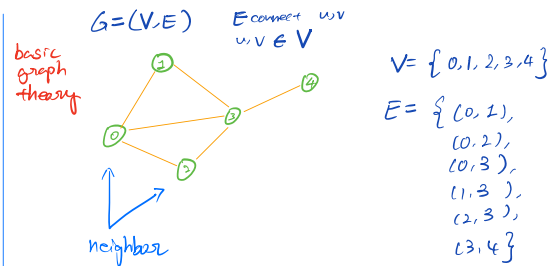


edge: dynamic/sensor model
 node: objective problem
 → solve the over determined problem!



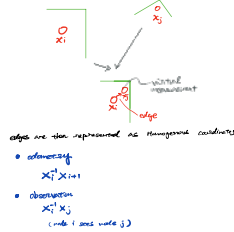
1. $\text{neighbor}(0) = \{0, 1, 2\}$
2. $\text{degree}(0) = 3$
 $\text{degree}(2) = 2$
3. path $0 \rightarrow 3 \rightarrow 2 \rightarrow 0$
4. cycle $0 \rightarrow 1 \rightarrow 3 \rightarrow 2 \rightarrow 0$
5. connectivity: graph is connected if \exists path between (u,v) $\forall u,v \in V$
 - graph is connected when all vertices are connected
 - connected component $V \subseteq V$

Edge Creation

• edge creation

• edge

• measurement



pose graph



edge: $e_{ij} = x_j - x_i$
 measurement: $x_j^T x_i$
 (node i and node j)

pose graph: $e_{ij} = x_j - x_i$
 measurement: $x_j^T x_i$
 (node i and node j)

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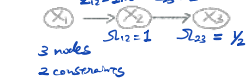
pose graph: $e_{ij} = x_j - x_i$
 measurement: $x_j^T x_i$
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 measurement: $x_j^T x_i$
 (node i and node j)

e.g.



$x_0 = \{x_1, x_2, x_3\} = \{0, 0, 0\}$
 initial guess

$e_{ij} = x_j - x_i$
 $e_{12} = \{1 - (0 - 0)\} = 1$
 $e_{23} = \{1 - (0 - 0)\} = 1$

$J_{ij} = \begin{pmatrix} \frac{\partial e_{ij}}{\partial x_1} & \frac{\partial e_{ij}}{\partial x_2} & \frac{\partial e_{ij}}{\partial x_3} \end{pmatrix}$
 $J_{12} = \begin{pmatrix} \frac{\partial e_{12}}{\partial x_1} & \frac{\partial e_{12}}{\partial x_2} & \frac{\partial e_{12}}{\partial x_3} \end{pmatrix}$

$J_{12} = \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}$
 $J_{23} = \begin{pmatrix} 0 & 1 & -1 \end{pmatrix}$

$b^T = \sum_{ij} e_{ij}^T J_{ij} J_{ij}^T$
 $= 1 \cdot 1 \cdot \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T$

$= 1 \cdot 1 \cdot \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T$
 $= \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T$

$H = \sum_{ij} J_{ij}^T J_{ij} J_{ij} J_{ij}^T$
 $= \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T + \begin{pmatrix} 0 & 1 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 & -1 \end{pmatrix}^T$

$= \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T + \begin{pmatrix} 0 & 1 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 & -1 \end{pmatrix}^T$
 $= \begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \end{pmatrix}^T + \begin{pmatrix} 0 & 1 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 & -1 \end{pmatrix}^T$

$\Delta x = -H^{-1}b \rightarrow \text{error}$
 when $\det(H) = 0$

change the relative constraints to global ones

$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$

types of graph

1. undirected graph (shown above)

2. directed graph



3. weighted graph

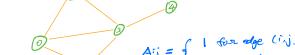


4. trees

1. connected and acyclic
2. removing edge disconnects graph
3. adding edge creates a cycle

graph representation

• Adjacency Matrix



$A_{ij} = \begin{cases} 1 & \text{for edge } (i,j) \\ 0 & \text{otherwise} \end{cases}$

edge set: $\{(0,1), (0,2), (0,3), (1,3), (2,3), (3,4)\}$

adjacency list: $0 \rightarrow \{1, 2, 3\}$
 $1 \rightarrow \{0, 3\}$
 $2 \rightarrow \{0, 3\}$
 $3 \rightarrow \{0, 1, 2, 4\}$
 $4 \rightarrow \{3\}$