- Term project
 - project proposal
 - term project report
 - online offline project presentation
- vector

$$X \in \mathbb{R}^{n}$$

$$X = [X_{1}, X_{2}, \dots, X_{n}]^{T} = \begin{bmatrix} X_{1} \\ X_{2} \\ \vdots \end{bmatrix}$$

- Matrix

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1}n \\ x_{21} & x_{22} & \dots & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ x_{m1} & x_{m2} & \dots & x_{mn} \end{bmatrix} = \begin{bmatrix} x_{1}^{T} \\ x_{2}^{T} \\ \vdots \\ x_{n}^{T} \end{bmatrix} \in \mathbb{R}^{m \times n}$$

=> ith row of X (Xi column') jth col of X XX

Tenson >2 axis

element - wise product



- Inverse

- norm

Vector norm Lp
$$P \ge ||X||_p = \left(\frac{Z}{r} |X_i|^p\right)^{1/p}$$

eg. P=1

$$||x||_{t} = 2||x_{i}||$$

11 XIloo = max 1 Xil

not IIXII. = refer to # of non zoro devent but used e.g. non zero m M x=10,1,0,3,2,0]

11×110 = 3

cg. 2 dinausion vector

$$|| \times ||_1 = 1$$
 $|| \times ||_1 = 1$
 $|| \times ||_1 = 1$



FACT

$$||x||_{\infty} = \max_{x} |x| = \max_{x} ||x||^2 = ||x||_2$$

· Matrix Norm

||A||_F = \[\frac{z_1}{b_1} A_{b_1}^2 \Rightarrow \text{ Le norm matrix} \]

(Snobenius norm)

· vector imer product

$$\langle x,y \rangle = ||x||_2 ||y||_1 \cos \theta$$

· Holder's inequality

P=1, 2=00

· Linear combination

Linear dependence, span

· othogonal : x = o 11 × 11, = 114112=1

Lz norm

matrix

11 Allz Dman(A)

11Allp = Sup 11Ax 11p

· remark:

norm will

used for regularizatim

be Dequently

· eigenvalue de composition

· quadratic form: $\times^{T}A \times = \times^{T}Q \wedge Q^{T} \times$ $= (a^{T}x)^{T} \wedge (a^{T}x)$

$$= \underbrace{z_{i=1}}_{i=1} \lambda_{i} l_{i}^{2} l_{i}^{T} \times J^{2} \leq \lambda_{i} \underbrace{z_{i}^{T} l_{i}^{T} \times J^{2}}_{1}$$
$$\leq \lambda_{i} || \times ||_{2}^{2}$$

(computational approach: QR decomposition?

· Positive definite

quadratic form W/ PD or SPD:

$$0 \le \times \sqrt{A} \times \le \lambda : || \times ||_2^2$$

Lo helpful sometimes

· SVD (singular vector de composition)

$$A = U \overline{V} \overline{V}$$
 o [] diagnal $u \overline{V} = I$

could be used in none ases

bounded

by xie lixiliz

vv⁷= I

- chain rule

$$f(x) = h(f(x))$$

$$\frac{df}{dx} = \frac{dh}{dx} \frac{dq}{dx}$$

- 8x) ER'

$$\begin{array}{c}
\times \in \mathbb{R}^{n} \\
\frac{\partial f(x)}{\partial x} = \frac{\partial f}{\partial x_{1}} \\
\frac{\partial f}{\partial x_{2}} \\
\frac{\partial f}{\partial x_{3}}
\end{array}$$

$$df = \sum_{i=1}^{n} \frac{\partial f}{\partial x_i} dx_i$$

· Jacobian

e.g.
$$S = a^{T} \times b$$

$$df = (da^{T}) \times b + a^{T}(dx)b + a^{T}x (db)$$

 $\frac{\partial f(x)}{\partial X} = \begin{bmatrix} \frac{\partial f_1}{\partial x} & \frac{\partial f_2}{\partial x} & \frac{\partial f_3}{\partial x} \end{bmatrix}$

$$df = tr(df)$$
trace =
$$df = aTd(x)^{n}$$

$$dt = a^{T}d(x)b$$

$$= + \lambda \left(b a^{T} (dx) \right)$$

$$= + \lambda \left[(ab^{T})^{T} dx \right]$$

$$\frac{df}{dx} = ab^{T}$$

· Probability

- standom vovicible

A (thA)

PMF (mass-function) Discrete: - mangiand probability
- conditional probability

- independence
- expectation variance covariance
- different kinda distribution
- Bayes Rules