```
& Kalman Filter 1. necursive algorithm
Con optimal recursive
                                                                                                                                                                                                2. Dorton fusion
Consulance Mortalix
                                                                                                                                                                                                                                                                                                                                                                  . b= [ 2x, 2x24 2x28]
             can optimal recursive data processing algorithms)
                                we consider the first term of the constant x \in \mathbb{R}^{n} and x \in \mathbb{
                                                                                                                                                                                                                                                                                                                                                                                      640× 460 465
                                                                                                                                                                                                           State Space
5 + & = + ( =+ =+ +++ == = )
                                                                                                                                                                                                             Observation
                                                                                                                                                                                                                                                                                                                                                                 • a = \begin{bmatrix} x_1 & y_1 & y_2 & y_3 \\ y_2 & y_3 & y_4 & y_3 \end{bmatrix} - \frac{1}{3} \begin{bmatrix} y_1 & y_2 & y_3 & y_4 & y_3 \\ y_2 & y_3 & y_4 & y_3 \end{bmatrix}
                                 = \ \frac{1}{k} \ \frac{k^{-1}}{k-1} \left( \ Z_{i} + Z_{1} + ... + Z_{k^{-1}} \right) + \frac{1}{k} \ \overline{Z}_{k}
                                                                                                                                                                                                 △ Data Fusion
                                =\frac{k-1}{k}|\hat{\chi}_{k-1}|+\frac{1}{k}\mathcal{Z}_{k}
                                                                                                                                                                                                                                                                                                                                                                            P= = ata
                                                                                                                                                                                                     -eg. Z=20 g T=23
                             = \hat{X}_{k-1} = \frac{1}{k} \hat{X}_{k+1} + \frac{1}{k} Z_k
                                                                                                                                                                                                                                                                                                                                                                 A State Space Representation
              \Rightarrow \hat{X}_k = \hat{X}_{k-1} + \left(\frac{1}{k}\right)(\hat{z}_k - \hat{X}_{k-1})
                                                                                                                                                                                                                                                                                                                                                                     A.J.
                                         KI L T # ware important
                                                                                                                                                                                                                                                                                                                                                                                                           m
                                                                                                                                                                                                                                 2 = Z+ K(Z-Z-)
                                                                                                                                                                                                                                                                                                                                                                          · mx + Bx + kx = F = u
                                                                                                                                                                                                                          o then what is K? opened K occurs @ Jig has min.
              △ Au+ I := Kk Kk
                                                                                                                                                                                                                                                                                                                                                                   dyramis x
                                                                                                                                                                                                                                                                                                                                                                                 T= = Vac ( Z + K (Z - Z.))
                    \hat{x}_k = \hat{x}_{k+1} + K_k \left( \mathbf{z}_k - \hat{x}_{k+1} \right)
                                                                                                                                                                                                                                        = V44 ( Z. + KZ2 - KZ1 )
              A induce exter him ausideation
                                                                                                                                                                                                                                      = Va ((1-K)2++ KB)
= Va ((1-K)2+) + Va (KB)
                       K_K = \frac{e_{est_{k+1}}}{e_{est_{k+1}} + e_{man_k}}
                                                                                                                                                                                                                                                                                                                                                                 messpressers = \frac{1}{m}(F-Bx_2-kx_1)
• Z_1 = x = x_1
                                                                                                                                                                                                                                      = (1-K)2 Var (2) + K2 Var (2)
                                                                                                                                                                                                                                    = (1-K)2 T12 + K2 T22
min. whe @ # T2 =0
                      @k @ if est pa >> e ment :

\begin{array}{l}
Z_{1} = \dot{X} = X_{2} \\
\begin{bmatrix} \dot{x}_{1} \\ \dot{x}_{2} \end{bmatrix} = \begin{bmatrix} o & 1 \\ \frac{1}{m} & \frac{B}{m} \end{bmatrix} \begin{bmatrix} X_{1} \\ X_{2} \end{bmatrix} + \begin{bmatrix} o \\ \frac{1}{m} \end{bmatrix} u
\end{array}

                                                      = d T8 = -2 (1-K) 51 + 2K 55 =0
                                                                                                                                                                                                                                                     = -41,+ K41,+ K41, = 0
                                       = ZK

(2) if easter << emark :
                                                                                                                                                                                                                                                   \mathcal{T} = K(\mathcal{T}_1^2 + \mathcal{T}_2^2) = \mathcal{T}_1^2
                                                                                                                                                                                                                                                                                                                                                                                   \dot{X}_t = A X_t + B u_t
                                                                                                                                                                                                                                                   45 \quad K = \frac{-4 t_0 + 4 t_0^2}{4 t_0}
                                                              × K<sub>k</sub> → 0
                                                                                                                                                                                                                                                                                                                                                                              \begin{bmatrix} g_1 \\ g_2 \end{bmatrix} = \begin{bmatrix} \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} g_2 \\ g_2 \end{bmatrix}
                                                     → & = X+-1
                                                                                                                                                                                                                                                                                           \begin{aligned} \sigma_{X}^{2} &= \frac{1}{2} \underbrace{\left[ (i \vec{r} + i t o s)^{2} + (i \vec{r} - i \vec{r} o s)^{2} \underbrace{\left[ \vec{r} - \vec{r} o s \right] \left[ \vec{r} \vec{r} - \vec{r} o s \right]}_{1} \underbrace{\left[ \vec{r} \vec{r} - \vec{r} o s \right] \left[ \vec{r} \vec{r} - \vec{r} o s \right]}_{1} \underbrace{\left[ \vec{r}
                                                                                                                                                                                                            △ Covarione Matrix
                                                                                                                                                                                                                                                                                                                                                                                      Bt = H Xt
                                                                                                                                                                                                                   × 8 8

Height might offer

P1 179 74 33

P2 187 80 31

P3 175 71 28

avg 1803 75 avg
           ▲ KF algorithm
                  ① calculate K_k = \frac{e_{e^+ k^-}}{e_{e^+ k^-}}
② calculate \hat{X}_k = \hat{X}_{k^-} + K_k (\vec{x}_k - \vec{X}_{k^-})
                                                                                                                                                                                                                                                                                                                                                                               XK = A XK-1 + BUK + WE-1
                                                                                                                                                                                                                                                                                                                                                                                  BE = HXK + VK
                   (3) update Ceste = (1- Ke) Ceste-1
                                                                                                                                                                                                                                                                                                                                                                                    How to get Xk
                                                                                                                                                                                      - dra(Pk) = 0-2(HPE)T+2KKHPEHT+2KER=0
        KF morth
         XK = AXx-1 + BUE + WE
                                                                                                                                                                                              .. Kk = PEHT (HPEHT+R)
                                                                                                                                                                                     A Botoni / Restantoni Born Courierce Mornix
. social
           BK = HXE + VE
        △ P(W) ~ (0, @)
                  Q = EI \omega \omega^{T}J
                                                                                                                                                                                                       Xx = AXx + Bux + Wx W~ P(0-@)
                                                                                                                                                                                                                                                                                                              V~ P(0-R)
                                                                                                                                                                                                        ZK = HXF + VK
                                  E[[w_j][w_k]][w_k]
                                                                                                                                                                                        . Privati

$\hat{k} = A \hat{k} \text{ km} + B u_k
                                   = [ E[wit] E[wiw]]
                                              [ ELMM] ELMI]
                                  · VAR = EIX2] - E2IX] FO fow WI
                                                                                                                                                                                                         x= x= + K+ (=++x+)
                                                                                                                    " E[a2] = Van
                               [E[w.w.] E[w.w.]]
                                                                                                                                                                                                                                            KE PEHT (HPEHT+R)"
                                   = \begin{bmatrix} \nabla_{w_1}^{2} & \nabla_{w_1} \nabla_{w_2}^{2} \end{bmatrix}
                                                                                                                                                                                         . P. := E[e'k ei']
                                                                                                                                                                                               \Rightarrow e_k^- = \chi_k - \hat{\chi}_k^-
                                                                                                                                                                                                              = Ax+1 + Ba++Wk - Ax+1-Bak
         - P(V) ~ (0, R)
       △ Paroni
                                                                                                                                                                                                               = A(Xx+ - 2x+) + WE
                                                                                                                        calculered
                                                                                                                                                                                                                = A exa + Wh
                   2= A 2x+1 + Bux 1
                                                                                                                                                                                            .. Pr = E[(Aeri+Wk) (Aeri+Wk)]]
                     ZK = H XK -> Xkmen = H ZK monsurad
                                                                                                                                                                                                             = ETA emeriAT+
                                                                                                                                                                                                                                ACHTOR + WEEK-AT
                  xx = xx + G(H-Zx - xx)
                                                                                                                                                                                                                            + WE WE ]
                             6= Kx H
                                                                                                                                                                                                                = A E[ex-ex] A" + E[W. W.]]
          = & = X=+ K* (Z=-HX=)
                                                                                                                                                                                                               = APMAT+Q
                                                                                                                                                                                         + PK = PK- KKHPK- PKHTKKT + KKHPKTHKKT+KKRKET
    s infor Ke
           get Kk S.T. \hat{X}_k \rightarrow X_k
                                                                                                                                                                                                       = (I - KkH) Pk
             A \quad e_k = x_k - x_k
P(e_k) \sim (0, P)
P = E[e_{ij}] = \begin{bmatrix} \sigma_{e_i}^{1} & \sigma_{e_i} \sigma_{e_i} \\ \sigma_{e_i} \sigma_{e_i} & \sigma_{e_i}^{1} \end{bmatrix}
                                                                                                                                                                                              To some :
                                                                                                                                                                                           priori \hat{X}_{k} = A\hat{X}_{k+1} + Bu_{k} PREDICT

cov. P_{k} = AP_{k+1}A^{T} + Q PREDICT
              · appenie: minimize +2(P) = Te1+ Te2
              . P= E[e e']
                         = E[(xk-2k) (Xk-2k)]
                                                                                                                                                                                            paterori & = & + Kk (Zk-H&k
                                                                                                                                                                                                                         Pk = (I- KxH) Px
                                               \times_k - \hat{x}_k = \times_k - (\hat{x}_k^- + K_k (\delta_k - H \hat{x}_k^-))
                                                                                                                                                                                                                    KK = PEHTCHPEHT+R)-1
                                                                                                                                                                                           Kelman
                                                                   = xx - xx - Kx 8x + Kx H xx
                                                                    = Xx - Xx - Kx H Xx - Kx Vx + Kx H &
                                                                     =(x+-x+) - K+(x+-x+) - K+ Vk
                                                                     =(I- K+H)(x+- x+-) -K+ Vk
                         = E[[(-K+H)e-+++Vk][(-KkH)e-+-KKVk)]]]
                          = E[ (I-K+H) e = E T (I-K+H)
                                          - (I-K+H) = + V+V+T = 0
- K+V+ E+ LI-K+H) = 0
+ K+V+V+TK+ ]
                          = (I- KkH) E(ekekt) (I-KkH)T
                                + KK E[VEVE] KET
                         = (I-K+H) Pk (I-K+H) + K+ EIV+V+ ] K+
                         = (PE-KKHPE) (I-KKH)+ KK RKE
   \Rightarrow \quad P_k = P_k^\top - K_k H P_k^\top - P_k^\top H^\top K_k^\top + K_k H P_k^\top H^\top K_k^\top + K_k R K_k^\top
   => +1 (PE) = +1 (PE) - 2 +1 (KEH R-) + +1 (KEH R-H-KE) + +1 (KEKK-)
             dr. (AB) = BT
                                                                                                                                                    \begin{array}{c} d_{11}(AB) \\ \vdots \\ AA \end{array} = \begin{bmatrix} \frac{\partial r_1(AB)}{\partial A_1} & \frac{\partial r_1(AB)}{\partial A_2} \\ \frac{\partial r_1(AB)}{\partial A_{21}} & \frac{\partial r_1(AB)}{\partial A_{22}} \end{bmatrix}
            AB = \begin{bmatrix} A_1 & a_{12} \\ A_2 & a_{13} \end{bmatrix} \begin{bmatrix} b_1 & b_{11} \\ b_{12} & b_{23} \end{bmatrix} = \begin{bmatrix} A_1 b_{12} + A_{12} b_{23} \\ A_2 b_{12} + A_{13} b_{13} \end{bmatrix}
\therefore \pi A(AB) = \begin{bmatrix} A_1 b_{12} + A_{13} b_{13} + A_{13} b_{13} \\ A_2 b_{13} + A_{13} b_{13} \end{bmatrix}
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