# **Greedy heuristics**

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## **Problem Description**

The task is to select a subset of nodes and form an optimal Hamiltonian cycle minimizing the total cost and travel distance. Each node is defined by three attributes: **x-coordinate**, **y-coordinate**, and **cost**. Exactly **50% of the nodes** must be selected (rounded up if the total number is odd). The goal is to minimize the sum of the **cycle length** and the **total cost** of the selected nodes.

Distances between nodes are computed using the **Euclidean distance**, rounded to the nearest integer. A **distance matrix** is precomputed after reading each instance and used throughout the optimization process, allowing instances to be represented solely by distance values.

### Methods

#### **Greedy Heuristics**

Four constructive heuristics are implemented and adapted to this problem:

- 1. Random Solution Generates a feasible cycle by randomly selecting nodes.
- 2. Nearest Neighbor (End Insertion) Adds the next node giving the best improvement when inserted only at the end of the path.
- 3. **Nearest Neighbor (Flexible Insertion)** Adds the next node at any position (beginning, end, or inside) that best improves the objective function.
- 4. Greedy Cycle Builds the cycle by repeatedly inserting nodes that minimize the total increase in distance and cost.

Here, "nearest" is understood as the **best improvement in the objective value**, not just geometric closeness. For each heuristic, **200 solutions** are generated from each starting node, and **200 random solutions** are also produced for comparison.

## Pseudocode

## 1. randomSolution(Instance instance)

Purpose: Generates a completely random solution by randomly selecting half the nodes and creating a random tour

#### How it works:

- Randomly selects n/2 nodes from all available nodes
- Randomly shuffles the order of selected nodes to create a tour
- Calculates total cost (travel distance + node costs)

```
FUNCTION randomSolution(instance):
    n = total number of nodes
    numToSelect = ceil(n / 2)

    shuffled = shuffle all nodes randomly
    selected = first numToSelect nodes from shuffled

    order = IDs of selected nodes
    shuffle order randomly

    totalDistance = 0
    FOR each consecutive pair (i, i+1) in order (wrapping around):
        totalDistance += distance from order[i] to order[i+1]

    totalNodeCost = sum of costs of selected nodes
    totalCost = totalDistance + totalNodeCost

    RETURN Solution(selected, order, totalCost, totalDistance)
END FUNCTION
```

# 2. nearestNeighborEndOnly(Instance instance)

**Purpose**: Greedy construction heuristic that always adds the next node at the end of the tour, choosing the one that minimizes the objective increase

- · Starts with a random node
- · Iteratively adds nodes at the end position only
- Selects the node that minimally increases the objective (distance increase + node cost)
- Considers the cycle closure (last node back to first)

```
FUNCTION nearestNeighborEndOnly(instance):
    startNode = random node from all nodes
    selected = [startNode]
    order = [startNode.id]
    remaining = all nodes except startNode
    numToSelect = ceil(n / 2)
    WHILE selected.size < numToSelect AND remaining not empty:
        lastNode = last node in selected
        firstNode = first node in selected
        bestCandidate = null
        minIncrease = infinity
        FOR each candidate in remaining:
            distToCandidate = distance[lastNode][candidate]
            distCandidateToFirst = distance[candidate][firstNode]
            distLastToFirst = distance[lastNode][firstNode]
            distanceIncrease = distToCandidate + distCandidateToFirst - distLastToFirst
            objectiveIncrease = distanceIncrease + candidate.cost
            IF objectiveIncrease < minIncrease:</pre>
                minIncrease = objectiveIncrease
                bestCandidate = candidate
        IF bestCandidate exists:
            append bestCandidate to selected
            append bestCandidate.id to order
            remove bestCandidate from remaining
    calculate totalDistance and totalCost
    RETURN Solution(selected, order, totalCost, totalDistance)
END FUNCTION
```

# 3. nearestNeighborAllPositions(Instance instance)

Purpose: Enhanced greedy construction that considers inserting the next node at any position in the tour, not just the end

#### How it works:

- Starts with a random node
- For each candidate node, tries inserting it at every possible position
- Selects the node-position combination that minimally increases the objective
- More sophisticated than nearestNeighborEndOnly

```
FUNCTION nearestNeighborAllPositions(instance):
    startNode = random node from all nodes
    selected = [startNode]
    order = [startNode.id]
    remaining = all nodes except startNode
    numToSelect = ceil(n / 2)
   WHILE selected.size < numToSelect AND remaining not empty:</pre>
        bestCandidate = null
        bestPosition = -1
        minIncrease = infinity
        FOR each candidate in remaining:
            FOR each position pos from 0 to order.size:
                prevNodeId = order[(pos - 1 + order.size) % order.size]
                nextNodeId = order[pos % order.size]
                distPrevToNext = distance[prevNodeId][nextNodeId]
                distPrevToCandidate = distance[prevNodeId][candidate]
                distCandidateToNext = distance[candidate][nextNodeId]
                distanceIncrease = distPrevToCandidate + distCandidateToNext - distPrevToNext
                objectiveIncrease = distanceIncrease + candidate.cost
```

# 4. greedyCycle(Instance instance, Node startNode)

Purpose: Greedy cycle construction with a specified starting node, similar to nearestNeighborAllPositions but deterministic start

#### How it works:

- Starts with a given node (not random)
- Iteratively inserts nodes at positions that minimize objective increase
- Evaluates all positions between consecutive nodes in the current tour

```
FUNCTION greedyCycle(instance, startNode):
    selected = [startNode]
    order = [startNode.id]
    remaining = all nodes except startNode
    numToSelect = ceil(n / 2)
    WHILE selected.size < numToSelect AND remaining not empty:
        bestCandidate = null
        bestPosition = -1
        minIncrease = infinity
        FOR each candidate in remaining:
            FOR each position pos from 0 to order.size - 1:
                prevNodeId = order[pos]
                nextNodeId = order[(pos + 1) % order.size]
                distPrevToNext = distance[prevNodeId][nextNodeId]
                distPrevToCandidate = distance[prevNodeId][candidate]
                distCandidateToNext = distance[candidate][nextNodeId]
                distanceIncrease = distPrevToCandidate + distCandidateToNext - distPrevToNext
                objectiveIncrease = distanceIncrease + candidate.cost
                IF objectiveIncrease < minIncrease:</pre>
                    minIncrease = objectiveIncrease
                    bestCandidate = candidate
                    bestPosition = pos + 1
        IF bestCandidate exists:
            insert bestCandidate at bestPosition in selected
            insert bestCandidate.id at bestPosition in order
            remove bestCandidate from remaining
    calculate totalDistance and totalCost
   RETURN Solution(selected, order, totalCost, totalDistance)
END FUNCTION
```

## 5. generateSolutions(Instance instance)

Purpose: Generates a large set of diverse solutions using all available construction methods

#### How it works:

- Creates 200 random solutions
- For each node in the instance, generates one solution from each greedy method
- Returns a comprehensive collection of solutions for comparison or further optimization

```
FUNCTION generateSolutions(instance):
    solutions = empty list
```

# Results

```
In [ ]: import pandas as pd
import numpy as np
import os
import matplotlib.pyplot as plt

tspa_df = pd.read_csv("../../raw_data/TSPA.csv", header=None)
tspb_df = pd.read_csv("../../raw_data/TSPB.csv", header=None)
```

#### Instance A

```
In [4]: experiment_summary_a = pd.read_csv("../Results/TSPA/experiment_summary.csv")
```

In [5]: experiment\_summary\_a

]:		Instance	Method	MinCost	MaxCost	AvgCost	NumSolutions	BestSolutionID
	0	TSPA	RandomSolution	235000	300212	265387.29	200	128
	1	TSPA	NearestNeighborEndOnly	90132	120393	103893.21	200	16
	2	TSPA	NearestNeighborAllPositions	71488	74410	72528.80	200	60
	3	TSPA	GreedyCycle	71488	74197	72639.63	200	18

Function to load each solution's method

```
In [6]:
    def load_solution(instance_name,method, solution_id):
        file_path = f"../Results/{instance_name}/{instance_name}_{method}_solutions.csv"
        if os.path.exists(file_path):
            df = pd.read_csv(file_path)
            return df[df['SolutionID'] == solution_id]
        else:
            print(f"File {file_path} does not exist.")
            return None
```

```
In [7]: solutions_A = pd.DataFrame()
    for method in experiment_summary_a['Method'].unique():
        method_data = experiment_summary_a[experiment_summary_a['Method'] == method]
        best_solution_id = method_data['BestSolutionID'].iloc[0]
        print(f"{method}: Best Solution ID = {best_solution_id}")
        solution = load_solution("TSPA", method, best_solution_id)
        solutions_A = pd.concat([solutions_A, solution], ignore_index=True)

solutions_A
```

RandomSolution: Best Solution ID = 128 NearestNeighborEndOnly: Best Solution ID = 16 NearestNeighborAllPositions: Best Solution ID = 60 GreedyCycle: Best Solution ID = 18

Out[7]: SolutionID TotalCost NumNodes TotalDistance ObjectiveFunction Cycle 0 128 235000 100 149144 384144 60-95-167-97-58-2-127-195-122-80-59-42-197-175... 1 16 90132 100 33374 123506 132-144-49-14-62-9-148-106-178-185-165-40-90-2... 2 60 71488 100 23578 95066 46-68-139-193-41-115-5-42-181-159-69-108-18-22... 18 71488 100 23578 95066 143-183-89-186-23-137-176-80-79-63-94-124-152-...

Parse the coordinates from tspa\_df

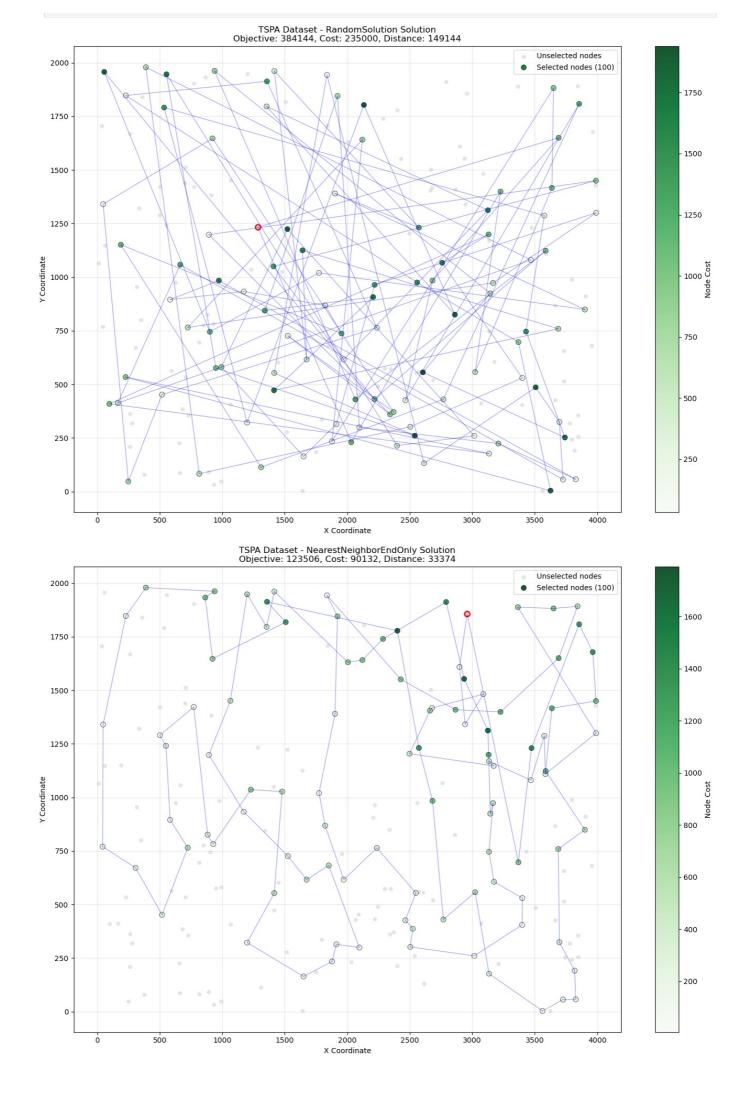
```
In [8]: coords = tspa_df.iloc[:, 0].str.split(';', expand=True)
x_coords = coords[0].astype(int)
```

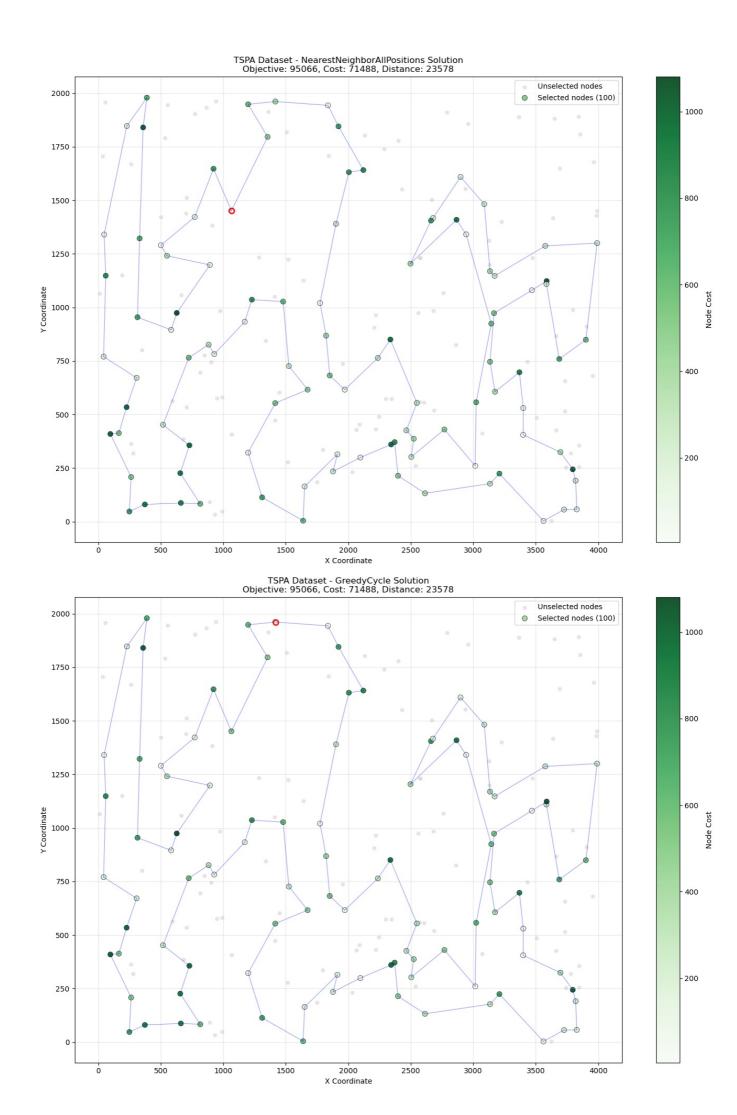
```
y_coords = coords[1].astype(int)
costs = coords[2].astype(int)
```

Graphs

```
In []: def plot solution(instance, method, solution_data):
            Plot a TSP solution showing the cycle and nodes.
            Parameters:
            instance: str - 'TSPA' or 'TSPB'
            method: str - Method name or 'Checker'
            solution data: dict or pandas. Series - Solution data containing cycle information
            if instance == 'TSPA':
                df = tspa_df
            else:
                df = tspb_df
            coords = df.iloc[:, 0].str.split(';', expand=True)
            x coords = coords[0].astype(int)
            y_coords = coords[1].astype(int)
            costs = coords[2].astype(int)
            if isinstance(solution data, dict):
                cycle_str = solution_data['Cycle']
                objective = solution data['ObjectiveFunction']
                total_cost = solution_data['TotalCost']
                total distance = solution data['TotalDistance']
            el se
                cycle str = solution data['Cycle']
                objective = solution_data['ObjectiveFunction']
                total_cost = solution_data['TotalCost']
                total_distance = solution_data['TotalDistance']
            cycle_nodes = [int(x) for x in cycle_str.split('-')]
            highlight x = x coords[cycle nodes]
            highlight y = y coords[cycle nodes]
            plt.figure(figsize=(14, 10))
            unselected_mask = ~x_coords.index.isin(cycle_nodes)
            \verb|plt.scatter(x_coords[unselected_mask], y_coords[unselected_mask],|\\
                       alpha=0.5, s=20, color='lightgray', label='Unselected nodes')
            selected_costs = costs[cycle_nodes]
            scatter = plt.scatter(highlight_x, highlight_y,
                                  c=selected_costs, cmap='Greens',
                                  alpha=0.9, s=50, label='Selected nodes (100)',
                                  edgecolors='black', linewidths=0.5)
            first node idx = cycle nodes[0]
            plt.scatter(x_coords[first_node_idx], y_coords[first_node_idx],
                       c=costs[first_node_idx], cmap='Greens',
                       alpha=0.9, s=50,
                       edgecolors='red', linewidths=2)
            for j in range(len(cycle_nodes)):
                current node = cycle nodes[i]
                next_node = cycle_nodes[(j + 1) % len(cycle_nodes)]
                plt.plot([x_coords[current_node], x_coords[next_node]],
                          [y coords[current node], y coords[next node]],
                          'b-', alpha=0.4, linewidth=0.8)
            plt.colorbar(scatter, label='Node Cost')
            plt.xlabel('X Coordinate')
            plt.ylabel('Y Coordinate')
            plt.title(f'{instance} Dataset - {method} Solution\n'
                      f'Objective: {objective},
                      f'Cost: {total_cost},
                      f'Distance: {total_distance}')
            plt.legend()
            plt.grid(True, alpha=0.3)
            plt.tight_layout()
            plt.show()
```

```
In [10]: methods = ['RandomSolution', 'NearestNeighborEndOnly', 'NearestNeighborAllPositions', 'GreedyCycle']
for i, method in enumerate(methods):
    best_solution = solutions_A[solutions_A.index == i].iloc[0]
    plot_solution('TSPA', method, best_solution)
```





### Instance B

```
Load summary solution of TSPB
In [11]: experiment summary b = pd.read csv("../Results/TSPB/experiment summary.csv")
In [12]: experiment summary b
Out[12]:
                                      Method MinCost MaxCost AvgCost NumSolutions BestSolutionID
             Instance
                                                                                                   17
          0
               TSPB
                               RandomSolution
                                               188700
                                                         239698
                                                                213188.32
                                                                                    200
          1
               TSPB
                        NearestNeighborEndOnly
                                                62606
                                                          77453
                                                                 69681.57
                                                                                    200
                                                                                                   22
          2
               TSPB NearestNeighborAllPositions
                                                49001
                                                         57078
                                                                 51337.26
                                                                                    200
                                                                                                   67
          3
               TSPB
                                  GreedyCycle
                                                49001
                                                          57324
                                                                 51498.08
                                                                                    200
                                                                                                   77
In [13]:
          solutions_B = pd.DataFrame()
          for method in experiment_summary_a['Method'].unique():
              method_data = experiment_summary_a[experiment_summary_a['Method'] == method]
              best_solution_id = method_data['BestSolutionID'].iloc[0]
              print(f"{method}: Best Solution ID = {best solution id}")
              solution = load solution("TSPB", method, best solution id)
              solutions B = pd.concat([solutions B, solution], ignore index=True)
          solutions B
        RandomSolution: Best Solution ID = 128
        NearestNeighborEndOnly: Best Solution ID = 16
        NearestNeighborAllPositions: Best Solution ID = 60
        GreedyCycle: Best Solution ID = 18
             SolutionID TotalCost NumNodes TotalDistance ObjectiveFunction
                                                                                                                 Cycle
          0
                   128
                          220425
                                        100
                                                  168576
                                                                    389001 45-107-142-97-85-193-18-11-134-68-106-88-155-1...
          1
                    16
                           66268
                                        100
                                                   27424
                                                                     93692
                                                                            159-143-106-124-62-18-55-34-35-0-109-29-33-111...
          2
                    60
                           51591
                                        100
                                                   19535
                                                                     71126 166-52-172-179-185-99-130-22-66-94-154-47-148-...
```

Parsing coordinates to plot

18

49891

100

20039

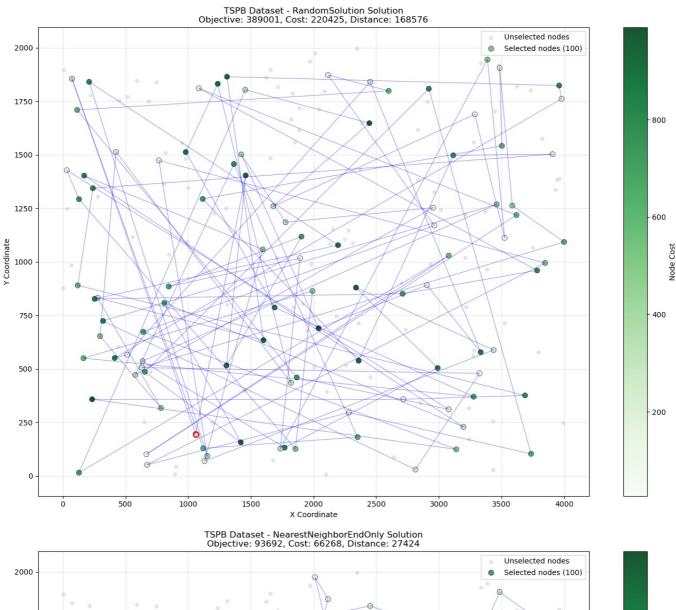
```
In [14]: coords = tspb_df.iloc[:, 0].str.split(';', expand=True)
    x_coords = coords[0].astype(int)
    y_coords = coords[1].astype(int)
    costs = coords[2].astype(int)
```

69930 126-195-168-29-109-35-0-111-81-153-163-180-176...

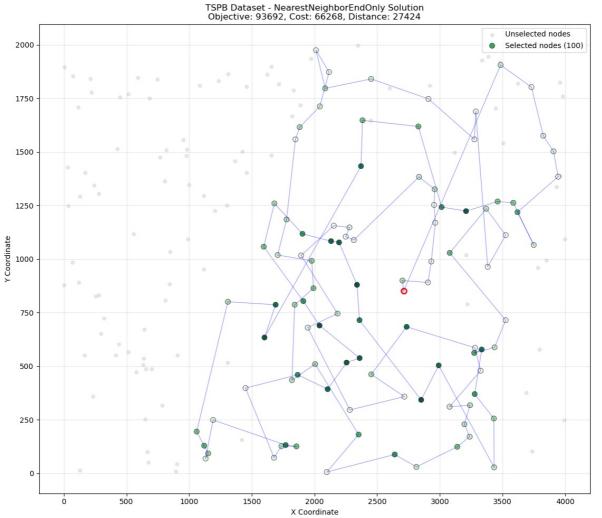
Graphs

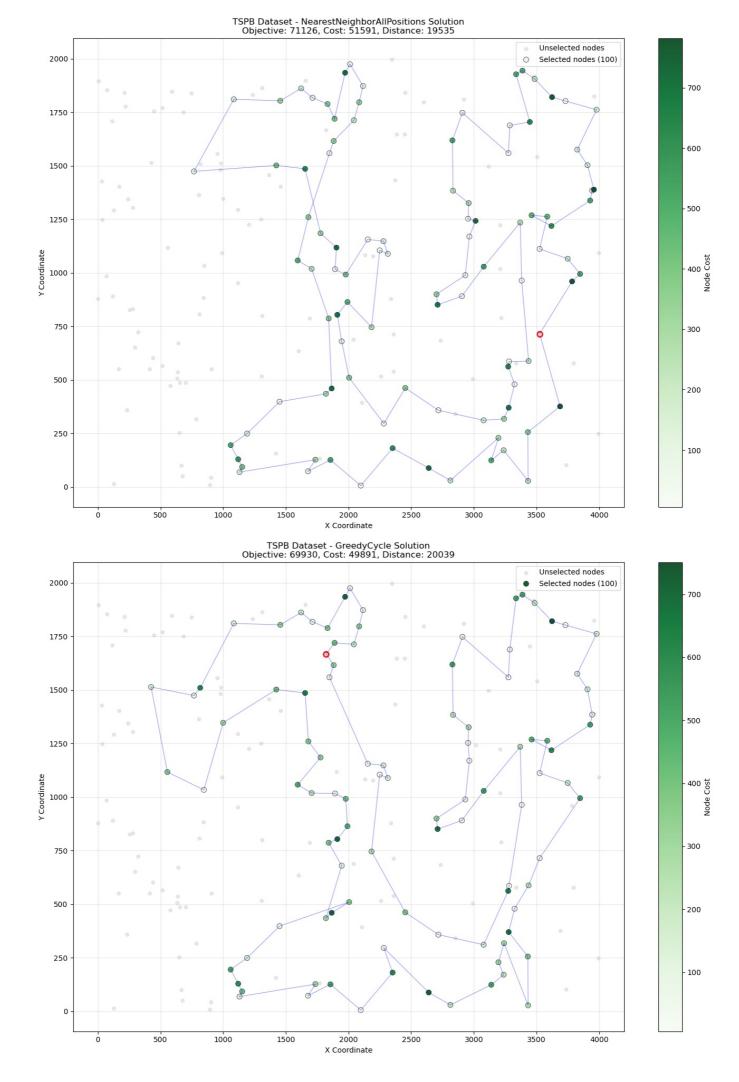
3

```
In [15]: for i, method in enumerate(methods):
    best_solution = solutions_B[solutions_B.index == i].iloc[0]
    plot_solution('TSPB', method, best_solution)
```



- 600





```
In [16]: solution_checker_a = pd.read_excel("../Results/Solution checker.xlsx", sheet_name="TSPA")
    solution_checker_b = pd.read_excel("../Results/Solution checker.xlsx", sheet_name="TSPB")
```

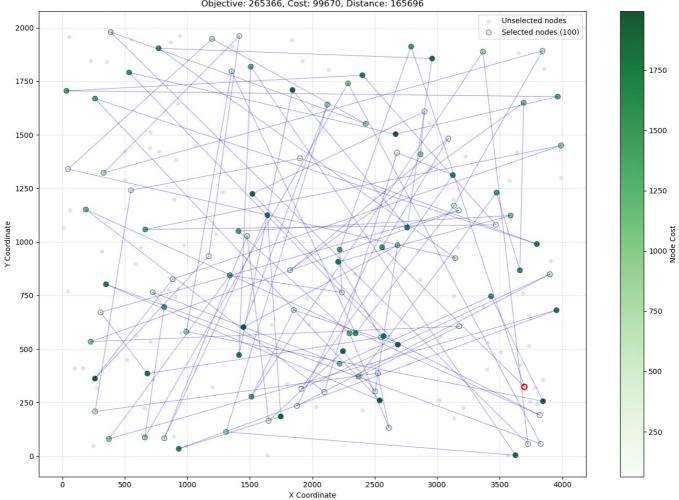
Extract solution in similar format as we had

```
In [17]: def extract checker solution(checker df, instance name):
                                                    total cost = checker df.loc[0, 'cost.1']
                                                    total distance = checker df.loc[0, 'Edge length']
                                                    objective function = checker df.loc[0, 'Objective function']
                                                    cycle nodes = []
                                                    for idx in range(1, len(checker_df)):
                                                                   node id = checker df.loc[idx, 'List of nodes']
                                                                    if pd.notna(node_id):
                                                                                    cycle nodes.append(int(node id))
                                                    cycle_str = '-'.join(map(str, cycle_nodes))
                                                    checker_solution = {
                                                                     'Instance': instance_name,
                                                                     'Method': 'Checker'
                                                                     'TotalCost': int(total_cost),
                                                                      'TotalDistance': int(total distance),
                                                                     'ObjectiveFunction': int(objective_function),
                                                                     'Cycle': cycle str
                                                    }
                                                    return checker_solution
                                     checker_solution_a = extract_checker_solution(solution_checker_a, 'TSPA')
                                     checker solution b = extract checker solution(solution checker b, 'TSPB')
                                     print("Checker Solution for TSPA:")
                                     for key, value in checker solution a.items():
                                                    print(f"{key}: {value}")
                                     print("\nChecker Solution for TSPB:")
                                     for key, value in checker solution b.items():
                                                    print(f"{key}: {value}")
                                Checker Solution for TSPA:
                                Instance: TSPA
                                Method: Checker
                                TotalCost: 99670
                                TotalDistance: 165696
                                ObjectiveFunction: 265366
                                Cycle: 31-111-14-80-95-169-8-26-92-48-106-160-11-152-130-119-109-189-75-1-177-41-137-174-199-150-192-175-114-4-7
                                7 - 43 - 121 - 91 - 50 - 149 - 0 - 19 - 178 - 164 - 159 - 143 - 59 - 147 - 116 - 27 - 96 - 185 - 64 - 20 - 71 - 61 - 163 - 74 - 113 - 195 - 53 - 62 - 32 - 180 - 81 - 154 - 102 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 120 - 
                                144 - 141 - 87 - 79 - 194 - 21 - 171 - 108 - 15 - 117 - 22 - 55 - 36 - 132 - 128 - 76 - 161 - 153 - 88 - 127 - 186 - 45 - 167 - 101 - 99 - 135 - 51 - 112 - 66 - 6 - 156 - 98 - 127 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 128 - 12
                                190-72-94-12-73-31
                                Checker Solution for TSPB:
                                Instance: TSPB
                               Method: Checker
                                TotalCost: 46383
                                TotalDistance: 162402
                                ObjectiveFunction: 208785
                                Cycle: 122-143-179-197-183-34-31-101-38-103-131-121-127-24-50-112-154-134-25-36-165-37-137-88-55-4-153-80-157-14
                                5 - 136 - 61 - 73 - 185 - 132 - 52 - 12 - 107 - 189 - 170 - 181 - 147 - 159 - 64 - 129 - 89 - 58 - 72 - 114 - 85 - 166 - 59 - 119 - 193 - 71 - 44 - 196 - 117 - 150 - 162 - 150 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 162 - 
                                66-169-0-57-99-92-122
                                     Graphs
```

## Instance A

```
In [18]: plot_solution('TSPA', 'Checker', checker_solution_a)
```

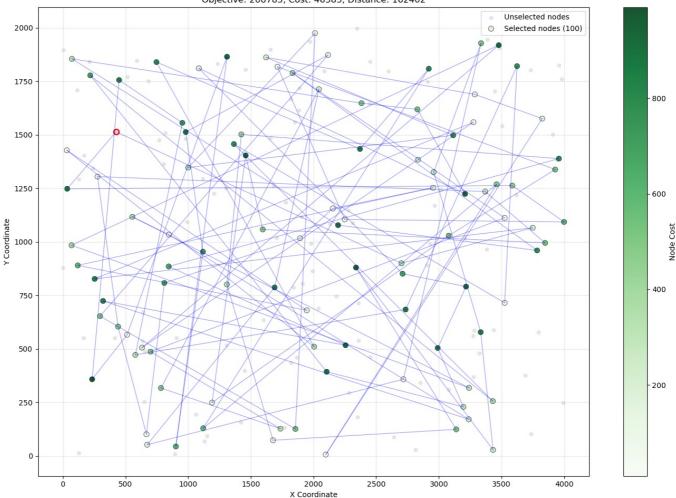
TSPA Dataset - Checker Solution Objective: 265366, Cost: 99670, Distance: 165696



# Instance B

In [19]: plot\_solution('TSPB', 'Checker', checker\_solution\_b)

TSPB Dataset - Checker Solution Objective: 208785, Cost: 46383, Distance: 162402



# Comparison of our solutions to the solution checker

Comparison Table: Heuristic Methods vs Solution Checker

Instance A (TSPA)

Method	Objective Function	<b>Total Distance</b>	<b>Total Cost</b>
Random Solution	384144	149144	235000
Nearest Neighbor (End Only)	123506	33374	90132
Nearest Neighbor (All Positions)	95066	23578	71488
Greedy Cycle	95066	23578	71488
Checker Solution	265366	165696	99670

# Instance B (TSPB)

Method	Objective Function	<b>Total Distance</b>	Total Cost
Random Solution	389001	168576	220425
Nearest Neighbor (End Only)	93692	27424	66268
Nearest Neighbor (All Positions)	71126	19535	51591
Greedy Cycle	69930	20039	49891
Checker Solution	208785	162402	46383

# **Key Findings**

### 1. Performance Comparison:

- The Random Solution method consistently produces the worst results, which is expected as it lacks any optimization strategy
- Greedy heuristics show significant improvement over random selection, demonstrating the value of constructive approaches
- Among the greedy methods, Nearest Neighbor (All Positions) and Greedy Cycle typically outperform the simpler End Only
  approach, as they explore more insertion possibilities

Conclusion: The comparison reveals that while our greedy heuristics produce feasible and competitive solutions efficiently, they

consistently fall short of the checker solution's quality. This gap emphasizes the need for more sophisticated optimization techniques, such as local search operators or population-based metaheuristics, to approach optimal solutions. The foundation provided by these constructive heuristics, however, serves as an excellent starting point for more advanced optimization methods in subsequent iterations.

# Link to the repository:

link GitHub Repository

# Conclusions

This study implemented and evaluated four greedy heuristic methods for TSP. The implemented algorithms: Random Solution, Nearest Neighbor (End Only), Nearest Neighbor (All Positions), and Greedy Cycle demonstrate varying levels of performance across both test instances.

**Algorithm Performance Hierarchy**: The results clearly show a performance hierarchy where sophisticated greedy methods significantly outperform random selection. Greedy Cycle and Nearest Neighbor (All Positions) achieved the best results, producing identical solutions for TSPA and very competitive solutions for TSPB.

## Why Nearest Neighbor (All Positions) and Greedy Cycle Outperform Other Methods:

- Comprehensive Search Space Exploration: Unlike the End Only variant that restricts insertions to the tour's end, both superior methods evaluate all possible insertion positions. This expanded search space allows them to find locally optimal placements that minimize the objective function increase at each step.
- Reduced Greedy Trap Susceptibility: By evaluating multiple insertion points, these algorithms are less likely to get trapped in poor local decisions early in the construction process. The End Only method, once it makes a suboptimal early choice, cannot recover by repositioning nodes.

The implemented greedy heuristics serve as effective constructive algorithms for this variant of TSP, providing good starting solutions.

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