# Homework Signal 1 (for assignment)

## Week 1

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Collaborators. ChatGPT (for LATEX styling and grammar checking)

# 1 Representing Signals

**Problem 1.** Sketch the following signals

#### TO SUBMIT

```
a) x(t) = \sin(\frac{\pi}{4}t + 20^{\circ})
```

**Solution.** Using Python and Matplotlib to plot the signal  $x(t) = \sin\left(\frac{\pi}{4}t + 20^{\circ}\right)$ :

```
import matplotlib.pyplot as plt
import numpy as np

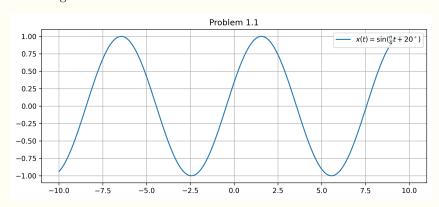
fig = plt.figure()

t = np.arange(-10, 10, 0.01)
x = np.sin(np.pi/4 * t + np.pi/9)

plt.title("Problem 1.1")
plt.plot(t, x, label=r"$x(t) = \sin(\frac{\pi}{4}t + 20^\circ)$")

plt.legend(loc="upper right")
plt.grid(True)
plt.show()
```

The plot of the signal is shown below:



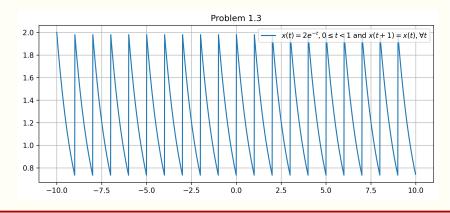
## TO SUBMIT

```
c) x(t) = 2e^{-t}, 0 \le t < 1 \text{ and } x(t+1) = x(t), \forall t
```

**Solution.** Using Python and Matplotlib to plot the piecewise signal  $x(t) = 2e^{-t}, 0 \le t < 1$  and  $x(t+1) = x(t), \forall t$ :

```
import matplotlib.pyplot as plt
2 import numpy as np
  def x3(t):
      if t >= 1:
         return x3(t - 1)
      if t < 0:
         return x3(t + 1)
     return 2 * (np.e ** (-t))
9
fig = plt.figure(figsize=(10, 4))
12
t = np.arange(-10, 10, 0.01)
x3_vectorize = np.vectorize(x3)
x = x3_{vectorize}(t)
plt.title("Problem 1.3")
plt.plot(t, x, label=r"x(t) = 2e^{-t}, 0 \leq t < 1 \
     text{ and } x(t + 1) = x(t), \forall t$")
plt.legend(loc="upper right")
plt.grid(True)
plt.show()
```

The plot of the signal is shown below:



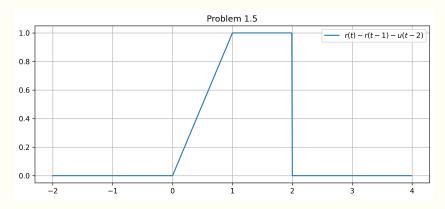
#### TO SUBMIT

```
e) x(t) = r(t) - r(t-1) - u(t-2)
```

**Solution.** Using Python and Matplotlib to plot the piecewise signal x(t) = r(t) - r(t - 1) - u(t - 2):

```
import matplotlib.pyplot as plt
  import numpy as np
  def unit_signal(t):
      return 1.0 if t \ge 0 else 0.0
  def ramp_signal(t):
      return t * unit_signal(t)
unit_signal_vectorize = np.vectorize(unit_signal)
ramp_signal_vectorize = np.vectorize(ramp_signal)
12
fig = plt.figure(figsize=(10, 4))
14
t = np.arange(-2, 4, 0.01)
r1 = ramp_signal_vectorize(t)
r2 = ramp_signal_vectorize(t - 1)
u1 = unit_signal_vectorize(t - 2)
20
  x = r1 - r2 - u1
21
22
plt.title("Problem 1.5")
plt.plot(t, x, label=r"r(t) - r(t-1) - u(t-2)")
plt.legend(loc="upper right")
plt.grid(True)
plt.show()
```

The plot of the signal is shown below:



**Problem 2.** For the discrete time signal x[n] shown in Figure below, sketch each of the following

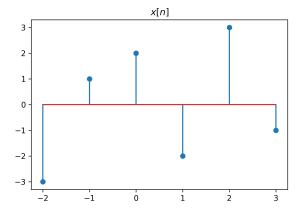
```
import matplotlib.pyplot as plt
import numpy as np

fig = plt.figure(figsize=(6, 4))

t = np.arange(-2, 4)
x_t = np.array([-3, 1, 2, -2, 3, -1])

plt.stem(t, x_t)
plt.title(r"$x[n]$")
plt.show()
```

With the resulting plot shown below:



**Solution.** By using Python, we can create a function to transform the signal based on the given transformation function:

#### TO SUBMIT

## a) x[2-n]

**Solution.** Using Python and Matplotlib to plot the signal x[2-n]:

```
import matplotlib.pyplot as plt
import numpy as np

fig = plt.figure(figsize=(6, 4))

t = np.arange(-2, 4)

x_t = np.array([-3, 1, 2, -2, 3, -1])

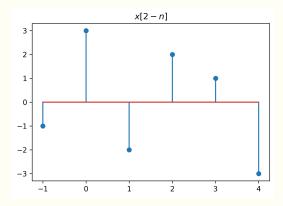
x_t, t = transform_signal(x_t, t, lambda x: 2 - x)

plt.stem(t, x_t)

plt.title(r"$x[2 - n]$")

plt.show()
```

With the resulting plot shown below:



## TO SUBMIT

# c) $x \left[ \frac{2}{3}n + 1 \right]$

**Solution.** Using Python and Matplotlib to plot the signal  $x[\frac{2}{3}n+1]$ :

```
import matplotlib.pyplot as plt
import numpy as np

fig = plt.figure(figsize=(6, 4))

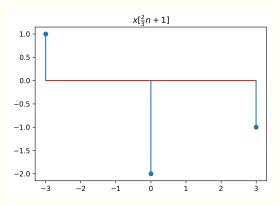
t = np.arange(-2, 4)

x_t = np.array([-3, 1, 2, -2, 3, -1])

x_t, t = transform_signal(x_t, t, lambda x: (x - 1) * 3 / 2)

plt.stem(t, x_t)
plt.title(r"$x[\frac{2}{3}n + 1]$")
plt.show()
```

With the resulting plot shown below:



# TO SUBMIT

**e)**  $x[n^3]$ 

**Solution.** Using Python and Matplotlib to plot the signal  $x[n^3]$ :

```
import matplotlib.pyplot as plt
import numpy as np

fig = plt.figure(figsize=(6, 4))

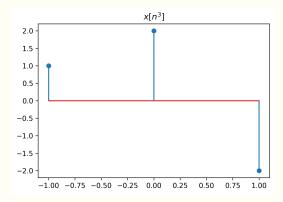
t = np.arange(-2, 4)

x_t = np.array([-3, 1, 2, -2, 3, -1])

x_t, t = transform_signal(x_t, t, lambda x: np.cbrt(x))

plt.stem(t, x_t)
plt.stem(t, x_t)
plt.title(r"$x[n^3]$")
plt.show()
```

With the resulting plot shown below:



**Problem 9.** Evaluate the following integrals

#### TO SUBMIT

a) 
$$\int_{-\infty}^{\infty} \left(\frac{2}{3}t - \frac{3}{2}\right) \delta(t-1) dt$$

Solution. Using the sifting property of the delta function, we have:

$$\int_{-\infty}^{\infty} \left(\frac{2}{3}t - \frac{3}{2}\right) \delta(t - 1) dt = \left(\frac{2}{3}(1) - \frac{3}{2}\right)$$
$$= \frac{2}{3} - \frac{3}{2}$$
$$\int_{-\infty}^{\infty} \left(\frac{2}{3}t - \frac{3}{2}\right) \delta(t - 1) dt = \boxed{-\frac{5}{6}}$$

## TO SUBMIT

c) 
$$\int_{-3}^{-2} \left[ e^{(-t+1)} + \sin\left(\frac{2\pi t}{3}\right) \right] \delta\left(t - \frac{3}{2}\right) dt$$

**Solution.** Because the argument of the delta function  $t - \frac{3}{2}$  has its root at  $t = \frac{3}{2}$ , which is outside the integration limits of -3 to -2, the integral evaluates to zero:

$$\int_{-3}^{-2} \left[ e^{(-t+1)} + \sin\left(\frac{2\pi t}{3}\right) \right] \delta\left(t - \frac{3}{2}\right) dt = \boxed{0}$$