

ABSTRACT

Title of dissertation:

EVALUATION OF STRENGTH AND
RELIABILITY OF SOLID-OXIDE FUEL
CELLS AT OPERATING CONDITIONS

Patrick Stanley, Doctor of Philosophy, 2018

Dissertation directed by:

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Solid-oxide fuel cells (SOFC) have the potential to help the energy economy transition to a more efficient generation method. A challenge in SOFCs is that the composite ceramic cell must maintain a gas-tight seal between the anode and cathode while minimizing the thickness to improve performance. This seal must hold through heating and changes in oxygen content, which effect the physical and mechanical properties of the materials. To understand these effects, it is needed to investigate the effects of environment, microstructure, and macrostructure interplay on the cell's strength, modulus, and fracture toughness.

It has been a challenge to measure the mechanical properties of the materials at the conditions they are used at in SOFCs. Most research to date investigates the material properties at ambient conditions after cycling a cell or at elevated temperatures in air. As part of this work, an enclosed three point bend apparatus has been built which can be heated to the same temperature and environment as an operating SOFC, measuring their properties in-situ.

With this technique, among others, a variety of materials and systems have been characterized, including established materials, nickel-oxide and gadolinium doped ceria, to new materials such as a strontium iron cobalt molybdenum oxide. It has been determined how the choice of pore former effects the strength up to elevated temperatures, how fracture toughness and strength can increase with temperature due to relaxation of intrinsic stresses, the most likely time for failure of an SOFC is under reduction due to uniform growth of microstructure flaws and how cell orientation does not impact mechanical properties.

This new knowledge into the changing mechanical properties of the different materials and structures tested will allow for the design and optimization of SOFC devices to maximize reliability and performance. In addition, the apparatus built to measure in-situ properties can also be applied to other temperatures and gaseous environments for different applications. This work helps bring SOFCs from a theoretical lab-based technology to a reliable means of efficient energy generation for use by society.

EVALUATION OF STRENGTH AND RELIABILITY OF
SOLID-OXIDE FUEL CELLS AT OPERATING CONDITIONS

by

Patrick Owen Stanley

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University of Maryland, College Park in partial fulfillment
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Dedication

I dedicate this work to my wife who has supported and encouraged me throughout.

Acknowledgments

I owe my gratitude to all the people who have made this thesis possible and because of whom my graduate experience has been one that I will cherish forever.

First and foremost I'd like to thank my advisor, Professor Rajarshi Roy for giving me an invaluable opportunity to work on challenging and extremely interesting projects over the past four years. He has always made himself available for help and advice and there has never been an occasion when I've knocked on his door and he hasn't given me time. It has been a pleasure to work with and learn from such an extraordinary individual.

Acknowledge Wachsman, George Quinn, Redox, lab-mates, AIMLab, XRCC, other specific people, family.

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List of Abbreviations and Symbols

SOFC Solid-Oxide Fuel Cell.

Chapter 1: Introduction

1.1 Solid-Oxide Fuel Cells

The world depends on fossil fuels for its daily energy needs. This is a fact that is going to stay with us for the foreseeable future. By 2040, it is estimated that fossil fuels will still supply 78% of total energy demand. [1] Traditionally, the annual increase in demand is met by an increase in supply of fuel. This increase is supplied by advances in mining and drilling operations, although recent advances have been found to be controversial, such as hydraulic fracturing. [2,3] These concerns do not even account for the increased emissions caused from combustion of fossil fuels and their effect on the global environment. [4–6]

An alternative to increasing the supply and usage of fossil fuels is to increase our efficiency of turning the fuel into useful work. Solid-oxide fuel cells (SOFCs) have the ability to solve this for applications where electrical power is desired. SOFCs allow for the direct conversion of chemical energy to electrical energy, where devices such as combustion generators must convert chemical energy to thermal energy, to mechanical energy, and finally to electrical energy. Each energy conversion has intrinsic losses, limiting efficiency. Power generation plants have efficiencies around 30%, while a stand-alone SOFC generator can convert fuel to electricity at 45 to

65% efficiency. [7, 8] SOFCs are able to run on a variety of fuel sources, such as hydrogen, methane or even biogas. [9, 10] This fuel flexibility and higher efficiency helps position SOFCs to bridge the gap in the energy economy as it transitions from fossil fuels to renewable sources.

Fuel cells operate by placing a fuel and an oxidizer (usually air) on separate sides of the cell. Ions are shuttled through the cell to react with the other species, while electrons are transported through an external circuit performing work. In the case of SOFCs, the transported ions are oxygen ions which move from the cathode to the anode through the electrolyte. Figure1.1 demonstrates how an SOFC works for a hydrogen fueled SOFC. The cathode and anode materials must facilitate the incorporation of oxygen into the cell and the reaction between the oxygen and the fuel. The cell operates at temperatures ranging from 600 °C to 1000 °C depending on the technology used in order to increase the ionic conductivity and performance. It is critical that the fuel and air remain separated by the cell. If there is a leak either through the cell or around it, then the electric potential across the cell will decrease, harming the performance.

SOFc materials rely on ionic conduction to transport oxygen from one side of the cell to the other. In ionic conduction, oxygen ions hop from site to site via oxygen vacancies, locations where an oxygen atom is missing from the lattice. Because conduction depends on vacancies, the more vacancies in the lattice, the more available sites for oxygen to move between, and the greater the conductance. The relationship between oxygen vacancy concentration and oxygen conductance is given by Equation1.1, where σ_i is the ionic conductivity, $[V_O^{••}]$ is the concentration

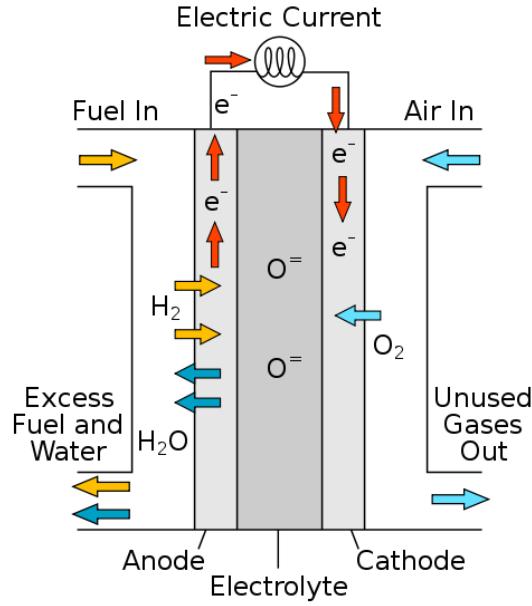


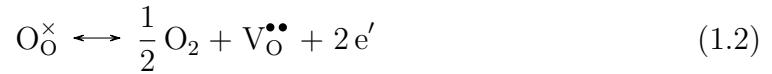
Figure 1.1: Diagram showing flow of materials in the operation of a SOFC. [11]

of oxygen vacancies in the lattice, μ is the ionic mobility of the oxygen, and Ze is the charge of the conducting species. [12]

$$\sigma_i = [V_O^{\bullet\bullet}] Ze \mu \quad (1.1)$$

Thus by adding more oxygen vacancies to the system, the ionic conductivity increases, but changes in point defect concentrations can have other effects on the materials.

During operation, oxygen vacancies are created by exposing the anode to an environment with a low partial pressure of oxygen (pO_2), as shown in Equation 1.2.



The oxygen on the surface of the anode side reacts with the fuel to prevent the oxygen from reincorporating into the material. The final concentration of oxygen defects will depend on the exact environmental and material conditions and location

in the cell, but some steady state value will eventually be reached. With one side of the cell exposed to low pO_2 , and the other side exposed to air, a chemical potential gradient is established across the cell. This gradient drives the motion of oxygen through the cell, the oxidation of the fuel, and generates the electric current. The electrical potential at open circuit conditions is expressed by the Nernst equation, given in Equation 1.4 for the reaction given in Equation 1.3, where f_A is the fugacity of species A, E^o is the standard potential for the reaction, and n is the number of charges involved in the reaction. [13]



$$E = E^o - \frac{RT}{nF} \ln \left(\frac{f_C^c f_D^d}{f_A^a f_B^b} \right) \quad (1.4)$$

For the case of a hydrogen fueled SOFC, Equation 1.4 can be simplified to Equation 1.5. [14]

$$E = E^o + \frac{RT}{2F} \ln \left(\frac{pH_2(pO_2)^{1/2}}{pH_2O} \right) \quad (1.5)$$

From these equations it can be seen that the partial pressures of the involved species have a large role to play in the performance of the cell.

Each component of a SOFC is fabricated from a single material or from combinations of materials designed to optimize that parts function. For example, a cell can be comprised of a nickel metal-gadolinium doped ceria (GDC) anode, a GDC electrolyte, and then a lanthanum strontium manganite cathode. [15, 16] These individual components are tape cast from bulk powders, with additives such as pore formers where appropriate, into thin flexible sheets that are then laminated together and fired to create a single cell. As a result, a completed cell has distinct layers in

it where the materials and its overall properties abruptly change. This composite structure can then have inter-diffusion between layers, smoothing out the abrupt changes, but creating new structures and compositions that were not present upon lamination. [17]

Nickel has traditionally been used as an anode material in SOFCs, due to its high catalytic properties. A challenge with nickel is that at ambient conditions it oxidizes into nickel oxide, but at operating conditions it reduces to the desired nickel metal. There is a large lattice parameter change between nickel and nickel oxide, so that as it reduces, it decreases volume by over 15%. This means that the overall porosity of the anode layer increases as the SOFC is put into service. [18, 19] This increased porosity can greatly decrease the flexural strength and modulus of the anode and of the overall cell. [20, 21] The effect on flexural strength follows an exponential decay as shown in Equation 1.6, where P is the porosity, and n and σ_o are experimentally determined. What was once a cell that could withstand the stresses of being sealed, can weaken to the point of fracture after reduction.

$$\sigma_f = \sigma_o \exp(-nP) \quad (1.6)$$

Porosity is not a completely undesirable trait of SOFCs. For the SOFC to efficiently function, gas must be able reach the active sites in the cell. These active sites, or triple phase boundaries (TPB), are the points where gas, electronic conductor, and ionic conductor meet, as demonstrated in Figure 1.2. For example, on the anode side of a Ni-GDC cell, this would be a point where nickel meets GDC and the gas. The more TPB that are present, the more exchange can occur between the gas and

the cell. To maximize TPBs, pores can be added, greatly increasing the available surface area of the anode. Again, this becomes a trade off between added porosity for performance and a reduction in strength. [22, 23]

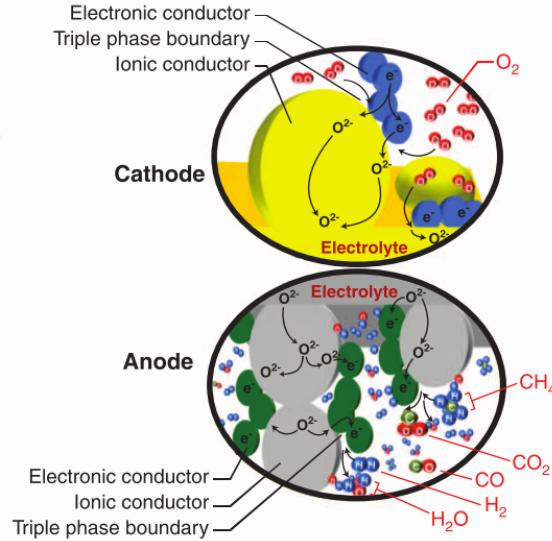


Figure 1.2: Diagram showing the triple phase boundary and the importance as being the site where incorporation and reactions occur. [7]

Ideally, a SOFC is as thin as possible to minimize diffusion path lengths and resistances in the cell. [24] Realistically, the cell must be able to withstand the stresses of being manufactured, sealed, heating, and use. This means that a compromise must be met as to how the cell is supported and which components do the supporting. Traditionally, electrolyte supported cells were used with yttria-stabilized zirconia electrolytes, but recently anode supported cells have been able to provide lower resistances while adequately supporting the cell. [25, 26] Now the anode layer, which is needed to be porous for gas diffusion, must support the majority of the stresses the cell is subjected to.

Many of the materials used in SOFC have a fluorite crystal structure, because of the crystal structure's high mobility for oxygen ions. As oxygen vacancies are produced, the interatomic bonding of the structure changes, which can change bulk properties of the crystal. [27, 28] If the strength of the atomic bonds weakens on average, due to added vacancies, it then follows that the modulus and strength of the crystal would also decrease. This relationship has been shown to fit for single grains of GDC, but this does not necessarily hold true for an actual cell. [29] Grain boundaries can play a large role in the mechanical properties of a bulk sample. For this reason microstructure combined with environmental conditions can play a large role on the overall mechanical properties of a fuel cell.

Chapter 2: Development of Testing Apparatus

2.1 Overview

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Chapter 3: High Temperature Mechanical Behavior of Porous Ceria and Ceria-Based SOFCs

3.1 Introduction

Solid oxide fuel cells (SOFCs) are a highly efficient energy conversion technology entering the market. Commercialization of these devices requires the development of effective manufacturing methods that involves solving a number of problems that are not present in the scientific research environment. The most immediate challenge is how to provide adequate sealing for full size SOFCs in a multi-cell stack. For planar SOFCs, a standard stack design consists of a number of square cells separated by metal interconnects. [30] These interconnects act as current collectors, gas channels, and separators to prevent fuel and air from mixing. Sealing of these stacks is accomplished by compressing the layered structure which includes sealing material. As more compressive force is applied to the stack, the quality of the seals improves. However, any cell which is not perfectly flat will experience flexural stress as a result and this can lead to cells fracturing. Due to the brittle nature of the ceramic materials that constitute SOFCs, a very thorough understanding of the mechanical limits of these devices is critical to their successful deployment.

The vulnerability of SOFCs to mechanical failure is a well-known issue. However, much of the research into this phenomenon has focused on yttrium stabilized zirconia (YSZ) based devices. [19, 31, 32] This material has been the standard for the field and has desirable mechanical properties but requires high temperatures to function well. As efforts are made to lower SOFC operating temperatures, a shift to ceria-based electrolytes has occurred. Less attention has been given to the mechanical behavior of doped ceria materials across SOFC operating conditions.

Much of the study of fracture in ceramic materials has been done on technical ceramics for medical applications and for coating metal components. [33–40] These materials are optimized for fracture toughness and durability and very rarely experience temperatures above a few hundred degrees Celsius. The fracture surface analysis and correlations between microstructure and strength described for these materials are a valuable starting point for investigating fuel cell materials. However, there is a lack of extensive investigation into the properties of IT-SOFC materials at their expected operating temperatures and environments.

Efforts have been made to comprehensively examine the mechanical properties of SOFC materials and the effect of non-standard conditions on those properties. Nakajo et al. conducted a wide ranging study of materials used in anode supported SOFCs which included some attention to temperature and atmosphere effects. [32] While providing a solid base of material knowledge, this work did not fully cover materials beyond YSZ and there remains a need for further testing, especially for doped ceria. Flexural strength and Young's modulus measurements for gadolinium doped ceria (GDC) have been carried out in ambient conditions by Yasuda et

al. [41] They characterized the effects of sintering temperature on density and the resulting mechanical properties. Further testing of this material system at elevated temperatures and anode gas reducing environments must be done to fully understand the mechanical behavior of GDC.

This article presents the results of a broad range of flexural tests involving the materials used in ceria-based anode supported SOFCs along with the assembled half-cells. Using a purpose-built temperature controlled environmental chamber installed in a universal testing machine (UTM), porous doped ceria bars, anode support layers (ASL) composed of nickel and doped ceria cermet, and half-cells composed of an ASL and a doped ceria electrolyte were tested. The various test conditions used included expected operating temperatures (450 °C–650 °C), and both reducing and oxygenated atmospheres. These variations in test conditions are important because these cells must maintain their integrity from when they are first placed in a sealed stack to when they reach operating conditions. In particular, this study was intended to determine at what point in their life SOFCs are most vulnerable to mechanical failure and the mechanisms involved. Additionally, the effect of the anode-electrolyte interface on flexural strength was explored.

3.2 Experimental

3.2.1 Sample Preparation

GDC bars of varying porosity were fabricated using uniaxial pressing in a rectangular die. GDC10 ($\text{Ce}_{0.9}\text{Gd}_{0.1}\text{O}_2$) powder was mixed with the desired volume

of poly(methyl methacrylate) (PMMA) microspheres (5 μm diameter) or graphite flake to create the green body, with 0.1wt% of polyvinyl butyral added to aid in pressing and a drop of fish oil to act as a dispersant during milling. The two different pore formers were used to create differing pore geometry. The PMMA or graphite was removed by a 400 $^{\circ}\text{C}$ pre-sintering step, and the remaining ceramic structure was sintered at 1500 $^{\circ}\text{C}$ for 4 hours. Archimedes density measurements were used to confirm porosity percent. Samples were polished with 600 grit sandpaper on all sides before testing.

The ASL and half-cell coupons used in the flexural testing were made using tape casting. NiO and GDC powders in a 6:4 weight ratio were mixed with ethanol, toluene, and fish oil. The mixture was ball milled on a rotary mill for 24 hours. Polyvinyl butyral and benzyl butyl phthalate were added, followed by another 24 hours milling. The resulting slurry was degassed and tape cast using a 700 micron blade height. The tapes were left to dry overnight before being cut into 12 cm by 12 cm squares. Three squares were stacked and hot pressed at 49 $^{\circ}\text{C}$ and 2 tons for 30 minutes. Following this lamination, the tape was cut into rectangular coupons measuring 25mm by 10mm. The coupons were fired at 1400 $^{\circ}\text{C}$ for 4 hours. Final bar dimensions were 8.16 by 24.15 by 2.98 mm on average. For half-cell coupons GDC electrolyte slurry was prepared and tape cast with a 40 micron blade height. After the lamination of the three ASL layers, a single layer of electrolyte tape was laminated to the ASL using the same pressure for 2 hours. The sintering procedure for half-cell coupons was identical to the ASL coupons. Samples were polished with 600 grit sandpaper on edges before testing.

3.2.2 Thermogravimetric Analysis

To understand the degree of reduction in test coupons, thermogravimetric analysis (TGA) was used to measure the mass loss as a function of time, temperature, and gas environment. A Cahn D200 microbalance was used to measure the weight changes as the sample was heated in a furnace with controlled atmosphere. A small section of test coupon was placed in a crucible suspended from the balance and heated to 650 °C at 10 °C/min, the environment was switched from 50 sccm of 21% O₂ in N₂ to 50 sccm of 3% H₂, 3% H₂O in N₂. Mass, temperature, and p_{O₂} measurements were taken at 30 second intervals. p_{O₂} measurements were taken using a calibrated YSZ sensor placed immediately before the sample. Samples were cooled at 10 °C/min in the desired atmosphere.

3.2.3 Development of Mechanical Test Apparatus

To develop a testing apparatus capable of simulating the various conditions experienced by operating SOFCs, appropriate materials were chosen based on thermal and chemical stability criteria. Alumina was chosen to build the bend fixture due to its chemical stability and high hardness. The sample rests crossways on two stationary 6.35mm diameter rods which are placed in troughs separated by 20mm. The upper half of the fixture consists of a 6.35mm rod used to apply stress to the sample from the UTM crosshead. Both pieces are attached using silica-based cement to 300 mm rods attached at the anchor points of the UTM. Assembly and alignment is assisted with the use of a 3D printed jig to ensure repeatability. The complete

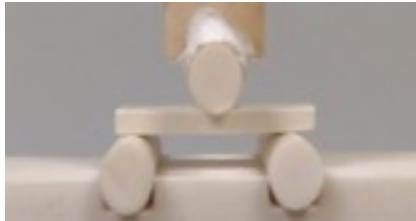


Figure 3.1: Assembled Alumina 3-Point Bend Fixture

alumina, 3-point bend fixture is seen in Figure 3.1 with the two bottom rollers, a sample, and the top roller making contact, applying flexural stresses to the sample.

To create the atmosphere control system, a combination of standard and custom vacuum system parts were used to enclose the bend fixture. For the main body of the chamber, a 3-inch inner diameter, stainless steel tee was made with QF80 and QF50 flanges. Welded NPT ports on top and bottom allow for gas inlet and outlet and the introduction of a thermocouple through a Swagelok Ultra-Torr fitting.

Figure 3.2 shows the engineering drawings and photo of the custom pieces from A&N Corp. Flexible bellows allow for the motion of the cross-bar to be translated into the fixture, requiring the subtraction of the spring force to be removed during analysis. The alumina fixture was then inserted through each end and the chamber incorporated into the furnace with QF50 to 1/2 inch tube adapters that fit over the alumina rods.

To heat the fixture and chamber, a 1 ft. cube was assembled from steel plates with cutouts on top, bottom and front. Steel wire mesh was used to create a framework inside to hold nickel-chromium alloy heating elements. Silica-based wool insulation was packed between the center cavity and the case walls. A K-type thermocouple was inserted into the chamber and used with an external PID controller

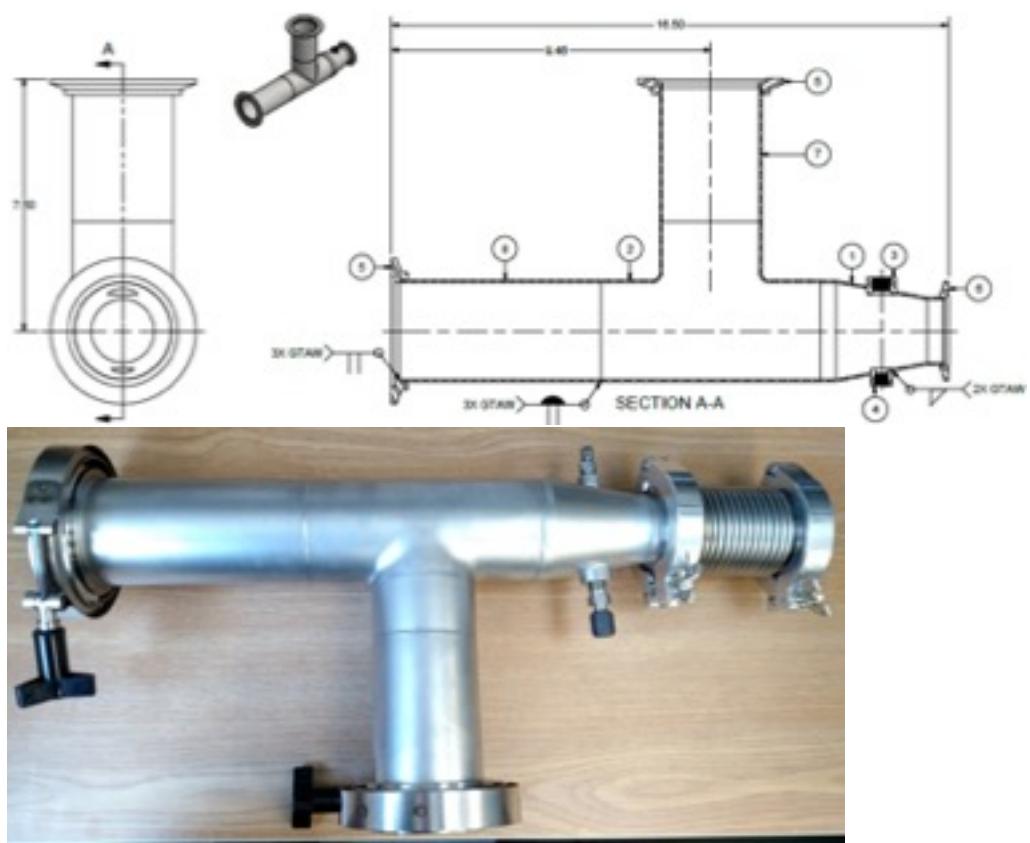


Figure 3.2: Design drawing and photo of mechanical testing atmospheric chamber

to cycle the heating elements. The furnace was placed on a supporting scaffold to hold it in position during tests. The test fixture, atmosphere chamber, and furnace were affixed together as one unit and inserted into the UTM. The design was compared and qualified to a regular steel 3-point bend apparatus to ensure accurate results at room temperature.

3.2.4 Bend Testing

All tests conducted in the UTM (Tinius Olsen 10ST with 250 N load cell) were done at a rate of 0.2 mm/min with a 20 mm lower span. After measuring the force at fracture, stress was calculated using Equation 3.1 for 3-point flexural of rectangular samples, where σ_f is the stress at failure, F is the load at failure, L is the span of the fixture, b is the width of the sample and d is the thickness of the sample. At room temperature, the coupons or bars were loaded into the fixture and tested in batches of 5 per condition. Occasionally samples would break or be damaged before testing, reducing the sample set. For sample sets at elevated temperatures in ambient atmosphere, the samples were loaded into the front of the chamber, acting as a staging area, prior to heating the on fixture in the center. Upon transferring the next coupon from the staging area to the fixture, a 20 minute waiting period was used to ensure that the coupon had reached thermal equilibrium prior to testing.

$$\sigma_f = \frac{3FL}{2bd^2} \quad (3.1)$$

Following the completion of the set, all coupon pieces were cooled at a rate of 10 °C/min. For testing in reducing atmosphere, each coupon was reduced and tested

individually. Half-cell coupons were tested in two orientations, "electrolyte-up" and "electrolyte-down." These orientations cause the dense electrolyte layer to experience compressive or tensile stress. The "electrolyte-up" orientation subjects the electrolyte to compressive stress and vice-versa.

Following the destructive tests, SEM analyses of the fracture surfaces were performed. The purpose of this was to observe the trans-granular, inter-granular, or mixed nature of crack propagation, and to find any anomalous features on the fracture surface, as well as to observe pore geometry.

3.2.5 Atmospheric Treatment

To test individual coupons under reducing environments, samples were loaded into the test chamber at 400 °C, after previous pre-heating in the staging area. After 20 minutes, the temperature would be increased to the desired set-point of 650 °C at a ramp rate of 10 °C/min and the gas would be switched first to N₂ to flush the chamber, then to humidified argon containing 3% H₂. It would then be allowed to sit for 18 hours before testing to allow reduction. After testing, the chamber would be flushed again with N₂ and cooled to 400 °C before opening to change samples and repeat the process.

If samples had been previously reduced as a batch by exposure to hydrogen in a tube furnace and cooled under hydrogen, the atmospheric treatment was shortened, as supported by TGA results. Pre-reduced samples were loaded into the chamber at or below 400 °C, the chamber flushed N₂, then with H₂ in Ar. After this the chamber

would be heated to 650 °C, the sample tested after a 30 minute period, and cooled back down to 400 °C. At this point, the chamber would be flushed with N₂. While the chamber maintained a positive pressure of N₂, it could be opened, a new sample loaded, closed, and allowed to flush. This procedure allows for the batch reduction of many test coupons and replaced the 18 hour reduction time with a shorter 30 minute period.

3.3 Results

3.3.1 Porosity and Pore Former Choice

As expected, GDC bars with greater porosity displayed lower flexural strength values as compared to less porous samples. The relationship between porosity and strength followed an exponential trend. This behavior is well established for porous ceramics and is described by Equation 3.2, where σ_f is the flexural strength with porosity, σ_o is the flexural strength without porosity, η is a geometric constant dependent on the system, and P is the volume percent porosity of the sample. [42]

$$\sigma_f = \sigma_o e^{-\eta P} \quad (3.2)$$

The data was fit using this equation and both a fixed geometric constant, η , of 0.047 (Figure 3.3a) and a variable geometric constant (Figure 3.3b).

Chi-squared values, indicating the divergence of the fit from the measured data for each sample set, were calculated for the two fitting methods and are displayed in Table 1.

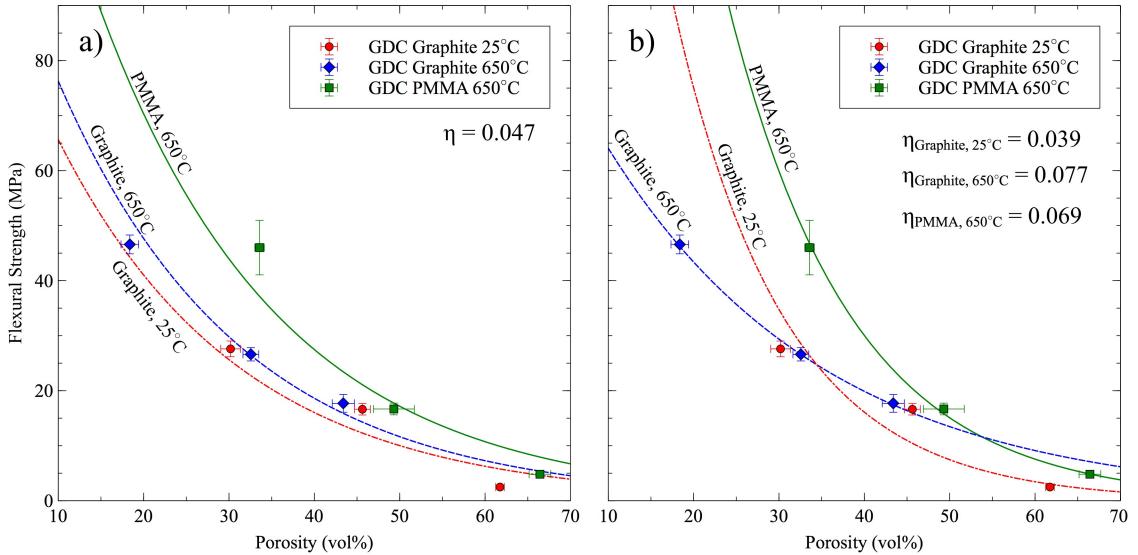


Figure 3.3: Flexural strength-porosity dependence for porous GDC10 at 650 °C and 25 °C using spherical PMMA or graphite flake pore former: a) Measured strengths fitted using fixed geometric constant; b) Measured strengths fitted using different geometric constants

Table 3.1: Chi-squared values for fixed η and variable η fits of porous GDC strength data (Figure 3.3)

Sample Set	χ^2 (Fixed η)	χ^2 (Variable η)
GDC PMMA 650 °C	3.406	0.062
GDC Graphite 650 °C	0.668	0.008
GDC Graphite 25 °C	3.575	5.063

The deviance from the fit curve for the fixed η method is quite large relative to the variable η fit for both sample sets tested at 650 °C. Both fitting methods are fairly poor in the case of the room temperature graphite set. The poor fitting results in this case is due to the >60% porosity samples. The flatter pore geometry caused by the graphite likely leads to comparatively greater strength loss at high porosity due to likely greater pore connectivity. The comparison between the high temperature data sets is the most useful, given this, and the fact that SOFCs operate at this temperature. The poor fit of fixed η models suggests that a material-specific η value may be an oversimplification of the porosity-stress relationship in ceramics.

Samples tested at higher temperatures displayed a slightly higher flexural strength. Generally, it is expected that increasing temperature lowers strength of dense ceramics once plastic deformation processes become activated at high temperatures. [43] Below the temperature at which plastic deformation starts to occur, temperature has a minimal effect on flexural strength of dense ceramics. For dense GDC it has been demonstrated that the strength decreases by 19% between room temperature and 800 °C. [12] Porosity changes this behavior, by essentially creating a composite material, keeping the rate of change constant or increasing with temperature. [44] For porous GDC, thermal expansion places a compressive stress on any surface flaws that are sites for crack initiation and propagation. Additionally, the porosity helps reduce bulk stresses caused by thermal expansion. These two effects increase the material's fracture strength more than any decrease from plastic deformation at 625 °C.

Cross-sectional SEM of the fracture surfaces of the porous GDC samples, both

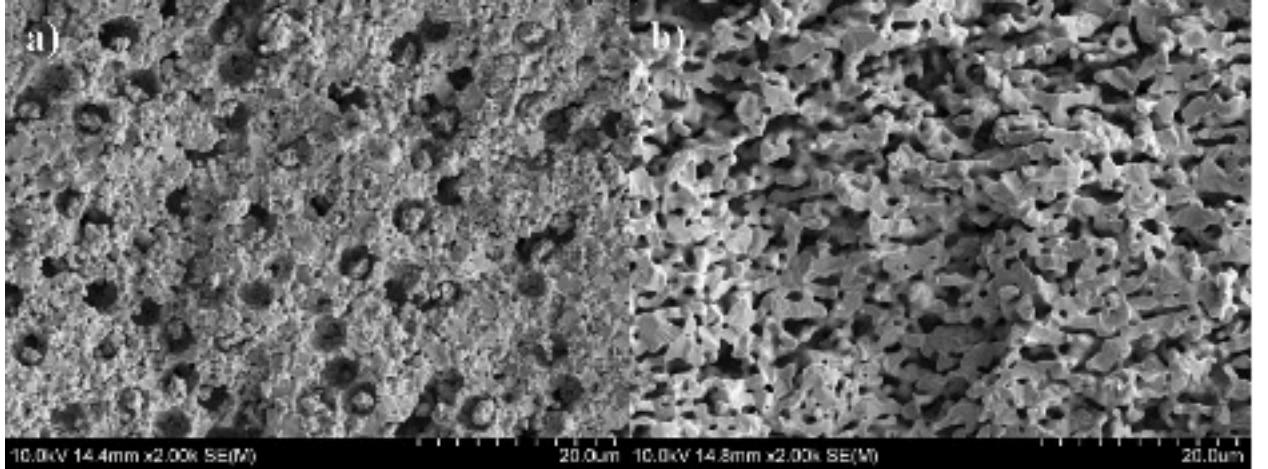


Figure 3.4: SEM micrographs of porous GDC bars made using: a) PMMA pore former; b) graphite flake pore former

PMMA and graphite, is shown in Figure 3.4. Figure 3.4a shows individual spherical pores left by the PMMA while Figure 3.4b has an inter-connected network of long pores left by the graphite flakes.

The differences in quality of fit between Figure 3.3a and Figure 3.3b shows that the geometric factor is microstructurally dependent. Samples with porosity formed using PMMA spheres showed significantly greater strength as compared to samples with graphite-formed porosity. This can be explained by the effect of pore geometry on crack initiation and propagation in the ceramic. If a crack enters a pore, the pore can now be considered the new crack tip. The energy required to advance the crack is highly dependent on the geometry of the tip. For a spherical pore, this geometric factor is maximized and results in higher resilience to fracture. This is summarized by Equation 3.3 where σ_o is the stress at the crack tip, c is the length of the crack

tip and ρ is the radius of curvature of the crack tip. [45]

$$\sigma_f = \frac{\sigma_o}{2} \sqrt{\frac{\rho}{c}} \quad (3.3)$$

Based on the mechanical behavior of these samples, porous ceramics should be designed and constructed such that the pore geometry is as low aspect ratio as possible to maximize strength.

3.3.2 Flexural Stress Orientation

Figure 3.5 shows the measure flexural strengths of a number of SOFC coupon samples. Anode support coupons were tested along with half-cells consisting of anode supports and electrolyte layers at temperatures ranging from 25 °C to 650 °C. The highest temperature test was repeated with coupons under reducing conditions (3% H₂, balance Ar).

All unreduced sample types showed increased strength at elevated temperatures with little difference between types at a given temperature. The high-temperature reduced coupons displayed large differences in strength depending on the orientation of the sample. Tests in which the dense electrolyte layer was placed in compression resulted in the highest strength values, while the samples were weakest when the electrolyte was placed in tension. In reduced samples, the anode support layer becomes a ceramic-metal composite and is therefore somewhat elastic while the electrolyte remains a brittle ceramic. The electrolyte-in-compression condition maximizes the mechanical performance of the coupon by placing the layers in their preferred stress state.

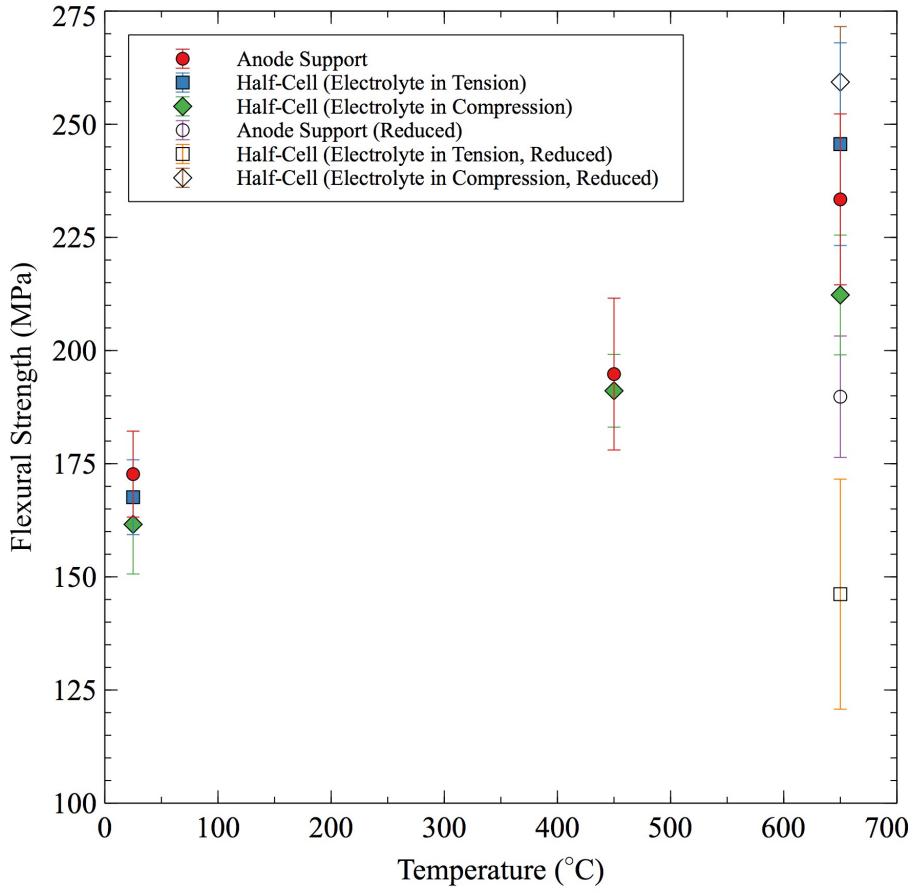


Figure 3.5: Temperature dependent strength of Ni-GDC anode supports and half-cells in both air (black data points), and reducing atmosphere (3% H₂, balance Ar, red data points), tested in both "electrolyte-up" and "electrolyte-down" orientations resulting in the electrolyte layer experiencing tension and compression, respectively

Figure 3.6 shows the box plots for the unreduced SOFC coupon samples. A Student's t-test was used to statically determine if the means of samples tested at different conditions were equal based on 95% confidence. There is no discernible difference in the strength between the three sample types at each temperature. At elevated temperature there was a significant difference in the modulus of ASL only samples and samples with electrolyte in tension with a p-value of 0.0091. This difference was not present at room temperature. As the materials reach elevated temperature, small differences in elasticity become magnified due to different thermal effects on dense and porous layers.

Additionally, SEM analysis of the fractured half-cells showed very good adhesion between layers (Figure 3.7). Delamination is a common failure mode in layered ceramics and one that would be particularly damaging to SOFCs due to resulting ionic conductivity loss between layers. [46] In the half-cell coupons, it was clear that the fracture plane contained mixed transgranular and intergranular fracture. Some grains were sheared through while others remained whole. The striations visible in Figure 3.7 are characteristic of fracture proceeding through a grain, while other grains remained whole.

3.3.3 Reduction and Strength

Mass loss of SOFC half-cell coupons exposed to reducing atmosphere at various elevated temperatures is shown in Figure 3.8. Mass loss is attributed to the reduction of NiO, used as a precursor in fabrication, to Ni metal, which serves as the catalyst

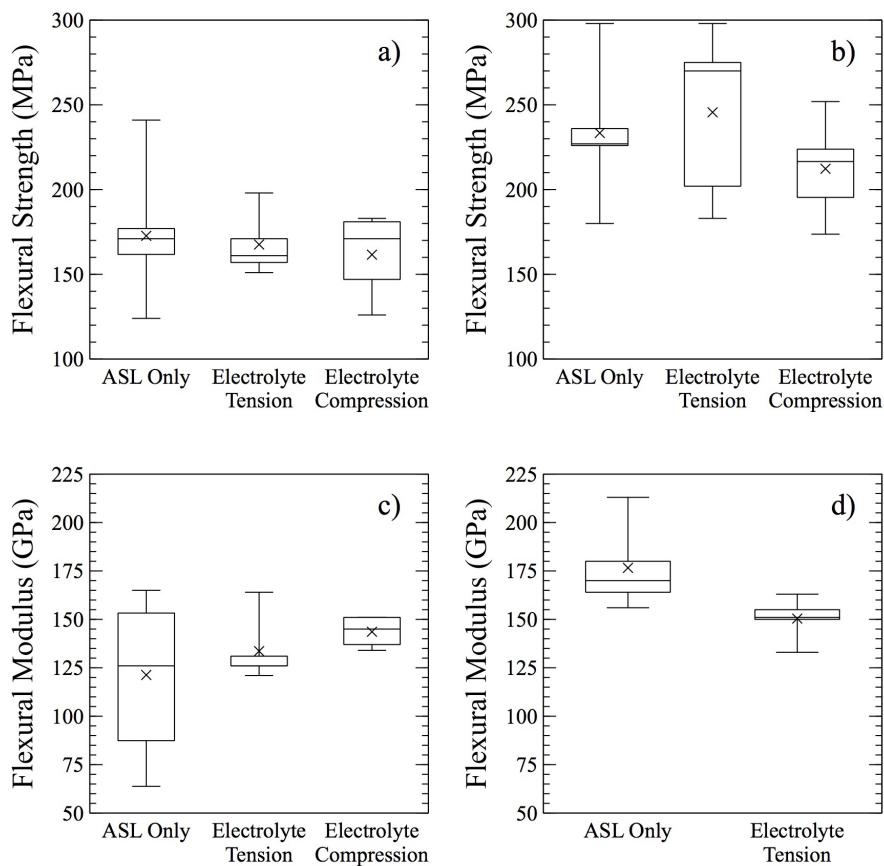


Figure 3.6: Flexural test measurements of coupons sample sets: a) Strength at 25 °C
b) Strength at 650 °C c) Modulus at 25 °C d) Modulus at 650 °C

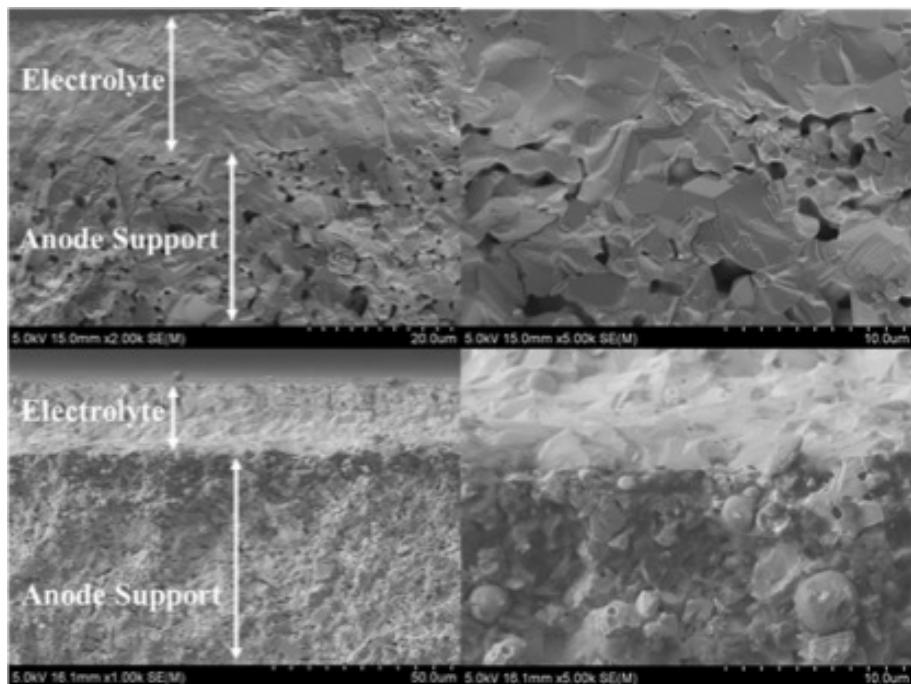


Figure 3.7: SEM micrographs of unreduced and reduced half-cell fracture surface: tested in air at 25 °C (top) and tested in reducing atmosphere at 650 °C (bottom), showing good adhesion between anode and electrolyte

Table 3.2: Summary of fit parameters for reduction of NiO-GDC/GDC half-cell coupons under 3% H₂, 3% H₂O, 94% N₂ at different temperatures.

Temperature (°C)	Exponential Rate (h ⁻¹)	Asymptote (Mass %)
550	0.0463	89.78
575	0.135	89.09
600	0.182	88.36
650	0.512	87.75
750	0.821	87.87

for fuel oxidation and electronic conductor, and the reduction of ceria to CeO_{2-δ}. Ni-GDC/GDC half cells showed the expected trend of increasing reduction rate at higher temperatures. Reduction curves were fit to an exponential decay and the summary of parameters is shown in Table 3.2. At 650 °C and 700 °C the reduction occurs very quickly, reaching steady state values after 18 hours. 550 °C showed a much slower mass loss than even 575 °C. At temperatures lower than 550 °C the kinetics are slow enough to tolerate a brief exposure to oxygen without re-oxidizing the sample. Of note in the reduction is that each temperature appears to approach a different asymptote, showing that the amount of NiO and GDC reduced at steady state is dependent on the temperature of the cell. This will affect the mechanical properties of the cells as it changes both the porosity and amount of nickel metal in the samples.

Ni-GDC/GDC fuel cells are sensitive to re-oxidation once reduced. Re-oxidation causes fracture of cells due to the large volume difference between NiO and Ni. [32]

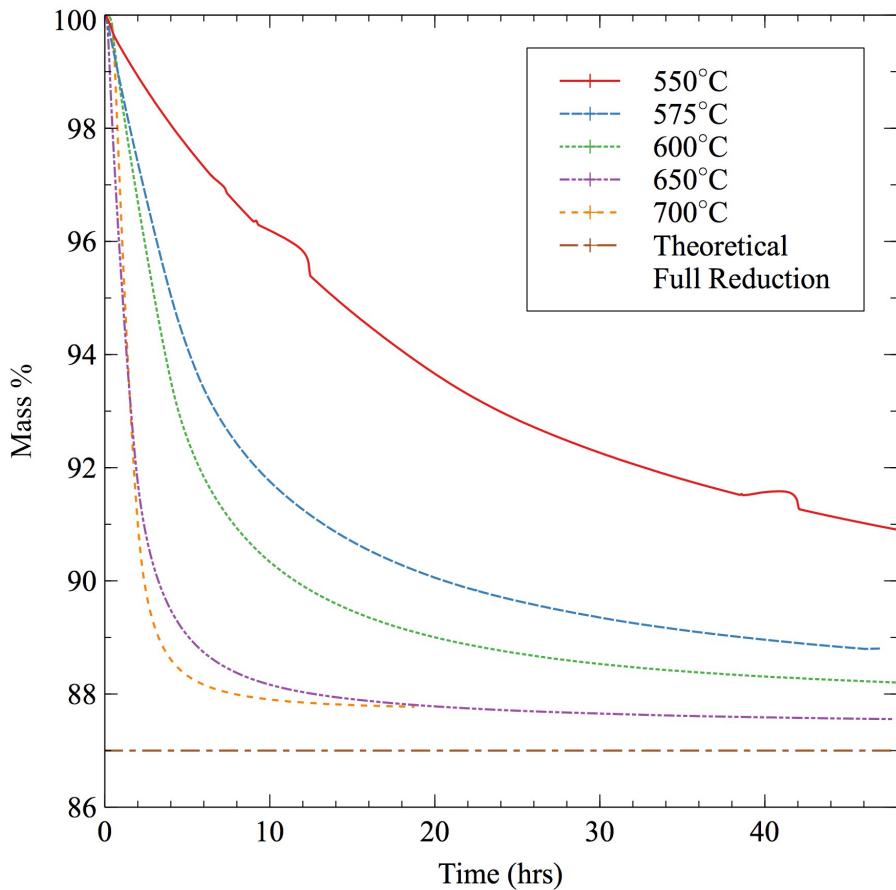


Figure 3.8: Thermogravimetric analysis curves for Ni-GDC/GDC half-cells showing mass loss over time at temperatures ranging from 550 °C to 750 °C in 3% H₂ 3% H₂O balance N₂, 50sccm flow.

Based on the results from the TGA, the reaction rates below 300 °C are sufficiently slow to allow for the exposure of a reduced cell to oxygen without detrimental results. [47] To confirm this a sample was measured by TGA to ensure no mass gain during oxygen exposure and the strength of samples were tested to ensure there was no discernible difference between reduction methods.

For TGA analysis, a piece of a half cell was heated to 650 °C with a 10 °C/min ramp rate and reduced. It was then cooled while still under reducing atmospheres. Once below 100 °C, it was exposed to simulated air (21% O₂) for 18 hours, placed back into reducing atmosphere, and heated back up to 650 °C. Figure 3.9 shows the change in mass overlaid onto the temperature and oxygen partial pressure experienced by the sample. Following this treatment, the cell showed no mass gain during the oxygen exposure and continued to reduce at the same rate as before once it was returned to the initial conditions. This shows that cells which are cooled appropriately do not re-oxidize and could be handled in between a batch reduction of cells, and their assembly into a stack configuration.

Box plots of flexural strength and modulus of the in-situ reduced and batch reduced coupons are shown in Figure 3.10. Mechanical strength of half-cell coupons which had been reduced in-situ with an 18 hour reduction time showed no difference in strength when compared with coupons which had been previously batch reduced, cooled, and reheated under reducing environments. Both of these sample types showed a dramatic decrease in strength and Young's modulus compared to the un-reduced samples, but no statistically significant difference between treatments. The decrease in strength and modulus is due to the increase in porosity and conversion of

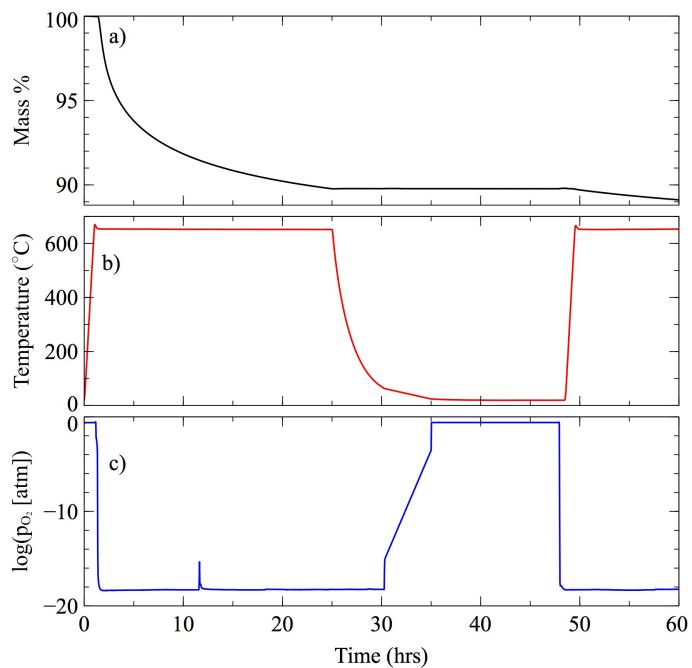


Figure 3.9: Thermogravimetric analysis of Ni-GDC/GDC half-cell showing no mass gain after reduction and exposure to room temperature and simulated air: a) Mass loss of interrupted reduction with exposure to ambient condition; b) Temperature of sample during cycle c) Oxygen partial pressure measured at the sample during cycle

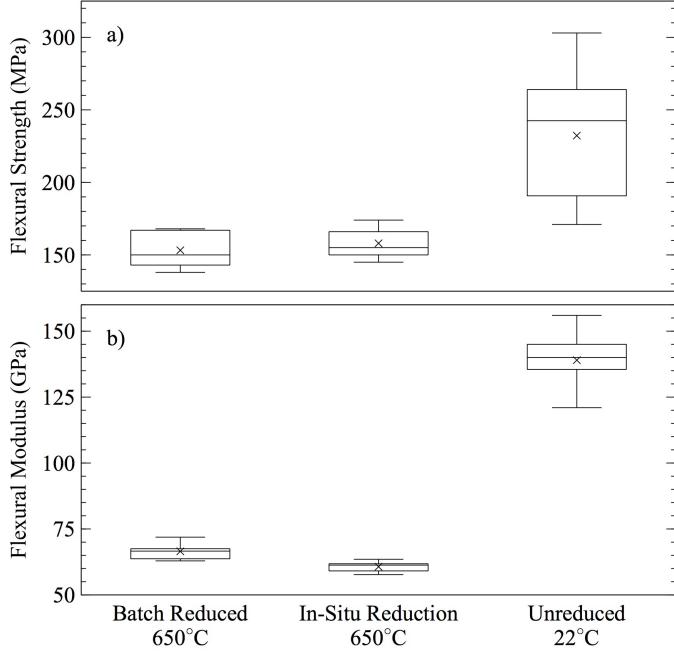


Figure 3.10: Flexural properties, a) strength and b) modulus, of Ni-GDC/GDC half-cell coupons after reduction via two different methods, compared to unreduced cells. Strength and modulus show decrease upon reduction but no significant difference between methods.

NiO to metallic nickel in the cells. The decrease in variation between measurements in reduced cells is likely due to the increased number of large voids that form during NiO reduction.

The statistical similarity of the properties of the samples reduced via each method indicates that planar, Ni-GDC/GDC based SOFC ASL and half-cells are able to be safely reduced, cooled, and handled in ambient conditions without leading to damaging re-oxidation of the nickel anode material. This resilience could enable some degree of large-batch reduction of cell anodes prior to SOFC stack assembly, leading to more rapid startup and a greater degree of sealing control.

3.4 Conclusions

A temperature and atmosphere controlled three-point bend fixture was designed and built for use in a universal testing machine. SOFC coupons and component materials were evaluated for flexural strength at room temperature and IT-SOFC operating temperatures. In addition, the effects of porosity percent and pore geometry on flexural strength in GDC were investigated. Furthermore, the impact of temperature on the reduction rate of NiO in NiO-GDC SOFC anodes was examined along with the resilience to re-oxidation at ambient conditions of this SOFC component.

Pore geometry had a significant impact on the flexural strength of GDC10, with spherical pores showing the greatest resistance to fracture. This supports the concept of pores acting as the new crack tip once a crack has advanced to the pore. Additionally, samples tested at 650 °C were stronger than those at room temperature. This is likely due to localized compressive stresses from thermal expansion of the material. This hypothesis is further supported by the results of testing NiO-GDC anode support coupons and half-cells. Coupons tested at 25 °C, 450 °C, and 650 °C displayed a linear strength dependence with temperature. There was no statistical difference in strength between anode support layers and half-cells composed of anode support and electrolyte at a given temperature in air. Half-cells in which NiO was reduced to Ni by exposure to H₂ at 650 °C displayed significant differences in strength when the electrolyte layer was subjected to compressive stress as opposed to tensile stress. Placing the ceramic electrolyte in compression and the metal-ceramic composite anode in tension resulted in the highest strength.

The reduction temperature of NiO-GDC/GDC half-cells was shown to have an effect on the rate of NiO reduction and amount of NiO reduced. At lower temperatures, the oxidation rate of Ni-GDC is slow enough that the anode can be exposed to air for significant periods below 100 °C. Any re-oxidation, combined with the cooling and re-heating of a cell back to 650 °C, showed no effect on the mechanical properties when compared to cells which had been reduced in-situ at 650 °C. These results indicate that it is possible to reduce and cool cell components to an extent without any additional effects to mechanical properties, allowing for more flexibility during cell manufacturing, stack assembly, and with quality control screenings.

This work leads to three important conclusions for the mechanical properties of GDC-based SOFCs using Ni anodes. Porous GDC used in anode supported SOFCs should be fabricated such that the pore geometry is spherical as this maximizes energy required to advance a crack through the ceramic. Care should be taken in stack construction to ensure any out-of-plane cells are placed to compress the electrolyte and place the reduced anode in tension so as to lower the chance of fracture. Finally, it is possible to reduce the anodes of Ni-GDC SOFCs and then handle them at ambient conditions for quality control and stack assembly. This will remove a degree of variability from the manufacture of cells and stacks.

Chapter 4: Defect chemistry and oxygen non-stoichiometry of double perovskite $\text{SrFe}_{0.2}\text{Co}_{0.4}\text{Mo}_{0.4}\text{O}_{3-\delta}$

4.1 Introduction

Solid-state electrochemical devices that perform energy conversion and storage rely on a material's abilities to transport charged carriers through the material. Devices such as solid-oxide fuel cells (SOFCs), oxygen separation membranes, and gas sensors can utilize materials which conduct both oxygen and electronic conductors, known as mixed ionic electronic conductors (MIEC), in the electrodes where both conductions need to occur simultaneously. [48] SOFCs, in particular, are limited in their application due to high operating temperatures, performance degradation due to fuel contamination, and inability to tolerate thermal and redox cycling. To improve the performance and reliability of SOFCs the operating temperature needs to be lowered from the intermediate temperature (IT) range ($650\text{ }^\circ\text{C}$ to $800\text{ }^\circ\text{C}$) to the low temperature range ($<650\text{ }^\circ\text{C}$). [7] Additionally, the use of an all-ceramic anode, as opposed to the traditional nickel metal anode, would improve long term performance, resistance to poisoning or coking, and better match the thermal expansion of the rest of the cell. [49]

Perovskite structures have yielded number of MIEC with potential uses as electrode materials. [50–52] $\text{Sr}_2\text{MgMoO}_6$ (SMM) and its related family of materials (Sr_2MMoO_6 , where M is a transition metal dopant) yield good conductivities and catalytic actives. [53] The mixed valence state of Mo(VI)/Mo(V) provides high electronic conduction while supporting oxygen vacancy formation. [54] If a dopant is used which has an overlapping redox couple band, such as Fe, electronic conduction can be further improved. Mo(VI) and Mo(V) are stable in both octahedral and tetrahedral coordination, further adding stability to oxygen vacancy formation. [55]

A new material, $\text{SrFe}_{0.2}\text{Co}_{0.4}\text{Mo}_{0.4}\text{O}_{3-\delta}$ (SFCM), is of particular interest because of its high conductivity (previously measured to be 35 S/cm at 600 °C) and stability. [56] SFCM takes advantage of the perovskite structure and a choice of cations similar to SMM, but the combination of both cobalt and iron further increase the performance of the material. It has been shown that a SOFC using SFCM as an anode support material is redox stable up to 30 cycles at 600 °C and that it infiltration with nanoparticles of nickel-gadolinium doped ceria provided long term catalytic activity without detriment to performance. [57, 58]

This work expands upon the fundamental knowledge of SFCM and to understand the defect chemistry and electronic structure which leads to its high conductivity. The non-stoichiometry of SFCM was measured under oxidizing and reducing environments, similar to what would be found in a LT-SOFCs, using thermogravimetry. X-ray diffraction supports the phase stability of SFCM though these conditions and the change in lattice parameters was determined after oxidation and reduction. Temperature programmed desorption spectroscopy was used to characterize at what

temperatures the oxygen loss is observed. A defect equilibrium model and diagram is proposed from non-stoichiometry and conductivity data and results are compared to SMM and other perovskite materials.

4.2 Experimental

4.2.1 Sample Preparation

SFCM was created from stoichiometric amounts of strontium carbonate (SrCO_3 , Sigma-Aldrich), iron oxide (Fe_2O_3 , Sigma-Aldrich), cobalt oxide (Co_2O_3 , Inframet Advanced Materials), and molybdenum oxide (MoO_3 , Alfa-Aesar) using conventional solid-state methods. The constituents were ball milled for 24 hours in ethanol and dried using a 100 °C oven. Afterwards the powder was calcined at 1100 °C for four hours.

Dense SFCM bars were used to maximize the total mass and mass changes during thermogravimetric testing. Samples were made by combining SFCM powder with 0.6 wt% polyethylene glycol 600, 1.8 wt% ethylene glycol, and 0.6 wt% glycerol in isopropyl alcohol and ball milling overnight. After drying at 100 °C, the powder was ground by mortar and pestle, then pressed uniaxially into rectangular bars at 30 MPa, then isostatically pressed at 30 MPa. Bars were sintered by heating to 400 °C for one hour and then 1340 °C for four hours, using a $3 \text{ }^\circ\text{C min}^{-1}$ heating and cooling rate. This produced bars with 97% theoretical density by Archimedes' technique.

4.2.2 X-ray Diffraction

X-ray diffraction (XRD) was used confirm phase purity of the SFCM after synthesis and during the testing process. A Bruker D8 Advance with LynxEye was used with a Cu K α source. A step size of 0.02° was used with a dwell of 0.8 s was used. Rietveld refinement was performed on samples as synthesized, after oxidation in pure O₂ and after reduction in pure H₂ at 600 °C for both. GSAS-II was used to perform the refinement calculations and VESTA was used to visualize the unit cell. [59, 60]

4.2.3 Conductivity

Total conductivity was measured using the four-wire technique and a Stanford SR 830 lock-in amplifier. A bar shape sample was used with dimensions of 6.46 mm × 3.3 mm × 1.3 mm. Gold paste was used as a current collector, and the current range was between 0.005 to 0.05 A. A yttria-stabilized zirconia (YSZ) oxygen sensor operating at 800 °C was used to monitor the changes in oxygen partial pressures. Intermediate p_{O₂} ranges were not tested due to the fact that SFCM reacts with the amounts of CO and CO₂ required to obtain those p_{O₂}.

4.2.4 Thermogravimetric Analysis (TGA)

Changes in mass of SFCM were measured by a Cahn D200 microbalance with the sample suspended down a quartz tube into a furnace. The furnace used to heat the sample and quartz tube was controlled by a PID controller with a K-type

thermocouple placed immediately below the sample inside the quartz tube. Gas flow was controlled at consistent 50 sccm by mass flow controllers, which mixed dry nitrogen, oxygen, hydrogen, and humidified nitrogen to obtain the p_{O_2} desired. Measurements of the p_{O_2} were taken by a calibrated YSZ oxygen sensor at 800 °C located before the sample. Again, intermediate p_{O_2} ranges were not able to be tested due to SFCM's incompatibility with the species required to create that environment.

To prepare the sample, it was pre-weighed, wrapped in platinum wire and suspended from the balance, placed in the furnace with simulated air (21% O₂, 79% N₂) flowing. Once the mass had stabilized, the furnace was heated to 800 °C to allow for any organic contamination to burn off. After the mass stabilized at this elevated temperature the sample was introduced to various environments. The mass of the sample would be noted only after steady state had been reached for a condition. After testing a sample, a bar of alumina was cut to the same dimensions as the sample and the process was repeated to obtain a blank which could be subtracted from the measurements to remove buoyancy effects.

Oxygen non-stoichiometry was calculated using Equation 4.1, where $\Delta\delta$ is the change in oxygen stoichiometry, MW_{SFCM} is the molecular weight of SFCM (208.74 g mol⁻¹), MW_O is the molecular weight of oxygen (16.0 g mol⁻¹), w_{sample} is the weight of the sample, and Δw is the weight change as recorded by the TGA. The oxygen vacancy concentration ($[V_O^{••}]$) is calculated using Equation 4.2, where ρ is the density of SFCM. To calculate the oxygen vacancy concentration, the non-stoichiometry of SFCM at a point needs to be established. For this work, based on the plateau present in the data at oxidizing conditions, it is assumed that in a pure

oxygen environment ($\log(p_{O_2}) = 0$) all oxygen vacancies are filled with no oxygen interstitial or surface species, thus $\delta = 0$.

$$\Delta\delta = \frac{MW_{SFCM}}{MW_O w_{sample}} \Delta w \quad (4.1)$$

$$[V_O^{\bullet\bullet}] = \frac{\delta\rho}{MW_{SFCM}} \quad (4.2)$$

4.2.5 Temperature Programed Desorption

The effluent from the TGA was used as the inlet to a mass spectrometer (MS) to perform temperature programmed desorption. The sample was prepared as before and heat treated to remove any carbon contaminants but was allowed to cool under simulated air. It was then heated to 800 °C at 5 °C min⁻¹ under a 50 sccm flow of nitrogen as the MS measured the 32 m/z signal which corresponded to O₂ desorption. Additional m/z signals were monitored to observed for other species.

4.3 Results and Discussion

The XRD patterns obtained after reduction and oxidation in addition to the fresh, as synthesized powder and the pattern obtained from Rietveld refinement are presented in Figure 4.1a. An ordered tetragonal, perovskite structure was used as a starting point for Rietveld refinement based on the structures of Sr₂CoMoO₆, Sr₂NiMoO₆ and Sr₂Fe_{0.75}Co_{0.25}MoO₆. [53, 61] Results from the Rietveld refinement calculations are given in Table 4.1. The ordered double perovskite unit cell from the refinement is presented in Figure 4.1b and was used to create the theoretical XRD pattern for visual comparison.

Table 4.1: Refinement results of SFCM before and after exposure to reducing and oxidizing environments

Condition	Oxidized	Fresh	Reduced
Space Group	I 4 \overline{m}	I 4 \overline{m}	I 4 \overline{m}
a (Å)	5.6327	5.5529	5.5583
c (Å)	7.89728	7.9080	7.9063
Volume (Å ³)	250.559	243.842	244.262
Sr-O1 (Å)	2.78256	2.78561	2.78633
Sr-O2 (Å)	2.69370	2.70315	2.69425
M1-O1 (Å)	1.9927	1.99488	1.99094
M1-O2 (Å)	1.90246	1.91309	1.77694
M2-O1 (Å)	1.95032	1.95245	1.94859
M2-O2 (Å)	2.04619	2.05763	2.17621
Phase Purity (% SFCM)	Evans	Evans	Evans
R	Evans	Evans	Evans

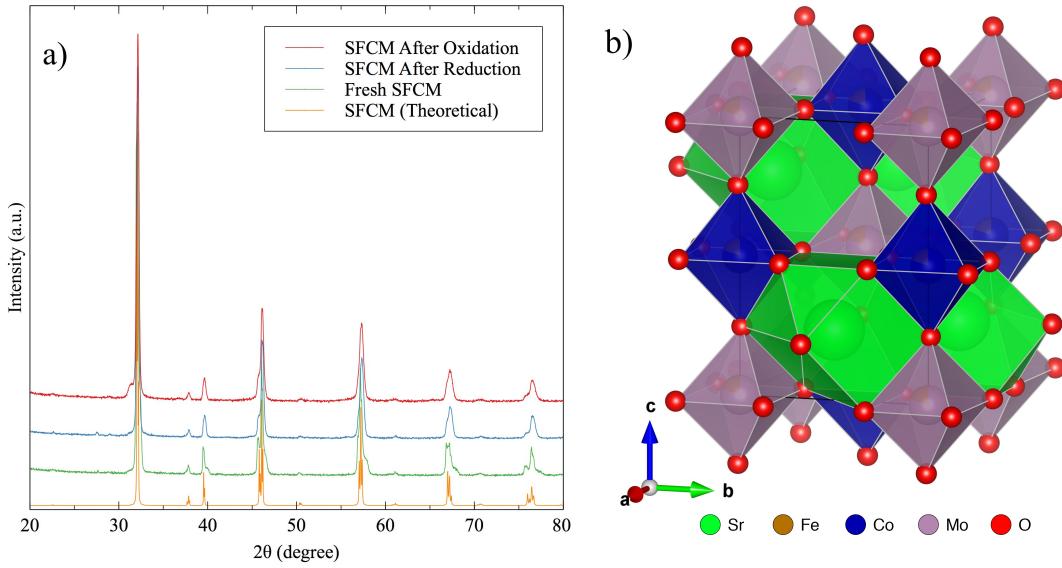


Figure 4.1: a) Powder XRD patterns of SFCM samples taken after synthesis, reduction, and oxidation compared to pure phase SFCM diffraction pattern. b) Crystal structure of ordered double perovskite SFCM.

(Note: The following 2 paragraphs will be updated once XRD refinement is finished.) While SFCM is considered to be stable under various redox conditions, a small amount of impurity phases do form, especially under oxidizing conditions. SrMoO_4 is a common impurity in SMM materials and can be seen in small concentrations in the oxidized sample. These secondary phases are minor and disappear under reducing conditions. Overall phase purity remains at greater than XX% as synthesized, XX% under oxidizing conditions and XX% after reduction. Ruddlesden-Popper phase was found to form, causing a broadening of the peak shoulders.

Small shifts in peak locations and shapes can be seen to occur in the XRD pattern attributed to SFCM after different treatments. These are attributed to the changes in oxidation state, defect concentrations, and thus lattice parameter of the

sample after reduction or oxidation. The changes to the lattice were calculated from Rietveld refinements of the XRD data and summarized in Table 4.1. Reduction of SFCM from an as synthesized state causes a small increase in a and the volume of the unit cell and a small decrease in c . Oxidizing the SFCM results in a larger increase a and a small decrease in c resulting in an increase in cell volume. Perovskite structures have been shown to have anisotropic chemical expansion, with a increasing upon reduction while c decreases for SFM. [62] Due to the presence of the Ruddlesden-Popper phase, the attribution of causes to the changes in lattice parameters is difficult as the rock-salt portion of the phase can behave differently than the rest of the perovskite phase. [27] Overall the increases in unit cell parameters for reduction can be attributed to the increase in ionic radii of B-site metals upon reduction and the generation of oxygen vacancies causing lengthening of metal oxygen bonds, while oxidation also causes an increase in cell parameters due to the Ruddlesden-Popper phase present.

SFCM has a conductivity dependence typical of MIEC conductors, as shown in Figure 4.2. At high p_{O_2} ranges ($10^{-1.5}$ atm to 1 atm) shows p-type conductivity, increasing conductivity with p_{O_2} . Down to 10^{-1} atm the change in conductivity is linear with a slope of 0.089 (log-log scale). Below 10^{-1} atm the slope changes away from the previous trend. At low p_{O_2} ranges (10^{-24} atm to 10^{-19} atm) the conductivity behaves linearly with n-type conductivity, increasing at lower p_{O_2} with a slope of -0.11 (log-log scale). Due to the inability to measure the intermediate p_{O_2} we were unable to determine in this work at what point the p_{O_2} dependence changes from n-type to p-type and if there is an ionic regime in between.

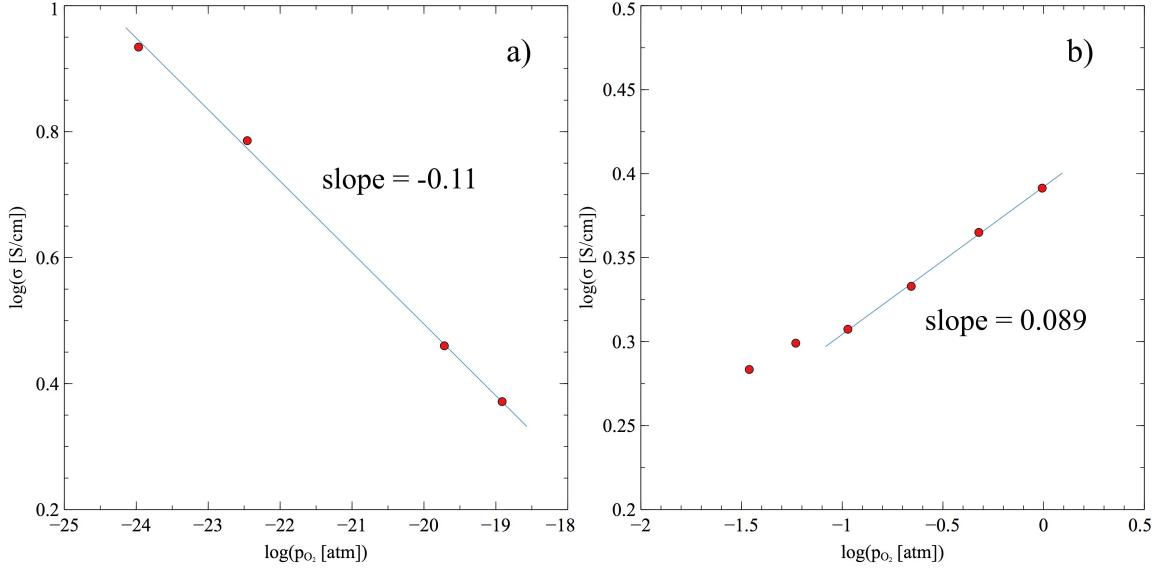


Figure 4.2: Total conductivity as the environment changes oxygen content at 600 °C.

Based on the slopes in the high p_{O_2} region, at least two defect regimes exist in that area changing near 10^{-1} atm. Both high and low p_{O_2} regions have slopes much lower than $+1/4$ or $-1/4$ respectively, which indicates that the relationship between electronic charge carries is not independent of the other defect species in the material. In fact, the lower than $1/4$ slope suggest that the electronic charge carries are taken up by the other species, decreasing the expected number based on p_{O_2} change. The different slopes between high and low p_{O_2} are the result of different defect species interacting with the electronic carriers at different points in the reduction.

To confirm that oxygen desorption readily occurs in SFCM, what temperatures it occurs at, and by what mechanisms, TPD was performed in conjunction with TGA. Figure 4.3 presents the data from the TGA on top with the mass and rate of mass change, while the 16 m/z signal from oxygen in the mass spectrometer is on bottom. The cyclic noise present in both mass and MS signals is due to an ill tuned

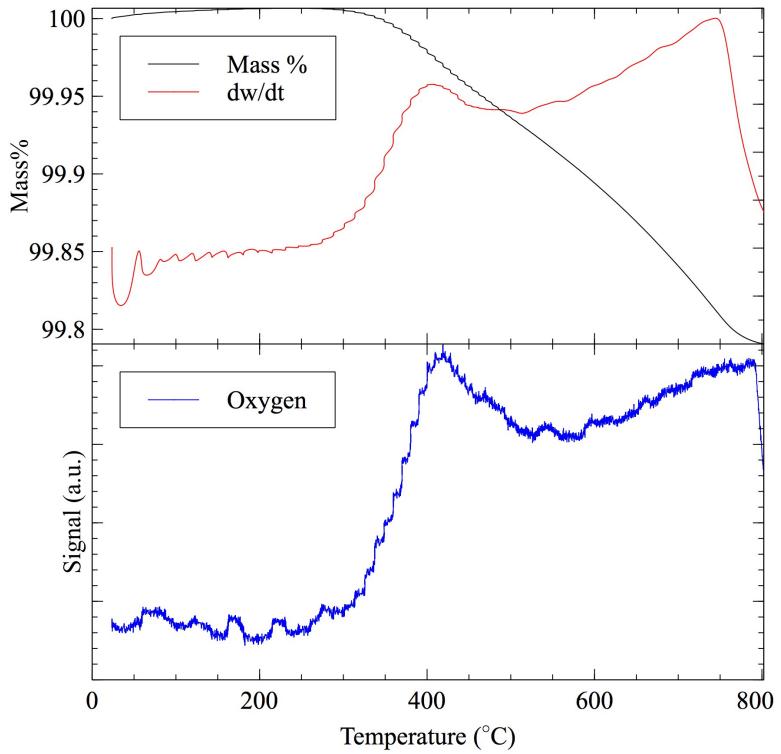


Figure 4.3: Temperature programmed desorption of oxygen in SFCM with mass loss from TGA (top) and oxygen desorption from MS (bottom) as it is heated to 800 °C in N₂.

PID controller on the TGA furnace. The rate of mass loss matches the oxygen signal from the MS, confirming that oxygen is generated from SFCM when heated under mild reducing conditions and is the cause for mass loss in the sample. SFCM shows two maxima for the rate of oxygen loss during heating. The first, α , occurs at 405 °C with the second peak, β , occurring near 800 °C. The MS monitored for other species, such as carbon and water, but no significant amounts were observed.

Perovskite materials have oxygen desorption classified based on the temperature which it occurs. Low temperature desorption (referred to as α), occurs due to the

reduction of metals and desorption of oxygen near the surface. High temperature desorption (referred to as β), takes place when oxygen is able to diffuse through the bulk and be released. [63] SFCM shows both α and β desorption, indicating that both the surface and lattice can generate oxygen vacancies due to the reduction of the different B-site cations and that those vacancies are mobile to move from the bulk to the surface. SMM shows only β desorption above 800 °C and while $\text{Sr}_2\text{Fe}_{1.5}\text{Mo}_{0.5}\text{O}_6$ (SFM) has α desorption from 400 °C to 800 °C and $\text{Sr}_2\text{CoMoO}_6$ (SCM) desorbs starting below 400 °C. [64, 65] In the case of SFM and SCM, the use of the multivalent iron or cobalt allows for reduction at a lower temperature than SMM. For SFCM, the same effect is seen through the combined use of cobalt and iron. This demonstrates SFCM's ability to begin to create oxygen vacancies at 400 °C and exchange oxygen with the bulk lattice starting as low as 450 °C and peaking near 800 °C.

Oxygen non-stoichiometry and oxygen vacancy concentrations are shown in Figure 4.4 at 600 °C for high and low p_{O_2} regions. At high p_{O_2} , SFCM has two linear regions, changing between them near $10^{-0.75}$ atm. The transition between regions in oxygen stoichiometry occurs at a similar p_{O_2} to where the conductivity changes in Figure 4.2. In the high p_{O_2} region, a linear trend occurs down until 10^{-21} atm where the non-stoichiometry rate increases.

SFCM shows similar trends in non-stoichiometry to SMM and SFM, but with the added complexity expected from the additional B-site species. SMM approaches a plateau in oxygen content as it reached 1 atm of oxygen the same as SFCM, but possesses a constant slope of -1/6 when plotted on a log-log scale. [66] In comparison,

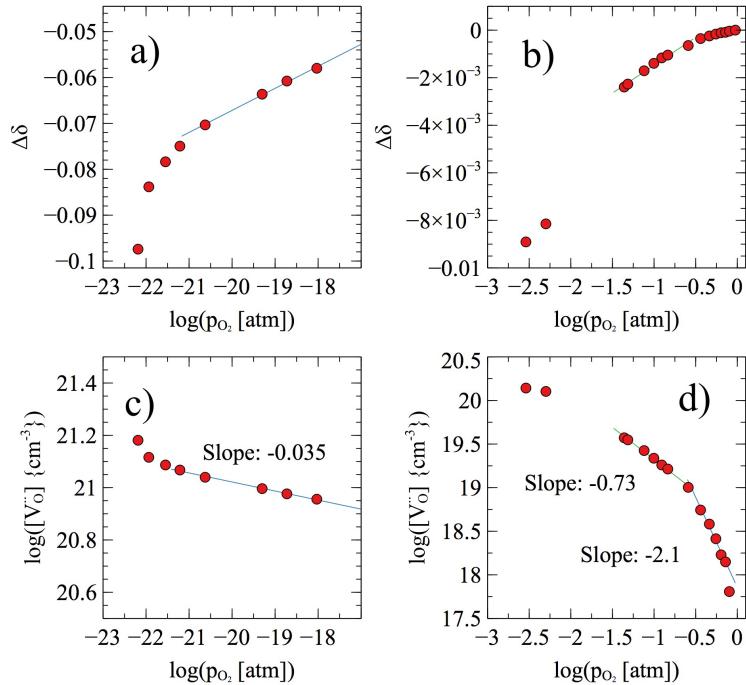


Figure 4.4: Non-stoichiometry (top) and corresponding oxygen vacancy concentration (bottom) of SFCM under oxidizing conditions (right) and reducing conditions (left) at 600 °C.

SFCM has multiple slopes associated with the degree of vacancy formation, as shown in Figures 4.4c and 4.4d. These different slopes can be attributed to the reduction of the three different B-site cations at different p_{O_2} . As an oxygen vacancy forms, the electrons required to maintain charge balance can be accommodated by the reduction of Mo, Fe, or Co, each with an independent equilibrium constant, whereas SMM only has Mo reduction to accommodate electrons from oxygen vacancy generation. The high slopes of Figure 4.4d show how SFCM can generate more oxygen vacancies at lower p_{O_2} because of the Fe and Co cations. SFM and SMM show similar amounts of non-stoichiometry at the same p_{O_2} but at 1000 °C. [67] SFCM shows almost twice the non-stoichiometry at a much lower temperature of 600 °C. SFCM's ability to create vacancies at higher p_{O_2} results in a larger accumulated vacancy concentration at low p_{O_2} .

TGA non-stoichiometry measurements were also performed at 400 °C and 500 °C which are temperatures in the LT-SOFC range. Figure 4.5 shows the non-stoichiometry measurements for the sample tested at three temperatures in the low p_{O_2} (a) and high p_{O_2} (b) regions.

As expected lowering the temperature reduces the non-stoichiometry at a given p_{O_2} and decreases the p_{O_2} at which transitions between regimes occur. At 400 °C oxygen vacancy formation decreases considerably compared to 500 °C and 600 °C. This aligns with the results of the TPD (Figure 4.3) where SFCM does not start desorbing oxygen until 350 °C to 400 °C.

To best understand what is occurring in SFCM a defect equilibrium diagram and model need to be created to relate the changes in conductivity and non-stoichiometry

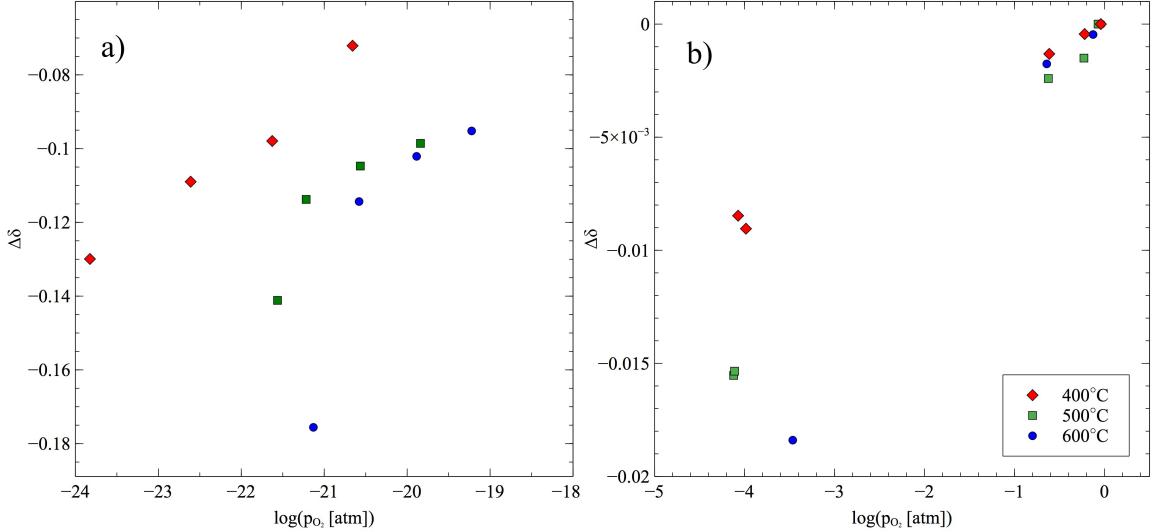
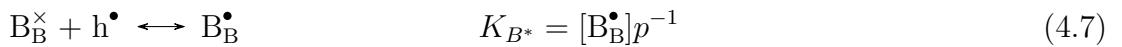
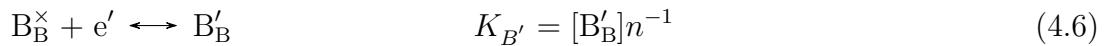
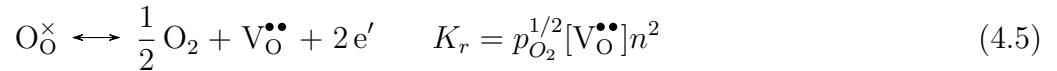
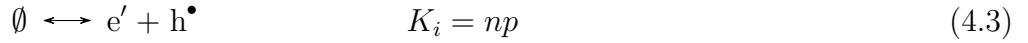


Figure 4.5: Non-stoichiometry of SFCM as p_{O_2} changes at 400 °C, 500 °C, and 600 °C.

to the concentration of the various defects present in the material. Defect reactions with their corresponding equilibrium equations are given in Equations 4.3–4.7, which use Kröger–Vink notation. Equations 4.6 and 4.7 represents the reduction or oxidation of any B-site cation (Co, Fe, or Mo).



Using a Brouwer approach for the different regions of defect dominance established by conductivity and TGA measurements, Equations 4.3–4.7 can be rearranged and simplified to give approximations of the defect concentrations within various p_{O_2} ranges. Table 4.2 summarize the result of using the Brouwer approach to determine

Table 4.2: Equations for Defect Equilibrium Diagram

Species	Region				
	I	IIa	IIb	IIc	III
n	$(2K_r)^{\frac{1}{3}} p_{O_2}^{-\frac{1}{6}}$	$\left(\frac{2K_r}{K_B}\right)^{\frac{1}{3}} p_{O_2}^{-\frac{1}{6}}$	-	$[B_B^\bullet]$	$\frac{K_i}{\left(\frac{K_i^6 K_B}{K_r^3} (4+2\beta)^{1+\beta}\right)^{\frac{1}{7+\beta}} p_{O_2}^{\frac{3}{14+2\beta}}}$
p	$\frac{K_i}{(2K_r)^{\frac{1}{3}}} p_{O_2}^{\frac{1}{6}}$	$K_i \left(\frac{2K_r}{K_B}\right)^{-\frac{1}{3}} p_{O_2}^{\frac{1}{6}}$	-	$K_i [B_B^\bullet]$	$\left(\frac{K_i^6 K_B}{K_r^3} (4+2\beta)^{1+\beta}\right)^{\frac{1}{7+\beta}} p_{O_2}^{\frac{3}{14+2\beta}}$
$[V_O^{**}]$	$\left(\frac{K_r}{4}\right)^{\frac{1}{3}} p_{O_2}^{-\frac{1}{6}}$	$[B'_B]$	-	$\frac{K_r}{[B'_B]^2} p_{O_2}^{-\frac{1}{2}}$	$\frac{K_r}{K_i^2} \left(\frac{K_i^6 K_B}{K_r^3} (4+2\beta)^{1+\beta}\right)^{\frac{2}{7+\beta}} p_{O_2}^{\frac{-1+\beta}{14+2\beta}}$
$[V_A'']$	$\frac{1}{\beta} \left(\frac{4K_s}{K_r}\right)^{\frac{1}{1+\beta}} p_{O_2}^{\frac{1}{2(1+\beta)}}$	$\frac{1}{\beta} \left(\frac{K_B}{[B'_B]^3}\right)^{\frac{1}{1+\beta}}$	-	$\frac{1}{\beta} \left(\frac{K_B}{K_r^3} [B_B^\bullet]^6\right)^{\frac{1}{1+\beta}} p_{O_2}^{\frac{3}{2(1+\beta)}}$	$\frac{1}{\beta} \left(\frac{K_B}{[V_O^{**}]^3}\right)^{\frac{1}{1+\beta}}$
$[V_B''']$	$\left(\frac{4K_s}{K_r}\right)^{\frac{1}{1+\beta}} p_{O_2}^{\frac{1}{2(1+\beta)}}$	$\left(\frac{K_B}{[B'_B]^3}\right)^{\frac{1}{1+\beta}}$	-	$\left(\frac{K_B}{K_r^3} [B_B^\bullet]^6\right)^{\frac{1}{1+\beta}} p_{O_2}^{\frac{3}{2(1+\beta)}}$	$\left(\frac{K_B}{[V_O^{**}]^3}\right)^{\frac{1}{1+\beta}}$

the defect concentrations at different p_{O_2} regions, starting with Region I at low p_{O_2} up to Region III at high p_{O_2} . The Region IIb is the mid- p_{O_2} for which currently there is no data on the behavior of the material. It is possible that this region consists of multiple regions, but within the scope of this work, that is unknown. (*Note: A few details of this part are still being finalized. Once finalized the values for equilibrium constants can be reported in addition and Figure 4.6 will be updated with the correct locations for data and fits.*)

Using the TGA and conductivity data with the equations given in Table 4.2 the reaction equilibrium constants can be fitted to obtain a general defect equilibrium diagram as shown in Figure 4.6. To calculate the carrier density from the electronic conductivity, a value of $0.04 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ was used based on literature values for small polaron defects in similar materials. [66] Additionally, the equilibrium constants can be plotted to fit the Arrhenius equation and obtain activation energies for the different reactions.

From Figure 4.6, it can be seen that at high p_{O_2} the predominant charge

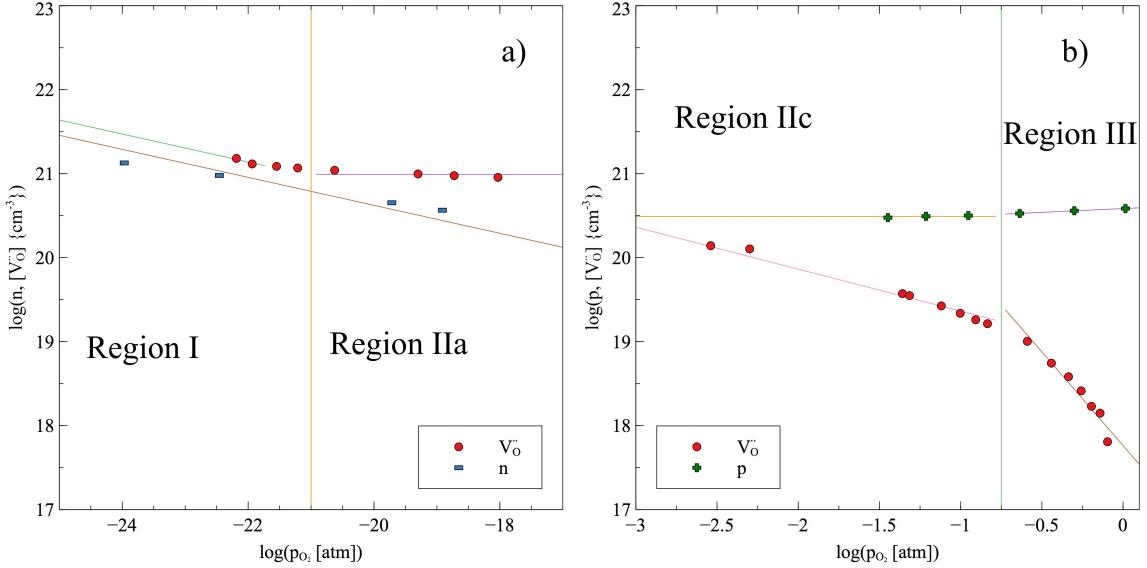


Figure 4.6: Oxygen vacancy and electronic defects in SFCM based on conductivity and TGA non-stoichiometry.

carriers are holes, until the $10^{-2.5}$ atm range, where oxygen vacancy concentration meets that of holes. At low p_{O_2} both electrons and oxygen vacancies are on the same order of magnitude though the entire region, leading to a truly mixed conduction mechanism. This large concentration of electronic and ionic carriers leads to SFCM's high performance.

4.4 Conclusions

SFCM has potential as an electrode material in a number of electrochemical device applications due to its high conductivity and redox stability. SFCM is an improvement over previous double perovskite materials because of the improved conductivity at low temperatures. This is in part because SFCM supports the formation of oxygen vacancies at both surface and lattice positions shown by overlapping α and

β oxygen desorption, starting as low at 350 °C and continuing up until above 800 °C.

Oxygen vacancies form more rapidly than other MIEC materials with decreasing p_{O_2} as combination of B-site cations enables reduction though a large range of p_{O_2} . A proposed defect diagram was given supported by thermogravimetric and conductivity measurements for the complex system. Thermogravimetry at lower temperatures demonstrated SFCM's activity until 400 °C at which the amount of oxygen vacancy formation slows dramatically.

Chapter 5: Flexural strength and flaw distributions of $\text{SrFe}_{0.2}\text{Co}_{0.4}\text{Mo}_{0.4}\text{O}_3$
based ceramic-supports for solid-oxide fuel cells at operating conditions

5.1 Introduction

New materials are regularly being developed for use in solid-oxide fuel cells (SOFCs) to lower operating temperatures and improve reliability and performance.

[7] Most of the development focuses on the catalytic activity and conductivity enhancement in the material. However, an important characteristic of these materials that needs to be studied are the mechanical properties. An SOFC must be able to be adequately compressed to create a gas tight seal between the anode and cathode compartments for it to function well. This means that the cell must withstand the induced stresses from sealing, heating, and reduction by fuels. Redox cycling presents an additional challenge, especially in nickel-based systems, because oxidation and reduction phase changes cause crack growth and failure after a few cycles.

[19, 22, 23, 68–71] A means of mitigating this problem is to use alternative, all ceramic anode system, such as $\text{La}_{1-x}\text{Sr}_x\text{Cr}_{1-y}\text{Mn}_y\text{O}_3$, $\text{Sr}_{0.94}\text{Ti}_{0.9}\text{Nb}_{0.1}\text{O}_{3-\delta}$, $\text{Ba}_{0.98}\text{La}_{0.02}\text{SnO}_3$, or $\text{Sr}_2\text{MgMoO}_6$ (SMMO). [48, 49, 72–76]

One new material of interest is the double perovskite $\text{SrFe}_{0.2}\text{Co}_{0.4}\text{Mo}_{0.4}\text{O}_3$ (SFCM). [56–58] SFCM is a mixed ionic electronic conductor (MIEC) based off SMMO and other similarly structured anodes. The double perovskite family of materials, similar to SFCM and SMMO, have potential use as SOFC components due to the ability of the stable perovskite structure to generate and conduct oxygen vacancies and the multivalent cations allowing for electronic conduction and catalytic activity. [54, 55, 77] A similar thermal expansion of SFCM to GDC increases the compatibility between the components and reduces the chances of cracking and cell failure. SFCM has a high conductivity of $\sim 35 \text{ S/cm}$ at 650°C and is stable to redox cycling making it a promising material.

As an SOFC cell is heated and reduced, there is the possibility for changes to occur in the fracture toughness or flaw distribution of the materials. Heating causes the materials to expand, increasing their interatomic distances, and reduction creates oxygen vacancies weakening bonds. [78, 79] Flaws can grow, combine, or change shape during these processes further affecting the overall strength. Equation 5.1 demonstrates how various factors impact the strength of a sample, where σ is the strength, K_{Ic} is the fracture toughness, Y is the shape factor for the flaw which caused failure and a is the size of the flaw. [80] The fracture toughness and flaw distributions play a direct role in the overall strength of the cell.

$$\sigma = \frac{K_{Ic}}{Y\sqrt{a}} \quad (5.1)$$

Most research focuses on measuring and comparing the Young's moduli of different materials as it changes with environment. [18, 44, 81, 82] While the modulus

can be correlated to the fracture strength of the cell, direct measurement of flexural strength remains the best means to characterize the strength of the cell. This work characterizes the changes which occur in fracture toughness and flaw distributions of SFCM, SFCM-GDC anode support layer (ASL), and SFCM-GDC/GDC half-cells when exposed to oxidizing and reducing conditions up to 600 °C by use of flexural testing and Weibull analysis. Additionally, electrical conductivity, thermogravimetric analysis, and thermal expansion are used to determine the causes for changes in mechanical properties under these conditions.

5.2 Experimental

5.2.1 Sample Preparation

SFCM powder was synthesized with conventional solid-state methods using stoichiometric amounts of strontium carbonate (SrCO_3 , Sigma-Aldrich), iron oxide (Fe_2O_3 , Sigma-Aldrich), cobalt oxide (Co_2O_3 , Inframat Advanced Materials), and molybdenum oxide (MoO_3 , Alfa-Aesar). The components were ball milled in ethanol for 24 hours, dried at 100 °C, and heated to 1100 °C for four hours.

To create fracture toughness test samples, SFCM powder was ball milled overnight with a mixture of 0.6 wt% polyethylene glycol 600, 1.8 wt% ethylene glycol, and 0.6 wt% glycerol in isopropyl alcohol. It was then dried at 100 °C, ground by mortar and pestle, pressed uniaxially into rectangular bars at 30 MPa, then isostatically pressed at 30 MPa. Sintering followed by heating to 1340 °C for four hours at 3 °C/min with a one hour hold at 400 °C to allow the binders to burn

out. This process achieved dense samples at 97% average theoretical density with no apparent flaws in the bars. Bars were then cut and sanded to final dimensions of 3 mm x 4 mm x 25 mm. The chevron notch was cut using the jig described by Jenkins, Chang and Okura following the ASTM procedure. [83, 84]

Tape casting was used to create test coupons of porous SFCM-GDC ASL and half-cells. Using ethanol as a solvent, SFCM-GDC was ball milled with polyvinyl butyral, benzyl butyl phthalate, 12 μm poly(methyl methacrylate) (16 wt% with respect to SFCM-GDC), and Menhaden fish oil. The tape was cast to a thickness of 110 μm on Mylar then laminated using a hot press to a final thickness of 660 μm . Dense GDC was casted to 30 μm and laminated to the top of the SFCM-GDC to create half-cells. Individual coupons were cut from the green tape, sintered at 1200 °C for four hours, with holds at low temperatures to burn out organic binder and pore former. The final thicknesses were measured to be 400 μm for the SFCM-GDC ASL and \sim 20 μm thick GDC electrolyte. Test coupons had their edges sanded to remove defects left from cutting, following ASTM standards. [85] Top and bottom surfaces were not sanded to preserve possible defects left from tape casting procedure, which would be representative of industrially manufactured SOFCs.

X-ray diffraction (XRD) was used to check and confirm phase purity of SFCM samples throughout the preparation and testing process. A Bruker D8 Advance with LynxEye was used with a Cu K α source. A step size of 0.02° was used with a dwell of 0.8 s to obtain diffraction patterns.

5.2.2 Conductivity

Direct current conductivity was measured using rectangular bars of SFCM and SFCM-GDC (2:1) composite. The samples were connected to a Keithley 2400 source meter by silver paste and wire. Using an in-house built reactor, the sample could be heated and the gas environment could be controlled. An initial measurement was taken after heating and 50 hours of exposure to 10% H₂ in N₂, then the sample exposed cycled between air and reducing conditions over a period of 14 days.

5.2.3 Thermogravimetric Analysis (TGA)

Mass of samples during oxidation and reduction cycling was measured using a Cahn D200 microbalance. The samples were placed in a crucible suspended from a platinum wire attached to the microbalance and enclosed by an alumina tube inside a furnace. Heating control was achieved with a PID loop and temperature measurement done by a K-type thermocouple placed immediately below the sample inside the alumina tube. Gas flow was controlled at a constant 50 sccm by mass flow controllers. 21% O₂ in dry N₂ was used for the oxidizing condition while 3% H₂ in N₂ humidified with 3% H₂O was used for the reducing conditions.

5.2.4 Mechanical Measurements

Measurements of mechanical properties were collected using a Tinius Olsen 10ST Universal Testing Machine equipped with a 250 N load cell. Experiments where any samples would be tested at elevated temperatures or under reducing

environments were conducted using a custom built three point flexural test fixture placed inside a gas-tight chamber and furnace. Otherwise, a fully-articulating four point flexural test fixture was used. Samples tested at ambient conditions were placed on the appropriate testing fixture and loaded until failure. For samples tested at elevated temperatures the sample was heated in the test chamber at $10\text{ }^{\circ}\text{C min}^{-1}$, allowed to equilibrate for 20 minutes, then tested. Samples to be reduced were placed in the chamber, heated and exposed to reducing gas for 18 hours before being tested.

5.2.4.1 Flexural Strength

A loading rate of 0.2 mm/min was used for all strength measurements. Strength was calculated from the maximum force measured before failure according to Equation 5.2 or 3.1 depending on if the four point or three point fixture is used respectively, where σ is the strength, P is the maximum force, L is the span width of the test fixture, b is the width of the sample and d is the thickness of the sample. Equation 5.2 is for a fixture where the top span is 1/2 the width of the bottom span. [85]

$$\sigma = \frac{3PL}{4bd^2} \quad (5.2)$$

5.2.4.2 Chevron Notch Fracture Toughness

The fracture toughness of chevron notched samples were measured using a loading rate of 0.001 mm/min. Fracture toughness was calculated from the maximum force using Equation 5.3 or 5.4 for four point or three point fixtures. [84, 86] Y_{min}^* is the shape factor as calculated by Equation 5.5, S_o and S_i are the outer and inner

spans, B is the width of the sample, W is the height of the sample, a_0 is the distance from the tip of the chevron notch to the bottom of the sample, and a_1 is the average distance from the side of the chevron notch to the bottom of the sample. Each sample was measured after failure, but in this study the approximate values were $S_o = 40mm$, $S_i = 20mm$, $B = 3.0mm$, $W = 4.0mm$, $a_0 = 0.80mm$, $a_1 = 3.8mm$. Fracture toughness was measured only under air at room temperature and up to 600 °C. Under reduction the fracture toughness bars would spontaneously fracture, preventing measurements under that condition.

$$K_{Ivb} = Y_{min}^* \left[\frac{P[S_o - S_i]}{BW^{3/2}} \right] 10^{-6} \quad (5.3)$$

$$K_{Ivb} = Y_{min}^* \left[\frac{P}{BW^{1/2}} \right] 10^{-6} \quad (5.4)$$

$$Y_{min}^* = \frac{0.38742 - 3.0919(a_0/W) + 4.2017(a_1/W) - 2.3127(a_1/W)^2 + 0.6379(a_1/W)^3}{1.0000 - 2.9686(a_0/W) + 3.5056(a_0/W)^2 - 2.1374(a_0/W)^3 + 0.0130(a_1/W)} \quad (5.5)$$

5.3 Results and Discussion

5.3.1 Redox Cycling Stability

SFCM has a high initial conductivity of 35 S/cm but decreases after 3 cycles to 19 S/cm and again at 9 cycles, shown in Figure 5.1a. The addition of GDC to create a SFCM-GDC composite decreases the initial conductivity to 15 S/cm. At 4 cycles, SFCM-GDC decreases conductivity and stabilizes to 8 S/cm for 19 cycles. The addition of the GDC improved the redox cycling stability by providing a very stable, contiguous framework for the SFCM. [12, 28, 79]

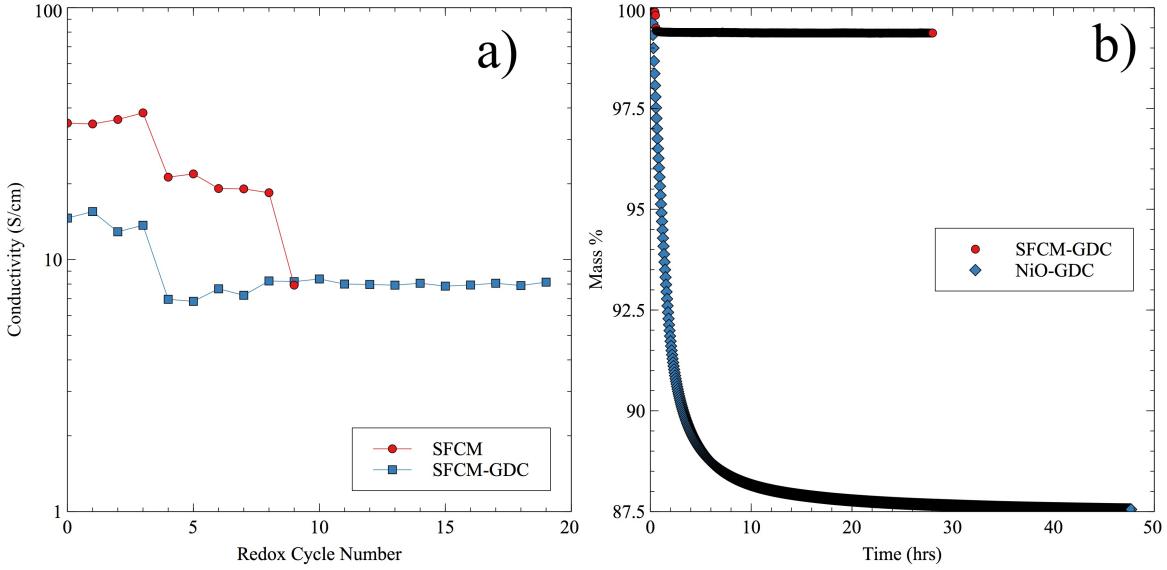


Figure 5.1: a) DC conductivity of SFCM and SFCM-GDC after cycling at 650 °C between 10% H₂ in N₂ and air. b) Mass loss of SFCM-GDC and NiO-GDC during reduction in 3% H₂/3% H₂O in N₂ at 650 °C.

Figure 5.1b shows the mass loss of SFCM-GDC as it is reduced in 3% humidified H₂. For comparison, another popular anode material, nickel oxide GDC, is plotted along with it. The reduction of SFCM-GDC results in a less than 1% reduction of mass from the formation of oxygen vacancies in the SFCM and GDC, and it reaches steady state in under two hours. NiO-GDC on the other hand loses a large amount of mass from the reduction and phase change of NiO to Ni metal taking over 30 hours to reach steady state.

Further cycling of SFCM in the thermogravimetric analyzer (TGA) was performed and results are given in Figure 5.2 with 5.2a showing the mass loss of SFCM with time as it is cycled between air and hydrogen and 5.2b being a summary of the total mass changes that occur with each cycle. With each cycle, less than 1% total

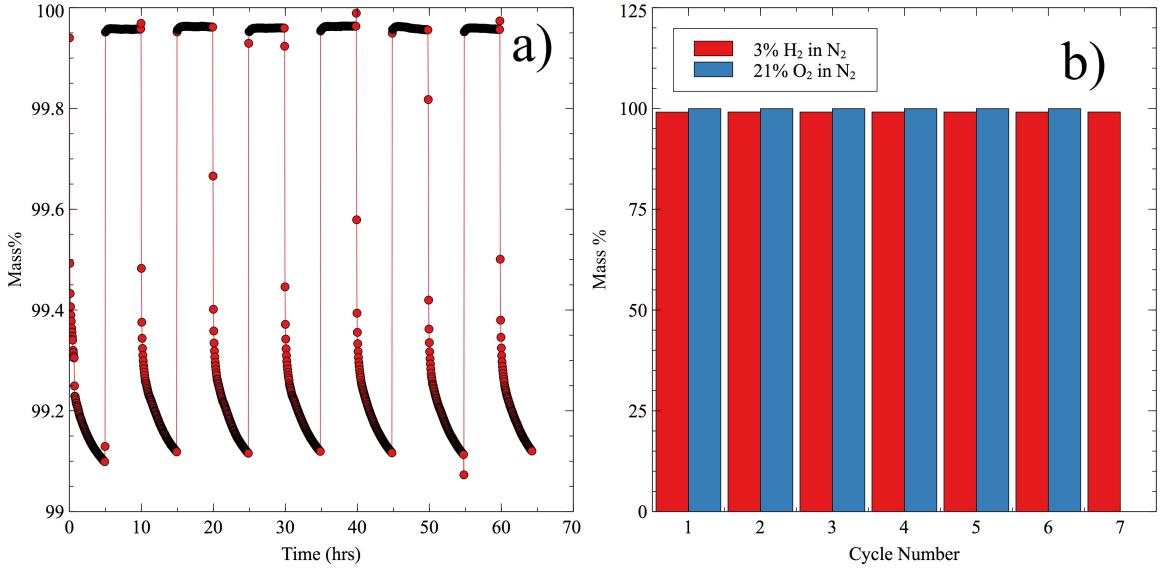


Figure 5.2: Mass changes of SFCM during cycling between 21% O₂ and 3% H₂/3% H₂O in N₂ at 600 °C. Each exposure was 5 hours. a) Percent mass change with time as the gas is switched back and forth. b) Summary of maximum and minimum changes with each cycle.

mass change is observed. Reduction occurs over a time period of five hours while oxidation happens at a faster rate, approximately one hour. Fitting the reduction and oxidation to exponential functions gives a biexponential with decay rates of 0.438 and 27.89 for reduction and an oxidation rate of 2.90. This demonstrates that SFCM does not generate any additional phases which cause the loss or gain of oxygen and that reduction and oxidation are reversible processes which occur over short periods.

5.3.2 Fracture Toughness

Fracture toughness was found to be (0.124 ± 0.023) MPa $\sqrt{\text{m}}$ at room temperature, increasing with temperature up to 600 °C, as shown in Figure 5.3a. From room

temperature to 500 °C, the rate of increase in K_{Ic} is low at $4.3 \times 10^{-5} \text{ MPa}\sqrt{\text{m}}/\text{°C}$.

From 500 °C to 600 °C the fracture toughness increases by 90%. The increase in fracture toughness is a result of the thermal expansion of the material. During process of creating the bar, the sample was cooled from 1340 °C to room temperature. This cooling and associated contraction induces stresses in the bar sample, which combine with the stresses added during testing to fracture the sample. As the sample is heated, the residual stresses are relaxed, increasing the amount of stress which must be applied externally to cause the bar to fracture. Any change in fracture toughness due to the weakening of bonds is masked by this effect. The increase in fracture toughness from 500 °C to 600 °C matches the temperature where the rate of thermal expansion also increases, as shown in Figure 5.3b.

Figure 5.3b also presents the thermal expansion of GDC and a SFCM-GDC composite. At temperatures below 550 °C the expansion of SFCM-GDC matches that of pure SFCM, greater than that of pure GDC. Above 550 °C, the rate of expansion slows in comparison to SFCM and matches the rate of expansion for GDC. Thus, below 550 °C, SFCM-GDC expands the same as SFCM and above 550 °C it expands the same as GDC. We would then expect that SFCM-GDC composites have the same increase in fracture toughness as SFCM up to 550 °C due expansion and relaxation of intrinsic stresses, but not further increase the rate above 500 °C, as SFCM does.

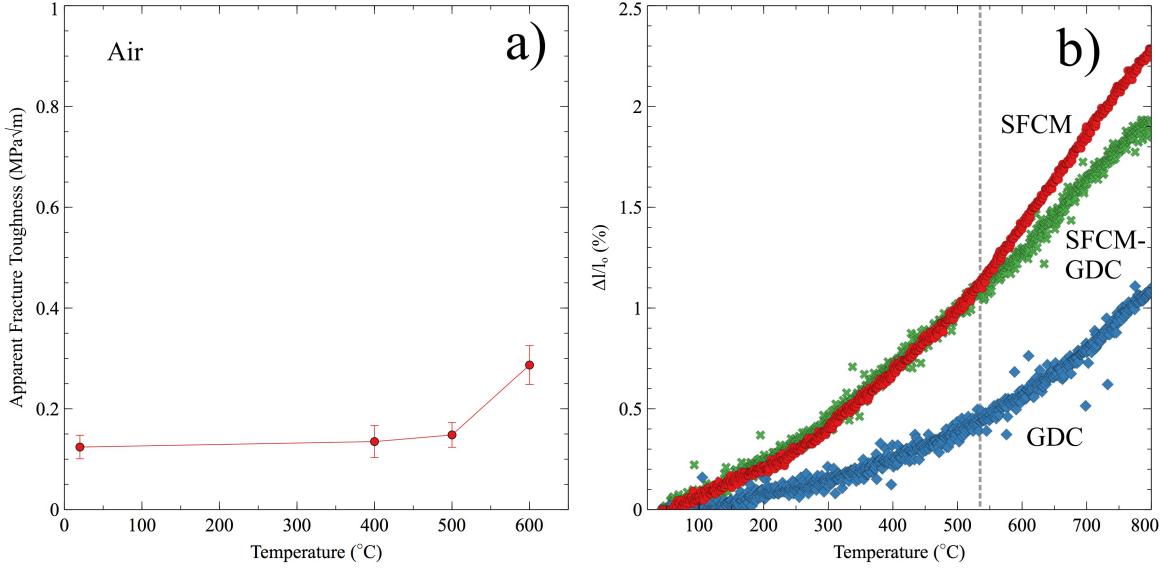


Figure 5.3: a) Fracture toughness of SFCM from 20 °C to 600 °C. b) Thermal expansion of SFCM, GDC, and SFCM-GDC.

5.3.3 Half-cell Strength of Anode-Supported SOFCs at Operating Conditions

Figure 5.4 gives box plots of the results of three point flexural testing of SFCM-GDC/GDC half-cells, and Table 5.1 summaries the strengths. The circles on the right of 5.4 represent the results of a Student's t-test, to determine if the means of the different data sets are the same. The more the circles overlap the more similar the data sets are. In this case, there is no overlap between circles at the 95% confidence interval, highlighting that the strengths tested at each condition are unique from each other.

At ambient conditions the strength of the half-cells was measured to be 57.7 MPa. Upon heating, the strength increases to 74.2 MPa. This result corre-

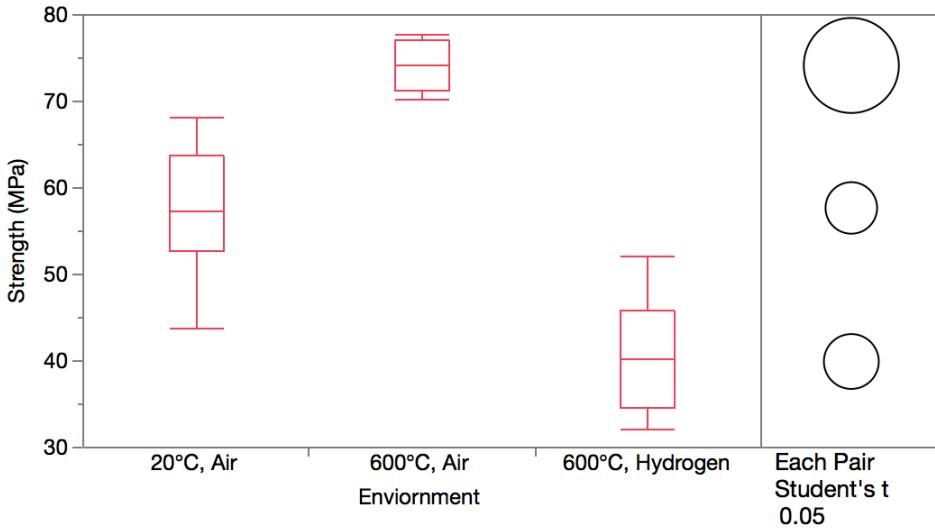


Figure 5.4: Flexural strengths of half-cell coupons made from SFCM-GDC anode with GDC electrolyte tested at 20 °C in air, 600 °C in air, and 600 °C in 5% H₂.

lates with the increase in fracture toughness discussed earlier, which is expected based on Equation 5.1. Another contributing factor to the increase in strength is the effect thermal expansion has on pre-existing cracks and flaws. Any expansion of the material helps push closed a surface crack which would lead to failure, decreasing its size and increasing the stress that would be required to cause that crack to open and propagate.

Upon reduction of the half-cell at 600 °C, the fracture strength decreases, below that of the ambient strength, to 39.9 MPa. This reduction of strength is likely due to the combination of the decrease in fracture toughness and the growth of microcracks as the materials reduce in volume.

Weibull analysis was performed to compare the distribution of flaws between the ambient tested half-cells and the in-situ reduced half-cells. Figure 5.5 displays

Table 5.1: Summary of strengths for SFCM-GDC/GDC half-cells at different environments

Temperature (°C)	Atmosphere	Number	Mean (MPa)	Std Dev (MPa)
20	Air	17	57.7	6.71
600	Air	5	74.2	2.98
600	5% H ₂	14	39.9	5.89

the fitting of Weibull distributions to the flexural strength of half-cell coupons tested at ambient conditions and during reduction at 600 °C. Table 5.2 summarizes the fitting parameter for the Weibull modulus with 95% confidence intervals using the maximum-likelihood method. Between the two conditions, there is an appreciable change in the Weibull modulus of the two samples. The Weibull modulus increases decreases from 10.4 at ambient conditions to 7.29 when at reducing conditions. This indicates that the distribution of flaws has changed by becoming wider, creating more variability between flaws. It is possible that this change is the result of an uneven growth of two different flaw types.

To confirm this, fractography would need to be performed on every sample, identifying the flaw, but this is not possible due to the porous nature of the fracture surface which obscures the fracture origin. Scanning electron microscopy was performed on fracture surfaces and epoxy filled samples from each condition to look for any microstructural changes. Figure 5.6 shows the epoxy filled and polished samples with no discernible difference between samples. No difference is observed because

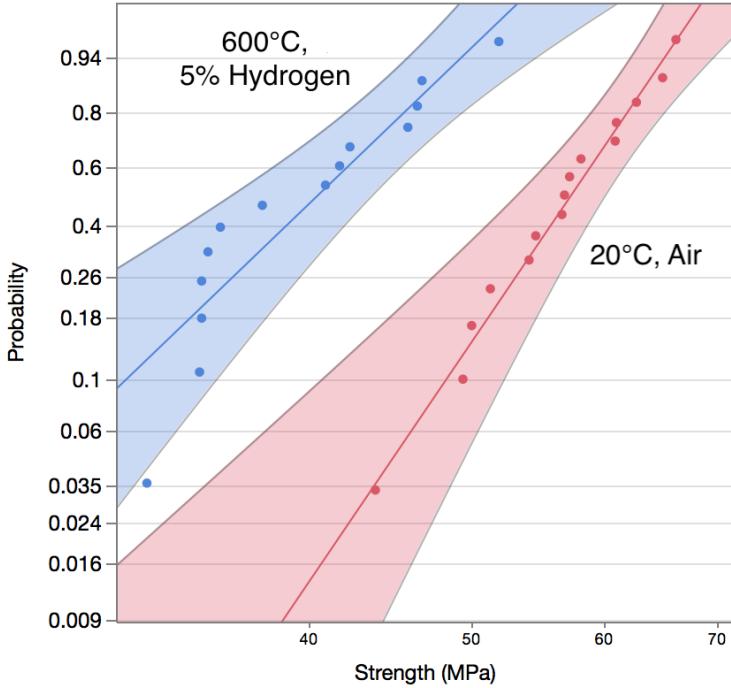


Figure 5.5: Fitted Weibull distributions of SFCM-GDC/GDC half-cells at different environments, plotted linearly with 95% confidence intervals shaded.

the likely cause of failure, microcracks, would exist along grain boundaries and are obscured by the grain boundaries and pores. [19, 87]

5.3.4 Strength of Anode Support Layer After Redox Cycling

To understand how redox cycling as the result of long term use affects the strength of SFCM based SOFCs, SFCM-GDC ASL test coupons were cycled for 10 times between nitrogen and 10% H₂ environments. Figure 5.7 shows the strength and modulus from the samples which were not cycled (0 cycles) and those cycled 10 times, tested using a four-point bend at ambient conditions. Table 5.3 summaries the means and standard deviations of the test results. The overlapping Student's

Table 5.2: Summary of Weibull fitting parameters (characteristic strength and Weibull modulus) for SFCM-GDC/GDC half-cells at different environments

Temp. (°C)	Environment	Cha.	α	α	Weibull	β	β
		Strength (α , MPa)	Lower CI	Upper CI	Modulus (β)	Lower CI	Upper CI
20	Air	60.6	57.4	63.6	10.4	6.89	14.7
600	Hydrogen	42.5	39.2	45.8	7.29	4.79	10.3

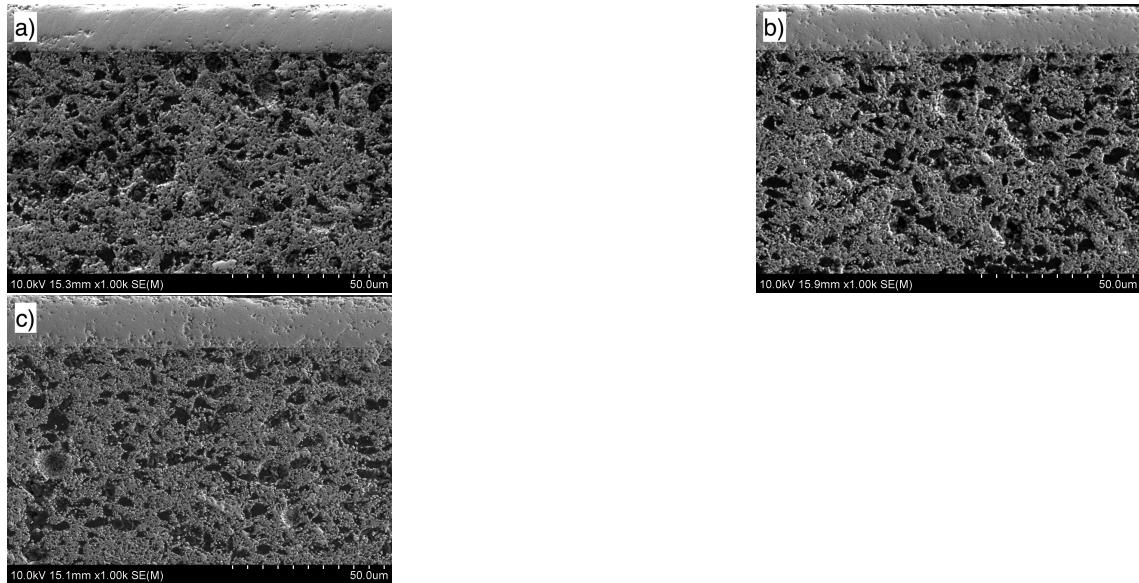


Figure 5.6: Scanning electron microscope images of epoxy filled and polished SFCM-GDC/GDC half-cell cross sections tested at a) 20 °C in air, b) 600 °C in air and c) 600 °C in 5% H₂.

Table 5.3: Summary of Cycled SFCM-GDC ASL Mechanical Properties

Number of Cycles	Number	Mean	Modulus	Mean	Strength
		Modulus (GPa)	Std Dev (GPa)	Strength (MPa)	Std Dev (MPa)
0	14	24.5	5.01	34.3	7.23
10	20	27.3	3.60	22.4	4.94

t circles in Figure 5.7b demonstrate that cycling did not significantly change the elastic modulus of the samples, while the strength did significantly decrease. This is the result of changes in microstructural flaws, rather than the change of an intrinsic material property.

The strengths of the cycled and un-cycled cells were fitted to Weibull distributions to observe how flaw distributions changed with redox cycling. Figure 5.8 presents the fitted data and distributions and Table 5.4 summarizes the fit parameters of the Weibull modulus with 95% confidence intervals. The Weibull moduli between the two data sets are very similar, indicating that the flaw distribution is the same between them. The decrease in characteristic strength is then due to the growth of flaws with cycling. SEM images in Figure 5.9 are of a sample which had not been cycled (a) and one which had been cycled 10 times (b) after being epoxy filled and polished. The sample which had been cycled 10 times has a greater number of pores at larger sizes compared to the un-cycled sample. This indicates that the finer microstructure of the pores is susceptible to changes during redox cycling due to chemical expansion, but the larger flaws which lead to complete cell failure do not

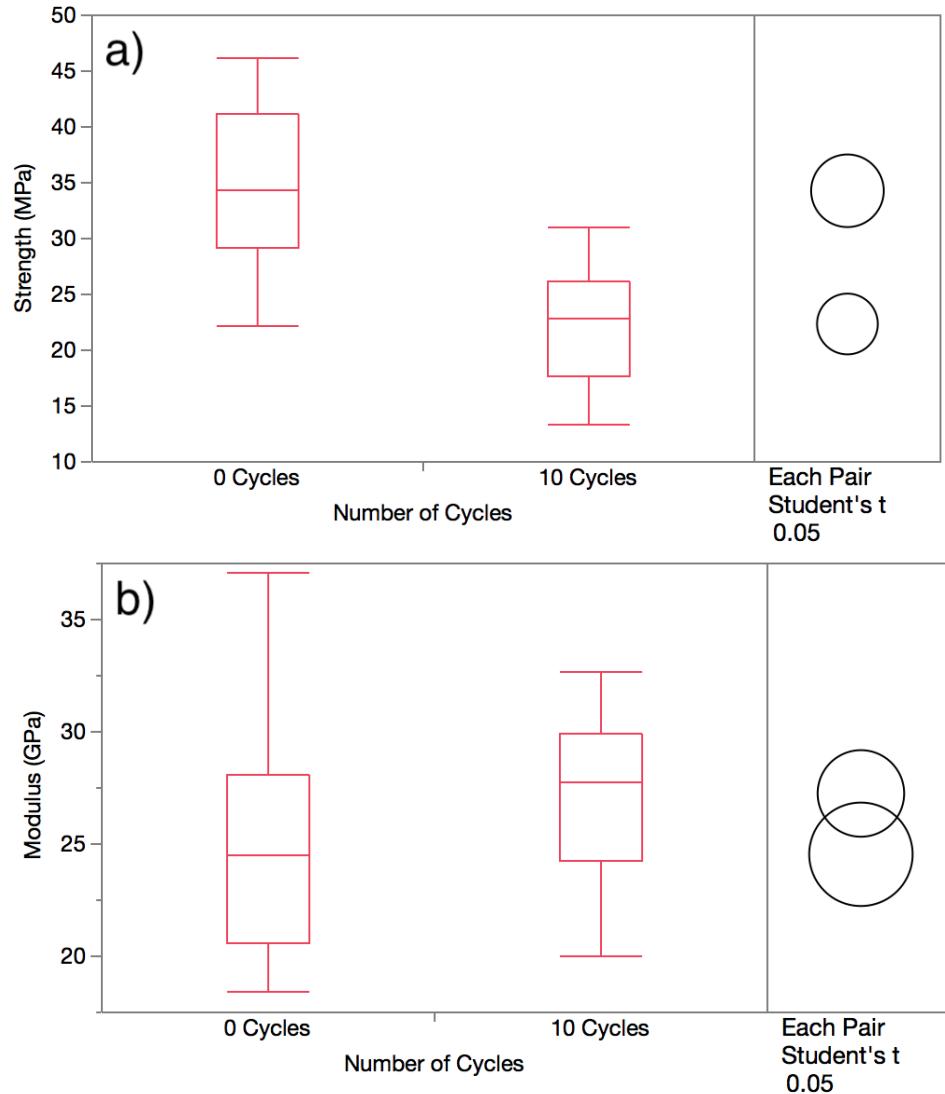


Figure 5.7: Results of four point bend test at ambient conditions of SFCM-GDC ASL with a) strength and b) modulus for samples before any cycling and after 10 redox cycles between 10% H₂ and N₂.

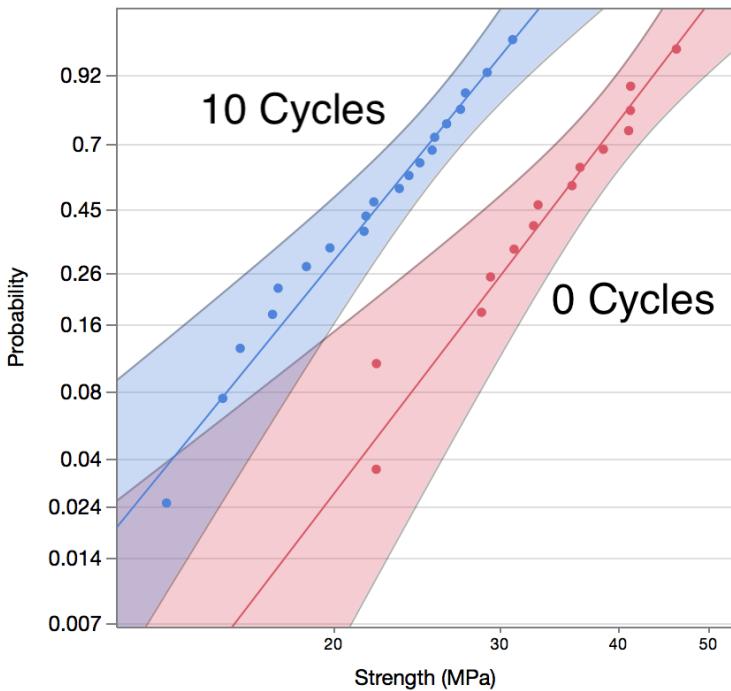


Figure 5.8: Fitted Weibull distributions of SFCM-GDC ASL before any cycling and after 10 redox cycles between 10% H₂ and N₂, plotted linearly with 95% confidence intervals shaded

change as the result of redox cycling. [88]

5.4 Conclusions

In this work the mechanical properties of SFCM and SFCM-GDC structures are characterized as the environment is changed from ambient to the working conditions of SOFCs and with redox cycling. The electrical conductivity of SFCM-GDC is stable up to 19 cycles due to the reversibility and phase stability of SFCM-GDC in the environment range. The fracture toughness of SFCM was found to be $(0.124 \pm 0.023) \text{ MPa}\sqrt{\text{m}}$ at room temperature and increases with temperature, due

Table 5.4: Summary of Weibull Fit Parameters (characteristic strength and Weibull modulus) for Cycled SFCM-GDC ASL

Number of Cycles	Char. Strength (α , MPa)	α	α	Weibull Modulus (β)	β	β
		CI Lower	CI Upper	CI Lower	CI Upper	
0	37.1	33.7	40.8	5.75	4.06	9.85
10	24.3	22.3	26.5	5.39	4.00	8.28

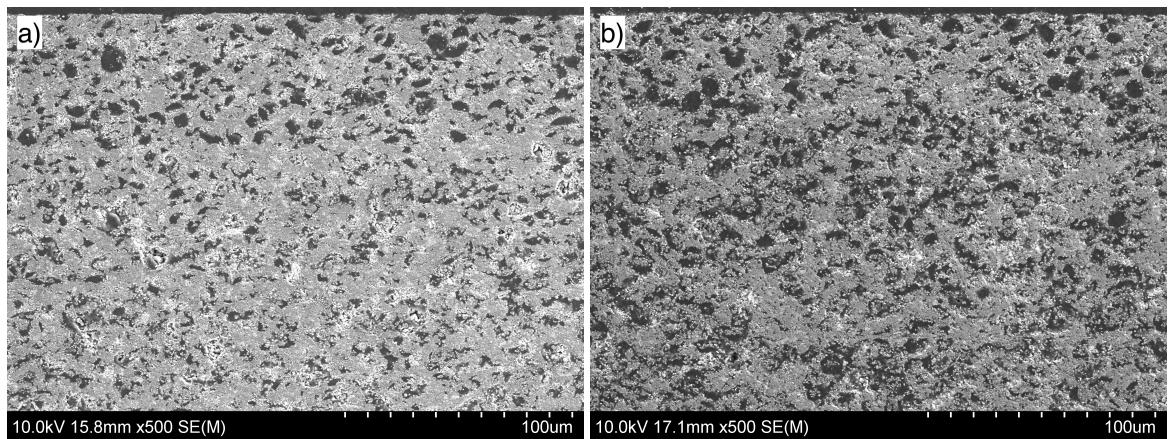


Figure 5.9: Scanning electron microscope images of epoxy filled and polished SFCM-GDC ASL cross sections tested a) before any cycling, b) after 10 cycles between 10% H_2 and N_2 .

to relaxation of residual stresses. The flexural strength of SFCM-GDC/GDC half-cells increases by 23.9% upon heating from room temperature to 600 °C. This is due to thermal expansion pushing cracks closed during heating, requiring additional stress to propagate surface cracks and the increase in fracture toughness. Once exposed to reducing conditions, the flexural strength decreases by 29.4% of the original strength, as SFCM and GDC generate oxygen vacancies. Reduction was shown to increase the size and variability of the distribution of flaws which lead to failure. Redox cycling led to the uniform increase in critical flaw size and changed the fine microstructural porosity, decreasing strength from 34.3 MPa to 22.4 MPa.

These findings show that SFCM, when combined with GDC, make a suitable anode material for SOFCs. SFCM-GDC is a stable material system, both in terms of conductivity and mechanically, with redox cycling. Reduction does increase the likelihood of failure by decreasing characteristic strength and the distribution of flaws, but repeated cycling only decreases characteristic strength and does not change the Weibull modulus.

Chapter 6: Conclusions

6.1 Solid-Oxide Fuel Cells

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Appendix A: Statistics

A.1 Student's t-test

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Appendix B: TGA Manual

B.1 Theory of Operation

Thermogravimetry works on the principle of measuring small changes in mass as the environment changes. Changes in environment can come from

B.2 Mass Measurement

The TGA uses a Cahn D200 microbalance for the mass sensing capability.

B.3 Gas Delivery

MKS Controllers are used.

B.4 pO₂ Measurement

Home built YSZ sensor.

B.5 Controls

Lab view on the computer.

B.6 Interfacing with other devices

Can be plumbed up to mass spec.

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Appendix C: Code

C.1 Arduino PID Relay Furnace Controller with Serial Connectivity

The purpose of this Arduino sketch is to power a heating furnace (controlled by a relay), with PID controls. In addition serial communications are added to monitor, log, and interact with the controller.

C.1.1 Hardware and other libraries

This was built to be used on a Arduino Uno R3, but should be easily run on a variety of different boards. For temperature sensing, an [Adafruit MAX31856](#) is used with the [library](#) from them. Also used is the PID controller [library by br3ttb](#). All I have really done is put the two together with the ability to communicate over serial.

C.1.2 Variables

Here are a list of variables for things you may want to change based on your setup.

- RelayPin: The physical pin your relay is connected to.
- Adafruit_MAX31856(CS, DI, DO, CLK): Pins for your MAX31856

- WindowSize: Length of on/off cycle, needed to account for AC power
- printdelay: Delay time in milliseconds for printout on serial
- MaxOP: Maximum operating power, used to extend life of elements
- myPID(&Input, &Output, &workingSet,P,I,D, DIRECT): PID need to be adjusted for your setup. If inverse behavior is experienced (e.g. heats when it should cool) switch DIRECT.
- workingSet and Setpoint: Initial setpoint for power on
- ramrate: Sets a ramp rate for the working setpoint. Measured in milliseconds for 1C change.

C.1.3 Serial communications

Baud rate is set to 9600. Output is tab delimited of Setpoint, Working Setpoint, Thermocouple Temperature, and Output Power. To change set point, send a new number over serial and press return. You may have to adjust your serial monitor to send \n as end of line.

```

1 #include <Adafruit_MAX31856.h> //loads library for thermocouple reader
2 #include <PID_v1.h> //loads PID library
3 #include <RunningAverage.h> //loads class for Running Average
   ↵ calculations
4 #define RelayPin 2 //set pin number which is connected to power relay
   ↵ for device
5

```

```

6 const byte numChars = 32;

7 char receivedChars[numChars]; // an array to store the received data

8

9 boolean newData = false; //trigger to determine if data needs to be
    ↵ read

10

11 Adafruit_MAX31856 max = Adafruit_MAX31856(4, 5, 6, 7); // Software SPI,
    ↵ Pin number for: CS, DI, DO, CLK

12

13 //Define Variables

14 double workingSet, Setpoint, Input, Output;

15 int WindowSize = 1000; //Length of cycle for power on/off

16 unsigned long prevprintMillis = 0;

17 const long printdelay = 5000; //delay amount before printing via serial

18 unsigned long windowStartTime;

19 unsigned long prevRampTimer = 0;

20 unsigned long MaxOP = .95; // Max Operating Power

21

22 RunningAverage myRA(10); //Set up running average with # of
    ↵ measurements

23

24 PID myPID(&Input, &Output, &workingSet, 250, 50, 8, DIRECT); //Specify the
    ↵ links and initial tuning parameters

25

26 void setup() {
27     pinMode(RelayPin, OUTPUT); //define RelayPin as an output
28

```

```

29 //staring serial communications
30 Serial.begin(9600);
31 Serial.println("PID Controller Output");
32 Serial.println("Setpoint\t Working SP\t TC Temp\t Output");//tab
   ↪ delimited for logging
33
34 //setup for thermocouple reader
35 max.begin();
36 max.setThermocoupleType(MAX31856_TCTYPE_K);//change type if needed
37
38 windowStartTime = millis(); //start timer for duty cycle window
39
40 myRA.clear(); // explicitly start clean
41
42 //initialize the variables we're linked to
43 workingSet = 20;
44 Setpoint = 20;
45
46 myPID.SetOutputLimits(0, MaxOP * WindowSize); //tell the PID to range
   ↪ between 0 and the full window size
47 myPID.SetMode(AUTOMATIC); //turn the PID on
48
49 }
50
51 //fuction to recieve data via serial and process when endmarker is
   ↪ received
52 void recvWithEndMarker() {

```

```

53 static byte ndx = 0;
54
55 char endMarker = '\n'; //define line endmarker for client
56
57 // if (Serial.available() > 0) {
58
59     while (Serial.available() > 0 && newData == false) {
60
61         rc = Serial.read();
62
63         if (rc != endMarker) {
64
65             receivedChars[ndx] = rc;
66
67             ndx++;
68
69             if (ndx >= numChars) {
70
71                 ndx = numChars - 1;
72
73             }
74
75
76             else {
77
78                 receivedChars[ndx] = '\0'; // terminate the string
79
80                 ndx = 0;
81
82                 newData = true;
83
84             }
85
86
87             }
88
89
90             //Function to repeat new setpoint for confirmation
91
92             void showNewData() {
93
94                 if (newData == true) {
95
96                     String recievedString = String(receivedChars);

```

```

80 Serial.print("Setpoint changed to ... ");
81 Serial.println(recievedString.toFloat());
82 Setpoint = recievedString.toFloat();
83 newData = false;
84 }
85 }
86
87 void loop() {
88 recvWithEndMarker(); //check for new setpoint
89 showNewData(); //sets new setpoint and displays it
90
91 // Input = max.readThermocoupleTemperature(); //read thermocouple
92
93 myRA.addValue(max.readThermocoupleTemperature());
94
95 Input = myRA.getAverage();
96
97 myPID.Compute(); //calculate PID output
98
99 //print delay for serial output so not to flood logs
100 unsigned long printMillis = millis();
101 if (printMillis - prevprintMillis >= printdelay) {
102     prevprintMillis = printMillis;
103     Serial.print(Setpoint); Serial.print("\t"); Serial.print(workingSet);
104     → Serial.print("\t"); Serial.print(max.readThermocoupleTemperature
105     → ()); Serial.print("\t"); Serial.println(Output/WindowSize*100);
106 }

```

```

105
106 //turn the output pin on/off based on pid output
107 if( millis() - windowStartTime >=WindowSize)
108 { //time to shift the Relay Window
109     windowStartTime += WindowSize;
110 }
111 if( Output < millis() - windowStartTime) digitalWrite(RelayPin,LOW); //  

    ↳ HIGH and LOW set to default off
112 else digitalWrite(RelayPin,HIGH);
113
114 //sets ramp rate functionality
115 unsigned long ramptimer = millis();
116 unsigned long ramprate = 6000;//milliseconds for 1C change
117 if( workingSet != Setpoint)
118 {
119     if( ramptimer - prevRampTimer >= ramprate && workingSet < Setpoint)
120     {
121         workingSet++;
122         prevRampTimer = ramptimer;
123     }
124     if( ramptimer - prevRampTimer >= ramprate && workingSet > Setpoint)
125     {
126         workingSet--;
127         prevRampTimer = ramptimer;
128     }
129 }
130 }
```

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