### STAT 222 - Feature Selection

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### **Recovery Stage**

#### **Stepwise Selection - Low Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.773" [1] "Adjusted R^2 for Full Model: 0.756"

		Dependent variable:				
	R1–RF					
	(1)	(2)	(3)	(4)		
CMA	0.259***	0.238***	0.016	0.238***		
	(0.061)	(0.054)	(0.181)	(0.054)		
CRD	-0.049*					
	(0.025)					
_IQ	-0.152***	-0.156***	-0.153***	-0.156***		
	(0.027)	(0.023)	(0.023)	(0.023)		
ИE	0.118***	0.140***	0.074	0.140***		
	(0.041)	(0.040)	(0.053)	(0.040)		
Mkt-RF	0.581***	0.571***	0.612***	0.571***		
	(0.028)	(0.027)	(0.039)	(0.027)		
RMW	-0.134**		-0.180**			
	(0.056)		(0.089)			
ROE	0.096*					
	(0.050)					
PC2			-0.234			
			(0.157)			
Constant	0.250***	0.222***	0.236***	0.222***		
	(0.052)	(0.050)	(0.051)	(0.050)		
Observations	175	175	175	175		

$R^2$	0.772	0.762	0.768	0.762
Adjusted R <sup>2</sup>	0.762	0.757	0.760	0.757
Residual Std. Error	0.626 (df = 167)	0.634 (df = 170)	0.629 (df = 168)	0.634 (df = 170)
F Statistic	80.654*** (df = 7; 167)	136.193*** (df = 4; 170)	92.747*** (df = 6; 168)	136.193*** (df = 4; 170)

Note: p<0.1; p<0.05; p<0.01

[1] "Selected Factors: CMA, LIQ, ME, Mkt-RF"

#### **Stepwise Selection - Medium Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.747" [1] "Adjusted R^2 for Full Model: 0.728"

	Dependent variable:				
	R2-RF				
	(1)	(2)	(3)	(4)	
CMA	0.221***	0.221***	0.221***	0.221***	
	(0.061)	(0.061)	(0.061)	(0.061)	
LIQ	-0.131***	-0.131***	-0.131***	-0.131***	
	(0.026)	(0.026)	(0.026)	(0.026)	
ME	0.154***	0.154***	0.154***	0.154***	
	(0.045)	(0.045)	(0.045)	(0.045)	
Mkt-RF	0.593***	0.593***	0.593***	0.593***	
	(0.031)	(0.031)	(0.031)	(0.031)	
Constant	0.467***	0.467***	0.467***	0.467***	
	(0.057)	(0.057)	(0.057)	(0.057)	
Observations	175	175	175	175	
$R^2$	0.742	0.742	0.742	0.742	
Adjusted R <sup>2</sup>	0.736	0.736	0.736	0.736	
Residual Std. Error (df = 170)	0.716	0.716	0.716	0.716	
F Statistic (df = 4; 170)	122.546***	122.546***	122.546***	122.546***	

Note: p<0.1; p<0.05; p<0.01

### **Stepwise Selection - High Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.704" [1] "Adjusted R^2 for Full Model: 0.682"

		Dependent variable:				
		R3	B-RF			
	(1)	(2)	(3)	(4)		
СМА	0.204***	0.204***	0.234***	0.289***		
	(0.074)	(0.074)	(0.072)	(0.070)		
PC3			-0.204***	-0.157***		
			(0.064)	(0.056)		
LIQ	-0.103***	-0.103***	-0.116***			
	(0.032)	(0.032)	(0.039)			
ME	0.176***	0.176***				
	(0.055)	(0.055)				
МОМ			-0.065**			
			(0.032)			
Mkt-RF	0.624***	0.624***	0.626***	0.583***		
	(0.038)	(0.038)	(0.038)	(0.031)		
Constant	0.687***	0.687***	0.734***	0.701***		
	(0.069)	(0.069)	(0.069)	(0.069)		
Observations	175	175	175	175		
$R^2$	0.700	0.700	0.700	0.685		
Adjusted R <sup>2</sup>	0.693	0.693	0.691	0.679		
Residual Std. Error	0.872 (df = 170)	0.872 (df = 170)	0.874 (df = 169)	0.891 (df = 171)		
F Statistic	99.101*** (df = 4; 170)	99.101*** (df = 4; 170)	78.932*** (df = 5; 169)	123.674*** (df = 3; 171)		

*P<0.1; p<0.05; p<0.01* 

<sup>[1] &</sup>quot;Selected Factors: CMA, LIQ, ME, Mkt-RF"

# **Expansion Stage**

# **Stepwise Selection - Low Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.784" [1] "Adjusted R^2 for Full Model: 0.78"

		Depender	nt variable:	
	R1–RF			
	(1)	(2)	(3)	(4)
СМА	0.174**		0.204***	0.267***
	(0.083)		(0.057)	(0.053)
CRD	-0.045**			
	(0.019)			
EG	0.077*			
	(0.046)			
LIQ			-0.006	
			(0.022)	
HML	0.276***	0.309***	0.294***	0.071*
	(0.035)	(0.026)	(0.054)	(0.041)
IA	-0.146 <sup>*</sup>			
	(0.078)			
МОМ	-0.064***	-0.084***		
	(0.021)	(0.019)		
PC5			-0.032	0.493***
			(0.097)	(0.047)
PC7			0.039	0.398***
			(0.069)	(0.050)
Mkt-RF	0.812***	0.797***	0.857***	0.590***
	(0.018)	(0.018)	(0.042)	(0.020)
RMW	0.361***	0.352***	0.404***	
	(0.035)	(0.032)	(0.069)	
PC4			-0.204***	
			(0.047)	
			•	

SMB	0.337***	0.331***	0.305***	
	(0.028)	(0.027)	(0.043)	
Constant	0.056*	0.060**	0.029	0.147***
	(0.032)	(0.030)	(0.036)	(0.031)
Observations	598	598	598	598
$R^2$	0.783	0.778	0.783	0.760
Adjusted R <sup>2</sup>	0.780	0.776	0.780	0.758
Residual Std. Error	0.715 (df = 588)	0.721 (df = 592)	0.715 (df = 588)	0.749 (df = 592)
F Statistic	235.712*** (df = 9; 588)	414.416*** (df = 5; 592)	235.986*** (df = 9; 588)	375.036*** (df = 5; 592)
Note:				p<0.1; <b>p&lt;0.05</b> ; p<0.01

[1] "Selected Factors: HML, MOM, Mkt-RF, RMW, SMB"

# **Stepwise Selection - Medium Return**

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.781" [1] "Adjusted R^2 for Full Model: 0.777"

Dependent variable:				
R2-RF				
(1)	(2)	(3)	(4)	
0.176*		0.185**	0.302***	
(0.092)		(0.073)	(0.046)	
0.120**				
(0.051)				
0.325***	0.306***	0.131**		
(0.037)	(0.028)	(0.057)		
-0.216**				
(0.087)				
0.047**	0.057***			
(0.021)	(0.021)			
-0.042*				
(0.022)				
	0.176* (0.092) 0.120** (0.051) 0.325*** (0.037) -0.216** (0.087) 0.047** (0.021) -0.042*	(1) (2)  0.176* (0.092) 0.120** (0.051) 0.325*** 0.306*** (0.037) (0.028) -0.216** (0.087) 0.047** 0.057*** (0.021) -0.042*	(1) (2) (3)  0.176*	

ME			-0.205*	
			(0.119)	
Mkt-RF	0.856***	0.836***	0.671***	0.609***
	(0.022)	(0.021)	(0.048)	(0.036)
PC5			0.436***	0.579***
			(0.113)	(0.075)
PC7			0.478***	0.571***
			(0.104)	(0.079)
RMW	0.358***	0.381***	0.191***	0.183***
	(0.040)	(0.036)	(0.073)	(0.061)
SMB	0.376***	0.350***	0.361***	0.094**
	(0.033)	(0.031)	(0.122)	(0.045)
CRD			0.117***	0.134***
			(0.034)	(0.031)
ROE			-0.165***	-0.248***
			(0.060)	(0.053)
Constant	0.195***	0.210***	0.286***	0.310***
	(0.035)	(0.034)	(0.037)	(0.035)
Observations	598	598	598	598
$R^2$	0.781	0.775	0.781	0.778
Adjusted R <sup>2</sup>	0.777	0.773	0.777	0.775
Residual Std. Error	0.795 (df = 588)	0.804 (df = 592)	0.795 (df = 587)	0.799 (df = 589)
F Statistic	232.687*** (df = 9;	406.890*** (df = 5;	209.513*** (df = 10;	258.286*** (df = 8;
	588)	592)	587)	589)
Note:			p	o<0.1; <b>p&lt;0.05;</b> p<0.01

[1] "Selected Factors: HML, LIQ, Mkt-RF, RMW, SMB"

### **Stepwise Selection - High Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.765" [1] "Adjusted R^2 for Full Model: 0.76"

Dependent variable:

		R3	–RF	
	(1)	(2)	(3)	(4)
СМА	0.158			
	(0.108)			
EG	0.176***	0.187***		
	(0.060)	(0.060)		
HML	0.350***	0.322***	0.076	0.193***
	(0.044)	(0.035)	(0.055)	(0.038)
IA	-0.245**			
	(0.104)			
MOM			0.290***	0.114***
			(0.067)	(0.032)
ME			-0.239 <sup>*</sup>	-0.328**
			(0.131)	(0.128)
ROE			-0.371***	
			(0.123)	
LIQ	0.153***	0.162***	-0.120**	
	(0.025)	(0.024)	(0.054)	
Mkt-RF	0.903***	0.903***	0.716***	0.790***
	(0.025)	(0.025)	(0.040)	(0.028)
RMW	0.367***	0.356***		
	(0.047)	(0.045)		
PC5			0.902***	0.475***
			(0.155)	(0.060)
SMB	0.402***	0.409***	0.267 <sup>*</sup>	0.516***
	(0.038)	(0.038)	(0.151)	(0.126)
PC7			0.357***	0.307***
			(0.068)	(0.064)
PC6			0.633***	0.343***
			(0.125)	(0.056)
Constant	0.319***	0.313***	0.540***	0.453***
	(0.042)	(0.042)	(0.050)	(0.040)
Observations	598	598	598	598
$R^2$	0.765	0.762	0.763	0.760
Adjusted R <sup>2</sup>	0.761	0.760	0.759	0.756
Residual Std. Error	0.952 (df = 589)	0.955 (df = 591)	0.956 (df = 587)	0.962 (df = 589)
F Statistic	239.157*** (df = 8; 589)	315.505*** (df = 6; 591)	189.293*** (df = 10; 587)	232.618*** (df = 8; 589)

[1] "Selected Factors: EG, HML, LIQ, Mkt-RF, RMW, SMB"

# **Downturn Stage**

#### **Stepwise Selection - Low Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.723" [1] "Adjusted R^2 for Full Model: 0.718"

Dependent variable:					
R1-RF					
(1)	(2)	(3)	(4)		
-0.108***	-0.108***	-0.064**	-0.065**		
(0.022)	(0.022)	(0.028)	(0.028)		
-0.108***	-0.108***				
(0.036)	(0.036)				
0.204***	0.204***				
(0.045)	(0.045)				
-0.064***	-0.064***				
(0.021)	(0.021)				
0.660***	0.660***	0.559***	0.568***		
(0.018)	(0.018)	(0.020)	(0.019)		
0.220***	0.220***	0.321***	0.349***		
(0.038)	(0.038)	(0.052)	(0.050)		
		0.115*	0.132**		
		(0.059)	(0.058)		
0.122***	0.122***	0.057*	0.057*		
(0.029)	(0.029)	(0.029)	(0.029)		
		-0.434***	-0.374***		
		(0.093)	(0.087)		
		-0.310***	-0.252***		
		(0.086)	(0.079)		
	-0.108*** (0.022) -0.108*** (0.036) 0.204*** (0.045) -0.064*** (0.021) 0.660*** (0.018) 0.220*** (0.038)	(1) (2)  -0.108*** -0.108*** (0.022) (0.022) -0.108*** -0.108*** (0.036) (0.036) 0.204*** 0.204*** (0.045) (0.045) -0.064*** -0.064*** (0.021) (0.021) 0.660*** (0.018) 0.220*** (0.038)  0.122*** 0.122***	(1) (2) (3)  -0.108*** -0.108*** -0.064** (0.022) (0.022) (0.028)  -0.108*** -0.108*** (0.036) (0.036) 0.204*** 0.204*** (0.045) (0.045) -0.064*** -0.064*** (0.021) (0.021) 0.660*** 0.660*** 0.559*** (0.018) (0.018) (0.020) 0.220*** 0.220*** 0.321*** (0.038) (0.038) (0.052) 0.115* (0.059) 0.122*** 0.122*** 0.057* (0.029) (0.029) -0.434*** (0.093) -0.310****		

ROE			0.088*	
			(0.049)	
Constant	0.101***	0.101***	0.139***	0.140***
	(0.032)	(0.032)	(0.032)	(0.032)
Observations	668	668	668	668
$R^2$	0.722	0.722	0.723	0.721
Adjusted R <sup>2</sup>	0.719	0.719	0.719	0.718
Residual Std. Error	0.813 (df = 660)	0.813 (df = 660)	0.812 (df = 659)	0.813 (df = 660)
F Statistic	244.342*** (df = 7; 660)	244.342*** (df = 7; 660)	214.746*** (df = 8; 659)	244.125*** (df = 7; 660)
Note:			ŗ	o<0.1; <b>p&lt;0.05;</b> p<0.01

[1] "Selected Factors: CRD, HML, IA, LIQ, Mkt-RF, RMW, SMB"

# **Stepwise Selection - Medium Return**

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.721" [1] "Adjusted R^2 for Full Model: 0.716"

		Dependent variable:  R2-RF				
	(1)	(2)	(3)	(4)		
CRD	-0.045*		-0.037			
	(0.025)		(0.023)			
EG	-0.082					
	(0.052)					
HML	-0.140***	-0.093**				
	(0.040)	(0.036)				
IA	0.234***	0.247***	0.168*			
	(0.049)	(0.049)	(0.087)			
LIQ	-0.065***	-0.066***				
	(0.023)	(0.023)				
ME	0.122***	0.134***	0.078***			
	(0.031)	(0.031)	(0.030)			

659)	661)	660)	663)
	0.04)	000)	000)
211.536*** (df = 8;	278.060*** (df = 6;	241.568*** (df = 7;	413.866*** (df = 4;
0.883 (df = 659)	0.887 (df = 661)	0.883 (df = 660)	0.889 (df = 663)
0.716	0.714	0.716	0.712
0.720	0.716	0.719	0.714
668	668	668	668
(0.035)	(0.035)	(0.036)	(0.035)
0.243***	0.222***	0.204***	0.188***
		(0.068)	(0.067)
		0.302***	0.307***
		(0.099)	(0.041)
		0.034	0.249***
(0.047)	(0.041)	(0.053)	(0.053)
0.263***	0.220***	0.399***	0.366***
(0.020)	(0.020)	(0.032)	(0.031)
0.699***	0.704***	0.795***	0.808***
	(0.020) 0.263*** (0.047) 0.243*** (0.035) 668 0.720 0.716 0.883 (df = 659) 211.536*** (df = 8;	(0.020) (0.020) 0.263*** 0.220*** (0.047) (0.041) 0.243*** 0.222*** (0.035) (0.035) 668 668 0.720 0.716 0.716 0.714 0.883 (df = 659) 0.887 (df = 661) 211.536*** (df = 8; 278.060*** (df = 6;	(0.020) (0.020) (0.032) 0.263*** 0.220*** 0.399*** (0.047) (0.041) (0.053) 0.034 (0.099) 0.302*** (0.068) 0.243*** 0.222*** 0.204*** (0.035) (0.035) (0.036)  668 668 668 0.720 0.716 0.719 0.716 0.714 0.716  0.883 (df = 659) 0.887 (df = 661) 0.883 (df = 660) 211.536*** (df = 8; 278.060*** (df = 6; 241.568*** (df = 7;

[1] "Selected Factors: Mkt-RF, RMW, CMA, PC5"

#### **Stepwise Selection - High Return**

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.739" [1] "Adjusted R^2 for Full Model: 0.735"

		Dependent variable:  R3-RF				
	(1)	(2)	(3)	(4)		
EG	-0.134**		-0.162***			
	(0.055)		(0.055)			
HML	-0.141***	-0.112***	-0.082*			
	(0.044)	(0.043)	(0.049)			
IA	0.186***	0.192***	0.127**			
	(0.057)	(0.057)	(0.057)			

ME	0.150***	0.167***		
	(0.034)	(0.033)		
МОМ	0.089***	0.081***		
	(0.025)	(0.025)		
Mkt-RF	0.762***	0.769***	0.840***	0.744***
	(0.021)	(0.021)	(0.039)	(0.018)
PC3			-0.169***	-0.209***
			(0.035)	(0.033)
RMW	0.277***	0.213***	0.309***	
	(0.051)	(0.044)	(0.065)	
PC5			0.210**	
			(0.087)	
Constant	0.375***	0.361***	0.369***	0.388***
	(0.039)	(0.039)	(0.041)	(0.039)
Observations	668	668	668	668
$R^2$	0.738	0.736	0.739	0.727
Adjusted R <sup>2</sup>	0.735	0.734	0.736	0.726
Residual Std. Error	0.987 (df = 660)	0.990 (df = 661)	0.986 (df = 660)	1.004 (df = 665)
F Statistic	265.956*** (df = 7;	307.077*** (df = 6;	266.588*** (df = 7;	884.675*** (df = 2;
r Statistic	660)	661)	660)	665)
Note:			4	o<0.1; <b>p&lt;0.05</b> ; p<0.01

[1] "Selected Factors: Mkt-RF, PC3"

# **Depression Stage**

### **Stepwise Selection - Low Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.909" [1] "Adjusted R^2 for Full Model: 0.905"

Dependent variable:					
R1–RF					
(1)	(2)	(3)	(4)		

Note:			p	o<0.1; <b>p&lt;0.05;</b> p<0.0
F Statistic	389.798*** (df = 7; 279)	450.185*** (df = 6; 280)	343.824*** (df = 8; 278)	389.078*** (df = 7; 279)
Residual Std. Error	1.153 (df = 279)	1.158 (df = 280)	1.149 (df = 278)	1.154 (df = 279)
Adjusted R <sup>2</sup>	0.905	0.904	0.906	0.905
$R^2$	0.907	0.906	0.908	0.907
Observations	287	287	287	287
	(0.071)	(0.071)	(0.072)	(0.072)
Constant	0.147**	0.159**	0.186***	0.183**
. 02			(0.075)	(0.071)
PC2	(3.333)	(0.000)	0.227***	0.176**
Sivid	(0.050)	(0.050)	(0.187)	(0.165)
SMB	0.468***	0.458***	0.748***	0.585***
ROL	(0.090)		(0.092)	
ROE	0.169*	(0.071)	(0.0 <i>97)</i> 0.171*	(0.074)
RMW	0.266*** (0.086)	0.356*** (0.071)	(0.097)	0.338*** (0.074)
DNAVA/	0.266***	0.256***	(0.209) 0.221**	(0.186)
ME			-0.396*	-0.215
N 45	(0.026)	(0.025)	(0.027)	(0.024)
Mkt-RF	0.926***	0.914***	0.957***	0.930***
	0.000***	0.04.4***	(0.097)	(0.095)
PC5			0.351***	0.314***
	(0.031)	(0.028)	***	***
MOM	-0.102***	-0.075***		
	(0.079)	(0.079)	(0.083)	(0.083)
EG	-0.292***	-0.281***	-0.330***	-0.307***
	(0.073)	(0.073)		
СМА	0.243***	0.229***		

[1] "Selected Factors: CMA, EG, MOM, Mkt-RF, RMW, SMB"

# **Stepwise Selection - Medium Return**

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC

#### 4. Forward BIC

[1] "R^2 for Full Model: 0.892" [1] "Adjusted R^2 for Full Model: 0.887"

		Depender	nt variable:	
		R2	-RF	
	(1)	(2)	(3)	(4)
СМА	0.119			
	(0.082)			
EG	-0.301***	-0.335***	-0.390***	-0.329***
	(0.088)	(0.085)	(0.090)	(0.087)
LIQ	0.067*			
	(0.037)			
Mkt-RF	0.900***	0.901***	0.932***	0.899***
	(0.030)	(0.024)	(0.029)	(0.025)
ME			-0.103	0.051
			(0.174)	(0.163)
RMW	0.310***	0.450***	0.369***	0.444***
	(0.092)	(0.064)	(0.083)	(0.067)
ROE	0.147*		0.181*	
	(0.087)		(0.093)	
PC5			0.194*	
			(0.104)	
SMB	0.476***	0.495***	0.606***	0.446***
	(0.057)	(0.053)	(0.176)	(0.164)
Constant	0.299***	0.320***	0.318***	0.318***
	(0.077)	(0.076)	(0.076)	(0.077)
Observations	287	287	287	287
$\mathbb{R}^2$	0.891	0.888	0.891	0.888
Adjusted R <sup>2</sup>	0.888	0.887	0.888	0.886
Residual Std. Error	1.238 (df = 279)	1.246 (df = 282)	1.239 (df = 279)	1.248 (df = 281)
F Statistic	326.060*** (df = 7; 279)	561.018*** (df = 4; 282)	325.089*** (df = 7; 279)	447.399*** (df = 5; 281)
Note:			Ķ	o<0.1; <b>p&lt;0.05;</b> p<0.01

[1] "Selected Factors: EG, Mkt-RF, RMW, SMB"

# **Stepwise Selection - High Return**

The table below contains the following regression information for the following stepwise selections:

- 1. Backward AIC
- 2. Backward BIC
- 3. Forward AIC
- 4. Forward BIC

[1] "R^2 for Full Model: 0.88" [1] "Adjusted R^2 for Full Model: 0.875"

		Dependen	nt variable:	
		R3-	-RF	
	(1)	(2)	(3)	(4)
EG	-0.349***	-0.349***	-0.515***	-0.515***
	(0.096)	(0.096)	(0.101)	(0.101)
LIQ	0.099***	0.099***		
	(0.038)	(0.038)		
CMA			0.318***	0.318***
			(0.082)	(0.082)
Mkt-RF	0.898***	0.898***	0.785***	0.785***
	(0.033)	(0.033)	(0.034)	(0.034)
RMW	0.323***	0.323***		
	(0.090)	(0.090)		
ROE	0.236**	0.236**		
	(0.094)	(0.094)		
ME			-0.027	-0.027
			(0.188)	(0.188)
PC4			-0.840***	-0.840***
			(0.123)	(0.123)
SMB	0.504***	0.504***	0.585***	0.585***
	(0.061)	(0.061)	(0.188)	(0.188)
Constant	0.430***	0.430***	0.594***	0.594***
	(0.083)	(0.083)	(0.084)	(0.084)
Observations	287	287	287	287
$R^2$	0.879	0.879	0.879	0.879
Adjusted R <sup>2</sup>	0.877	0.877	0.877	0.877
Residual Std. Error (df = 280)	1.347	1.347	1.347	1.347
F Statistic (df = 6; 280)	340.484***	340.484***	340.379***	340.379***
Note:			p<0.1; <b>p&lt;0</b> .	<b>05;</b> p<0.01

[1] "Selected Factors: EG, LIQ, Mkt-RF, RMW, ROE, SMB"

# **Final Factors**

**Note**: I simply took the union of the selected factors for each return level. While this works fine for *Recovery* and *Expansion*, we will probably have to handpick the factors for *Downturn* and *Depression*.

#### Recovery

	Dependent variable:		
	R1-RF	R2-RF	R3-RF
	(1)	(2)	(3)
CMA	0.238***	0.221***	0.204***
	(0.054)	(0.061)	(0.074)
LIQ	-0.156***	-0.131***	-0.103***
	(0.023)	(0.026)	(0.032)
ME	0.140***	0.154***	0.176***
	(0.040)	(0.045)	(0.055)
Mkt-RF	0.571***	0.593***	0.624***
	(0.027)	(0.031)	(0.038)
Constant	0.222***	0.467***	0.687***
	(0.050)	(0.057)	(0.069)
Observations	175	175	175
$R^2$	0.762	0.742	0.700
Adjusted R <sup>2</sup>	0.757	0.736	0.693
Residual Std. Error (df = 170)	0.634	0.716	0.872
F Statistic (df = 4; 170)	136.193***	122.546**	* 99.101***
Note:	p<	:0.1; <b>p&lt;0.0</b>	<b>5;</b> p<0.01

### **Expansion**

	Dep	Dependent variable:			
	R1–RF	R1-RF R2-RF R3-F			
	(1)	(2)	(3)		
HML	0.313***	0.314***	0.319***		
	(0.027)	(0.030)	(0.036)		
MOM	-0.094***	-0.049**	-0.011		
	(0.020)	(0.022)	(0.026)		
Mkt-RF	0.818***	0.856***	0.906***		
	(0.020)	(0.022)	(0.026)		

RMW	0.317***	0.341***	0.353***
	(0.035)	(0.038)	(0.046)
SMB	0.362***	0.385***	0.413***
	(0.029)	(0.032)	(0.039)
LIQ	-0.035*	0.051**	0.160***
	(0.019)	(0.021)	(0.025)
EG	0.077*	0.131**	0.191***
	(0.046)	(0.051)	(0.061)
Constant	0.054*	0.192***	0.314***
	(0.032)	(0.035)	(0.042)
Observations	598	598	598
$R^2$	0.780	0.778	0.762
Adjusted R <sup>2</sup>	0.778	0.776	0.759
Residual Std. Error (df = 590)	0.719	0.798	0.956
F Statistic (df = 7; 590)	299.121**`	*296.200**	* 270.080***
Note:		n-01: <b>n-0</b>	<b>05</b> · n<0.01

Note:

*p<0.1; p<0.05; p<0.01* 

#### **Downturn**

	Dependent variable:		
	R1–RF	R2-RF	R3-RF
	(1)	(2)	(3)
CRD	-0.086***	-0.051*	-0.004
	(0.027)	(0.029)	(0.033)
HML	-0.119***	-0.071	-0.034
	(0.044)	(0.048)	(0.054)
IA	0.170*	0.191**	0.253**
	(0.088)	(0.095)	(0.107)
LIQ	-0.064**	-0.029	0.026
	(0.029)	(0.031)	(0.035)
Mkt-RF	0.659***	0.759***	0.872***
	(0.036)	(0.039)	(0.044)
RMW	0.231***	0.311***	0.324***
	(0.074)	(0.080)	(0.090)
SMB	0.155***	0.087*	0.059
	(0.044)	(0.048)	(0.054)
CMA	0.093	0.036	-0.116
	(0.092)	(0.100)	(0.112)

PC5	-0.014	0.162	0.292**
	(0.101)	(0.109)	(0.123)
PC3	0.053	-0.020	-0.109**
	(0.043)	(0.047)	(0.053)
Constant	0.096***	0.220***	0.347***
	(0.034)	(0.037)	(0.042)
Observations	668	668	668
$R^2$	0.723	0.720	0.737
Adjusted R <sup>2</sup>	0.718	0.716	0.733
Residual Std. Error (df = 657)	0.813	0.884	0.992
F Statistic (df = 10; 657)	171.206**	* 168.830***	184.092***
Note:		p<0.1; <b>p&lt;0.</b>	<b>05;</b> p<0.01

# Depression

	Dependent variable:		
	R1-RF	R2-RF	R3-RF
	(1)	(2)	(3)
CMA	0.267***	0.125	0.012
	(0.076)	(0.082)	(0.089)
EG	-0.265***	-0.308***	-0.351***
	(0.082)	(0.089)	(0.097)
MOM	-0.088***	-0.036	-0.013
	(0.034)	(0.036)	(0.039)
Mkt-RF	0.914***	0.899***	0.898***
	(0.028)	(0.030)	(0.033)
RMW	0.259***	0.304***	0.316***
	(0.086)	(0.092)	(0.101)
SMB	0.450***	0.475***	0.503***
	(0.053)	(0.057)	(0.062)
LIQ	0.041	0.054	0.096**
	(0.036)	(0.039)	(0.043)
ROE	0.152*	0.192*	0.253**
	(0.091)	(0.098)	(0.107)
Constant	0.139*	0.298***	0.429***
	(0.071)	(0.077)	(0.084)
Observations	287	287	287
$R^2$	0.908	0.891	0.880

Adjusted R <sup>2</sup>	0.905	0.888	0.876
Residual Std. Error (df = 278)	1.152	1.238	1.351
F Statistic (df = 8; 278)	341.601**	* 285.390**	* 253.669***
Note:		p<0.1; <b>p&lt;0</b>	<b>0.05;</b> p<0.01