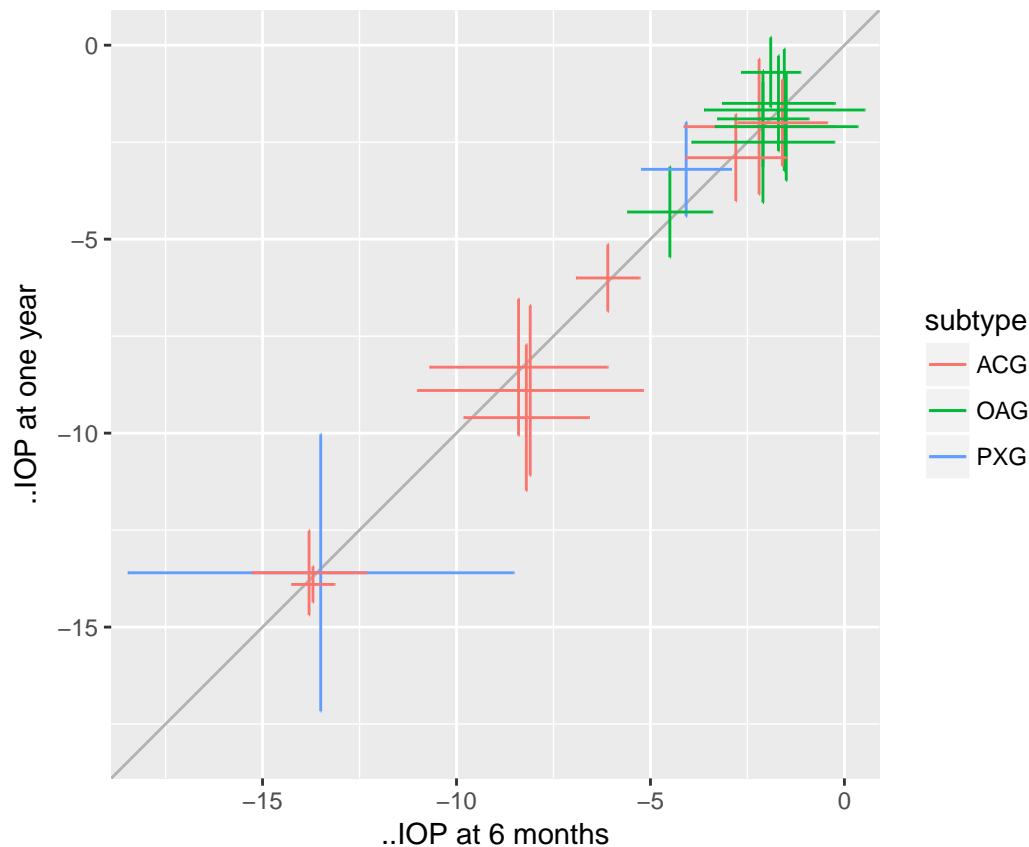
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot
## substituted for <ce>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot
## substituted for <94>

```

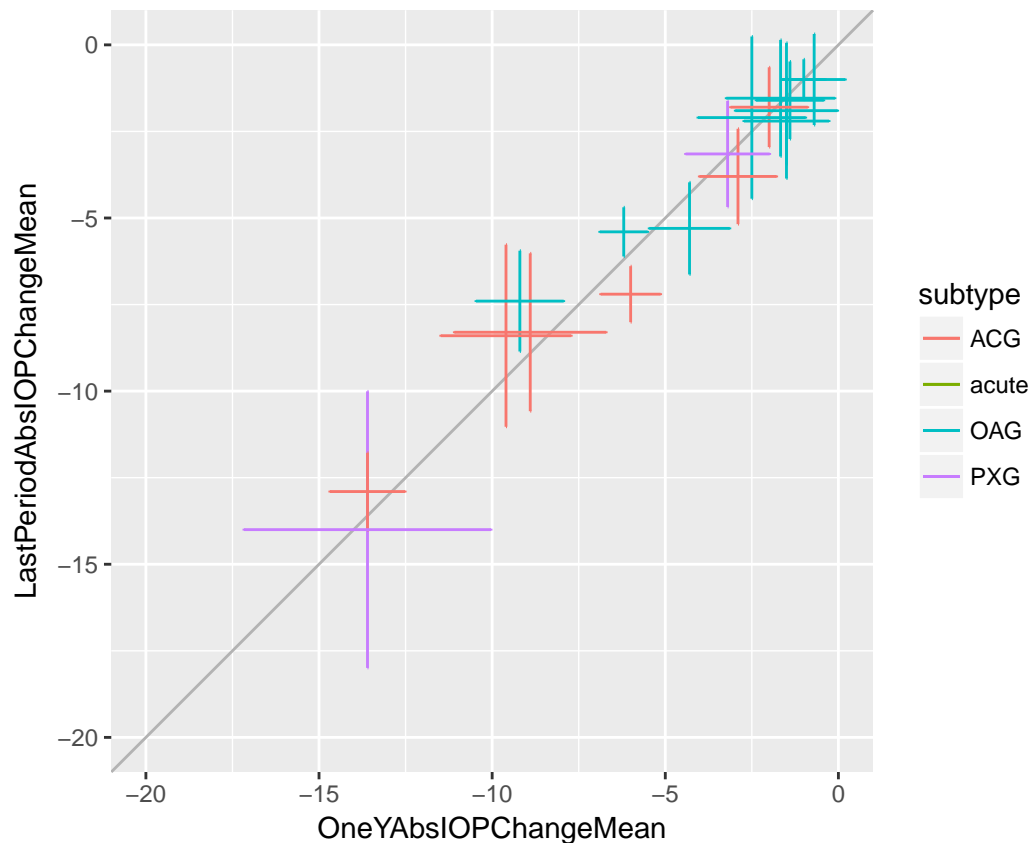
It's very clear that six months and 12 months IOP are highly correlated.

Similarly for one-year vs. last period:

```
ggplot(df, aes(y = LastPeriodAbsIOPChangeMean,
  ymin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
  ymax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
  x = OneYAbsIOPChangeMean,
  xmin= OneYAbsIOPChangeMean - 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  xmax= OneYAbsIOPChangeMean + 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  label=study.name,
  color=subtype
)) +
  geom_abline(slope = 1, color="gray70") +
  geom_errorbar() + geom_errorbarh() +
  coord_fixed(xlim=c(-20, 0), ylim=c(-20,0))
```

```
## Warning: Removed 26 rows containing missing values (geom_errorbar).
```

```
## Warning: Removed 26 rows containing missing values (geom_errorbarh).
```



Again, correlations are very high. Present this in another way.

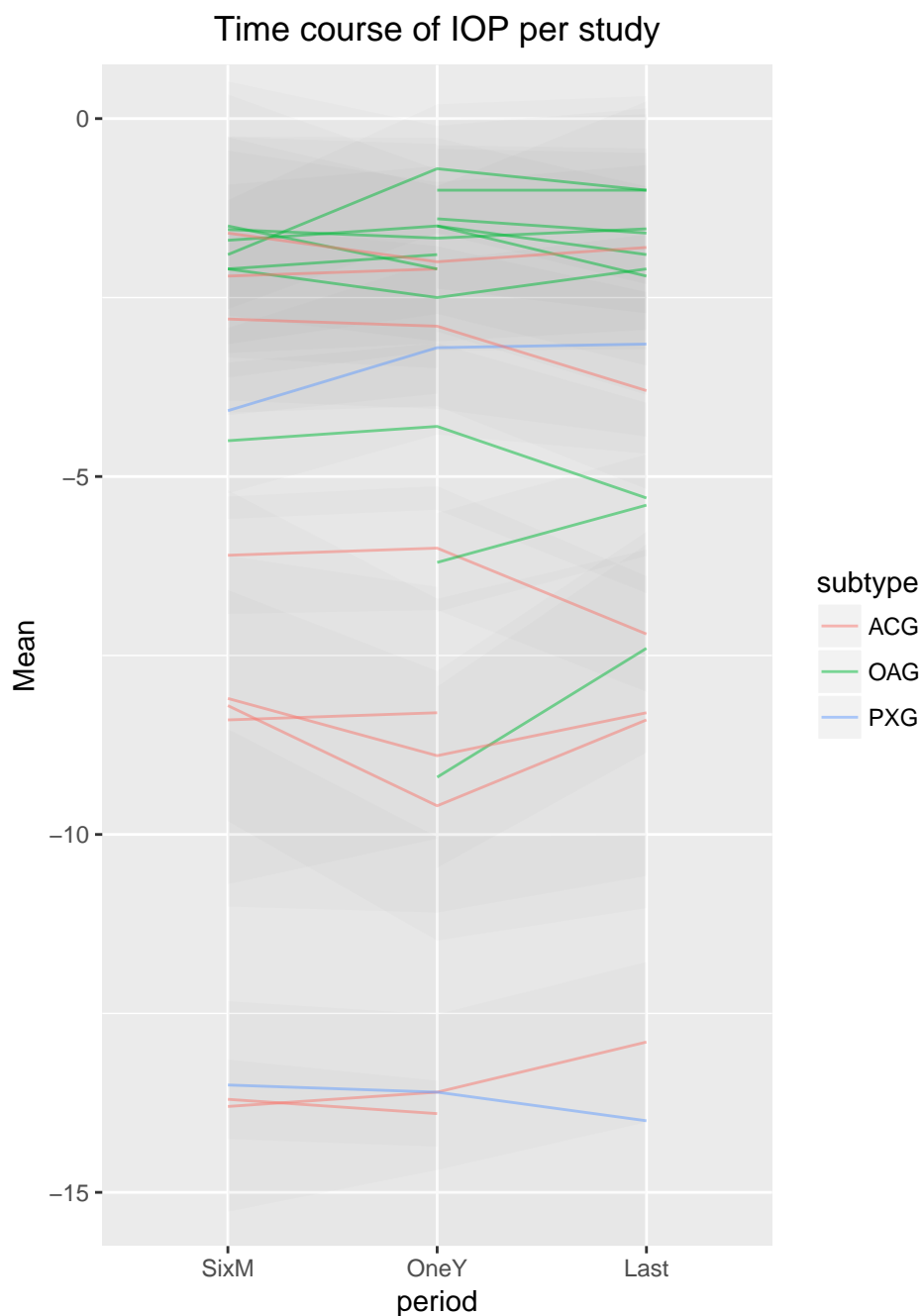
```
library(reshape2)
```

```
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
## smiths
nd <- melt(df %>%
  filter(MIGsYorN == 'N',
         subtype != 'acute',
         1*is.na(SixMoAbsIOPChangeMean) +
         1*is.na(OneYAbsIOPChangeMean) +
         1*is.na>LastPeriodAbsIOPChangeMean) < 2) %>%
  mutate(SixMoChangeSEM = SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
         OneYChangeSEM = OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
         LastPeriodChangeSEM = LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes)) %>%
  select(study.name, subtype,
         SixMoAbsIOPChangeMean,
         OneYAbsIOPChangeMean,
         LastPeriodAbsIOPChangeMean,
         SixMoChangeSEM,
         OneYChangeSEM,
         LastPeriodChangeSEM), id.vars=c("study.name", "subtype"))
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable)))
nd$period <- substr(nd$variable, 0, 4)
```

```

df_ <- dcast(nd, formula = study.name + subtype + period ~ metric)
df_ <- df_ %>% mutate(period = factor(period, c('SixM', 'OneY', 'Last')),
                      g = paste(study.name, as.character(subtype))) %>% filter(!is.na(Mean))
ggplot(df_, aes(y = Mean,
                ymin=Mean - 1.96*eSEM,
                ymax=Mean + 1.96*eSEM,
                x = period,
                label=study.name,
                group=g)) +
  geom_ribbon(alpha=.02) +
  geom_line(alpha=.5, aes(color=subtype)) +
  coord_cartesian(y=c(-15, 0)) + ggtitle('Time course of IOP per study') + theme(plot.title = element_t

```



It's remarkable how consistent measurements are between time periods. At most, we find a change of ± 2.5 mm Hg between the first and last period.

```
df_ <- df %>% filter(subtype=='OAG')
drawn.corr <- with(df_, replicate(n = 100,
  draw.corr(SixMoAbsIOPChangeMean,
    SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
    OneYAbsIOPChangeMean,
    OneYAbsIOPChangeStdDev / sqrt(OneYEyes))))
cat("Mean +- SE correlation, OAG only\n")

## Mean +- SE correlation, OAG only
```

```

print(mean(drawn.corrs))

## [1] 0.6338953
print(sd(drawn.corrs))

## [1] 0.1782464
df_ <- df
drawn.corrs <- with(df_, replicate(n = 100,
                                   draw.corr(SixMoAbsIOPChangeMean,
                                              SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
                                              OneYAbsIOPChangeMean,
                                              OneYAbsIOPChangeStdDev / sqrt(OneYEyes))))
cat("Mean +- SE correlation, All subtypes\n")

## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))

## [1] 0.9922153
print(sd(drawn.corrs))

## [1] 0.00318651

```

This is also reflected in the correlations - even accounting for noise, the correlations are $> .9$ between month 6 and month 12.

Multivariate inference

Let's use mvmeta to infer the effect size for all periods together.

```

library(mvmeta)

## This is mvmeta 0.4.7. For an overview type: help('mvmeta-package').
fill.na <- function(x, y, z) {
  return(ifelse(!is.na(x),
                x,
                ifelse(is.na(y),
                      z,
                      ifelse(is.na(z),
                            y,
                            sqrt((y**2 + z**2) / 2 )))))
}

get.correlation.matrices.tri <- function(x, y, z, assumed.rho) {
  S <- list()
  for(i in 1:length(x)) {
    xx <- fill.na(x[i], y[i], z[i])
    yy <- fill.na(y[i], x[i], z[i])
    zz <- fill.na(z[i], x[i], y[i])
    S[[i]] <- matrix(c(xx ** 2, xx * yy * assumed.rho, xx * zz * assumed.rho ** 2,
                      xx * yy * assumed.rho, yy ** 2, zz * yy * assumed.rho,
                      xx * zz * assumed.rho ** 2, zz * yy * assumed.rho, zz ** 2), ncol=3)
  }
}

```

```

S
}

df_ <- df %>% filter(!is.na>LastPeriodAbsIOPChangeStdDev) |
               !is.na(SixMoAbsIOPChangeStdDev) |
               !is.na(OneYAbsIOPChangeStdDev), subtype %in% c('OAG', 'ACG'), MIGsYorN == 'N')

thefit <- mvmeta(cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean, LastPeriodAbsIOPChangeMean) ~ subtype,
                S=get.correlation.matrices.tri(df_$SixMoAbsIOPChangeStdDev / sqrt(df_$SixMoEyes),
                                                df_$OneYAbsIOPChangeStdDev / sqrt(df_$OneYEyes),
                                                df_$LastPeriodAbsIOPChangeStdDev / sqrt(df_$LastPeriodEyes), .7),
                data=df_,
                method="reml")

summary(thefit)

## Call: mvmeta(formula = cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean,
## LastPeriodAbsIOPChangeMean) ~ subtype, S = get.correlation.matrices.tri(df_$SixMoAbsIOPChangeStdDev,
## df_$OneYAbsIOPChangeStdDev/sqrt(df_$OneYEyes), df_$LastPeriodAbsIOPChangeStdDev/sqrt(df_$LastPeriodEyes),
## 0.7), data = df_, method = "reml")
##
## Multivariate random-effects meta-regression
## Dimension: 3
## Estimation method: REML
##
## Fixed-effects coefficients
## SixMoAbsIOPChangeMean :
##      Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -5.9098    0.7513 -7.8665  0.0000  -7.3823  -4.4374
## subtypeOAG    2.9020    1.0528  2.7565  0.0058   0.8386   4.9655
##
## (Intercept) ***
## subtypeOAG **
## OneYAbsIOPChangeMean :
##      Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -6.0950    0.7609 -8.0102  0.0000  -7.5863  -4.6036
## subtypeOAG    3.3757    1.0581  3.1904  0.0014   1.3019   5.4495
##
## (Intercept) ***
## subtypeOAG **
## LastPeriodAbsIOPChangeMean :
##      Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -6.2590    0.6797 -9.2084  0.0000  -7.5912  -4.9268
## subtypeOAG    3.5727    0.9342  3.8244  0.0001   1.7417   5.4036
##
## (Intercept) ***
## subtypeOAG ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Between-study random-effects (co)variance components
## Structure: General positive-definite
##
##      Std. Dev      Corr
## SixMoAbsIOPChangeMean 2.9887 SixMoAbsIOPChangeMean

```

```

## OneYAbsIOPChangeMean      3.0250      0.9981
## LastPeriodAbsIOPChangeMean 2.6049      0.9918
##
## SixMoAbsIOPChangeMean      OneYAbsIOPChangeMean
## OneYAbsIOPChangeMean
## LastPeriodAbsIOPChangeMean      0.9820
##
## Multivariate Cochran Q-test for residual heterogeneity:
## Q = 1622.3062 (df = 62), p-value = 0.0000
## I-square statistic = 96.2%
##
## 36 studies, 68 observations, 6 fixed and 6 random-effects parameters
##      logLik      AIC      BIC
## -118.7214    261.4428    286.9685

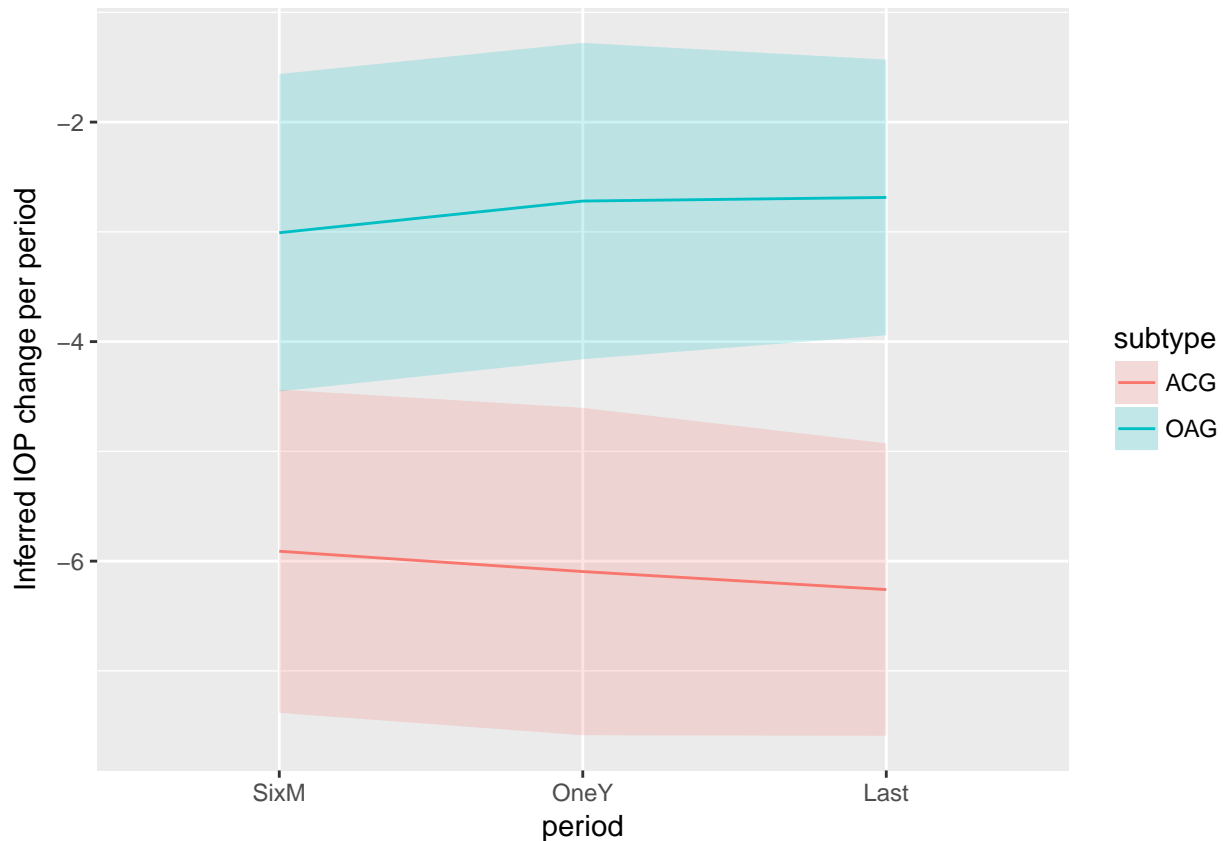
newdata <- data.frame(subtype=c('OAG', 'ACG'))
pred <- predict(thefit, newdata, se=TRUE)
newdata$SixMoAbsIOPChangeMean <- pred$fit[,1]
newdata$OneYAbsIOPChangeMean <- pred$fit[,2]
newdata$LastPeriodAbsIOPChangeMean <- pred$fit[,3]
newdata$SixMoAbsIOPChangeSEM <- pred$se[,1]
newdata$OneYAbsIOPChangeSEM <- pred$se[,2]
newdata$LastPeriodAbsIOPChangeSEM <- pred$se[,3]

library(reshape2)
nd <- melt(newdata)

## Using subtype as id variables

nd$period <- substr(nd$variable, 0, 4)
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable)))
df_ <- dcast(nd, formula = subtype + period ~ metric)
df_$period <- factor(df_$period, c('SixM', 'OneY', 'Last'))
ggplot(df_, aes(x=period,
                y=Mean,
                ymin=Mean - 1.96*eSEM,
                ymax=Mean + 1.96*eSEM,
                group=subtype,
                fill=subtype)) + geom_ribbon(alpha=.2) + geom_line(aes(color=subtype)) + ylab("Inferred

```



Meta-regression

Consider relationships between different covariates and outcomes. Focus on the IOP drop at one year and its correlation with different factors.

```
df <- read.data()

## These retrospective studies are losing eyes per period - not impossible, but unusual:
## Mathalone et al. (2005)
## Leelachaikul et al. (2005)
## Shoji et al. (2007)
## Liu et al. (2011)
## Arthur et al. (2014)
## Tetz et al. (2015)

## These retrospective studies are gaining eyes as the study goes
## Samuelson et al. (2011)
df_ <- df %>% filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen>LastPeriodAbsIOPChangeMean,
  LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
  study.name,
  data=df_,
  byvar=subtype,
  n.e=OneYEyes)
```



```

print(metareg(~ LastPeriodEyes, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      26.2889 (SE = 9.7171)
## tau (square root of estimated tau^2 value):             5.1273
## I^2 (residual heterogeneity / unaccounted variability): 98.62%
## H^2 (unaccounted variability / sampling variability):    72.68
## R^2 (amount of heterogeneity accounted for):             0.00%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 2253.1681, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.7930, p-val = 0.3732
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt          -3.5079  1.4751  -2.3781  0.0174  -6.3990  -0.6168 *
## LastPeriodEyes   -0.0231  0.0259  -0.8905  0.3732  -0.0739   0.0277
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ LastPeriodEyes * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      15.5751 (SE = 5.9007)
## tau (square root of estimated tau^2 value):             3.9465
## I^2 (residual heterogeneity / unaccounted variability): 97.52%
## H^2 (unaccounted variability / sampling variability):    40.31
## R^2 (amount of heterogeneity accounted for):             36.33%
##
## Test for Residual Heterogeneity:
## QE(df = 27) = 1088.2629, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 13.4471, p-val = 0.0195
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb
## intrcpt          -2.0693  1.8551  -1.1155  0.2646  -5.7052
## LastPeriodEyes   -0.0135  0.0329  -0.4120  0.6804  -0.0779
## subtypeACG        -2.2003  2.4998  -0.8802  0.3788  -7.0998
## subtypePXG       -12.1589  5.1416  -2.3648  0.0180 -22.2362
## LastPeriodEyes:subtypeACG -0.0323  0.0421  -0.7661  0.4436  -0.1149
## LastPeriodEyes:subtypePXG  0.2999  0.1514   1.9815  0.0475   0.0033
##               ci.ub
## intrcpt          1.5666

```

```

## LastPeriodEyes          0.0509
## subtypeACG              2.6993
## subtypePXG             -2.0816 *
## LastPeriodEyes:subtypeACG 0.0503
## LastPeriodEyes:subtypePXG 0.5966 *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ Year, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):    22.3626 (SE = 8.2491)
## tau (square root of estimated tau^2 value):           4.7289
## I^2 (residual heterogeneity / unaccounted variability): 98.40%
## H^2 (unaccounted variability / sampling variability):  62.31
## R^2 (amount of heterogeneity accounted for):           8.59%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 1931.7117, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.0819, p-val = 0.7747
##
## Model Results:
##
##      estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt  88.5741  325.2895   0.2723  0.7854  -548.9816  726.1299
## Year    -0.0463   0.1619  -0.2862  0.7747   -0.3636   0.2709
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ Year * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):    13.5468 (SE = 4.9600)
## tau (square root of estimated tau^2 value):           3.6806
## I^2 (residual heterogeneity / unaccounted variability): 97.20%
## H^2 (unaccounted variability / sampling variability):  35.66
## R^2 (amount of heterogeneity accounted for):           44.63%
##
## Test for Residual Heterogeneity:
## QE(df = 27) = 962.7471, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 12.3857, p-val = 0.0299
##
## Model Results:
##
##      estimate      se      zval      pval      ci.lb

```

```

## intrcpt          101.1538   357.3868   0.2830   0.7771  -599.3116
## Year             -0.0517    0.1779  -0.2906   0.7713   -0.4003
## subtypeACG       214.7869   582.6862   0.3686   0.7124  -927.2571
## subtypePXG      -2425.5918  1161.6203  -2.0881   0.0368 -4702.3259
## Year:subtypeACG   -0.1086    0.2898  -0.3746   0.7079   -0.6766
## Year:subtypePXG    1.2078    0.5791   2.0857   0.0370    0.0728
##               ci.lb      ci.ub
## intrcpt          801.6191
## Year              0.2969
## subtypeACG       1356.8308
## subtypePXG       -148.8578 *
## Year:subtypeACG    0.4594
## Year:subtypePXG    2.3428 *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ PreOpIOPMean, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      5.0212 (SE = 1.8093)
## tau (square root of estimated tau^2 value):             2.2408
## I^2 (residual heterogeneity / unaccounted variability): 92.99%
## H^2 (unaccounted variability / sampling variability):    14.27
## R^2 (amount of heterogeneity accounted for):             79.48%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 442.4006, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 57.3287, p-val < .0001
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt          11.3282   2.1248   5.3314 <.0001    7.1637   15.4927 ***
## PreOpIOPMean     -0.7855   0.1037  -7.5716 <.0001   -0.9889   -0.5822 ***
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ PreOpIOPMean * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      1.3334 (SE = 0.5546)
## tau (square root of estimated tau^2 value):             1.1547
## I^2 (residual heterogeneity / unaccounted variability): 77.07%
## H^2 (unaccounted variability / sampling variability):    4.36
## R^2 (amount of heterogeneity accounted for):             94.55%
##
## Test for Residual Heterogeneity:

```

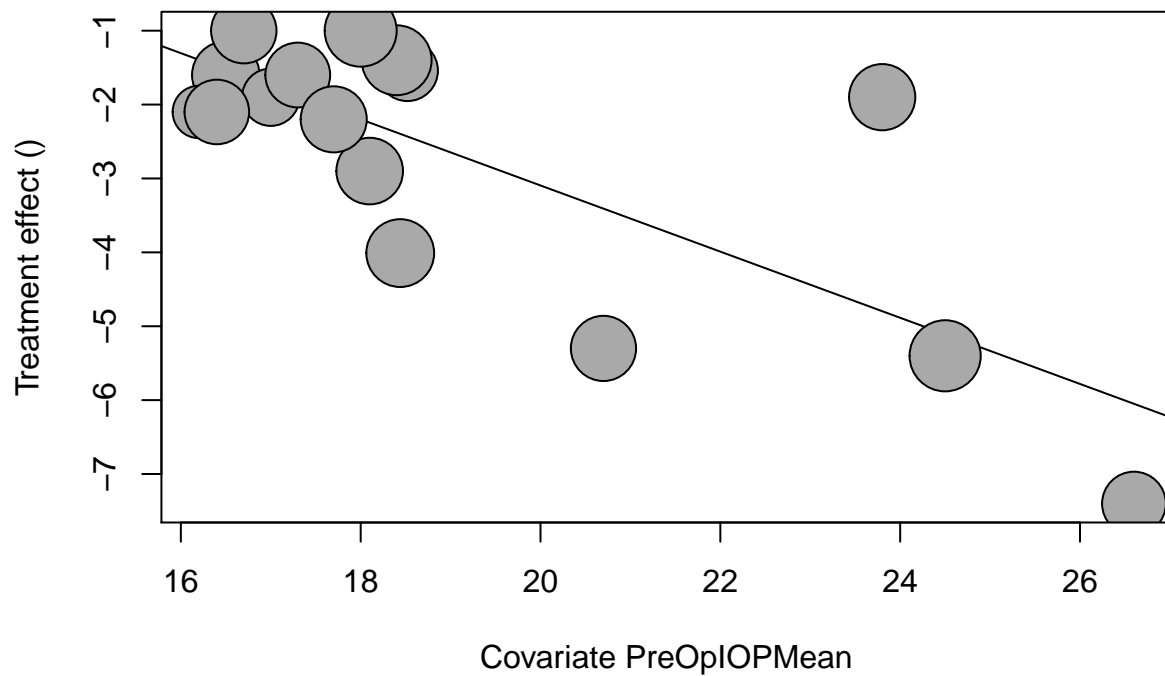
```

## QE(df = 27) = 117.7706, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 202.5133, p-val < .0001
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb
## intrcpt          5.8523  2.1039   2.7816  0.0054   1.7287
## PreOpIOPMean     -0.4475  0.1084  -4.1298 <.0001  -0.6598
## subtypeACG        5.6044  2.7819   2.0146  0.0439   0.1521
## subtypePXG        8.8320  4.5158   1.9558  0.0505  -0.0189
## PreOpIOPMean:subtypeACG -0.4148  0.1374  -3.0181  0.0025  -0.6841
## PreOpIOPMean:subtypePXG -0.4778  0.2177  -2.1947  0.0282  -0.9046
##               ci.ub
## intrcpt          9.9759  **
## PreOpIOPMean     -0.2351  ***
## subtypeACG       11.0568   *
## subtypePXG       17.6829   .
## PreOpIOPMean:subtypeACG -0.1454  **
## PreOpIOPMean:subtypePXG -0.0511   *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# Same, restricted to OAG only
df_ <- df %>% filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "OAG", MIGsYorN == 'N') %>%
  mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)

bubble(metareg(~ PreOpIOPMean, x=m))

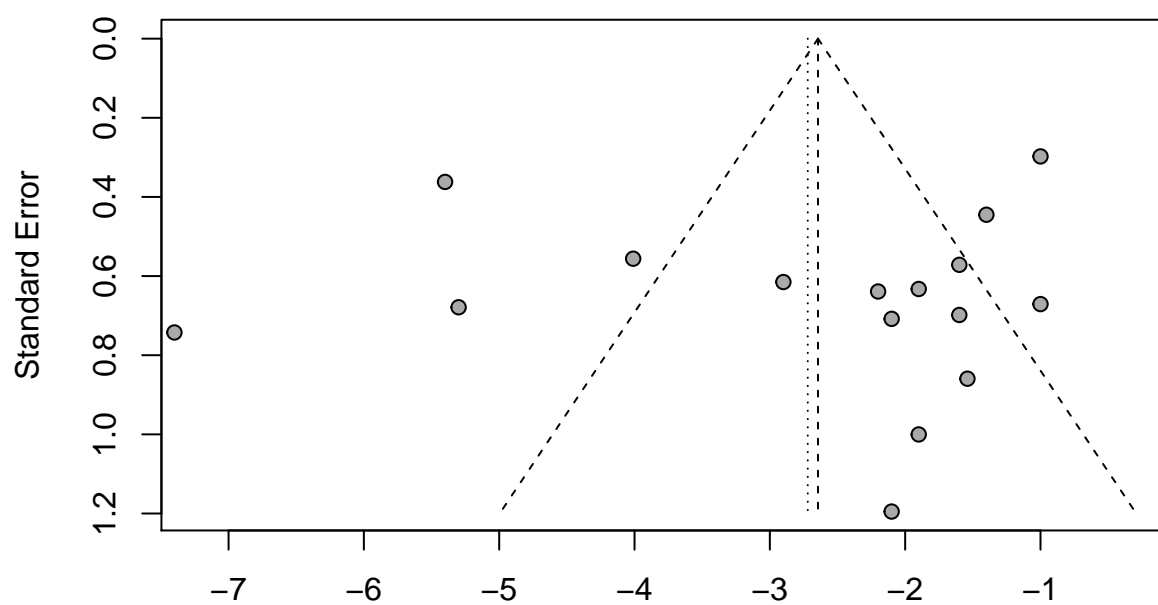
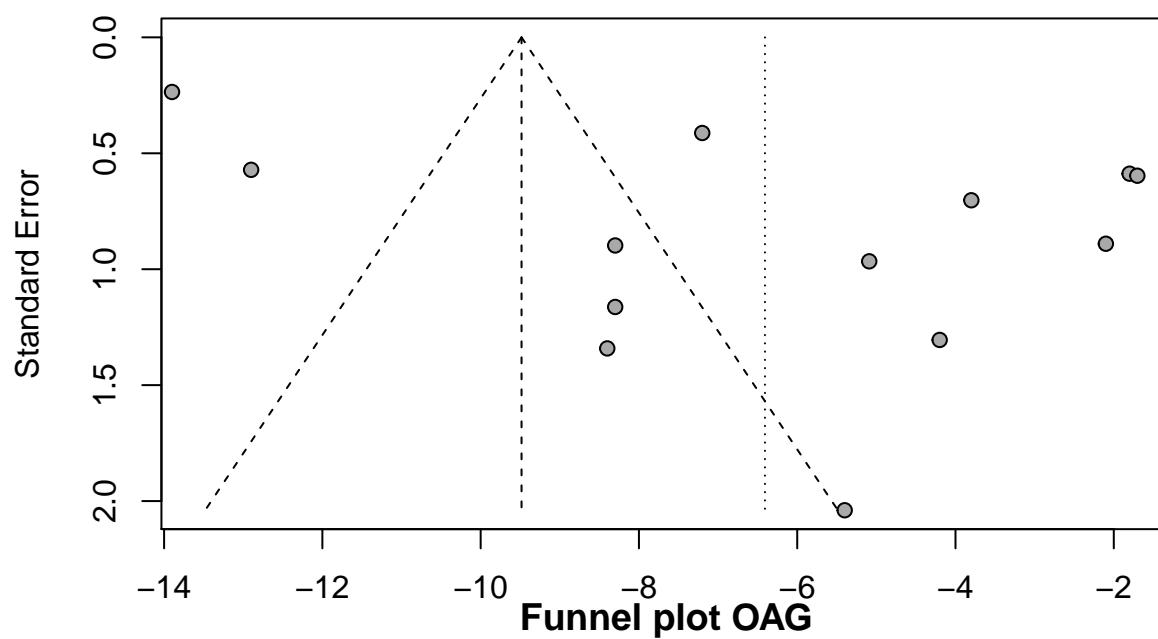
```



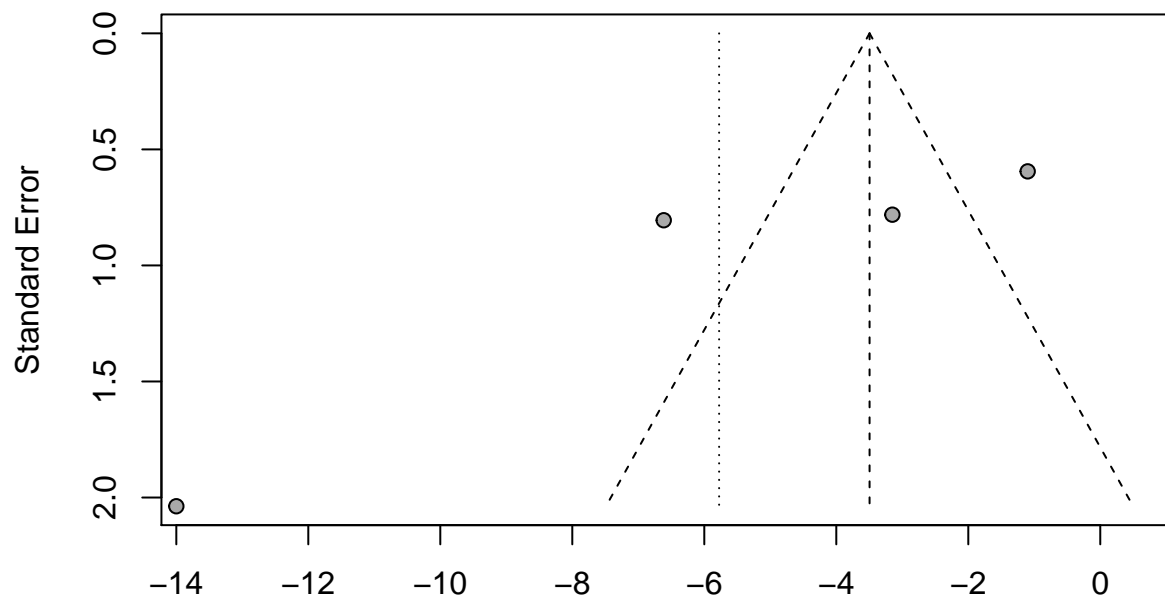
Small study bias

```
df_ <- df %>% filter(!is.na(df$LastPeriodAbsIOPChangeMean),
                     df$subtype != "acute",
                     MIGsYorN == 'N') %>% mutate(subtype=factor(subtype))
for(l in levels(df_$subtype)) {
  m <- metagen(LastPeriodAbsIOPChangeMean,
               LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
               study.name,
               data=df_ %>% filter(subtype == l),
               n.e=LastPeriodEyes)
  funnel(m)
  title(paste('Funnel plot', l))
}
```

Funnel plot ACG

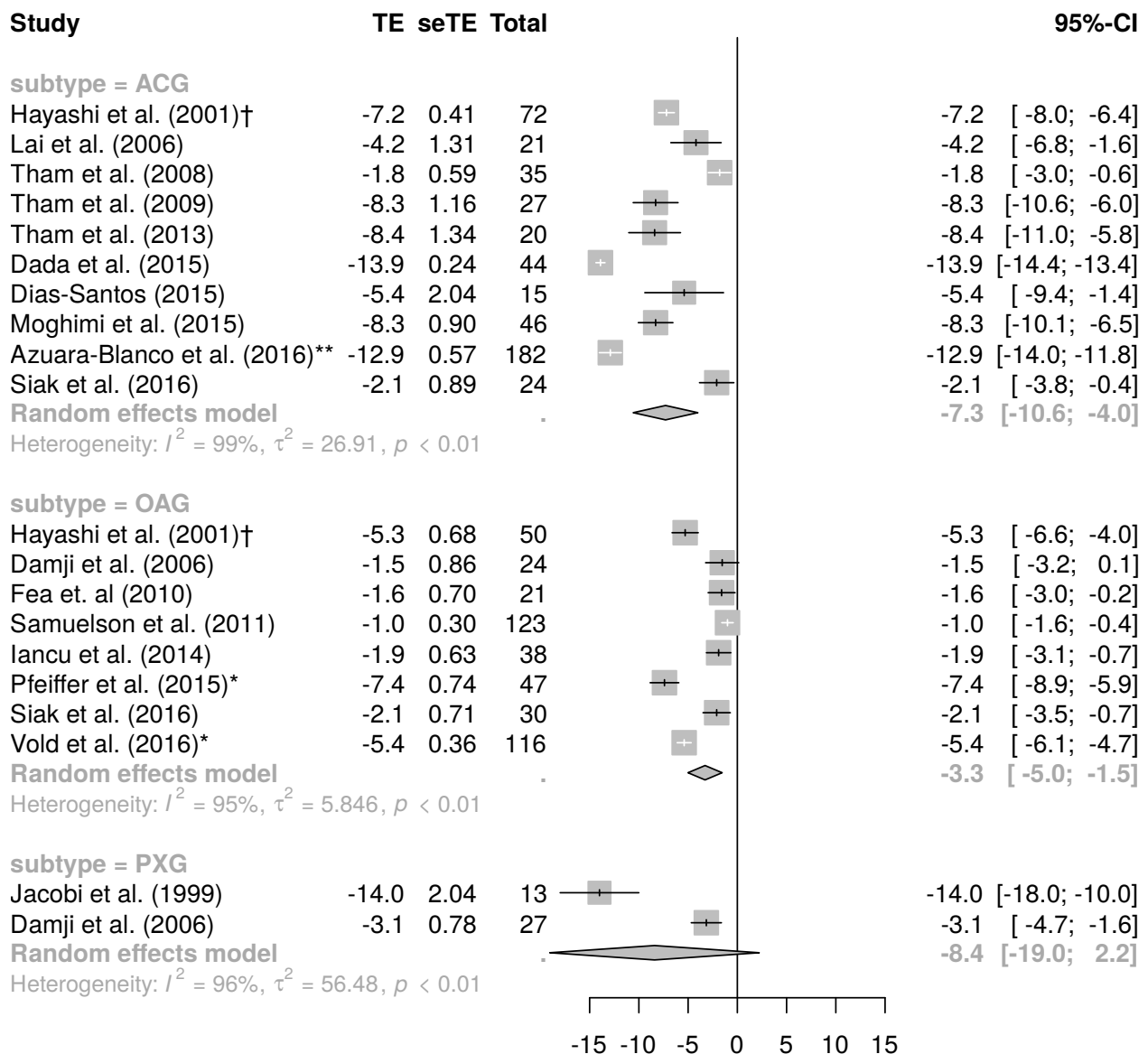


Funnel plot PXG



Alternative filterings of the data

Prospective studies only



Meds

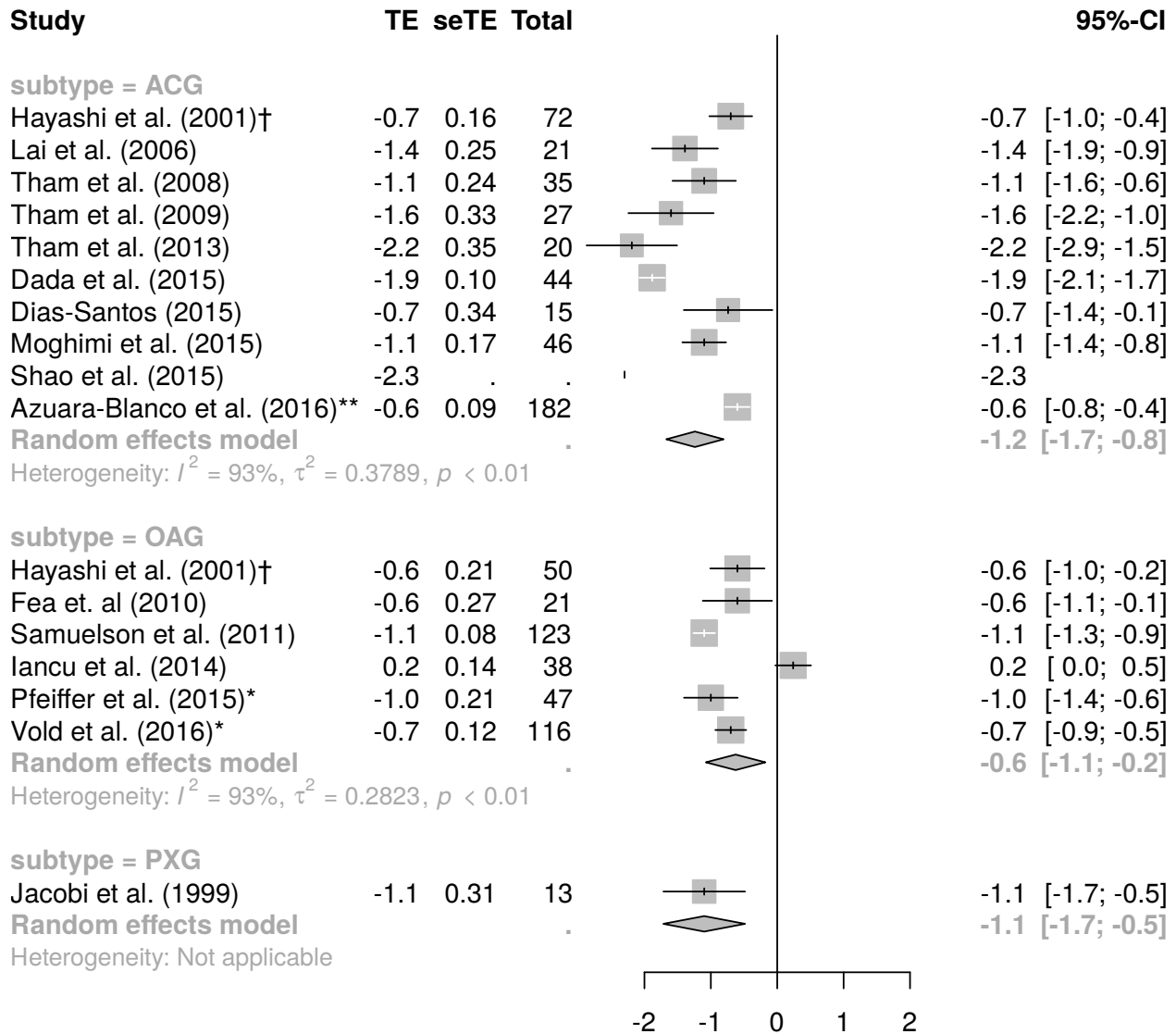
```
df_ <- df %>%
  filter(!is.na(RxChangeMean), !is.na(RxChangeStdDev),
         df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             sqrt(RxPostOpStdDev** 2 + RxPreOpStdDev ** 2) / sqrt>LastPeriodEyes),
           study.name,
           data=df_,
```



```

byvar=subtype,
n.e=LastPeriodEyes)
forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=FALSE,
  leftcols=c("studlab", "TE", "seTE", "n.e"))

```



Excluding washout studies

Last period

```

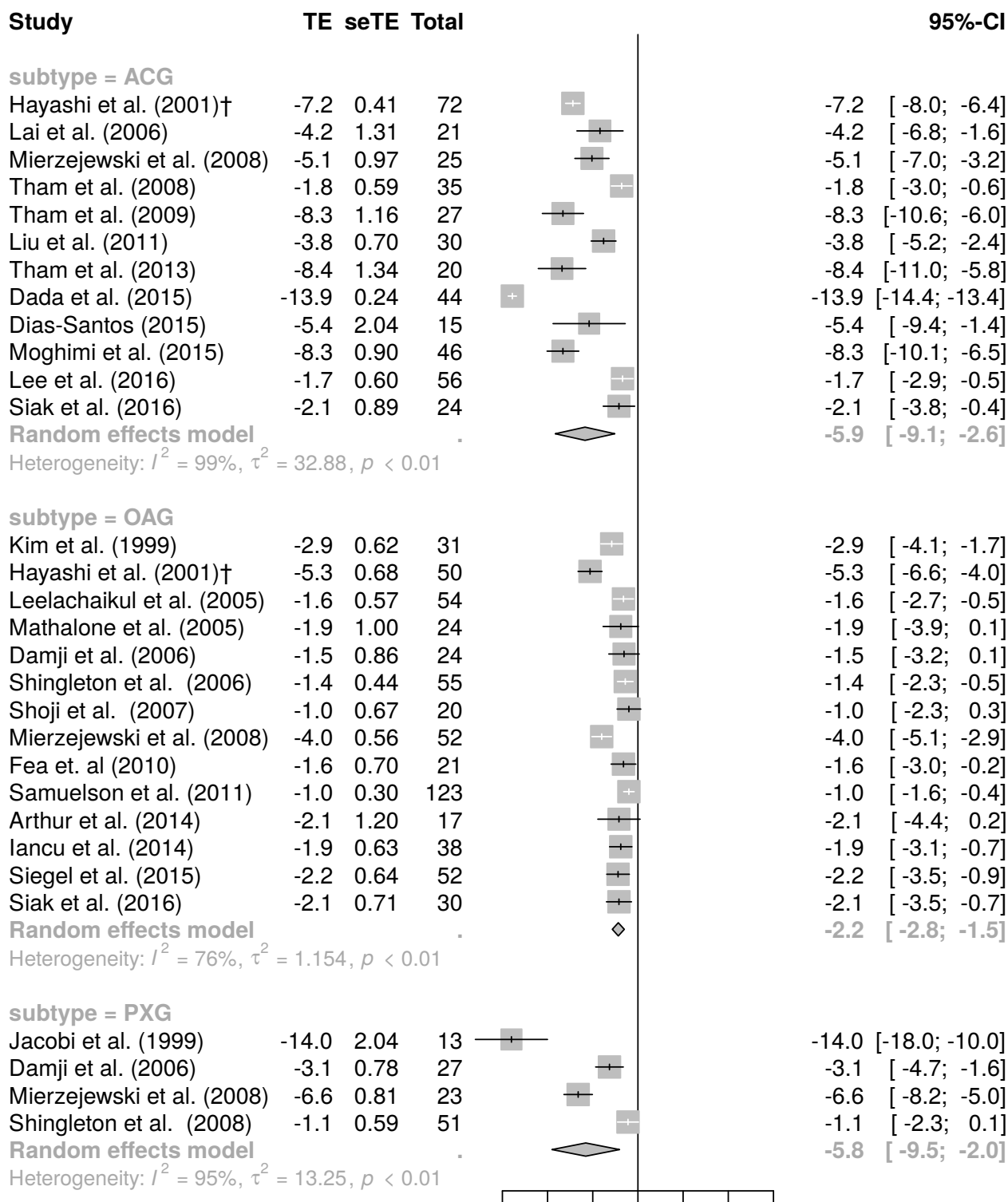
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))

```

```

m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"))

```



Meds

```
df_ <- df %>%
  filter(!is.na(RxChangeMean), !is.na(RxChangeStdDev),
```

```

      df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             sqrt(RxPostOpStdDev** 2 + RxPreOpStdDev ** 2) / sqrt>LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e>LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"))

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

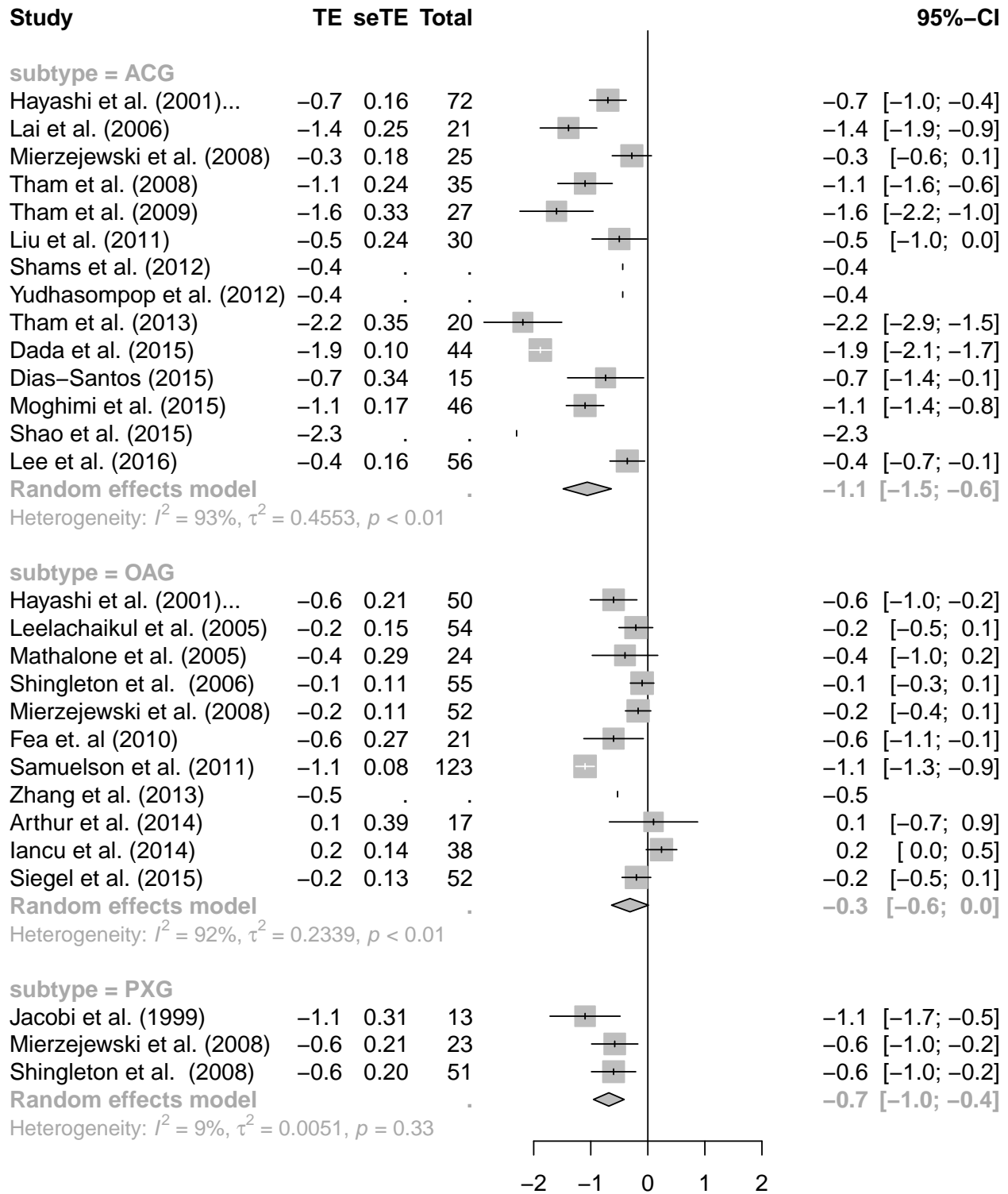
```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```
## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>
```



Sensitivity to missingness

Simulate what the results would look like if there was no effect in the eyes lost to follow up ($\Delta IOP = 0$).

```
meta.analysis.with.sensitivity <- function(missingness='zero') {
  df <- read.data()
  df <- filter.data(df, 'prospective')

  df_ <- df %>%
    filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute") %>%
    mutate(subtype=factor(subtype))

  # Simulate a 0 effect in the unobserved fraction.
  df.missing <- df_
  if(missingness == 'zero') {
    # Zero out.
    df.missing <- df.missing %>% mutate>LastPeriodEyes = PreOpEyes - LastPeriodEyes,
      LastPeriodAbsIOPChangeMean = 0)
  } else {
    # Add 5 mm Hg to each missing eye.
    df.missing <- df.missing %>% mutate>LastPeriodEyes = PreOpEyes - LastPeriodEyes,
      LastPeriodAbsIOPChangeMean = LastPeriodAbsIOPChangeMean + 5)
  }

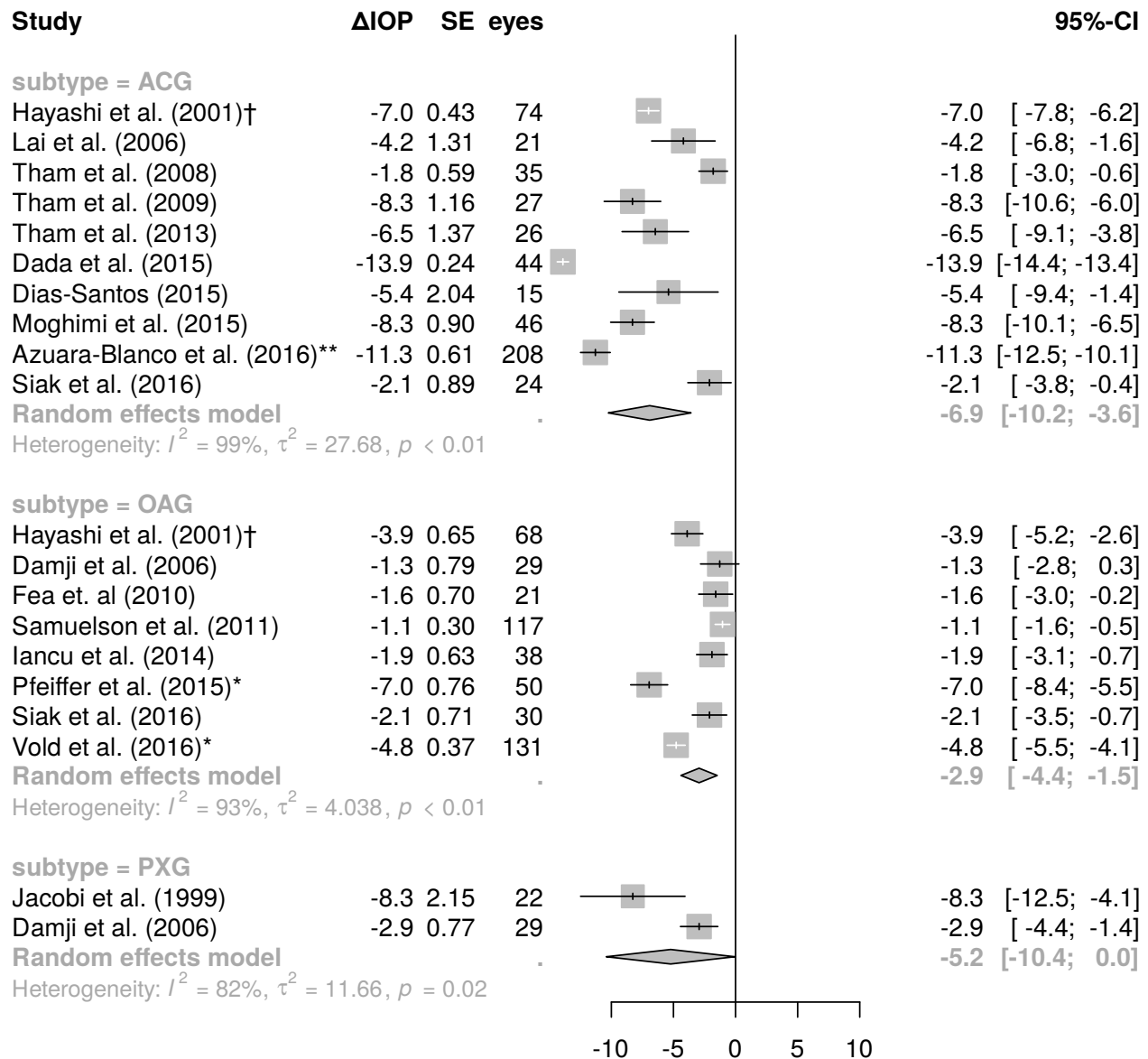
  df_ <- rbind(df_, df.missing)
  # Aggregate two by two
  for(i in seq(nrow(df.missing), 1)) {
    idx <- rep(FALSE, nrow(df_))
    idx[i] <- TRUE
    idx[i*2] <- TRUE
    df_ <- agg.arms(df_, idx)
  }

  df_ <- df_ %>% dplyr::arrange(Year, study.name)

  m <- metagen>LastPeriodAbsIOPChangeMean,
    LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
    study.name,
    data=df_,
    byvar=subtype,
    n.e=LastPeriodEyes)
  forest(m,
    comb.fixed=FALSE,
    digits=1,
    digits.se = 2,
    overall=FALSE,
    leftcols=c("studlab", "TE", "seTE", "n.e"),
    leftlabs=c("Study", " $\Delta IOP$ ", "SE", "eyes"))
}

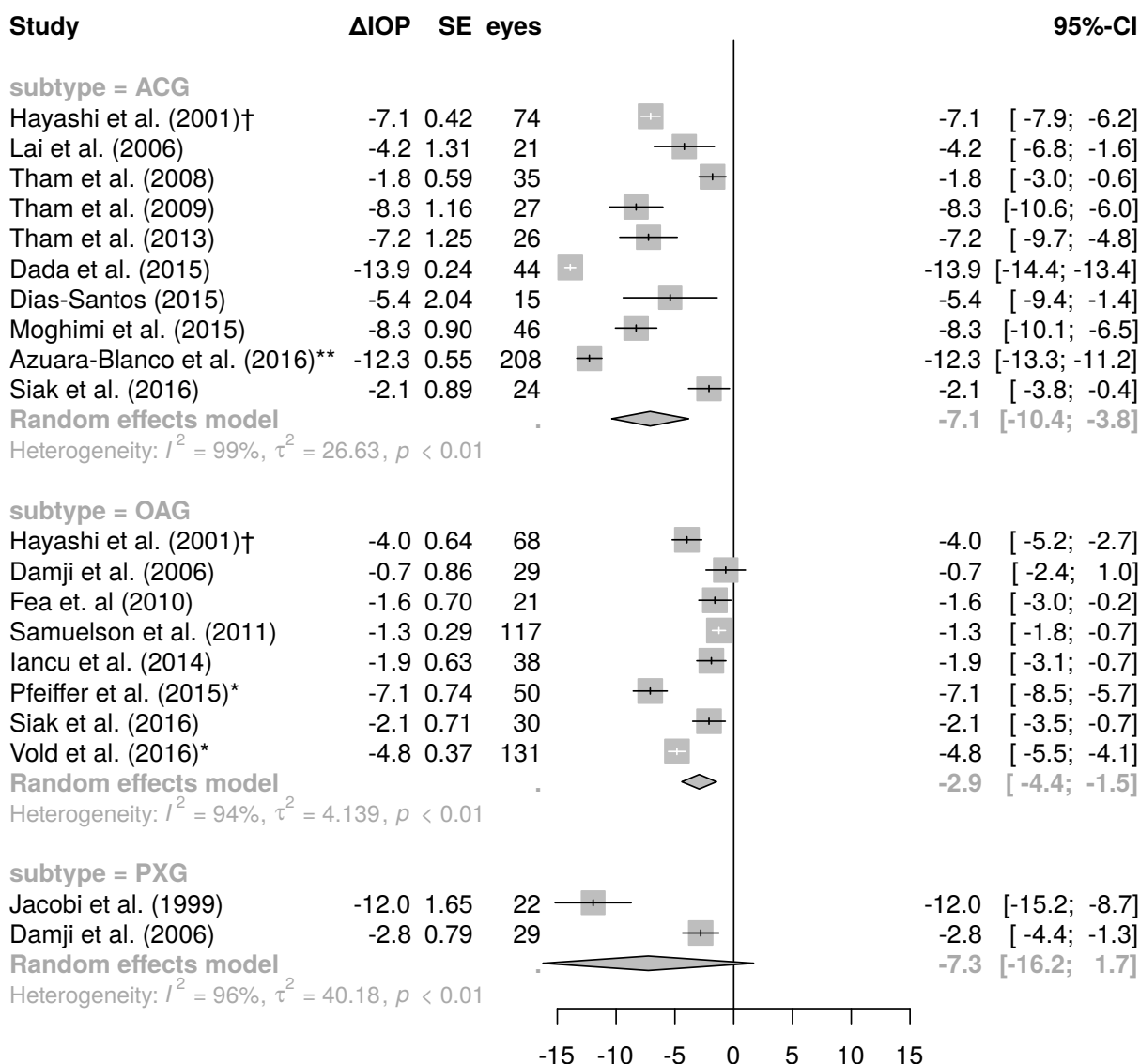
meta.analysis.with.sensitivity()
grid.text(paste0("Simulated net change IOP when  $\Delta IOP = 0$  in eyes lost to follow up"), .5, .97, gp=gpar(
```

Simulated net change IOP when $\Delta IOP = 0$ in eyes lost to follow up



```
meta.analysis.with.sensitivity('five')
grid.text(paste0("Simulated net change IOP when  $\Delta IOP = 5$  mm Hg higher in eyes lost to follow up"), .5,
```

Simulated net change IOP when $\Delta\text{IOP} = 5$ mm Hg higher in eyes lost to follow up



MIGS

We don't report these results because it's a bit misleading – the studies aren't very similar to each other, and we don't use the information in their control arms. We can do a much better job through, for example, network meta-analysis, which we plan to do in a future paper.

```
df <- read.data(drop.migs = FALSE)
```

```
## These retrospective studies are losing eyes per period - not impossible, but unusual:
## Mathalone et al. (2005)
## Leelachaikul et al. (2005)
## Shoji et al. (2007)
## Liu et al. (2011)
```



```
## Arthur et al. (2014)
## Tetz et al. (2015)

## These retrospective studies are gaining eyes as the study goes

## Samuelson et al. (2011)

df_ <- df %>%
  filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'Y') %>%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(TypesofMIGSifany, Year)
m <- metagen>LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
  study.name,
  data=df_,
  n.e>LastPeriodEyes)

forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=TRUE,
  leftcols=c("studlab", "TE", "seTE", "n.e", "TypesofMIGSifany"),
  leftlabs=c("Study", "TE", "seTE", "Total", "Type"))
```

