· Goal:



· accomptions here:

O convex function

PACT of is called convex i.f.t.

$$f(tx_1 + (1-t)x_2) \leq tf(x_1) + (1-t)f(x_2)$$

- saler 40 ELECS470 lah ...-

FACT of is convex Pot. f. f(x) = f(x) + \nabla f(x)^T(x-x),
\[
\text{V} \times x \times x. \times \times \text{V} \times \text

EACT & IS convex S.f. + Pf(x) = 0 lf(xxx) & min.

eg. Ilmen regression, logistic regression

· Gradient Rescent

- 
$$\alpha > 0$$
 is the step size / being note (hyper-

$$\nabla f(x) \rightarrow 0$$

- first - order toylor expension  $f(w+d) \approx g(d) := f(w^{\tau}) + \nabla f(w^{\tau}) d + \frac{1}{2d} ||d||^{2}$ 

recall:

$$g(d) = f(w^{\tau}) + \nabla f(w^{\tau}) d + \frac{1}{2d} ||d||^2$$

$$d^* = arg min & g(d)$$

$$\nabla g (d^*) = 0 \Rightarrow \nabla f(w^t) + \frac{1}{\alpha} d^* = 0 \Rightarrow d^* = -\alpha \nabla f(w^t)$$

- we can also do newoods nether yet two slow

a function is L-smooth if its Gradient is Lipschitz continuous:  $|| Pf(x_1) - Pf(x_2)|_2 \le L|| x_1 - x_2||_2$ 

 $\nabla^{2} f(x) \leq LI$  $f(y) \leq f(x) + \nabla f(x)^{T}(y-x) + \frac{1}{2} L \|y-x\|^{2}$ 

FACT let L be a Lipschitz constant

72f(x) & LI for all,

gradient descent converges of  $\alpha < \frac{1}{L}$