- · Term project:
 - project proposal
 - torm project repart
 - online offline project presentation
- vector X $X = [X_1, X_2, \dots, X_n]^T = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix}$
- Matrix X XERMXN

$$X = \begin{bmatrix} x_{11} & x_2 & \cdots & x_1 n \\ x_{21} & x_{22} & \cdots & \vdots \\ \vdots & \vdots & \ddots & \vdots \\ x_{m1} & x_{m2} & \cdots & x_{mn} \end{bmatrix} = \begin{bmatrix} x_1^T \\ x_2^T \\ \vdots \\ x_n^T \end{bmatrix} \in \mathbb{R}^{m \times n}$$

×i: (Xi column')

- X:5
- matrix product axis Cij = Arik Bk.j element - wise product
 - Cij = Aj Bj

- Inverse A-1A = I
- norm P=1 vector norm LP $\|\mathbf{x}\|_{\mathbf{P}} = \left(\mathbf{z} \|\mathbf{x}_i\|^{\mathbf{P}} \right)$

eg. P=1 $||\mathbf{x}||_{t} = 2||\mathbf{x}_{i}||$ 11 ×1/00 = max 1 ×1

not IIXII = refer to # of indial e.g. non zero dement mul x=10,1,0,3,2,0]

11×110 = 3

eg. 2 dinousion vector 1, norm: 1

FACT

11×1100 5 11×112 5 11×112 5 11 11×1100

 $||x||_{\infty} = \max_{x \in \mathbb{R}} |x| = \max_{x \in \mathbb{R}} ||x||^2 = ||x||_2$

· Matrix Norm (Snobenius norm)

· vector imer product <x14> = 11×112 |141112 C € 0

18 1141 ET

∠× b> = ||x||2 cast (projection on y space)

· Holder's inequality

eg p=2, 8=2 P=1, 8,500

· Linear combination Ax

Linear dependence, span

orthogonal orthonormal: all chun vector are in imer-predict = 0" relations:

· othogonal: x = 0 11 × 11/2 = 114112=1

La norm

11 All, Ducon(A)

11Allp = SWD 11AXIIp

· remark:

norm will

be Enguerally

regularization

used for

• othogond: ATA = I

· eigenvalue de composition

Q, QT are orthogonal

1 is diagonal W trubbes (square matrix)

· quadratic form: $\int_{X^T} A \times = X^T Q \Lambda Q^T X$ = (@Tx) T/(@TX) $= \tilde{\mathcal{Z}}_{\lambda_i} l_{g_i}^{\mathsf{T}} \times J^2 \leq \lambda_i \tilde{\mathcal{Z}}_{i_i}^{\mathsf{Z}} l_{g_i}^{\mathsf{T}} \times J^2$ Computational approach: QR = 2: ||x||_2

· Positive definite

YX XMX >0 SPD Y×, ×TA X ≥D

a quadratic form W/ PD or SPD:

$$0 \le \times \sqrt{A} \times \le \lambda : || \times 1|_2^2$$

Lo helpful sometimes

1 SVD (singular vector de composition) doubt he to be square metrix

$$A = UPV^{T} \circ [:] \text{ diagnal}$$

$$uu^{T} = I$$

$$vv^{T} = I$$

bounded L by NellxIll

· Derivative

- chan rule
$$f(x) = h(f(x))$$

$$\frac{df}{dx} = \frac{dh}{dx} \frac{dx}{dx}$$

$$\begin{array}{ccc}
\times \in \mathbb{R}^{n} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f(x)}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} \\
\frac{\partial f}{\partial x} = & \frac{\partial f}{\partial x} = &$$

$$\begin{array}{c}
\mathbb{R}^{n} \\
= \begin{bmatrix}
\frac{\partial f}{\partial x_{1}} \\
\frac{\partial f}{\partial x_{1}}
\end{bmatrix}$$

· trace =

· Jacobian

$$\frac{\partial \chi}{\partial x} = \left[\frac{\partial \chi}{\partial t} \frac{\partial \chi}{\partial t} - \frac{\partial \chi}{\partial x} \right]$$

$$\times e^{-\frac{1}{2}} \left[\frac{\partial \chi}{\partial t} \frac{\partial \chi}{\partial x} - \frac{\partial \chi}{\partial x} \right]$$

$$df = \mathop{\stackrel{\triangle}{\approx}} \frac{\partial f}{\partial x_i} dx_i$$

eg
$$f = a^{T} \times b$$

 $\frac{\partial f}{\partial x} = ?$
 $df = (da^{T}) \times b + a^{T}(dx)b$
 $+ a^{T} \times (db)$

$$df = tr(dt)$$

 $dt = aTMx)b$

$$= +n(a^{T}(d\times)b)$$

$$= +n(ba^{T}(d\times))$$

$$= +n[(ab^{T})^{T}d\times]$$

· Probability

- standard postable

 Describe: PMF (Abory-lucta)

 manginal probability

 conditional probability

 independent

- expectation variance constituce
- different kinda distribution Bayes Rules