M

Hello Haskell!

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Preliminaries

Homework

- Read chapter 2 of *Haskell programming from first principles*, covering basic Haskell syntax.
- To the end-of-chapter exercises.

- The lambda calculus is a *formal system* (i.e., a logic) for reasoning about *functions*.
- In the lambda calculus, computation is modelled as a form of simplification, using the following rules:
    - β-reduction. $(\lambda x.f(x))(y) \Rightarrow f(y)$
    - α-conversion. $\lambda x.x \Rightarrow \lambda y.y$
    - η-reduction. $\lambda x.f(x) \Rightarrow f$
- Haskell can be thought of as a kind of lambda calculi, where *running a program* amounts to reducing a complex expression until we reach normal form.
- Reduction doesn't always converge on a normal form; sometimes expressions diverge; this corresponds to *non-terminating computations* (imagine, for example, a program implementing a timer that runs indefinitely).

$$(\lambda xyz.xz(yz))(\lambda x.z)(\lambda x.a)$$

1. Curry arguments: $(\lambda x.\lambda y.\lambda z.xz(yz))(\lambda x.z)(\lambda x.a)$
2. α-conversion: $(\lambda x.\lambda y.\lambda z_1.xz_1(yz_1))(\lambda x.z)(\lambda x.a)$
3. β-reduce: $(\lambda y.\lambda z_1.(\lambda x.z)z_1(yz_1))(\lambda x.a)$
4. β-reduce: $\lambda z_1.(\lambda x.z)z_1((\lambda x.a)z_1)$
5. β-reduce: $\lambda z_1.(\lambda x.z)z_1 a$
6. β-reduce: $\lambda z_1.za$
7. Normal form!

Getting started with Haskell

- Everything you write in Haskell is either an *expression* or a *declaration*.
    - Expressions can be values, functions, functions applied to values, etc.
    - Declarations are bindings that allow us to name complex expressions.

Here are some examples of expressions in Haskell:

```haskell
1
1 + 1
"Icarus"
```

The REPL

- The GHCi REPL stands for the *Glasgow Haskell Compiler interactive Read-Eval-Print-Loop*.
- It allows us to evaluation Haskell expressions directly without the need to save the program in a source file.
- There are a few different ways to get a GHCi instance:
  - In the browser: `https://tryhaskell.org/`
  - By installing GHC and running `ghci` in the terminal.

REPL cont.

- When we type an expression into the REPL it automatically evaluates it for us.
- The following expressions are already in normal form, so they simply evaluate to themselves.

```
ghci> 1
1
ghci> "Icarus"
"Icarus"
```

A complication

- In reality, it's a bit more complex than that.
- An expression like 1 evaluates to an *integer*, but technically speaking integers aren't the kind of things that can be printed to an output, rather their *string representations*.
- Under the hood, GHCi exploits Haskell's type system to determine whether an expression is *showable*; what we see is given by the function associated with the showable type class.
    - We'll learn more about what this means later in the semester.

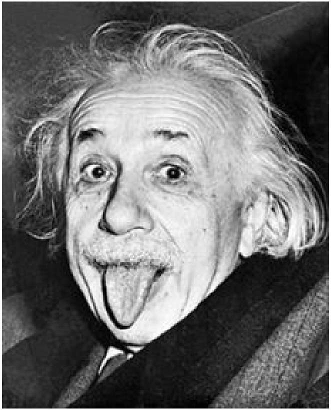
Evaluating arithmetic expressions

- GHCi can be used as a basic calculator by inputting arithmetic expressions.
- Complex expressions are evaluated until we reach normal form:

```
ghci> ((1 + 2) * 3) + 100
109
```

- Note that GHCi doesn't show us any of the intermediate steps.
- N.b. expressions that can be reduced are called redexes (i.e., *reducible expressions*).

- *Functions* in haskell are particular kinds of expressions, which play a very important role.
- Just like mathematical functions, they map inputs to outputs, in a determinate fashion.
- A Haskell function always evaluates to the same result when given the same argument values.
  - This property is known as *referential transparency*, and makes Haskell programs extremely straightforward to reason about.
  - For those of you with some experience programming in an imperative language like C, this is quite a departure! In imperative languages, evaluating a line of code might affect the state in a way which changes subsequent evaluations.



"Insanity is doing the same thing over and over and expecting different results." (Albert Einstein)

There are a number of different ways of declaring functions in haskell. Here is the simplest way:

```
ghci> triple x = x * 3
ghci> triple 4
12
```

Function names always start with lower case letters in haskell. It's good practice to use descriptive function names, which conventionally use camel case, e.g.:

```
ghci> multiplyByThree x = x * 3
ghci> multiplyByThree 4
12
```

- Note that the equals sign `=` indicates that this is a *declaration* rather than an expression.
- Note that declarations are much like abstractions, in the sense that the variable(s) to the left of the `=` bind the corresponding variable(s) to the right.
- In fact it's also possible to define functions directly as abstractions, using the following syntax:

```
ghci> triple = \x -> x * 3
ghci> triple 4
12
ghci> (\x -> x * 3) 4
12
```

- Remember when I said that printing values in GHCi is more complicated than it first appears?
- Try evaluating an abstraction, e.g.,

```
ghci> (\x -> x * 3)
```

How would we declare a function that has one parameter and words for al the following expressions?

```
pi * (5 * 5)
pi * (10 * 10)
pi * (2 * 2)
pi * (4 * 4)
```

Note that `pi` is an expression that is given by the Haskell `Prelude`. The prelude is a module (i.e., a set of declarations) that is implicitly imported by default.

```
ghci> circleArea radius = pi * (radius * radius)
ghci> circleArea 5
78.53981633974483
```

Note that as well descriptive function names, we can also use descriptive *variable* names; there's no reason (aside from brevity) that we have to use single letters as variable names.

As you've probably gathered, the syntax for *function application* in Haskell just involves whitespace, i.e.., `f x` means $f(x)$.

The arithmetic operators like `+` are *infix operators*; they can be used as ordinary functions by enclosing them in paretheses:

```
ghci> 200 + 300
500
ghci> (+) 200 300
500
ghci> ((+) 200) 300
500
```