

Types and strings

PATRICK D. ELLIOTT

APRIL 13, 2023

Types and strings

Types in Haskell are a way of *categorizing values*; they provide a syntactic restriction on how complex expressions are built.

You might be familiar with types if you've ever taken a semantics course before.

- *is happy*: $\langle e, t \rangle$
- *Henning*: e

- Haskell has a more complex and powerful type-system than the one you might be used to from formal semantics.
 - Formal semantics typically uses the *simply-typed lambda calculus* as a basis.
 - Haskell is based on System F, i.e., the *polymorphic lambda calculus*, which allows for universal quantification over types.
 - Various *language extensions* exist to make Haskell's type system even more powerful (dependent types, linear types, etc).
 - In this course, we won't go much beyond simple types and some basic polymorphism.

You can find out the type of any haskell expression quite easily using the `:type` command in GHCi:

```
ghci> :t "hello haskell!"  
"hello haskell!" :: String  
ghci> :t 'a'  
'a' :: Char
```

- Note that single characters are enclosed in single quotes.
- The double colon `::` is interpreted as *has the type*.

Type annotations

We explicitly annotate expressions with their type using `::`.

```
ghci> :t ("hello haskell!" :: String)
"hello haskell!" :: String
```

If we annotate an expression with the wrong type, we'll get an error:

```
ghci> :t ("hello haskell!" :: Char)
<interactive>:1:2: error:
    • Couldn't match type '[Char]' with 'Char'
      Expected: Char
      Actual: String
```

String is actually a name for a *complex type*, `[Char]`.

That is to say, strings in haskell are actually just *lists of characters*.

In general, for any type `a`, the type `[a]` is the type of a list of things of type `a`.

Printing strings

We can print strings to the standard output in GHCi using the `putStrLn` or `putStr` functions.

```
ghci> putStrLn "hello haskell!"  
hello haskell!
```

Examine the type of `putStrLn`. You'll notice something quite interesting.

```
ghci> :t putStrLn  
putStrLn :: String -> IO ()
```

In Haskell, we use arrow notation for function types (we'll come back to this later). `IO ()` is a special type to indicate that the program has some effect beyond evaluation of functions and arguments.

Printing strings from a source file

```
-- print1.hs

module Print1 where

main :: IO ()
main = putStrLn "hello world!"
```

If we load `print1.hs` from GHCi and execute `main`, *hello world!* will be printed to the standard output.

The `main` function

In Haskell `main` is the default action when building an executable, or running it in GHCi, and it must always be of type `IO ()`.

Input/output is much more complicated in Haskell than in most other programming languages, since it involves exploiting Haskell's type system to reason about *side effects*. This will be a topic for later in the semester.

There are two functions for concatenating strings in the haskell prelude:

```
(++) :: [a] -> [a] -> [a]  
concat :: [[a]] -> [a]
```

- `++` is an infix operator, whereas `concat` is just an ordinary function.
- Note that `a` in the type signature is a *type variable*. Free variables in type signatures are implicitly universally quantified in Haskell.
- This means that both `++` and `concat` are *polymorphic* functions; they can be used to combine lists more generally.

In formal semantics, functional types are often written using angled-brackets (e.g., $\langle e, t \rangle$), following the convention used by (Heim, Irene and Kratzer, Angelika, 1998).

Haskell uses arrow notation, which is more commonly found in the computer science/programming language literature, although some semantics texts use arrow notation (Carpenter, Bob, 1998).

Arrow notation in Haskell is *right associative*:

$$\cdot \quad a \rightarrow b \rightarrow c \iff a \rightarrow (b \rightarrow c)$$

Let's look again at the type for list concatenation:

```
(++) :: [a] -> [a] -> [a]
```

- `(->)` is a type *constructor*. It takes two types **a**, **b** and returns the type of a function from *as* to *bs*.
- One important feature of haskell is the possibility of defining arbitrary constructors; `([.])` takes a type **a** and returns the type of a list of *as*.
- Remember, free type variables are implicitly universally quantified, which means that list concatenation is defined for something of type `[a]`, where **a** can be *any type*.

Strings as lists of chars

```
"hello haskell!"
```

```
['h','e','l','l','o',' ','h','a','s','k','e','l','l','!']
```

- Strings surrounded by double quotes are really just *syntactic sugar* for lists of characters.
- Syntactic sugar is just a notational convention built into the language that makes our lives as programmers easier.
- Lists are actually also syntactic sugar! We'll learn what lists really are in a bit.

What do you think the following evaluates to?

```
[1,2,3] ++ [4,5,6]
```

What happens if we try to evaluate the following:

```
"hello" ++ [4,5,6]
```

More list manipulation

```
ghci> head "Henning"
'H'
ghci> tail "Henning"
"enning"
ghci> take 0 "Henning"
""
ghci> take 3 "Henning"
"Hen"
ghci> drop 3 "Henning"
"ning"
ghci> "Henning" !! 2
'n'
```


What happens when you run the following in GHCi:

```
ghci> "yo" !! 2
```

Let's examine the type of `!!`; as expected, its a function from a list of *as*, to an integer, to an *a*.

```
(!!) :: [a] -> Int -> a
```

Note however, that this isn't a *total* function; there are some lists and integers for which this function will be undefined.

Partial functions in haskell are considered *unsafe*, because the type system doesn't prevent us from providing an illicit value as an argument to the function.

The final list manipulation function we'll look at is an important one: `cons`.

```
ghci> 'h' : []  
[h]  
ghci> 'h' : "enning"  
"henning"
```

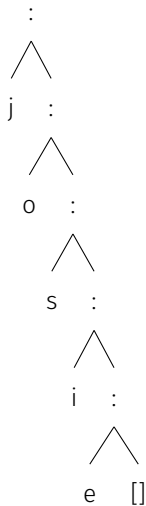
In haskell, lists are built up by successive application of `cons`:

```
'h' : ('e' : ('n' : ('n' : ('i' : ('n' : ('g' : [])))))
```

Since `:` is right associative we can drop the parentheses.

Lists in haskell are therefore *singly-linked lists of characters*.

Singly-linked lists



- For most industrial applications, singly-linked lists of chars would be a terrible choice.
- On the other hand, this means that strings “come for free” on the basis of chars and extremely general list manipulation functions.
- For anything we do in this class, performance won’t be an issue. For serious work with strings, the standard is the Haskell **text** library.

Prolegomenon to types

- In preparation for next week's class with type.
- Types are syntactic categories used to restrict what counts as a valid expression.
- Basic ingredients:
 - A set of primitive types.
 - A recursive rule for constructing complex (i.e., functional) types.
 - Rules for computing the type of a complex expression from the types of its parts.

- Let's keep things simple, and start with just two primitive types:

Typ := {Int, Bool}

- We'll assume that integers are possible values and have the type **Int**:

73 :: Int

- We'll also assume two primitive values with the type **Bool**:

true :: Bool, **false** :: Bool

We'll now state a recursive rule for complex (functional) types, using the Haskell convention for types.

- If $a \in \mathbf{Typ}$, then a is a type.
- If a is a type, and b is a type, then $a \rightarrow b$ is a type.
- Nothing else is a type.

This means that we have many complex types like the following:

- $(\mathbf{Bool} \rightarrow \mathbf{Bool}) \rightarrow \mathbf{Int}$
- $\mathbf{Int} \rightarrow \mathbf{Int}$

- We can assign some useful operations their types:

$(+) :: \text{Int} \rightarrow \text{Int} \rightarrow \text{Int}$

$(-) :: \text{Int} \rightarrow \text{Int} \rightarrow \text{Int}$

factorial $:: \text{Int} \rightarrow \text{Int}$

odd $:: \text{Int} \rightarrow \text{Bool}$

even $:: \text{Int} \rightarrow \text{Bool}$

and $:: \text{Bool} \rightarrow \text{Bool} \rightarrow \text{Bool}$

Functional applications: Let $\beta :: a \rightarrow b$, $\alpha :: a$ be an expression of the SLTC. $\beta(\alpha)$ is an expression of type b .

Abstractions: Let $\beta :: b$ be an expression of the SLTC, and v a variable of type a . $\lambda v. \beta$ is an expression of type $a \rightarrow b$.

Can you infer the types of the following expressions? Go step by step.

$\text{and}(\text{odd}(4))(t)$

$\lambda x.\text{odd}(\text{factorial}(x))$

$\lambda f.f(\lambda x.(+)(x)(2))$

Often, you can *infer* the type of an expression without specifying the type of all of its sub-parts.

When you try to compile a haskell source file, or evaluate an expression in GHCi, the compiler will attempt to check that it is well-typed, by inferring the types of any expressions that don't have an explicit type provided.

Since haskell's type system is more expressive than we have here, the type-inference algorithm is quite complicated (the compiler is based on an algorithm called *Hindley-Milner*).

In a first order type-system, we can only state typed identity functions.
What is the type of *the* identity function?

$$\lambda x.x :: ?$$

Consider the following functions:

$$\mathbf{not} :: \text{Bool} \rightarrow \text{Bool}$$
$$\mathbf{not}' :: \lambda f.\lambda x.\mathbf{not}(f(x))$$
$$\mathbf{not}'' :: \lambda r.\lambda x.\lambda y.\mathbf{not}(r(x)(y))$$

- What are the types of \mathbf{not}' and \mathbf{not}'' ?
- Is there a way of expressing all three functions as a single-operation? If not, why not?

Remember the expression ω :

$$(\lambda x.xx)(\lambda x.xx)$$

- Try to give it a concrete type.
- This problem is related to the lack of Turing completeness of the SLTC.
- On the other hand, because the SLTC is relatively constrained it has some extremely nice logical properties:
 - The SLTC is a sound and complete logic.
 - *Type-checking* (checking whether an expression is well-typed), and *type inference* are **decidable**.

- Next time we'll learn much more about Haskell's type system.
- Haskell's type system is more expressive than the SLTC - we can do everything we can in the SLTC and more.
- We'll learn about *polymorphic functions* corresponding *polymorphic datatypes*; a first step in understanding the kinds of powerful abstractions that Haskell provides to reason about computation.

Fin

Carpenter, Bob (1998). *Type-Logical Semantics*, MIT Press.

Heim, Irene and Kratzer, Angelika (1998). *Semantics in Generative Grammar*, Blackwell.