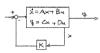
## -LQR



@ in Liver system Set K = (A-BK) x @ LQR, ne optimize K

## SLOR formulation

# J= J (= ax+u an) dt

=> K=-K × ⇒ ×=A>+Bu No Cx + Du

aso, Rso

## A Ricarri equation

minimize J= \$ (x2x+uiRu)dt S.T. ×=Ax+Bu >> [k,P] = lga (A.B.Q.R)

## sil

- 1. Bruse-funce
- 2. Lewing Algorithms (Gradient descent)
- 3. Analysic opposit
  - · Introduce Perpy J= x7px -x px + Jo(x70x +4 Ru)dt PJ: xiPx+ JItwas -xiz-waje ([x"Px] = 0-x.p"x ( | (x/bx) = x/bx + x/bx |

= /Ax+Bus Px+x\*P(Ax+Bu)

- # J=x736+J[(2x+31)7x+x70(2x+81)+x70x+1776
- = XTPX + TIX (ATP+FRAME ) X+WTR++XPB++ WBB AT

# uTRU+X\*PBU+UTBTPX (M+R\*BTPX)\*R(U+R\*B\*PX)-X\*(PBR\*B\*P)X

= x="P>= t }"[ x7(x"P+P4+@-PB&"8"P)> + (m+R"8"P>) TR(n=R"8"P) Det on "" st. the S is minimized

ATP+P4+Q-PBR"B"P = D (Algebraic Riccomi Bywain - ARE) 

## Attacking Trajectories

 $\times \!\!\!\! \to \!\!\!\! \to \!\!\!\! \times_{\!\!\! o \zeta}$ AT e= x-xd

v= u-ud Sixing fix+ pixxu \* = fex.uj

=> e=x-x

- = f(x)+ g(x) u-(f(xx) + g(xr) m)
- = f(e1xx)-f(xx)
- \* flexu) (mul) pixilul
- = Flev. XH LOWER)

streetik would ezo v= Ke=K(x-xe)

= u= k(x-xx)+ud

## ATLIDE OF OCP

ogeneral OCP

minimize food (xct), u(t)) dt x(0) + x6 x(t) = f(x(t), a(t)) } {y(c(0,0)) x(t) & X u(t) & U

· LOR

minimize Joo X(1)[QX(1)+ U(1)RU(1) de 4. ×10)=x6

x(t)=Ax(t)+8 a(t) } x(t) & X u(t) & U \*(1) + W

MPC mininge StW 2(xee), u(t)) dt

\*(T)=f(x(T), W(T)) \*(T) & X

W(T) & U

\*(T) & U

## A Standard Samulation

lex, u) = 1 x - x = 1 2 + 1/4 - 1 1/8  $J_N(x,u) = \underset{k=0}{\overset{N-1}{\smile}} \ell(x_k(k), u(k))$ 

=> mininge Jr (xo, e)

s.T. × n(k+1) = f(x,(k), a(k))

×4(0)=16 nck) ell v k e so. N-1] × L k) e X. V k e so NJ

 $x = I \times 4.0J^{T}$  $\begin{bmatrix} \dot{\hat{y}} \\ \dot{\hat{y}} \\ \dot{\hat{y}} \end{bmatrix} = \frac{2}{\Delta} \begin{bmatrix} (\hat{p}_{\Delta} + \hat{p}_{\hat{q}}) \cos \theta \\ (\hat{p}_{\Delta} - \hat{p}_{\hat{q}}) \sin \theta \\ (\hat{p}_{\Delta} - \hat{p}_{\hat{q}}) / D \end{bmatrix}$ 

 $\begin{bmatrix} V \\ \omega \end{bmatrix} = \begin{bmatrix} \frac{\pi}{2} (\vec{p}_A + \vec{p}_L) \\ \frac{\pi}{2p} (\vec{p}_A - \vec{p}_L) \end{bmatrix}$ 

\[ \frac{1}{2} \]
\[ \frac{1}{

## a Optimal Noulineer Coronal

- $\frac{d}{dx} \times = \frac{1}{2} (2 \times (\tau), \mu(\tau), +) d\tau$
- J(xxt), nx+), to, tf)
- $= Q(x(t), t) + \int_{t}^{t} \ell(x(t), u(t)) dt$ = y/setel, bully) in the distance to the distance of the party of the
- x(40) x(4)  $\begin{aligned} & \times^{(n)} \\ & \vee (\times (\tau_0), \tau_0, \tau_{\ell}) \\ & = \vee (\times (\tau_0), \tau_{\ell}, \tau_{\ell}) + \vee (\times (\tau_0), \tau_{\ell}, \tau_{\ell}) \end{aligned}$
- = 2V and (M) (monant) + Moreover)

  Hamilto Jechi Belliner (HJB) age