

clustering

January 14, 2026

1 Homework 1 | Clustering Part

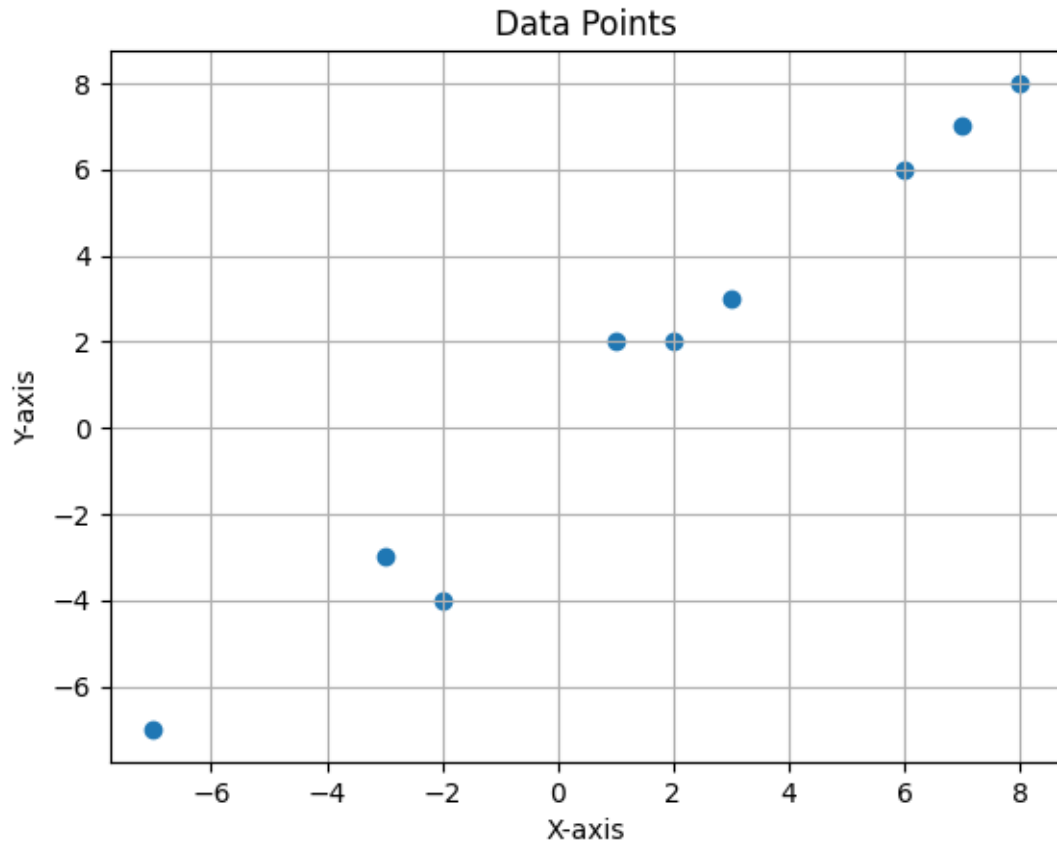
1.1 Import Libraries

```
[1]: import numpy as np
import matplotlib.pyplot as plt
```

1.2 Initialization

```
[2]: # define list of points
points = np.array([
    [1, 2],
    [3, 3],
    [2, 2],
    [8, 8],
    [6, 6],
    [7, 7],
    [-3, -3],
    [-2, -4],
    [-7, -7],
])

# plot points
plt.scatter(points[:, 0], points[:, 1])
plt.title("Data Points")
plt.xlabel("X-axis")
plt.ylabel("Y-axis")
plt.grid()
plt.show()
```



```
[3]: # define functions
def assign_clusters(points, centroids):
    clusters = []
    for point in points:
        distances = np.linalg.norm(point - centroids, axis=1)
        cluster = np.argmin(distances)
        clusters.append(cluster)
    return np.array(clusters)

def update_centroids(points, centroids, clusters, k):
    new_centroids = []
    for i in range(k):
        cluster_points = points[clusters == i]
        if len(cluster_points) > 0:
            new_centroid = np.mean(cluster_points, axis=0)
        else:
            new_centroid = centroids[i]
        new_centroids.append(new_centroid)
    return np.array(new_centroids)
```

```

def plot_centroids_movement(
    points,
    clusters,
    iteration,
    new_centroids,
    old_centroids=None,
    show_fig=True,
    save_fig=True,
    save_path="../images/centroid_movement"
):
    plt.figure()
    plt.scatter(points[:, 0], points[:, 1], c=clusters, cmap="viridis",
        ↪marker="o")

    if old_centroids is not None:
        plt.scatter(old_centroids[:, 0], old_centroids[:, 1], c="blue",
            ↪marker="o", s=50, label="Old Centroids")

        for old, new in zip(old_centroids, new_centroids):
            plt.plot([old[0], new[0]], [old[1], new[1]], color="gray",
                ↪linestyle="--")

    plt.scatter(new_centroids[:, 0], new_centroids[:, 1], c="red", marker="X",
        ↪s=50, label="New Centroids")
    plt.title(f"Centroid Movement - Iteration {iteration}")
    plt.xlabel("X-axis")
    plt.ylabel("Y-axis")
    plt.legend()

    if save_fig:
        plt.savefig(save_path + f"_iter_{iteration}.png")

    if show_fig:
        plt.show()

def run_kmeans(
    points,
    initial_centroids,
    max_iters=10,
    show_fig=True,
    save_fig=True,
    save_path="../images/centroid_movement"
):
    centroids = initial_centroids

```

```

k = len(centroids)

plot_centroids_movement(
    points,
    assign_clusters(points, centroids),
    0,
    new_centroids=centroids,
    show_fig=show_fig,
    save_fig=save_fig,
    save_path=save_path
)
print(f"Initial Centroids: \n{centroids}")

for i in range(max_iters):
    clusters = assign_clusters(points, centroids)
    print(f"Iteration {i+1}: Cluster assignments \n{clusters}")

    new_centroids = update_centroids(points, centroids, clusters, k)
    plot_centroids_movement(
        points,
        clusters,
        i + 1,
        new_centroids=new_centroids,
        old_centroids=centroids,
        show_fig=show_fig,
        save_fig=save_fig,
        save_path=save_path
    )
    centroids = new_centroids

    print(f"Iteration {i+1}: Centroids updated to \n{centroids}\n\n")

    if np.all(centroids == new_centroids):
        plot_centroids_movement(
            points,
            clusters,
            i + 2,
            new_centroids=new_centroids,
            show_fig=show_fig,
            save_fig=save_fig,
            save_path=save_path
        )
        break

final_clusters = assign_clusters(points, new_centroids)
print(f"Final Cluster assignments \n{final_clusters}")
print(f"Final Centroids: \n{new_centroids}")

```

```
return new_centroids, final_clusters
```

1.3 T5.

```
[4]: # define starting centroids
centroids = np.array([
    [3, 3],
    [2, 2],
    [-3, -3],
])

# k-means algorithm
final_centroids, final_clusters = run_kmeans(
    points, centroids, max_iters=5, show_fig=False, save_path="../images/
    ↳centroid_movement_T5"
)
```

Initial Centroids:

```
[[ 3  3]
 [ 2  2]
 [-3 -3]]
```

Iteration 1: Cluster assignments

```
[1 0 1 0 0 0 2 2 2]
```

Iteration 1: Centroids updated to

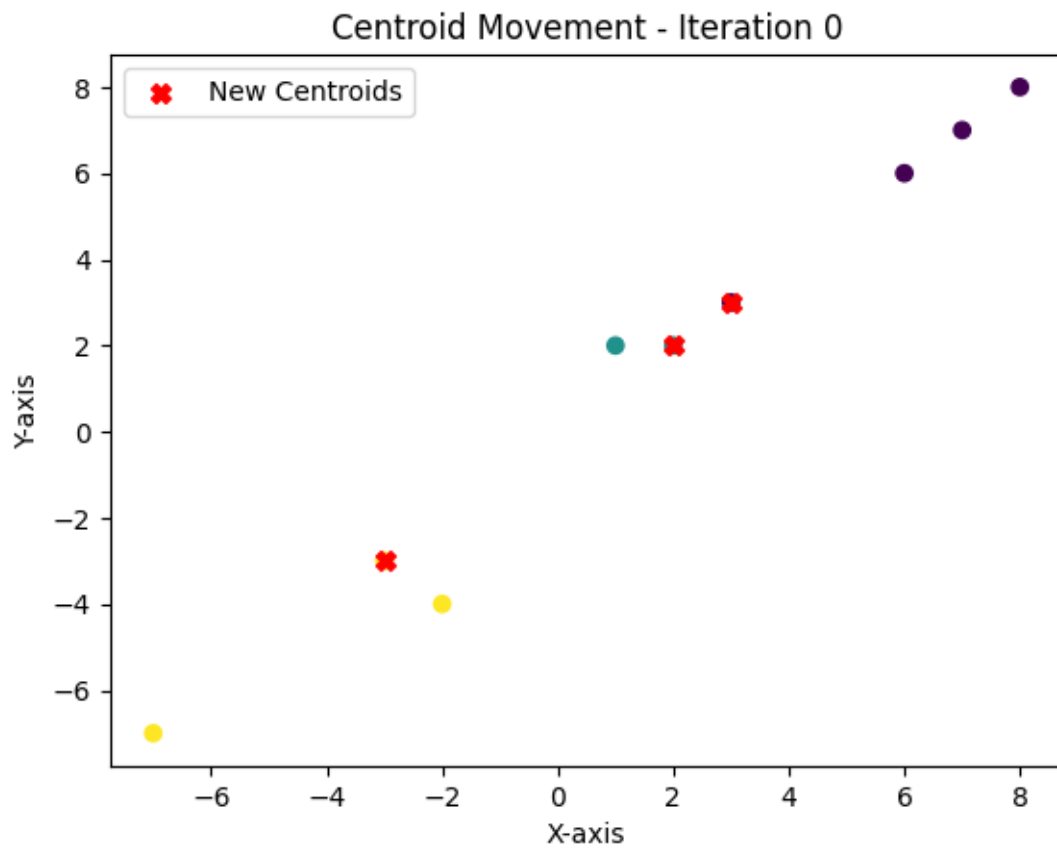
```
[[ 6.          6.          ]
 [ 1.5         2.          ]
 [-4.         -4.66666667]]
```

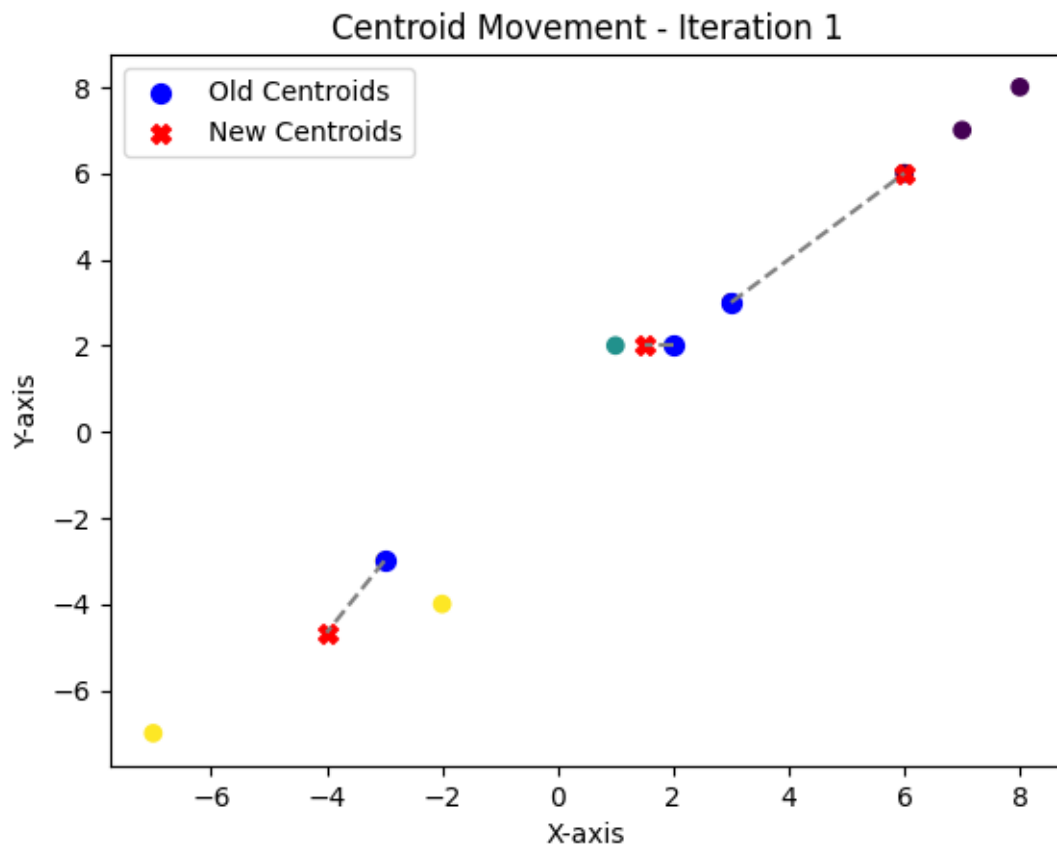
Final Cluster assignments

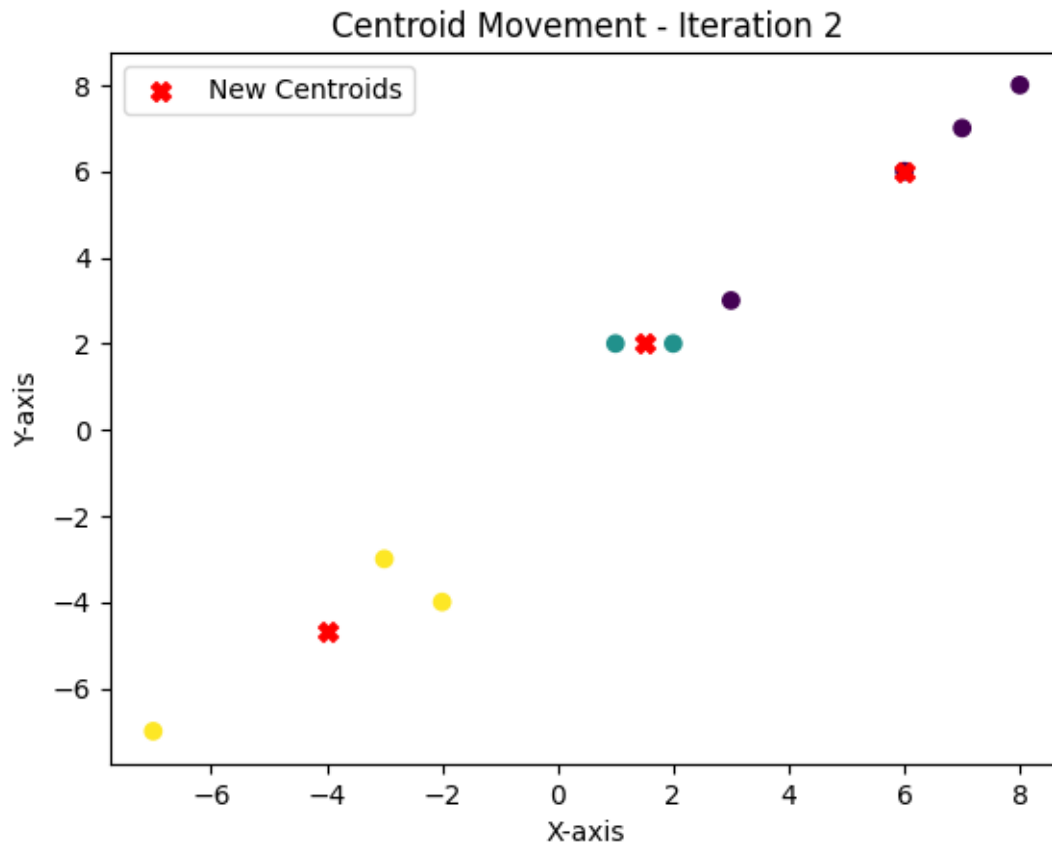
```
[1 1 1 0 0 0 2 2 2]
```

Final Centroids:

```
[[ 6.          6.          ]
 [ 1.5         2.          ]
 [-4.         -4.66666667]]
```







1.4 T6.

```
[5]: # define starting centroids
centroids = np.array([
    [-3, -3],
    [2, 2],
    [-7, -7],
])

# k-means algorithm
final_centroids, final_clusters = run_kmeans(
    points, centroids, max_iters=5, show_fig=False, save_path="../images/
    ↪centroid_movement_T6"
)
```

Initial Centroids:

```
[[ -3  -3]
 [  2   2]
 [- 7  -7]]
```

Iteration 1: Cluster assignments

```
[1 1 1 1 1 1 0 0 2]
```

Iteration 1: Centroids updated to

```
[[ -2.5      -3.5      ]
```

```
 [ 4.5      4.66666667]
```

```
[-7.      -7.      ]]
```

Final Cluster assignments

```
[1 1 1 1 1 1 0 0 2]
```

Final Centroids:

```
[[ -2.5      -3.5      ]
```

```
 [ 4.5      4.66666667]
```

```
[-7.      -7.      ]]
```

