

Phaco meta analysis

Patrick Mineault

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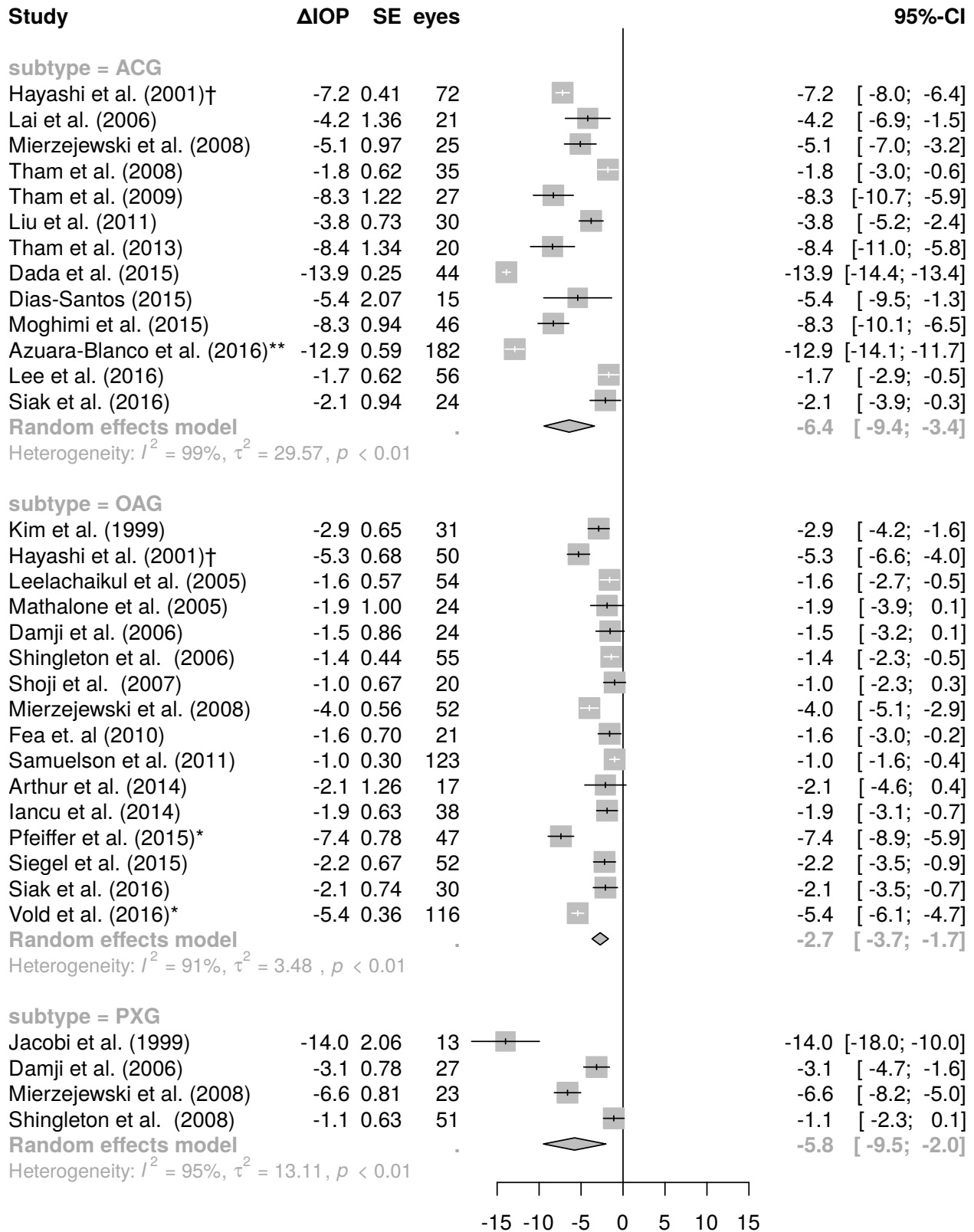
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Analysis of full dataset

Main analysis: 12-month+ follow up

```
df_ <- df %>%
  filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen>LastPeriodAbsIOPChangeMean,
      LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
      study.name,
      data=df_,
      byvar=subtype,
```

```
        n.e=LastPeriodEyes)
forest(m,
      comb.fixed=FALSE,
      digits=1,
      digits.se = 2,
      overall=FALSE,
      leftcols=c("studlab", "TE", "seTE", "n.e"),
      leftlabs=c("Study", "ΔIOP", "SE", "eyes"))
```



Acute

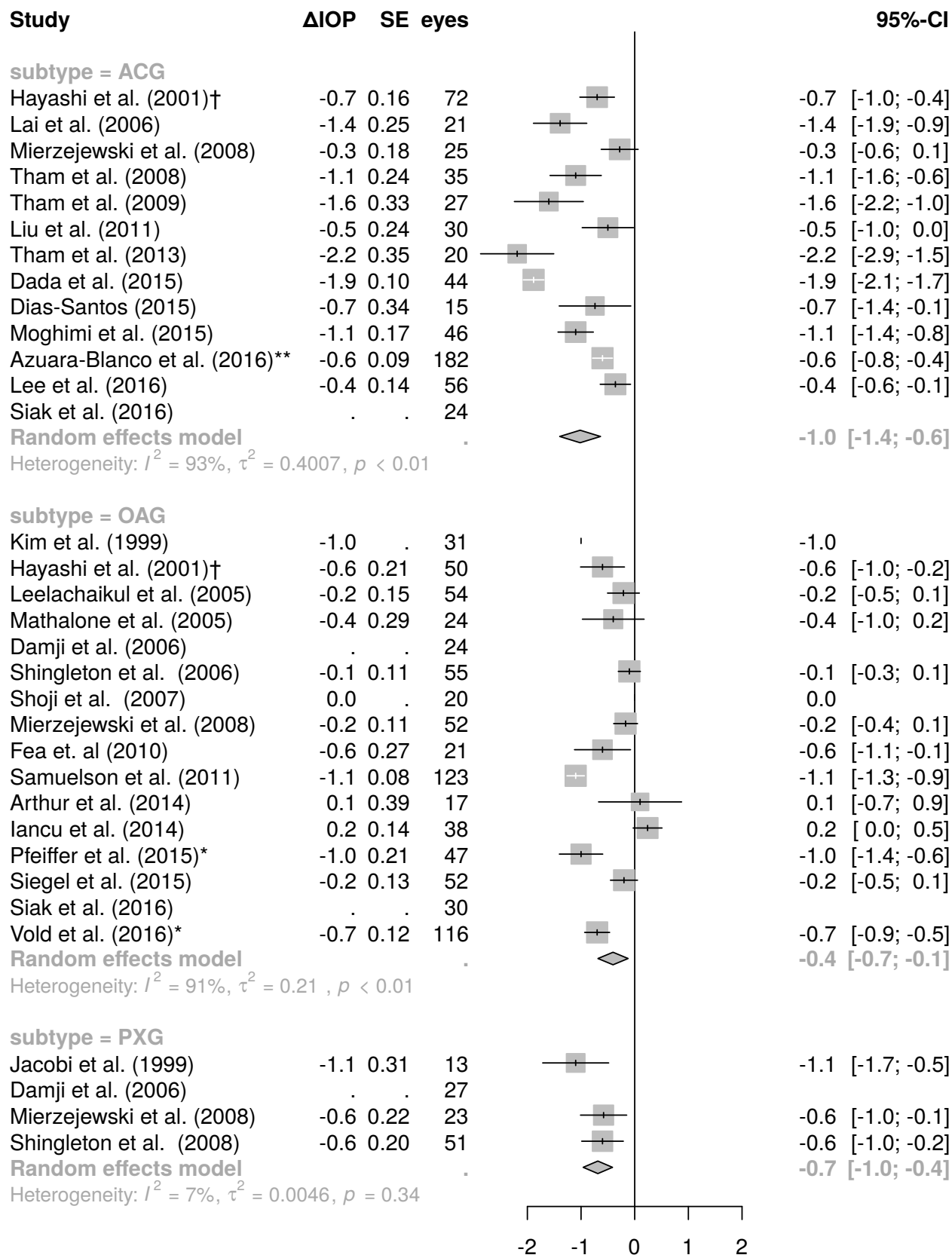
```
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(Year)
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             n.e=LastPeriodEyes, comb.fixed = FALSE)
print(m)
```

```
##                                     95%-CI %W(random)
## Lam et al. (2008)      -47.1000 [-50.0948; -44.1052]      26.8
## Lee et al. (2010)     -35.8000 [-39.6379; -31.9621]      25.9
## Husain et al. (2012) -44.5000 [-52.0026; -36.9974]      20.6
## Hou et al. (2015)     -35.9600 [-39.0429; -32.8771]      26.7
##
## Number of studies combined: k = 4
##
##                                     95%-CI      z  p-value
## Random effects model -40.665 [-47.1528; -34.1772] -12.28 < 0.0001
##
## Quantifying heterogeneity:
## tau^2 = 38.5307; H = 3.36 [2.26; 4.99]; I^2 = 91.1% [80.4%; 96.0%];
## Rb = 87.9% [68.9%; 100.0%]
##
## Test of heterogeneity:
##      Q d.f.  p-value
## 33.84    3 < 0.0001
##
## Details on meta-analytical method:
## - Inverse variance method
## - DerSimonian-Laird estimator for tau^2
```

Meds

```
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean),
         df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             RxChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
```

```
leftcols=c("studlab", "TE", "seTE", "n.e"),  
leftlabs=c("Study", "ΔIOP", "SE", "eyes"))
```



Correlation between meds and drop in IOP

How is IOP drop related to change in meds? Two hypotheses:

- Those studies that see the largest IOP drops also have drop in meds, as doctors see that can use the newfound *slack* to decrease the number of meds people take
- The studies that see the largest IOP drops are those that don't change meds, because dropping meds would also increase IOP

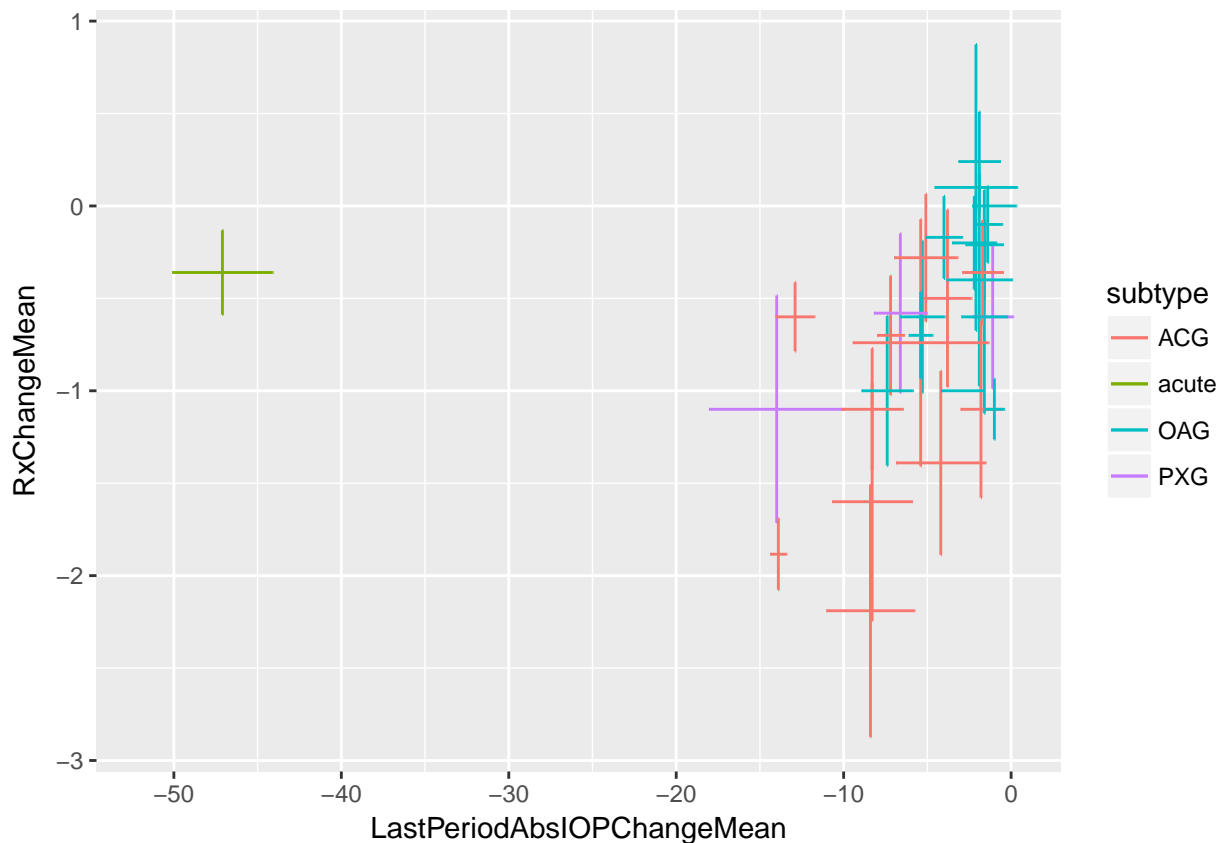
So which is it?

```
df_ <- df %>% mutate(RxChangeSEM = RxChangeStdDev / sqrt>LastPeriodEyes),
                    LastPeriodAbsIOPChangeSEM = LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes))

ggplot(df_, aes(x =LastPeriodAbsIOPChangeMean,
                xmin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeSEM,
                xmax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeSEM,
                y =RxChangeMean,
                ymin=RxChangeMean - 1.96*RxChangeSEM,
                ymax=RxChangeMean + 1.96*RxChangeSEM,
                color=subtype
            )) + geom_errorbar() + geom_errorbarh()
```

Warning: Removed 17 rows containing missing values (geom_errorbar).

Warning: Removed 15 rows containing missing values (geom_errorbarh).



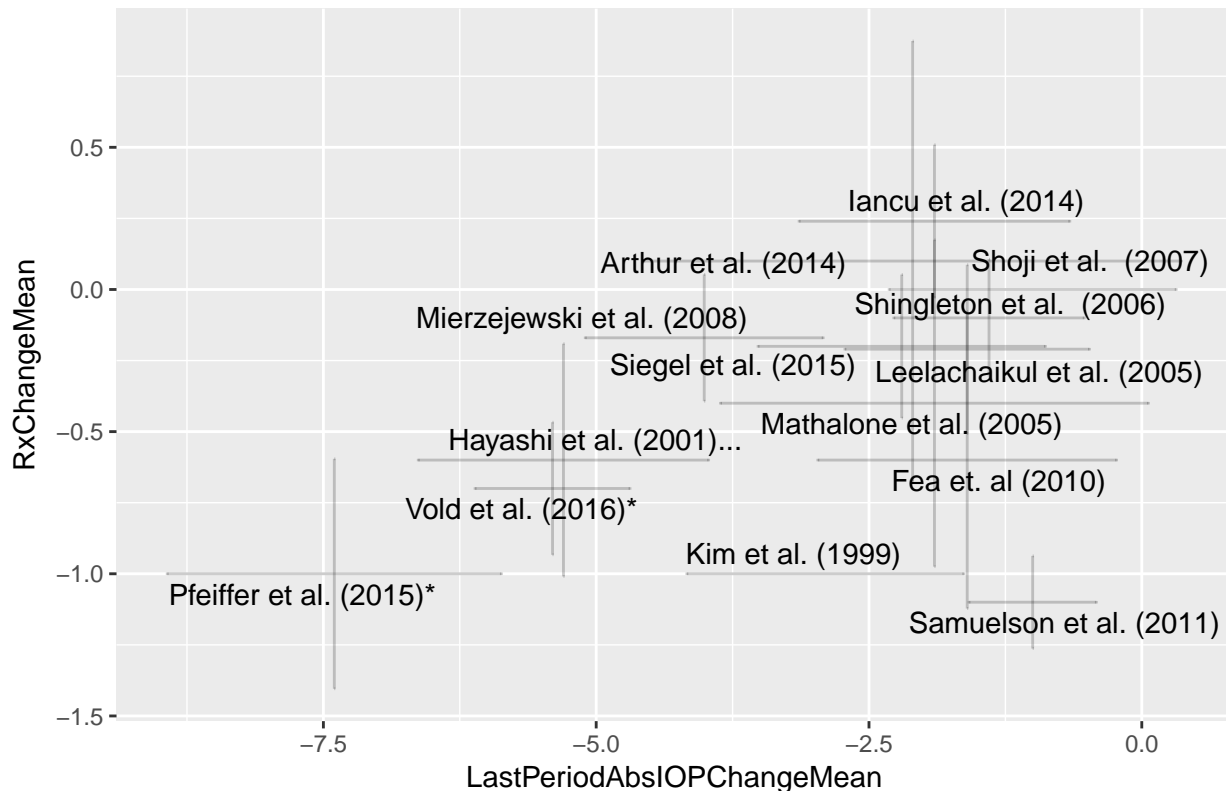
```
ggplot(df_ %>% filter(subtype=='OAG' & MIGsYorN == 'N'),
       aes(x =LastPeriodAbsIOPChangeMean,
```

```

xmin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeSEM,
xmax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeSEM,
y =RxChangeMean,
ymin=RxChangeMean - 1.96*RxChangeSEM,
ymax=RxChangeMean + 1.96*RxChangeSEM,
label=study.name
)) + geom_errorbar(alpha=.2) + geom_errorbarh(alpha=.2) + ggtitle('OAG only') + geom_text_rep

```

OAG only



There is an apparent positive correlation between the two effect sizes: studies with larger drops in IOP also tend to see larger drops in Rx.

```

draw.corr <- function(x.mean, x.sem, y.mean, y.sem) {
  d_ <- data.frame(x = rnorm(n = length(x.mean), mean=x.mean, sd = x.sem),
                    y = rnorm(n = length(x.mean), mean=y.mean, sd = y.sem))
  with(d_ %>% filter(!is.na(x) & !is.na(y)), cor(x, y))
}

cat("Mean +- SE correlation, all studies\n")

## Mean +- SE correlation, all studies

df_ <- df %>% filter(subtype=='OAG', MIGsYorN == 'N')
drawn.corr <- with(df_, replicate(n = 100,
  draw.corr(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             RxChangeMean,
             RxChangeStdDev / sqrt(LastPeriodEyes))))
mean(drawn.corr)

```



```
## [1] 0.3812048
sd(drawn.corrs)

## [1] 0.1348602
cat("Mean +- SE correlation, no washout\n")

## Mean +- SE correlation, no washout
df_ <- filter.data(df, 'nowashout') %>% filter(subtype=='OAG', MIGsYorN == 'N')
drawn.corrs <- with(df_, replicate(n = 100,
                                   draw.corr(LastPeriodAbsIOPChangeMean,
                                              LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
                                              RxChangeMean,
                                              RxChangeStdDev / sqrt(LastPeriodEyes))))
mean(drawn.corrs)

## [1] -0.02253974
sd(drawn.corrs)

## [1] 0.1941081
```

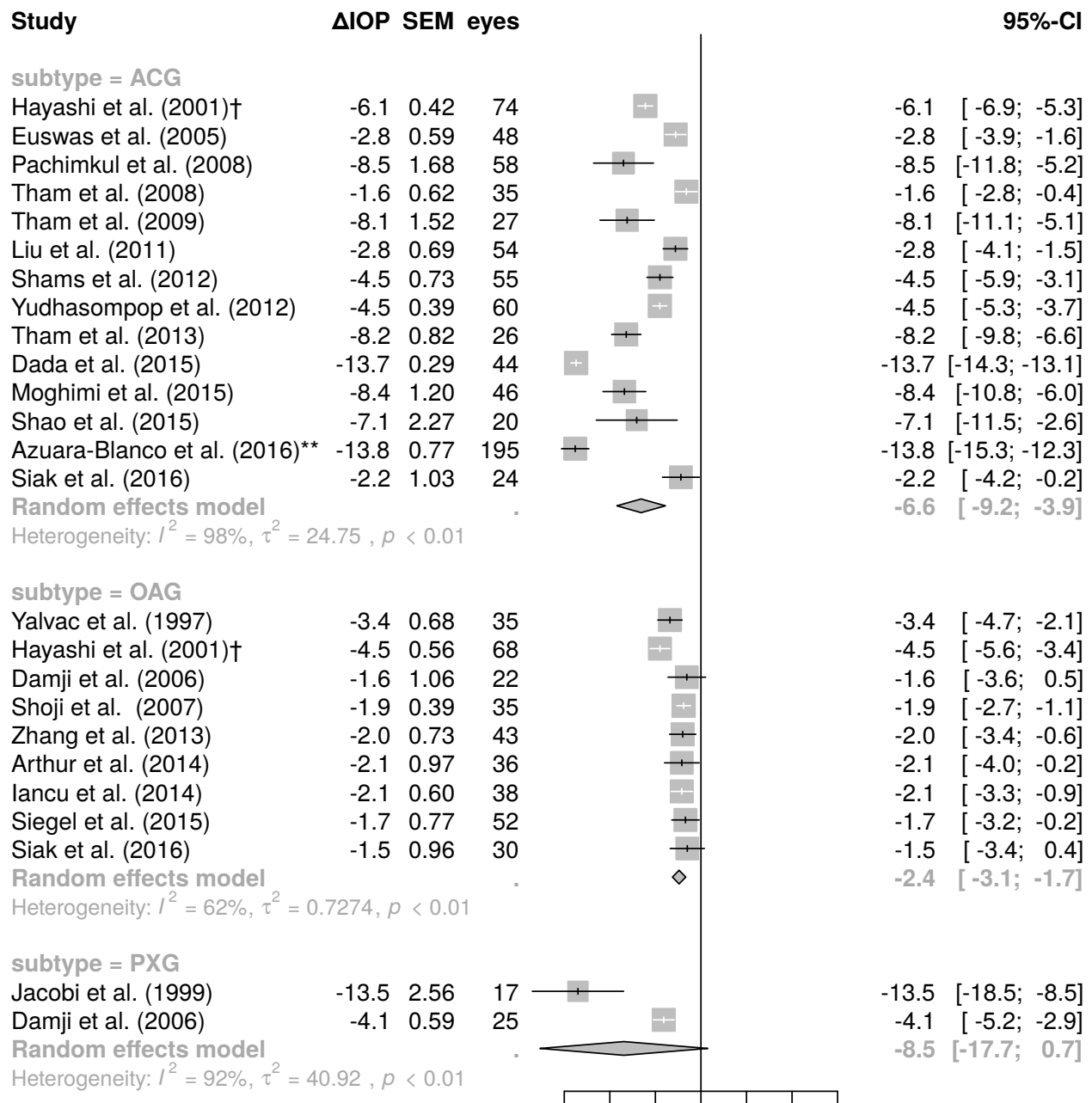
However, this effect goes away when we focus on the studies which don't have washout.

Separate meta-analysis for each time period

```
df <- read.data(fill.last = FALSE)
```

6 month follow-up

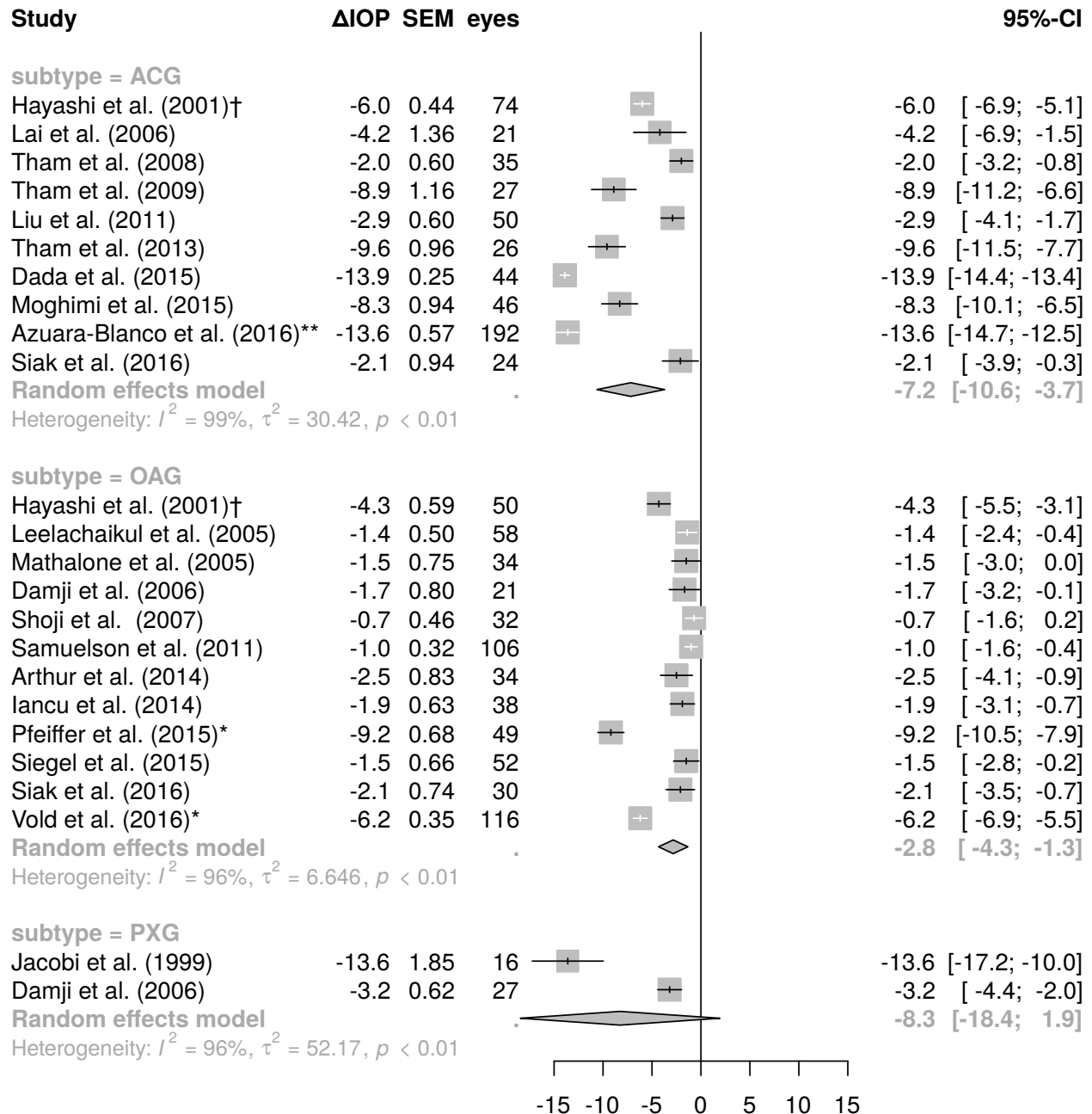
```
df_ <- df %>%
  filter(!is.na(SixMoAbsIOPChangeMean), subtype != "acute") %>%
  mutate(subtype=factor(subtype))
m <- metagen(SixMoAbsIOPChangeMean,
             SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=SixMoEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"),
       leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



12-month follow up

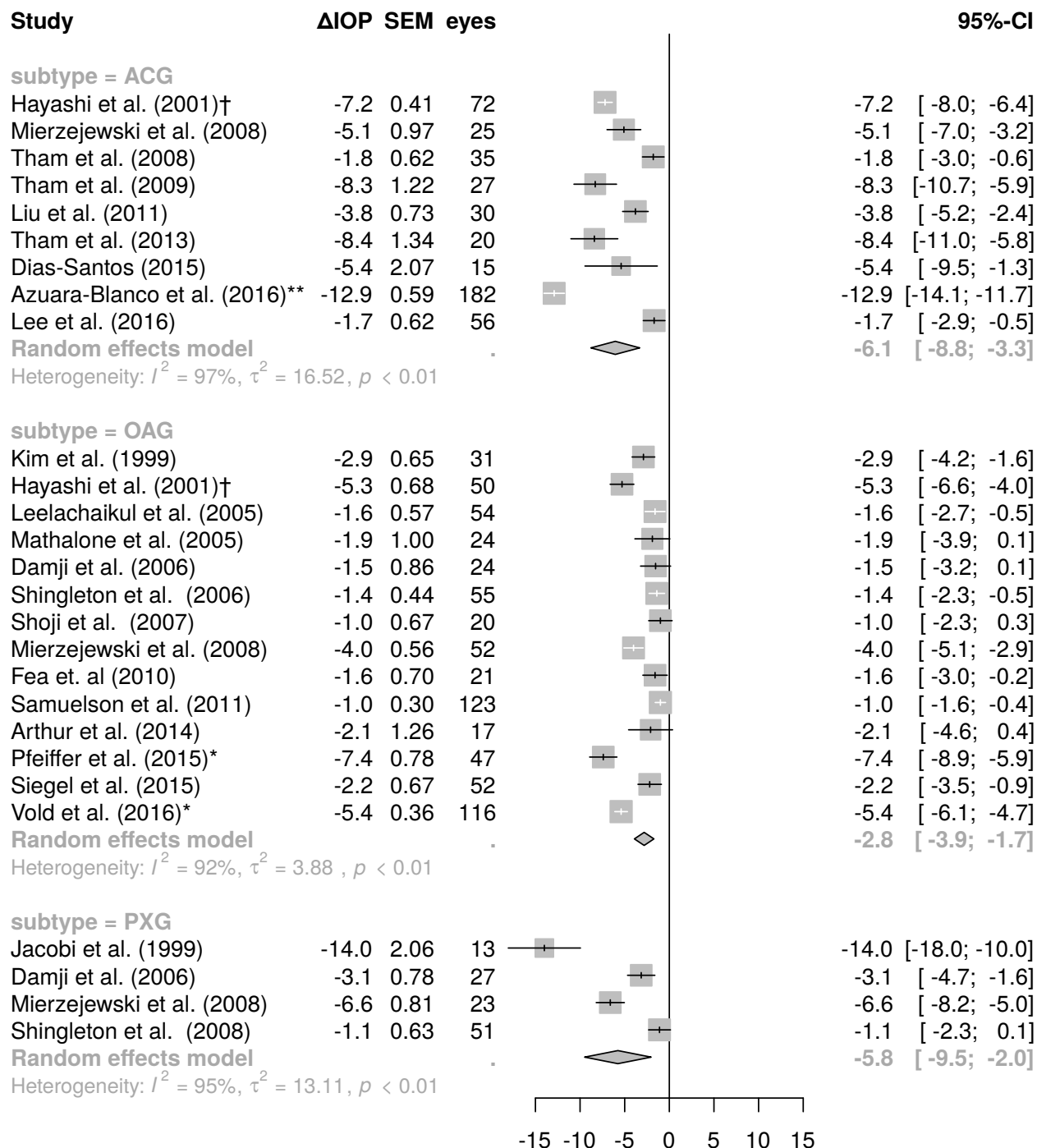
```
df_ <- df %>%
  filter(!is.na(OneYAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(OneYAbsIOPChangeMean,
  OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  study.name,
  data=df_,
  byvar=subtype,
  n.e=OneYEyes)
```

```
forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=FALSE,
  leftcols=c("studlab", "TE", "seTE", "n.e"),
  leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



Last period

```
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"),
       leftlabs=c("Study", "ΔIOP", "SEM", "eyes"))
```



Correlation among time points

Measure the correlation between different outcomes (IOP at 6 months vs. 12 months).

```
ggplot(df %>% filter(subtype != 'acute') %>% mutate(subtype = factor(subtype)),
  aes(x = SixMoAbsIOPChangeMean,
      xmin=SixMoAbsIOPChangeMean - 1.96*SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
      xmax=SixMoAbsIOPChangeMean + 1.96*SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
      y = OneYAbsIOPChangeMean,
```

```

      ymin= OneYAbsIOPChangeMean - 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
      ymax= OneYAbsIOPChangeMean + 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
      label=study.name,
      color=subtype
    )) +
  geom_abline(slope = 1, color="gray70") +
  geom_errorbar() +
  geom_errorbarh() +
  xlab('ΔIOP at 6 months') +
  ylab('ΔIOP at one year') +
  coord_fixed(xlim=c(-18, 0), ylim=c(-18,0))

```

```

## Warning: Removed 22 rows containing missing values (geom_errorbar).
## Warning: Removed 22 rows containing missing values (geom_errorbarh).
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted for <ce>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted for <94>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted for <ce>
## Warning in grid.Call(L_stringMetric, as.graphicsAnnot(x$label)): conversion
## failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on 'ΔIOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :

```

```

## conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot
## substituted for <ce>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at 6 months' in 'mbcsToSbcs': dot
## substituted for <94>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

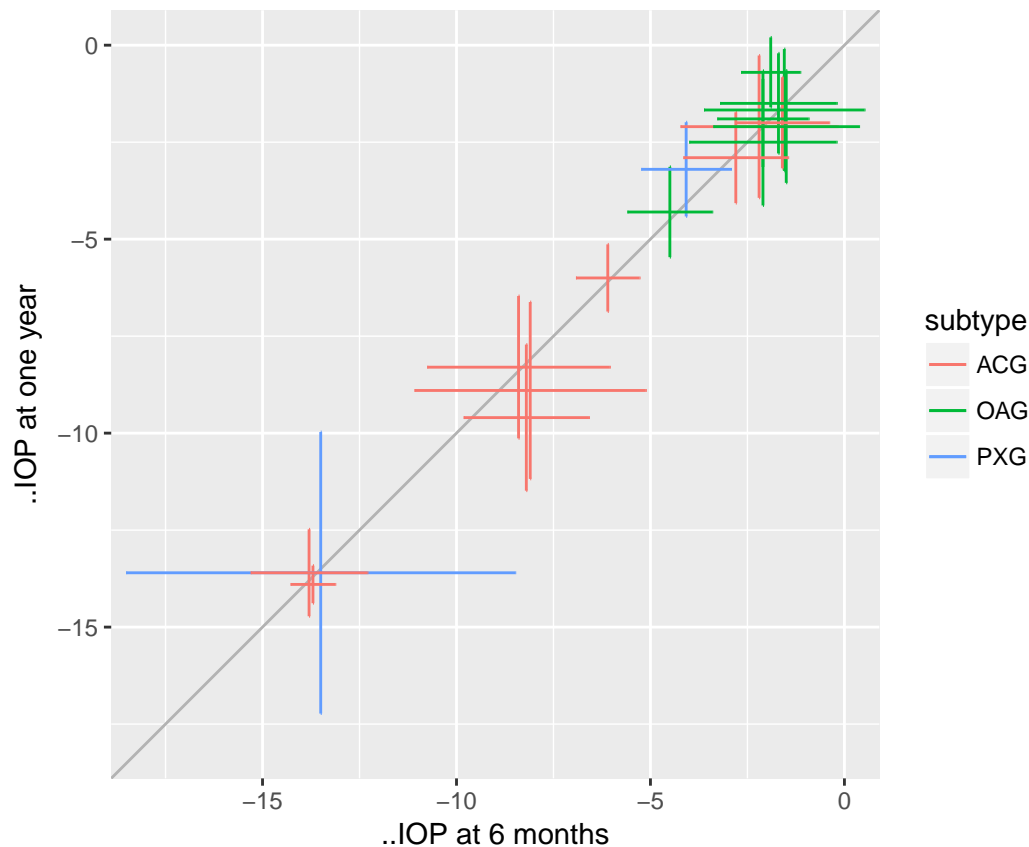
## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <ce>

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x$y, :
## conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot substituted
## for <94>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot
## substituted for <ce>

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on ' $\Delta$ IOP at one year' in 'mbcsToSbcs': dot
## substituted for <94>

```

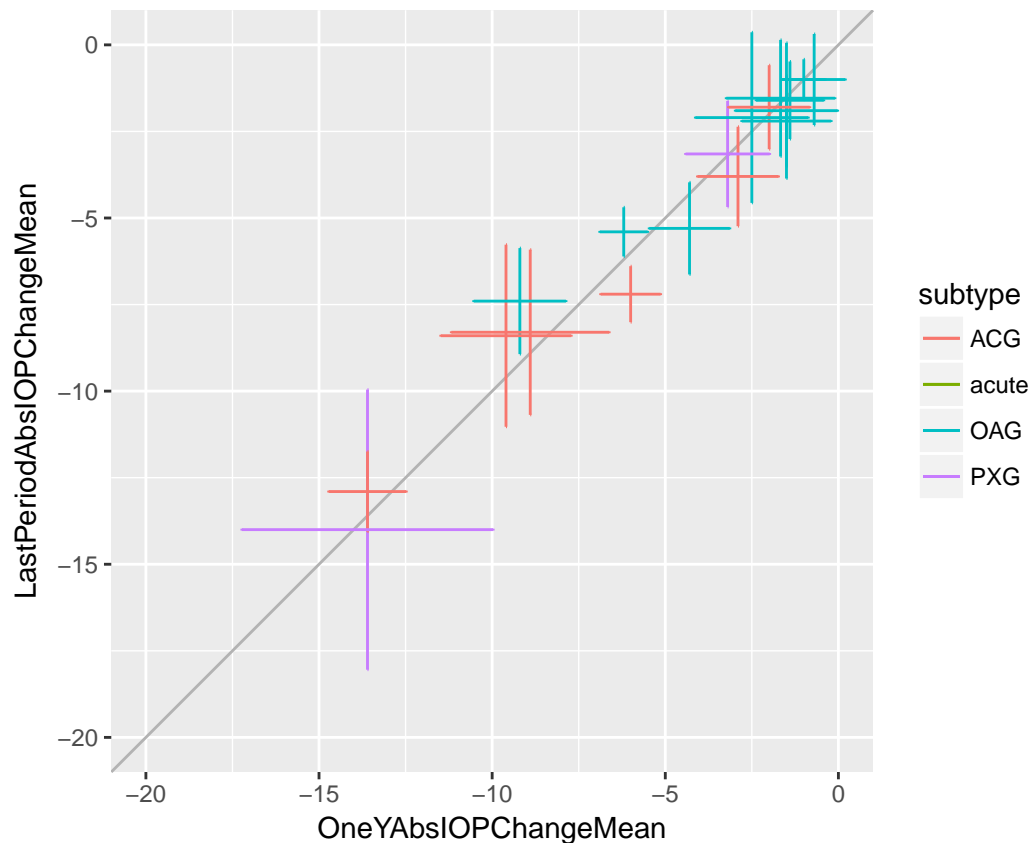
It's very clear that six months and 12 months IOP are highly correlated.

Similarly for one-year vs. last period:

```
ggplot(df, aes(y = LastPeriodAbsIOPChangeMean,
  ymin=LastPeriodAbsIOPChangeMean - 1.96*LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
  ymax=LastPeriodAbsIOPChangeMean + 1.96*LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
  x = OneYAbsIOPChangeMean,
  xmin= OneYAbsIOPChangeMean - 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  xmax= OneYAbsIOPChangeMean + 1.96*OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
  label=study.name,
  color=subtype
)) +
  geom_abline(slope = 1, color="gray70") +
  geom_errorbar() + geom_errorbarh() +
  coord_fixed(xlim=c(-20, 0), ylim=c(-20,0))
```

```
## Warning: Removed 26 rows containing missing values (geom_errorbar).
```

```
## Warning: Removed 26 rows containing missing values (geom_errorbarh).
```



Again, correlations are very high. Present this in another way.

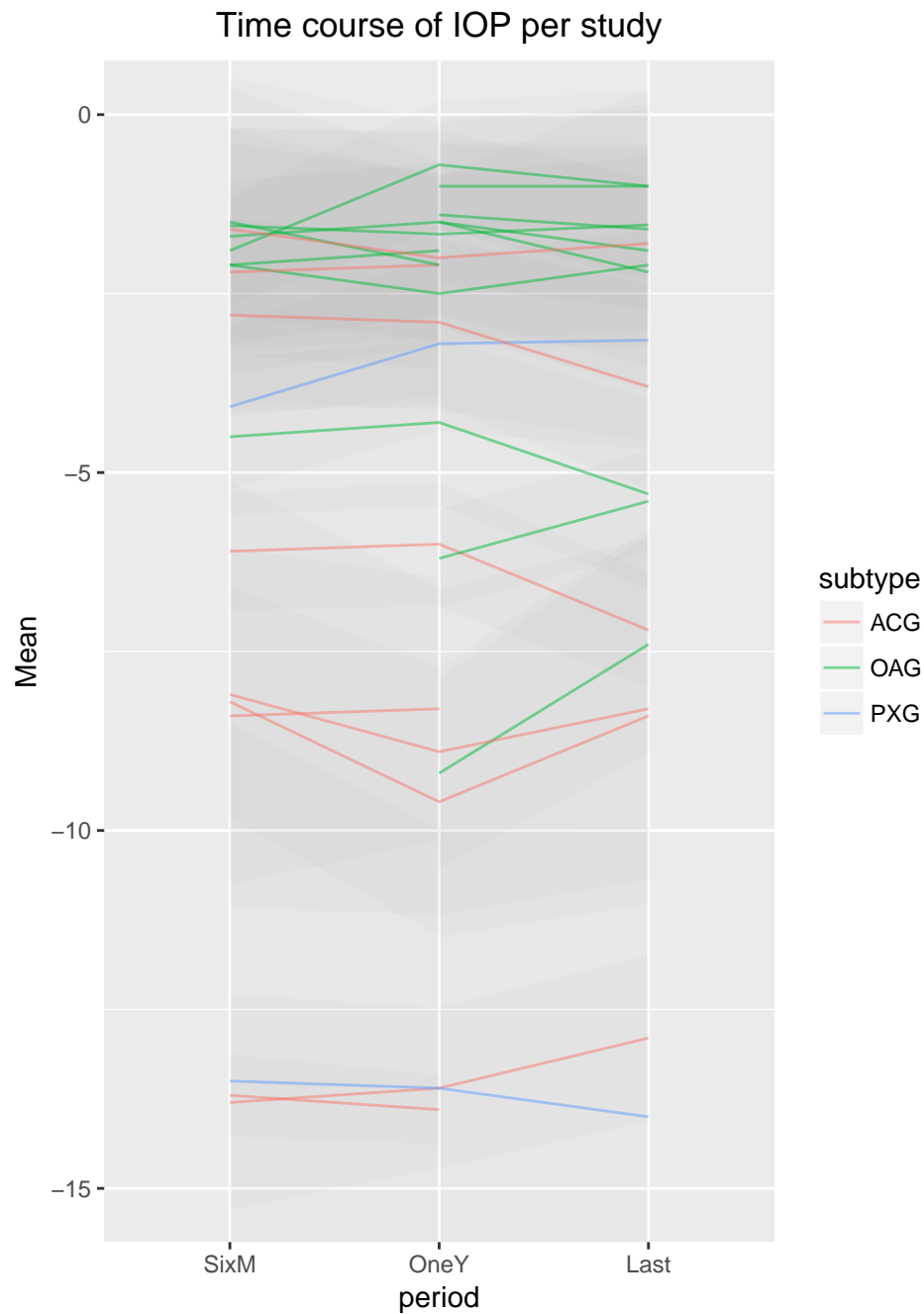
```
library(reshape2)
```

```
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
## smiths
nd <- melt(df %>%
  filter(MIGsYorN == 'N',
    subtype != 'acute',
    1*is.na(SixMoAbsIOPChangeMean) +
    1*is.na(OneYAbsIOPChangeMean) +
    1*is.na>LastPeriodAbsIOPChangeMean) < 2) %>%
  mutate(SixMoChangeSEM = SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
    OneYChangeSEM = OneYAbsIOPChangeStdDev / sqrt(OneYEyes),
    LastPeriodChangeSEM = LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes)) %>%
  select(study.name, subtype,
    SixMoAbsIOPChangeMean,
    OneYAbsIOPChangeMean,
    LastPeriodAbsIOPChangeMean,
    SixMoChangeSEM,
    OneYChangeSEM,
    LastPeriodChangeSEM), id.vars=c("study.name", "subtype"))
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable)))
nd$period <- substr(nd$variable, 0, 4)
```

```

df_ <- dcast(nd, formula = study.name + subtype + period ~ metric)
df_ <- df_ %>% mutate(period = factor(period, c('SixM', 'OneY', 'Last')),
                      g = paste(study.name, as.character(subtype))) %>% filter(!is.na(Mean))
ggplot(df_, aes(y =Mean,
                ymin=Mean - 1.96*eSEM,
                ymax=Mean + 1.96*eSEM,
                x = period,
                label=study.name,
                group=g)) +
  geom_ribbon(alpha=.02) +
  geom_line(alpha=.5, aes(color=subtype)) +
  coord_cartesian(y=c(-15, 0)) + ggtitle('Time course of IOP per study') + theme(plot.title = element_t

```



It's remarkable how consistent measurements are between time periods. At most, we find a change of ± 2.5 mm Hg between the first and last period.

```
df_ <- df %>% filter(subtype=='OAG')
drawn.corr <- with(df_, replicate(n = 100,
                                draw.corr(SixMoAbsIOPChangeMean,
                                           SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
                                           OneYAbsIOPChangeMean,
                                           OneYAbsIOPChangeStdDev / sqrt(OneYEyes))))
cat("Mean +- SE correlation, OAG only\n")
```

```
## Mean +- SE correlation, OAG only
```

```

print(mean(drawn.corrs))

## [1] 0.6287425
print(sd(drawn.corrs))

## [1] 0.1808015
df_ <- df
drawn.corrs <- with(df_, replicate(n = 100,
                                   draw.corr(SixMoAbsIOPChangeMean,
                                              SixMoAbsIOPChangeStdDev / sqrt(SixMoEyes),
                                              OneYAbsIOPChangeMean,
                                              OneYAbsIOPChangeStdDev / sqrt(OneYEyes))))
cat("Mean +- SE correlation, All subtypes\n")

## Mean +- SE correlation, All subtypes
print(mean(drawn.corrs))

## [1] 0.9912487
print(sd(drawn.corrs))

## [1] 0.003900496

```

This is also reflected in the correlations - even accounting for noise, the correlations are $> .9$ between month 6 and month 12.

Multivariate inference

Let's use mvmeta to infer the effect size for all periods together.

```

library(mvmeta)

## This is mvmeta 0.4.7. For an overview type: help('mvmeta-package').
fill.na <- function(x, y, z) {
  return(ifelse(!is.na(x),
                x,
                ifelse(is.na(y),
                      z,
                      ifelse(is.na(z),
                            y,
                            sqrt((y**2 + z**2) / 2 )))))
}

get.correlation.matrices.tri <- function(x, y, z, assumed.rho) {
  S <- list()
  for(i in 1:length(x)) {
    xx <- fill.na(x[i], y[i], z[i])
    yy <- fill.na(y[i], x[i], z[i])
    zz <- fill.na(z[i], x[i], y[i])
    S[[i]] <- matrix(c(xx ** 2, xx * yy * assumed.rho, xx * zz * assumed.rho ** 2,
                      xx * yy * assumed.rho, yy ** 2, zz * yy * assumed.rho,
                      xx * zz * assumed.rho ** 2, zz * yy * assumed.rho, zz ** 2), ncol=3)
  }
}

```

```

S
}

df_ <- df %>% filter(!is.na>LastPeriodAbsIOPChangeStdDev) |
               !is.na(SixMoAbsIOPChangeStdDev) |
               !is.na(OneYAbsIOPChangeStdDev), subtype %in% c('OAG', 'ACG'), MIGsYorN == 'N')

thefit <- mvmeta(cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean, LastPeriodAbsIOPChangeMean) ~ subtype,
  S=get.correlation.matrices.tri(df_$SixMoAbsIOPChangeStdDev / sqrt(df_$SixMoEyes),
                                df_$OneYAbsIOPChangeStdDev / sqrt(df_$OneYEyes),
                                df_$LastPeriodAbsIOPChangeStdDev / sqrt(df_$LastPeriodEyes), .7),
  data=df_,
  method="reml")

summary(thefit)

## Call: mvmeta(formula = cbind(SixMoAbsIOPChangeMean, OneYAbsIOPChangeMean,
##   LastPeriodAbsIOPChangeMean) ~ subtype, S = get.correlation.matrices.tri(df_$SixMoAbsIOPChangeStdDev/
##   df_$OneYAbsIOPChangeStdDev/sqrt(df_$OneYEyes), df_$LastPeriodAbsIOPChangeStdDev/sqrt(df_$LastPeriod
##   0.7), data = df_, method = "reml")
##
## Multivariate random-effects meta-regression
## Dimension: 3
## Estimation method: REML
##
## Fixed-effects coefficients
## SixMoAbsIOPChangeMean :
##           Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -5.9092    0.7536  -7.8415   0.0000  -7.3862  -4.4322
## subtypeOAG    2.9191    1.0558   2.7648   0.0057   0.8497   4.9884
##
## (Intercept) ***
## subtypeOAG    **
## OneYAbsIOPChangeMean :
##           Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -6.0973    0.7637  -7.9839   0.0000  -7.5941  -4.6004
## subtypeOAG    3.3817    1.0607   3.1882   0.0014   1.3028   5.4606
##
## (Intercept) ***
## subtypeOAG    **
## LastPeriodAbsIOPChangeMean :
##           Estimate Std. Error      z Pr(>|z|) 95%ci.lb 95%ci.ub
## (Intercept)  -6.2665    0.6835  -9.1681   0.0000  -7.6061  -4.9268
## subtypeOAG    3.5782    0.9378   3.8157   0.0001   1.7402   5.4162
##
## (Intercept) ***
## subtypeOAG    ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Between-study random-effects (co)variance components
## Structure: General positive-definite
##
##           Std. Dev           Corr
## SixMoAbsIOPChangeMean      2.9873 SixMoAbsIOPChangeMean

```

```

## OneYAbsIOPChangeMean      3.0257      0.9969
## LastPeriodAbsIOPChangeMean 2.6062      0.9901
##
## SixMoAbsIOPChangeMean      OneYAbsIOPChangeMean
## OneYAbsIOPChangeMean
## LastPeriodAbsIOPChangeMean      0.9823
##
## Multivariate Cochran Q-test for residual heterogeneity:
## Q = 1520.2986 (df = 62), p-value = 0.0000
## I-square statistic = 95.9%
##
## 36 studies, 68 observations, 6 fixed and 6 random-effects parameters
##      logLik      AIC      BIC
## -118.9294    261.8587    287.3844

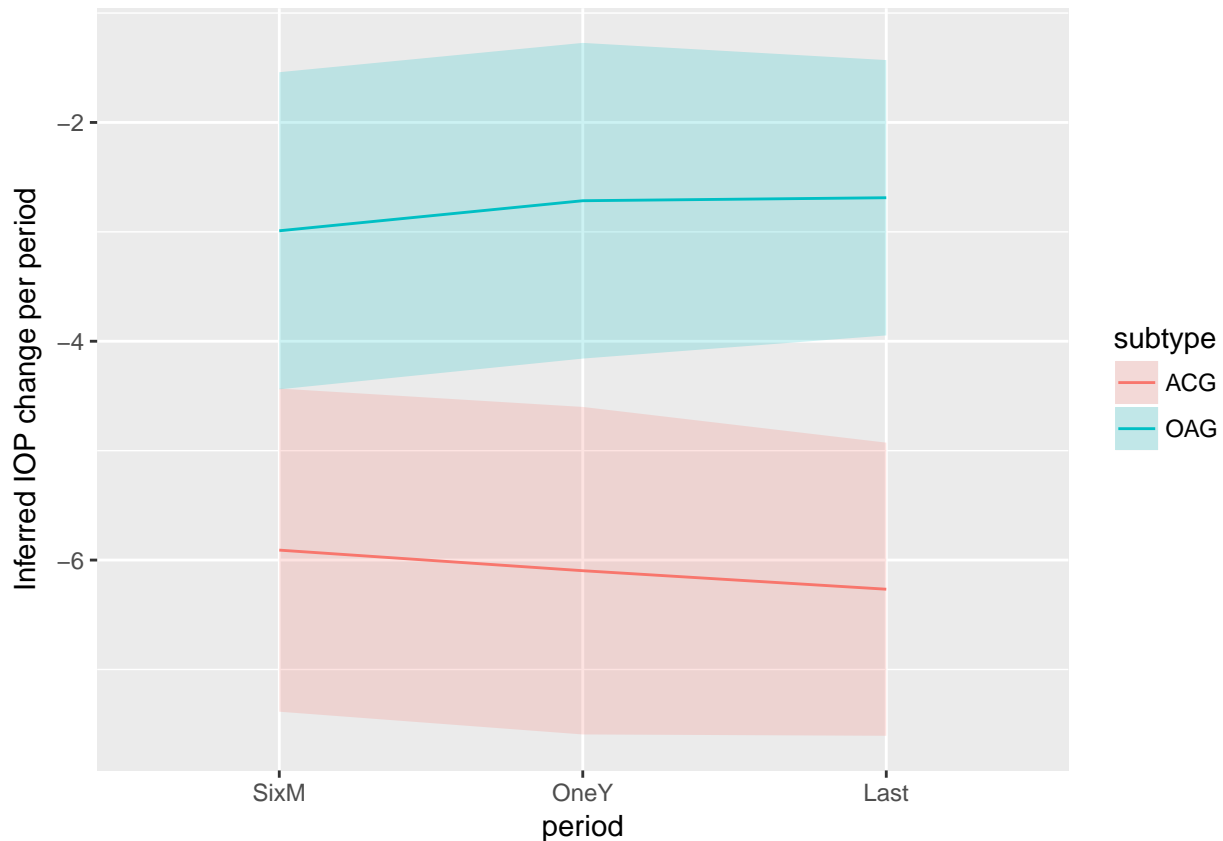
newdata <- data.frame(subtype=c('OAG', 'ACG'))
pred <- predict(thefit, newdata, se=TRUE)
newdata$SixMoAbsIOPChangeMean <- pred$fit[,1]
newdata$OneYAbsIOPChangeMean <- pred$fit[,2]
newdata$LastPeriodAbsIOPChangeMean <- pred$fit[,3]
newdata$SixMoAbsIOPChangeSEM <- pred$se[,1]
newdata$OneYAbsIOPChangeSEM <- pred$se[,2]
newdata$LastPeriodAbsIOPChangeSEM <- pred$se[,3]

library(reshape2)
nd <- melt(newdata)

## Using subtype as id variables

nd$period <- substr(nd$variable, 0, 4)
nd$metric <- substr(nd$variable, nchar(as.character(nd$variable)) - 3, nchar(as.character(nd$variable)))
df_ <- dcast(nd, formula = subtype + period ~ metric)
df_$period <- factor(df_$period, c('SixM', 'OneY', 'Last'))
ggplot(df_, aes(x=period,
                y=Mean,
                ymin=Mean - 1.96*eSEM,
                ymax=Mean + 1.96*eSEM,
                group=subtype,
                fill=subtype)) + geom_ribbon(alpha=.2) + geom_line(aes(color=subtype)) + ylab("Inferred

```



Meta-regression

Consider relationships between different covariates and outcomes. Focus on the IOP drop at one year and its correlation with different factors.

```
df <- read.data()

## These retrospective studies are losing eyes per period - not impossible, but unusual:
## Mathalone et al. (2005)
## Leelachaikul et al. (2005)
## Shoji et al. (2007)
## Liu et al. (2011)
## Arthur et al. (2014)
## Tetz et al. (2015)

## These retrospective studies are gaining eyes as the study goes
## Samuelson et al. (2011)
df_ <- df %>% filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen>LastPeriodAbsIOPChangeMean,
  LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
  study.name,
  data=df_,
  byvar=subtype,
  n.e=OneYEyes)
```



```

print(metareg(~ LastPeriodEyes, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      25.5650 (SE = 9.4030)
## tau (square root of estimated tau^2 value):             5.0562
## I^2 (residual heterogeneity / unaccounted variability): 98.53%
## H^2 (unaccounted variability / sampling variability):    67.85
## R^2 (amount of heterogeneity accounted for):             0.00%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 2103.4367, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.8172, p-val = 0.3660
##
## Model Results:
##
##              estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt          -3.5035  1.4564  -2.4055  0.0161  -6.3580  -0.6489 *
## LastPeriodEyes   -0.0231  0.0256  -0.9040  0.3660  -0.0733   0.0270
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ LastPeriodEyes * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      14.9914 (SE = 5.6935)
## tau (square root of estimated tau^2 value):             3.8719
## I^2 (residual heterogeneity / unaccounted variability): 97.33%
## H^2 (unaccounted variability / sampling variability):    37.41
## R^2 (amount of heterogeneity accounted for):             36.88%
##
## Test for Residual Heterogeneity:
## QE(df = 27) = 1010.2000, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 13.8935, p-val = 0.0163
##
## Model Results:
##
##              estimate      se      zval      pval      ci.lb
## intrcpt          -2.0689  1.8225  -1.1352  0.2563  -5.6409
## LastPeriodEyes   -0.0135  0.0323  -0.4193  0.6750  -0.0767
## subtypeACG        -2.2014  2.4577  -0.8957  0.3704  -7.0184
## subtypePXG       -12.1290  5.0623  -2.3959  0.0166 -22.0509
## LastPeriodEyes:subtypeACG -0.0323  0.0414  -0.7804  0.4352  -0.1134
## LastPeriodEyes:subtypePXG  0.2992  0.1490   2.0089  0.0445   0.0073
##              ci.ub
## intrcpt          1.5031

```

```

## LastPeriodEyes          0.0497
## subtypeACG              2.6156
## subtypePXG             -2.2071 *
## LastPeriodEyes:subtypeACG 0.0488
## LastPeriodEyes:subtypePXG 0.5912 *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ Year, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):    21.8899 (SE = 8.0755)
## tau (square root of estimated tau^2 value):           4.6787
## I^2 (residual heterogeneity / unaccounted variability): 98.30%
## H^2 (unaccounted variability / sampling variability):  58.68
## R^2 (amount of heterogeneity accounted for):           7.84%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 1818.9826, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 0.0863, p-val = 0.7690
##
## Model Results:
##
##      estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt  90.1158  322.2445   0.2797  0.7797  -541.4717  721.7034
## Year    -0.0471   0.1603  -0.2937  0.7690   -0.3614   0.2672
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ Year * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):    13.0995 (SE = 4.8228)
## tau (square root of estimated tau^2 value):           3.6193
## I^2 (residual heterogeneity / unaccounted variability): 96.99%
## H^2 (unaccounted variability / sampling variability):  33.20
## R^2 (amount of heterogeneity accounted for):           44.85%
##
## Test for Residual Heterogeneity:
## QE(df = 27) = 896.4438, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 12.7238, p-val = 0.0261
##
## Model Results:
##
##      estimate      se      zval      pval      ci.lb

```

```

## intrcpt          101.1478   352.0056   0.2873   0.7738  -588.7705
## Year             -0.0517    0.1752  -0.2951   0.7680   -0.3951
## subtypeACG       215.6321   574.0691   0.3756   0.7072  -909.5227
## subtypePXG      -2423.4415  1148.3040  -2.1105   0.0348 -4674.0761
## Year:subtypeACG   -0.1090    0.2855  -0.3817   0.7027   -0.6686
## Year:subtypePXG    1.2067    0.5724   2.1080   0.0350    0.0847
##               ci.lb      ci.ub
## intrcpt          791.0661
## Year              0.2917
## subtypeACG       1340.7869
## subtypePXG       -172.8070 *
## Year:subtypeACG    0.4506
## Year:subtypePXG    2.3287 *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ PreOpIOPMean, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      4.9949 (SE = 1.8128)
## tau (square root of estimated tau^2 value):             2.2349
## I^2 (residual heterogeneity / unaccounted variability): 92.72%
## H^2 (unaccounted variability / sampling variability):    13.73
## R^2 (amount of heterogeneity accounted for):             78.97%
##
## Test for Residual Heterogeneity:
## QE(df = 31) = 425.7653, p-val < .0001
##
## Test of Moderators (coefficient(s) 2):
## QM(df = 1) = 57.2596, p-val < .0001
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb      ci.ub
## intrcpt          11.3366   2.1268   5.3304 <.0001    7.1682   15.5051 ***
## PreOpIOPMean    -0.7858   0.1038  -7.5670 <.0001   -0.9894   -0.5823 ***
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(metareg(~ PreOpIOPMean * subtype, x=m))

##
## Mixed-Effects Model (k = 33; tau^2 estimator: DL)
##
## tau^2 (estimated amount of residual heterogeneity):      1.3179 (SE = 0.5551)
## tau (square root of estimated tau^2 value):             1.1480
## I^2 (residual heterogeneity / unaccounted variability): 76.22%
## H^2 (unaccounted variability / sampling variability):    4.21
## R^2 (amount of heterogeneity accounted for):             94.45%
##
## Test for Residual Heterogeneity:

```

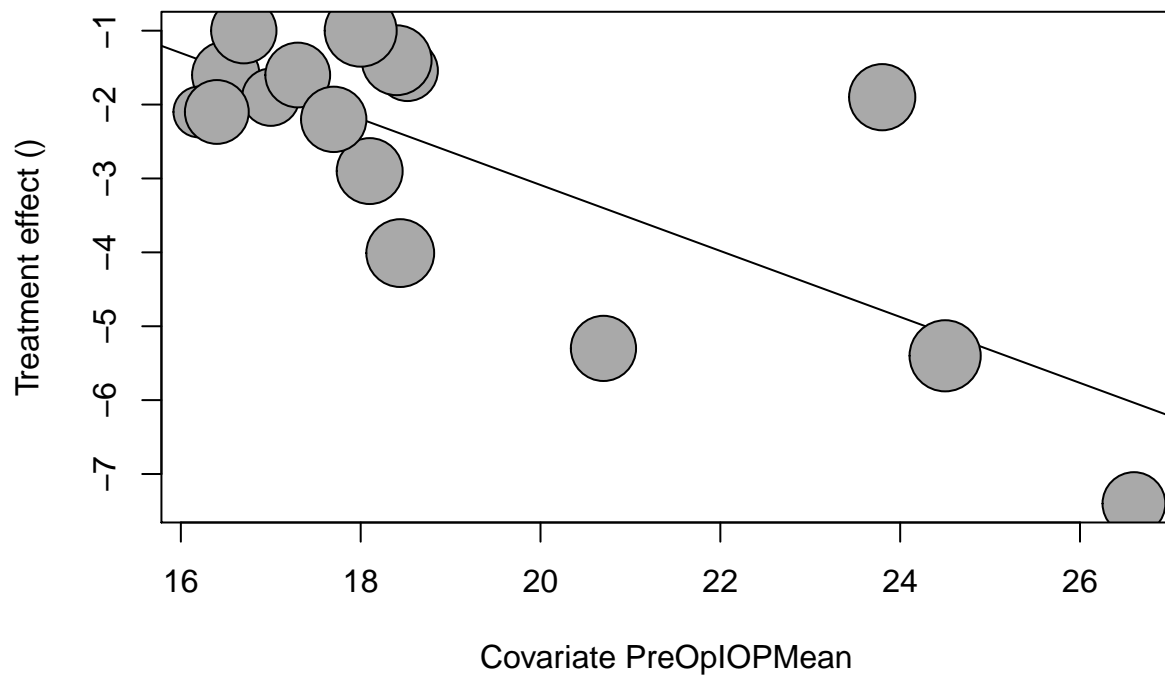
```

## QE(df = 27) = 113.5553, p-val < .0001
##
## Test of Moderators (coefficient(s) 2,3,4,5,6):
## QM(df = 5) = 202.0496, p-val < .0001
##
## Model Results:
##
##               estimate      se      zval      pval      ci.lb
## intrcpt          5.8390  2.1095   2.7679  0.0056   1.7044
## PreOpIOPMean     -0.4465  0.1086  -4.1095 <.0001  -0.6594
## subtypeACG        5.6249  2.7917   2.0149  0.0439   0.1533
## subtypePXG        8.8496  4.5438   1.9476  0.0515  -0.0560
## PreOpIOPMean:subtypeACG -0.4165  0.1378  -3.0217  0.0025  -0.6867
## PreOpIOPMean:subtypePXG -0.4795  0.2191  -2.1878  0.0287  -0.9090
##               ci.ub
## intrcpt          9.9736  **
## PreOpIOPMean     -0.2335  ***
## subtypeACG       11.0965   *
## subtypePXG       17.7552   .
## PreOpIOPMean:subtypeACG -0.1463  **
## PreOpIOPMean:subtypePXG -0.0499   *
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# Same, restricted to OAG only
df_ <- df %>% filter(!is.na(LastPeriodAbsIOPChangeMean), subtype == "OAG", MIGsYorN == 'N') %>%
  mutate(subtype=relevel(factor(subtype), ref="OAG"))
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)

bubble(metareg(~ PreOpIOPMean, x=m))

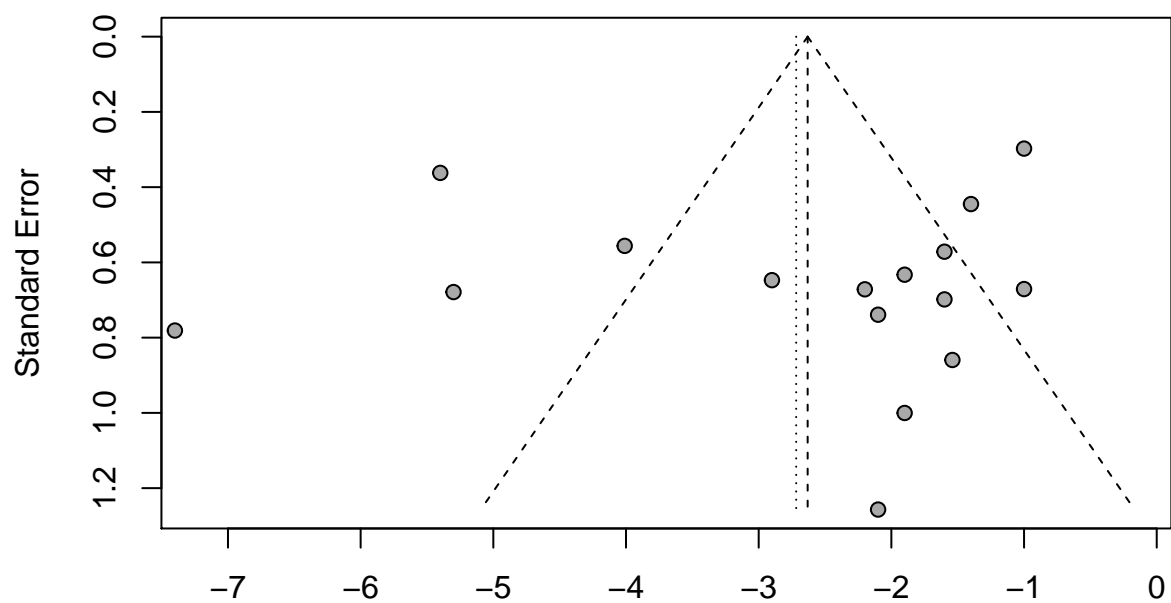
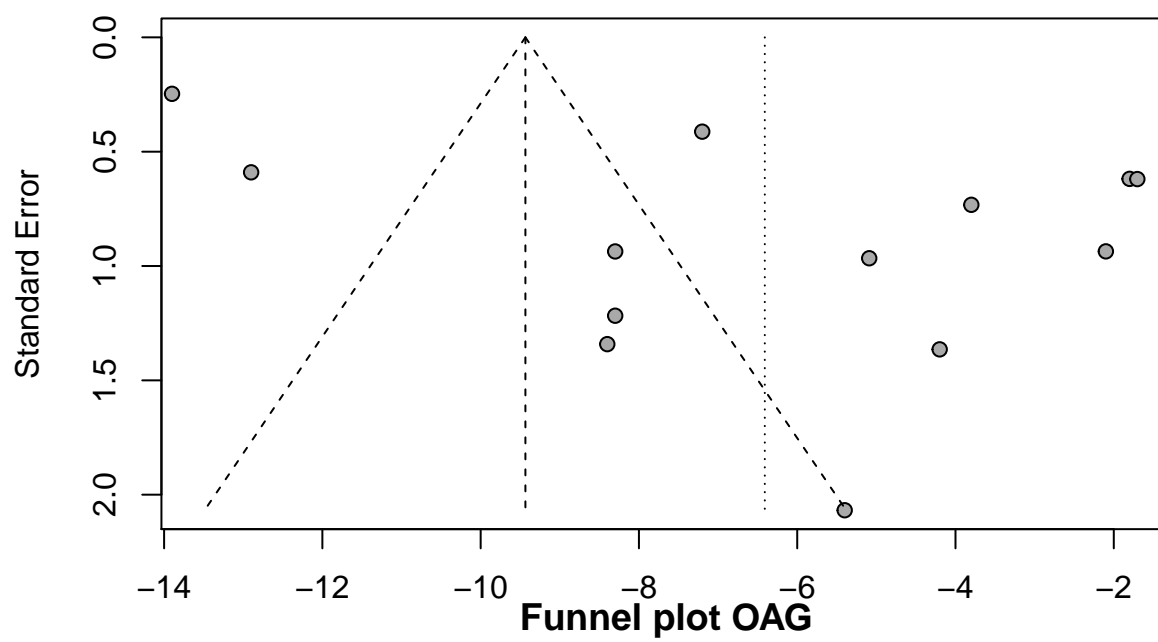
```



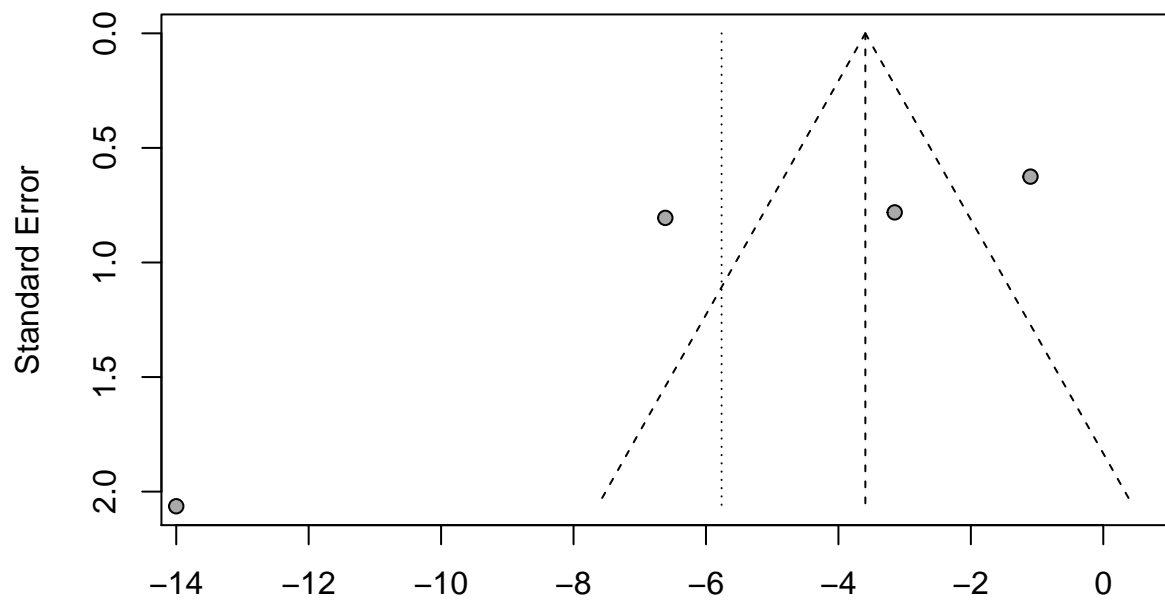
Small study bias

```
df_ <- df %>% filter(!is.na(df$LastPeriodAbsIOPChangeMean),
                     df$subtype != "acute",
                     MIGsYorN == 'N') %>% mutate(subtype=factor(subtype))
for(l in levels(df_$subtype)) {
  m <- metagen(LastPeriodAbsIOPChangeMean,
               LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
               study.name,
               data=df_ %>% filter(subtype == l),
               n.e=LastPeriodEyes)
  funnel(m)
  title(paste('Funnel plot', l))
}
```

Funnel plot ACG

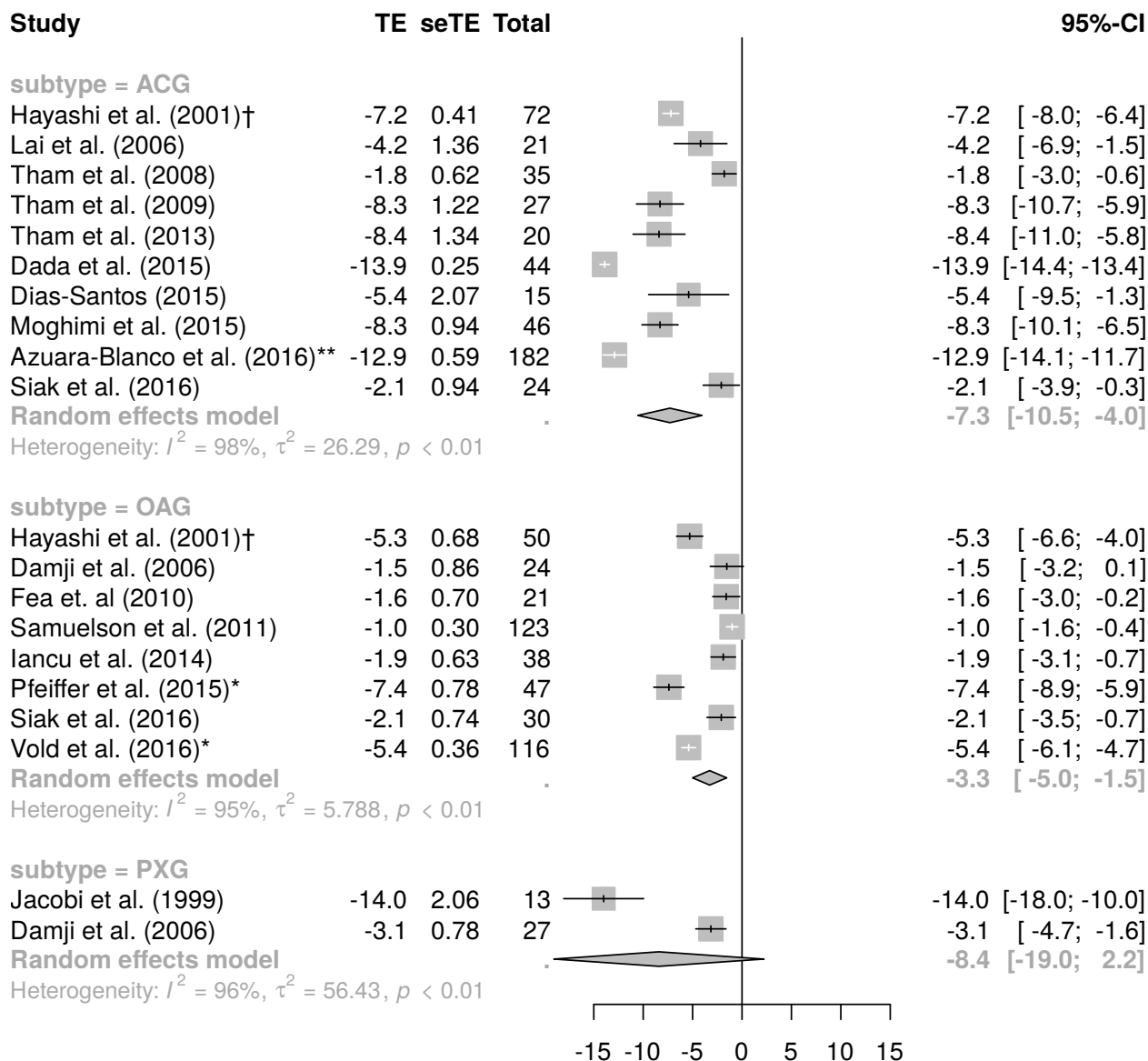


Funnel plot PXG



Alternative filterings of the data

Prospective studies only



Meds

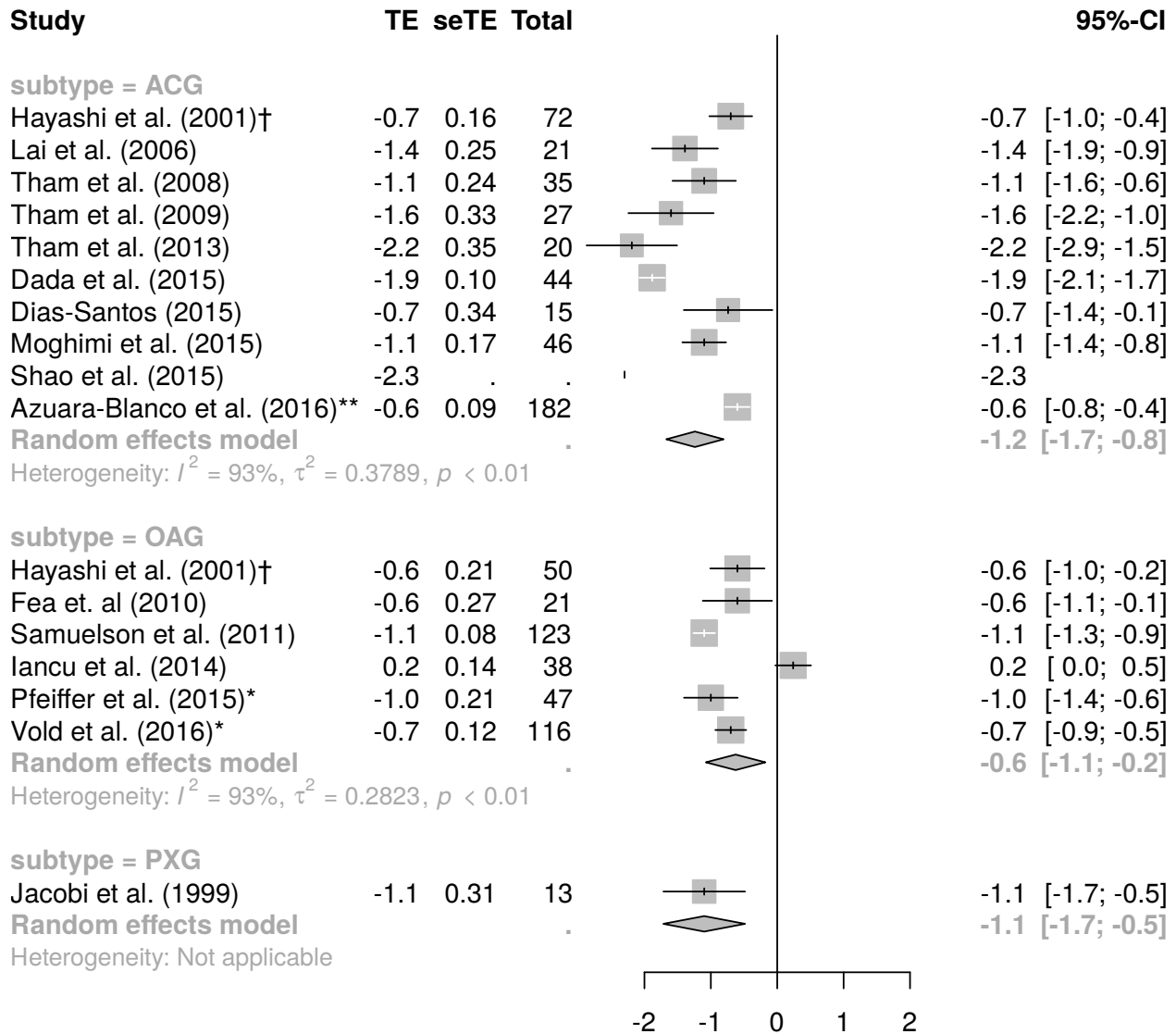
```
df_ <- df %>%
  filter(!is.na(RxChangeMean), !is.na(RxChangeStdDev),
         df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             sqrt(RxPostOpStdDev** 2 + RxPreOpStdDev ** 2) / sqrt>LastPeriodEyes),
           study.name,
           data=df_,
```



```

byvar=subtype,
n.e=LastPeriodEyes)
forest(m,
  comb.fixed=FALSE,
  digits=1,
  digits.se = 2,
  overall=FALSE,
  leftcols=c("studlab", "TE", "seTE", "n.e"))

```



Excluding washout studies

Last period

```

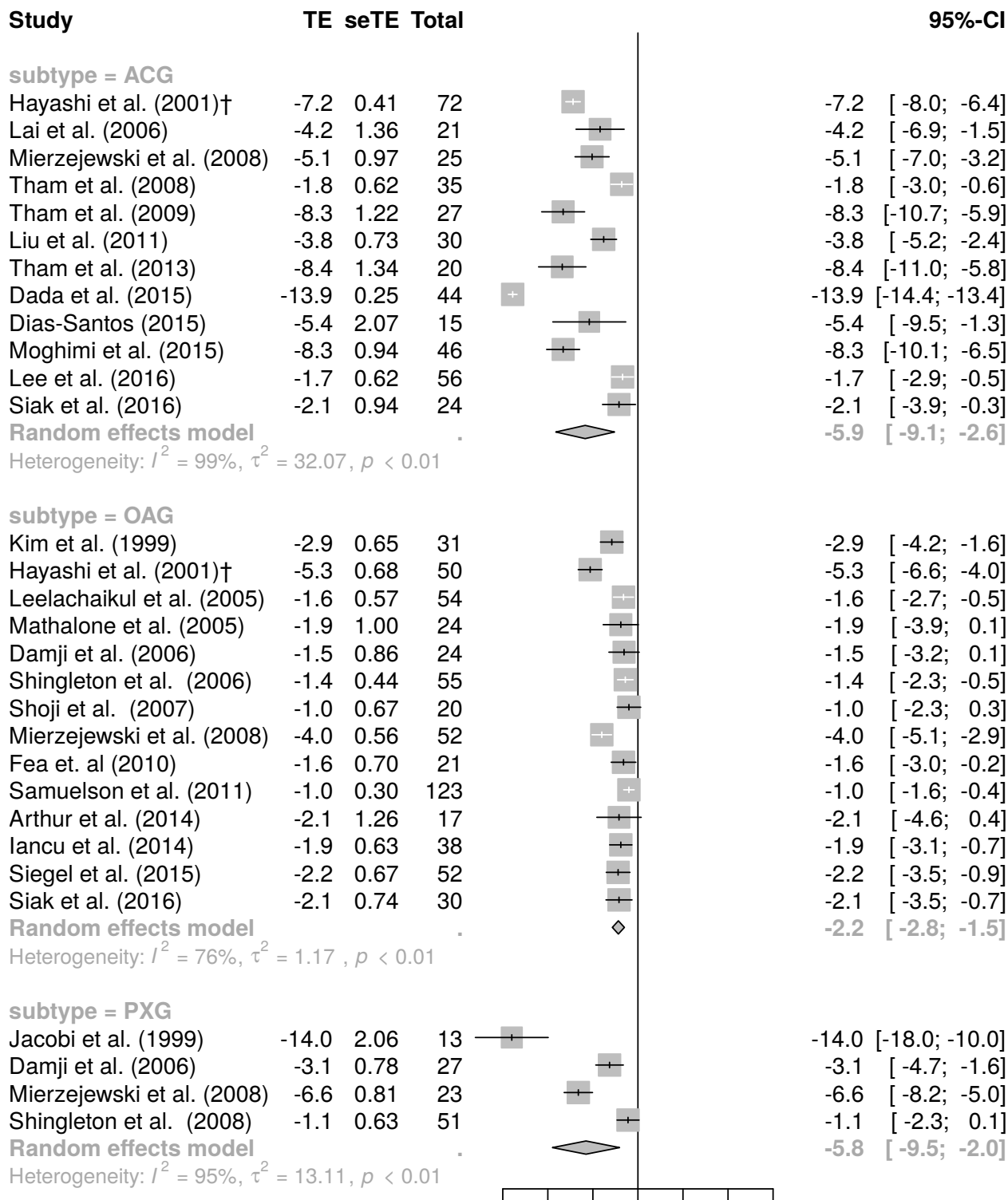
df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))

```

```

m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e=LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"))

```



Meds

```
df_ <- df %>%
  filter(!is.na(RxChangeMean), !is.na(RxChangeStdDev),
```

```

      df$subtype != "acute", MIGsYorN == 'N') %>%
  mutate(subtype=factor(subtype))
m <- metagen(RxChangeMean,
             sqrt(RxPostOpStdDev** 2 + RxPreOpStdDev ** 2) / sqrt>LastPeriodEyes),
             study.name,
             data=df_,
             byvar=subtype,
             n.e>LastPeriodEyes)
forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=FALSE,
       leftcols=c("studlab", "TE", "seTE", "n.e"))

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call(L_textBounds, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>

```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <e2>

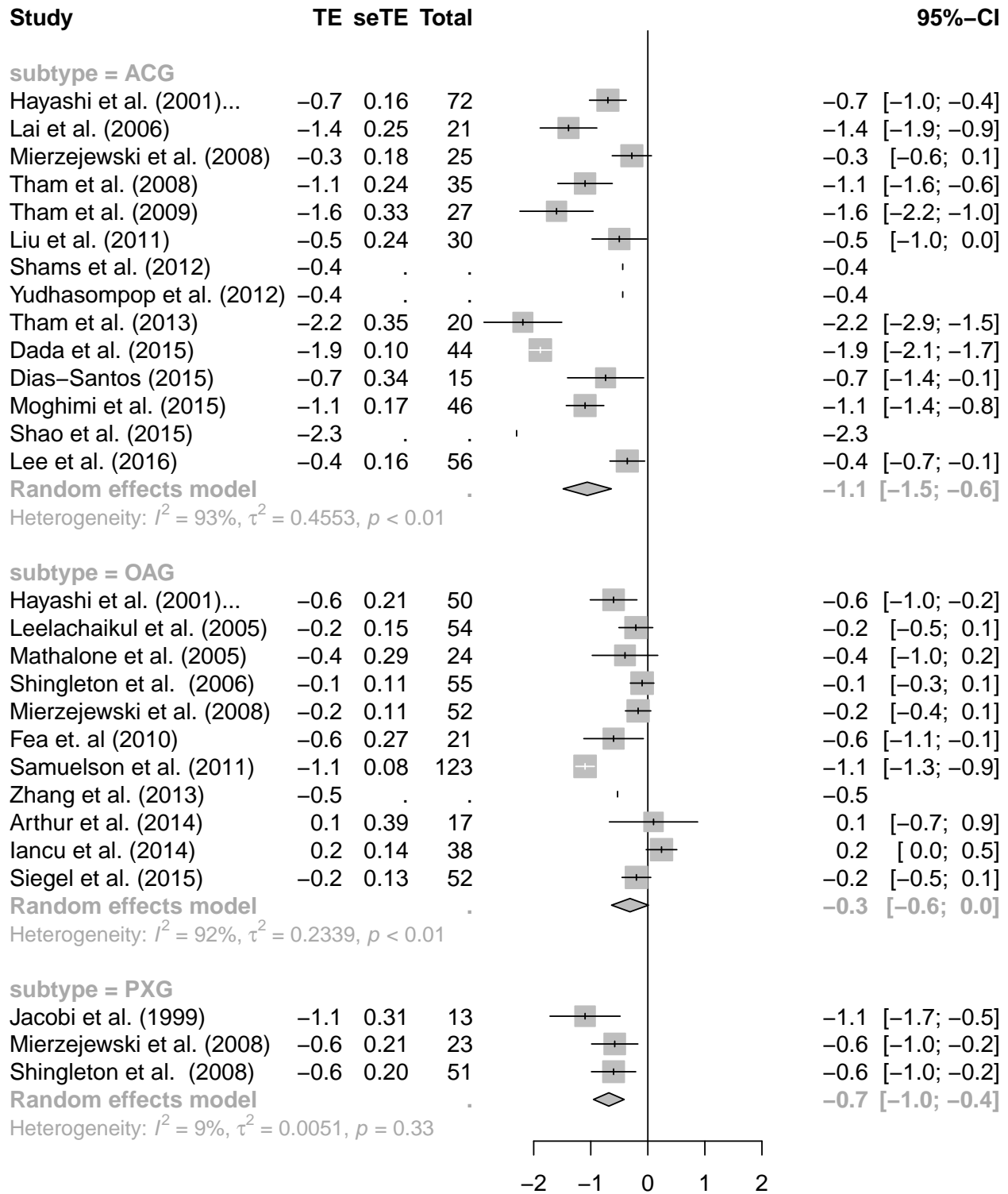
```

```

## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <80>

```

```
## Warning in grid.Call.graphics(L_text, as.graphicsAnnot(x$label), x$x, x
## $y, : conversion failure on 'Hayashi et al. (2001)†' in 'mbcsToSbcs': dot
## substituted for <a0>
```



Sensitivity to missingness

Simulate what the results would look like if there was no effect in the eyes lost to follow up ($\Delta IOP = 0$).

```
meta.analysis.with.sensitivity <- function(missingness='zero') {
  df <- read.data()
  df <- filter.data(df, 'prospective')

  df_ <- df %>%
    filter(!is.na>LastPeriodAbsIOPChangeMean), subtype != "acute") %>%
    mutate(subtype=factor(subtype))

  # Simulate a 0 effect in the unobserved fraction.
  df.missing <- df_
  if(missingness == 'zero') {
    # Zero out.
    df.missing <- df.missing %>% mutate>LastPeriodEyes = PreOpEyes - LastPeriodEyes,
      LastPeriodAbsIOPChangeMean = 0)
  } else {
    # Add 5 mm Hg to each missing eye.
    df.missing <- df.missing %>% mutate>LastPeriodEyes = PreOpEyes - LastPeriodEyes,
      LastPeriodAbsIOPChangeMean = LastPeriodAbsIOPChangeMean + 5)
  }

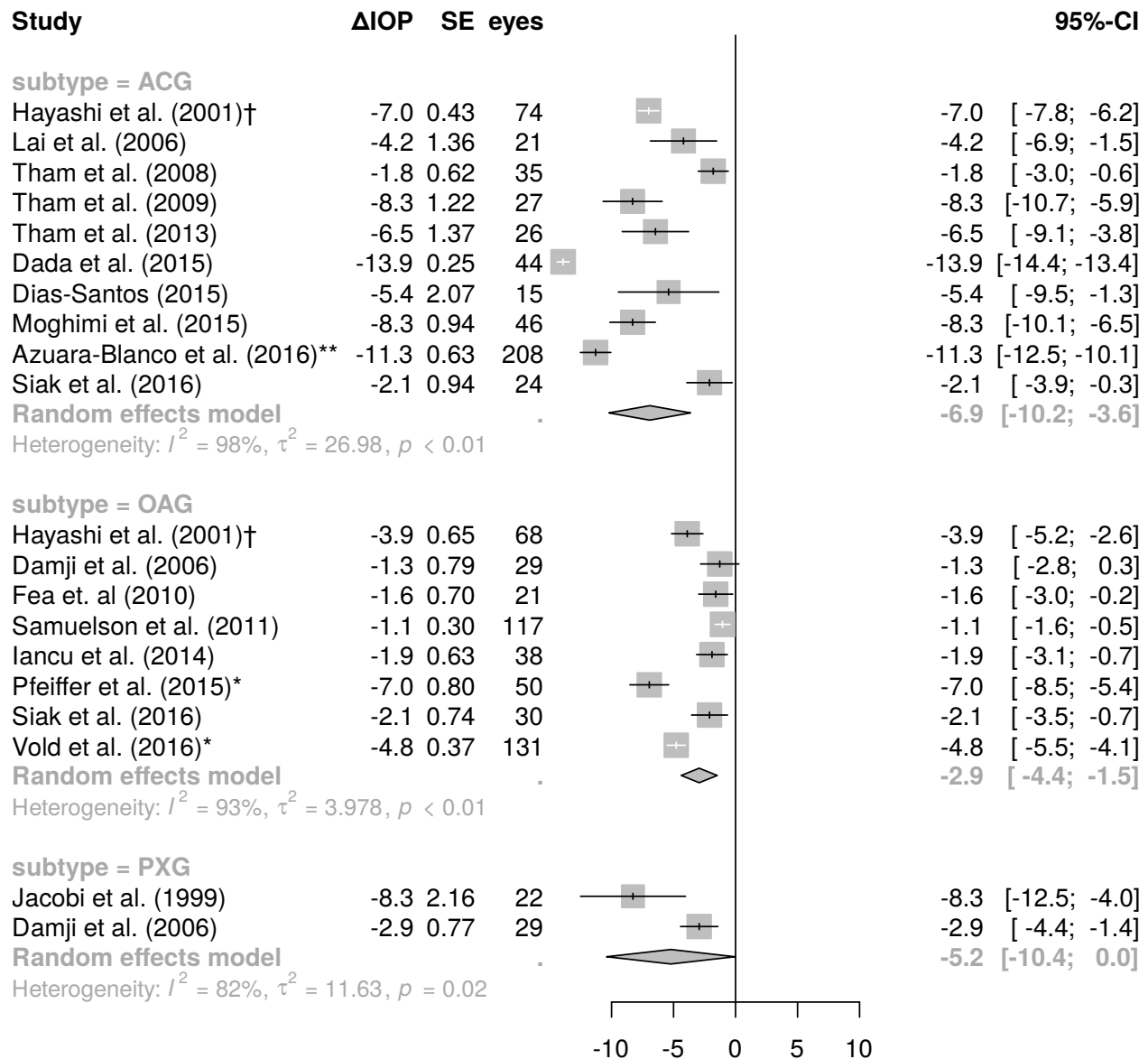
  df_ <- rbind(df_, df.missing)
  # Aggregate two by two
  for(i in seq(nrow(df.missing), 1)) {
    idx <- rep(FALSE, nrow(df_))
    idx[i] <- TRUE
    idx[i*2] <- TRUE
    df_ <- agg.arms(df_, idx)
  }

  df_ <- df_ %>% dplyr::arrange(Year, study.name)

  m <- metagen>LastPeriodAbsIOPChangeMean,
    LastPeriodAbsIOPChangeStdDev / sqrt>LastPeriodEyes),
    study.name,
    data=df_,
    byvar=subtype,
    n.e=LastPeriodEyes)
  forest(m,
    comb.fixed=FALSE,
    digits=1,
    digits.se = 2,
    overall=FALSE,
    leftcols=c("studlab", "TE", "seTE", "n.e"),
    leftlabs=c("Study", " $\Delta IOP$ ", "SE", "eyes"))
}

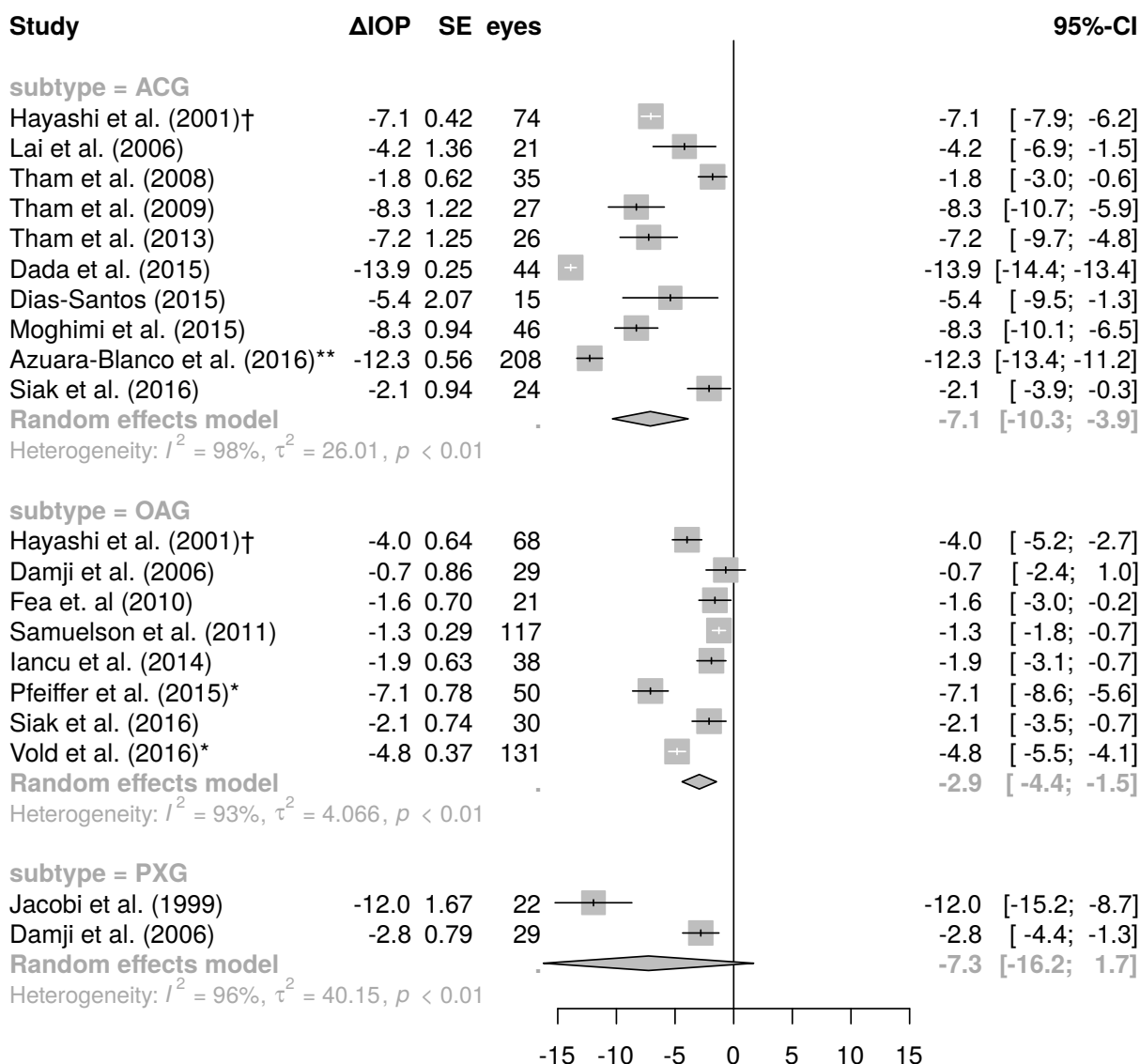
meta.analysis.with.sensitivity()
grid.text(paste0("Simulated net change IOP when  $\Delta IOP = 0$  in eyes lost to follow up"), .5, .97, gp=gpar(
```

Simulated net change IOP when $\Delta IOP = 0$ in eyes lost to follow up



```
meta.analysis.with.sensitivity('five')
grid.text(paste0("Simulated net change IOP when  $\Delta IOP = 5$  mm Hg higher in eyes lost to follow up"), .5,
```

Simulated net change IOP when $\Delta IOP = 5$ mm Hg higher in eyes lost to follow up



MIGS

We don't report these results because it's a bit misleading – the studies aren't very similar to each other, and we don't use the information in their control arms. We can do a much better job through, for example, network meta-analysis, which we plan to do in a future paper.

```
df <- read.data(drop.migs = FALSE)
```

```
## These retrospective studies are losing eyes per period - not impossible, but unusual:
## Mathalone et al. (2005)
## Leelachaikul et al. (2005)
## Shoji et al. (2007)
## Liu et al. (2011)
```



```
## Arthur et al. (2014)
## Tetz et al. (2015)

## These retrospective studies are gaining eyes as the study goes

## Samuelson et al. (2011)

df_ <- df %>%
  filter(!is.na(LastPeriodAbsIOPChangeMean), subtype != "acute", MIGsYorN == 'Y') %>%
  mutate(subtype=factor(subtype)) %>% dplyr::arrange(TypesofMIGSifany, Year)
m <- metagen(LastPeriodAbsIOPChangeMean,
             LastPeriodAbsIOPChangeStdDev / sqrt(LastPeriodEyes),
             study.name,
             data=df_,
             n.e=LastPeriodEyes)

forest(m,
       comb.fixed=FALSE,
       digits=1,
       digits.se = 2,
       overall=TRUE,
       leftcols=c("studlab", "TE", "seTE", "n.e", "TypesofMIGSifany"),
       leftlabs=c("Study", "TE", "seTE", "Total", "Type"))
```

