

MA2822:
ADVANCED STATISTICS
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Regression Analysis of Used Car Prices

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1 Introduction

In this project we study the price of used cars based on a number of relevant characteristics. Using regression analysis tools implemented in the open source language *R* (which is widely used for statistical analysis), we aim to model the sales price as well as detect correlations between factors. The dataset includes 172 observations of cars with a 12 characteristics including the following: *price*, in thousands of Euros; *age*, in months; *km*, the total distance traveled in kilometers; *TIA*, the number of months until the next vehicle inspection. The data also includes dummy variables (which are equal to 1 or 0 depending on whether the factor is true or false) such as *ABS* and *SunRoof* representing the presence of ABS-technology or a sunroof respectively.

2 Charectaristics of and Correlations in the Data

Before procededing it is a good idea to get a general idea of the correlations between the variables. Figure 1 is a scatter plot showing the dependencies between the *price*, *age*, *km*, and *TIA*. It shows a relativety strong postive correlation between *price* and *age* and some negative correlation between *age* and *km* as well as postitive correlation between *price* and *km*. These relationships are in accord with our existing knowledge of the used car market. *TIA* seems to explain the other variables in this model poorly.

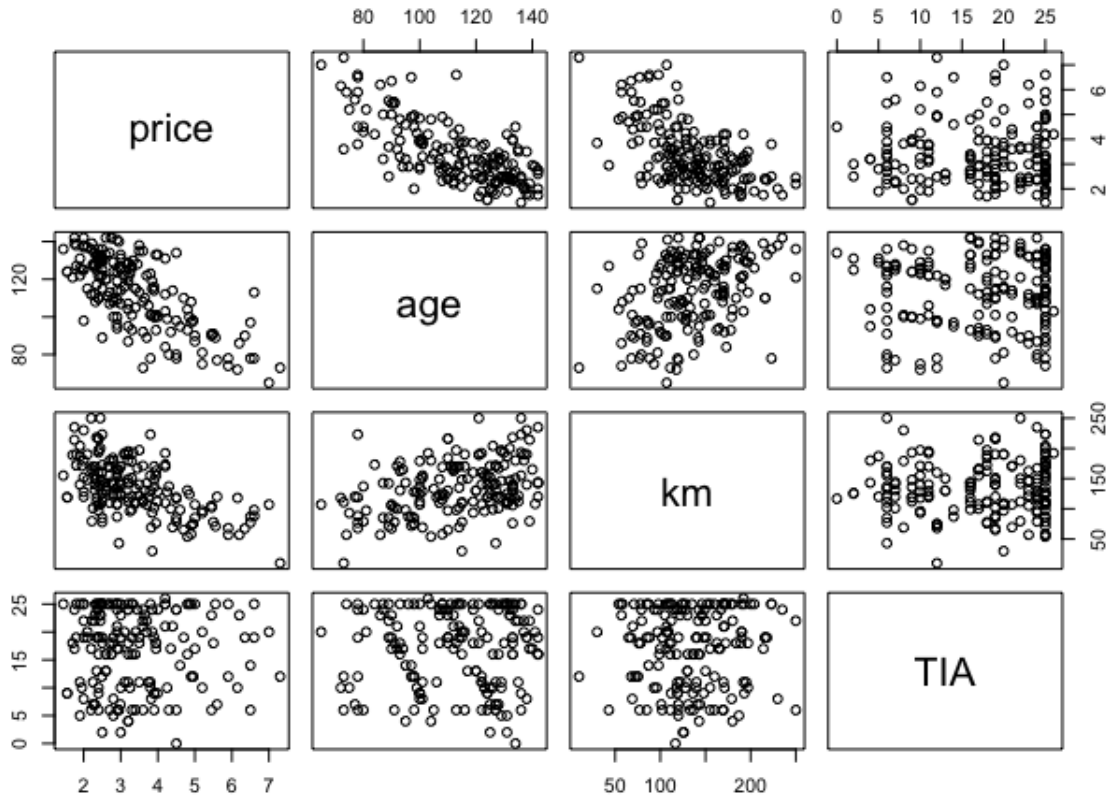


Figure 1: Scatter plot of the variables *price*, *age*, *km*, and *TIA*.

In addition to this we can use boxplots to analyze whether the presence of ABS technology or a sunroof, represented here by the dummy variables *ABS* and *SunRoof*, have an effect on price. Figure 2 displays this analysis for each variable. To the left the boxplots for vehicles with and without ABS show a few perhaps expected charectaristics of the dataset. The median price of a car with ABS is significantly higher than their counterparties (compare 3 200 EUR to 2 625 EUR). Also, the variance of the price of cars having an ABS-technology is much lower than for those that without it. Since 50% of all “ABS” cars have a price that ranges between 2.6 and 4 with pretty much no “ABS” car having a price higher than 6, where as 50% of

all “Non-ABS” cars have a price that ranges between 2.5 and 4.5 and a maximum of 7. It can be concluded that the price is somewhat correlated to the dummy variable *ABS*, but not very strongly.

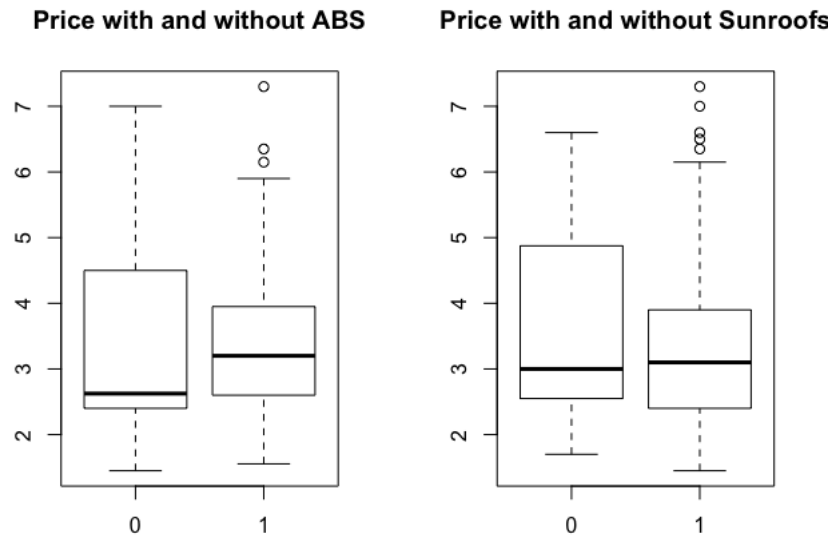


Figure 2: Pairs of boxplots of price of vehicles with and without ABS (left) and sunroofs (right).

A similar analysis can be done for the presence of a sunroof. The second set of boxplots in Figure 2 show values for vehicles with and without them. The medians are quite similar for “Non-OpenRoof” and “OpenRoof” cars. The “box range” around the median is smaller for cars with sunroofs, but apart from that they are no visible differences. The correlation between price and OpenRoof seems to be rather small; further analysis is needed to confirm this observed relationship.

3 Study of price as a function of the prescene of ABS-technology

As seen in Section 2 cars with ABS seem to generally have a higher price than cars without this technology. We will further analyze how well *price* can be explained by the *ABS*.

To better understand how the *R* software works we created two simple regression models with all variables provided with *ABS* as qualitative and quantitative variable. In implementation qualitative means that the variable is given a numerical value, 1 representing the presence of ABS or 0 otherwise. The quantitative variable is a logical data type meaning it can be either *TRUE* or *FALSE*. No difference can be seen in the *summary* function (which provides values and different significance metrics for each coefficient) between those two models. It may be pertinent to remember that the logical variable cannot be calculated upon, e.g. we cannot calculate its mean value. This should not make a difference in the final model as regression requires that the logical variable be implemented as a dummy variable (i.e. qualitatively) anyways.

The simplest of regressions can be a good way to analyze the explanatory power of *ABS*. We created a regression model of *price* as only a function of *ABS* corresponding to the following model.

$$price = \beta_0 + \beta_1 \times ABS + \epsilon \quad (1)$$

Here β_0 is the intercept and β_1 is the slope of the equation. Regression on our dataset resulted in the following estimations. $\hat{\beta}_0 = 3.45363$ and $\hat{\beta}_1 = -0.08321$. It is clear that the variable *ABS* does not account for any of the variance of the price, since its coefficient of determination, R^2 is very low (0.00097). That means that the model does not do a very good job predicting the price. This fact is also reflected by the p-value for *ABS*, $p = 0.686$. the p-value is the probability of obtaining a result as more extreme given the null hypothesis (which in this case is that the coefficient $\beta_1 = 0$.) For these reasons it is clear that *ABS* on its own explains the price very poorly. Arguably, the intercept alone would be a better model as the model would just create a nearly constant line.

4 Étude du prix en fonction du kilométrage