Pose Estimation via Vision ( )

- pinhole model
- thrangulation (29-30)
- ICP problem (3D-3P)
- optimization

## pinhale model

$$\frac{3}{5} = \frac{\times}{X'} = \frac{Y}{Y'}$$

$$\therefore \int x' = f \frac{x}{3}$$

$$Y' = f \frac{x}{3}$$

$$\Rightarrow \begin{cases} u = \alpha + \frac{3}{3} + Cx \\ v = \beta + \frac{3}{3} + Cy \end{cases}$$

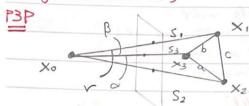
$$= \begin{cases} V = \int_{X} \frac{x}{3} + Cx \\ V = \int_{Y} \frac{x}{3} + Cy \end{cases}$$

 $\leq W$ 

$$\frac{(u-cx)}{\delta x}$$
 ,  $>$ 

$$\frac{376-635}{630} \cdot 4.3 = -1.76$$

## Triangulation (2D-3D)



known X1 X2 X3 OX B >

$$a^{2} = S_{2}^{2} + S_{3}^{2} - 2S_{2}S_{3} \cos \alpha$$

$$b^{2} = S_{1}^{2} + S_{3}^{2} - 2S_{1}S_{2} \cos \beta$$

$$c^{2} = S_{1}^{2} + S_{2}^{2} - 2S_{1}S_{2} \cos \gamma$$

0 a=5=+53= 25153 cosx

set 
$$u = \frac{S_2}{S_1}$$
,  $V = \frac{S_2}{S_1}$ ,  
 $A^2 = S_1^2 (u^2 + v^2 - 2u v \cos s x)$ 

$$51^{2} = \frac{a^{2}}{4^{2} + 4^{2} - 24 \times \cos 4}$$

$$: S_1^2 = \frac{b^2}{1 + V^2 - 2V\cos \beta}$$

3 C= 5, +5, 2- 25, 52 COSH

$$S_1^a = \frac{a^a}{u^2 4 V^2 - 2 u V \cos x} = \frac{b^2}{1 + v^2 - 2 v \cos \beta} = \frac{c^2}{1 + u^2 - 2 u \cos x}$$

parameterize U as V

## EPAP

-we need reference points P to do adomosy.

-any resence points P

can be expressed by control points

C3 X44

5=1 J=1 J=1 Side v

side note 1:

-how to get Given side note 2:

-why 4 points,

not 3, 2?

now my to get a limitermediate media)

as 
$$\frac{3}{J-1} \propto ij = 1$$
  
 $t = \frac{3}{J-1} \propto ij t$ 

Both {c} {w} share same ox

get uknown dij -> known

PC = 3 aij (Rew Gw+t) = 3 dijeje

our objective is to get Pie

side note 3:

odr5?

$$P_{i}^{C} = \frac{1}{3}\alpha^{i}j(R_{cw}C_{j}^{w}+t) = \frac{1}{3}\alpha^{i}jC_{j}^{C}$$

$$\Rightarrow W_{i} \begin{bmatrix} W_{i} \\ V_{i} \end{bmatrix} = \begin{bmatrix} 5n & 0 & u_{c} \\ 0 & 5v & v_{c} \end{bmatrix} \begin{bmatrix} 3i & 0 \\ 3i & 0 \end{bmatrix} \begin{bmatrix} 3i & 0 \\ 3i & 0 \end{bmatrix}$$
From Last Row:
$$W_{i} = \int_{z_{i}}^{z_{i}} \alpha^{i}j3_{j}^{C}$$

$$W_{i}^{C} = \int_{z_{i}}^{z_{i}} \alpha^{i}j3_{j}^{C}$$

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$$W_{i}^{C} = \int_{z_{i}}^{z_{i}} \alpha^{i}j3_$$

SNe nove 1: how to got Cos? Oas long as cow is invertible @ as per Leperit et al .: get centre of weight as C3 (5=1)

ATA get > 20,1 value i=1,2,3 Va .: year i= 1.2.3

why 4 - not others ? 23 × 5=1

4 equations w/ 3 unknown

side note &: how to get aij?

 $P_i^{W} = \underbrace{3}_{3} \alpha \cdot j C_j^{W} \qquad w / \underbrace{5}_{5=1}^{M} \alpha \cdot j = 1$ 4 equations solve linear system

remark 30-217 Ads -7 vailes. 4016 -> consy

## ICP Problem

known duta association Y= {4, ... 41} } ~ c= {i,j}

Z || y; - kx; - t||² -> min

matched points pairs:

Xn Yn

X= RX+++X5-AXX

211 Th- Il pn -> min

exist & let's device direct solveron

Yo= BynPn Xo= BxnPn

H= Z(Jn-y.)(Xn-X.) TPn

Sval(H) = UDVT

- PLANTED - MINE - MINE - MINE - MINE T = 40 - RX0

why is this a good solution? ->

Zn=RXn+1 Xn-40=RXn+t-40 Xn-40= R(Xn+RT+-RT40) Xn-Yo= R (Xn-Xo) set as unknown variable X Ry= argman & bn Ran Ph Zlyn-Xnll pn -> min RT = argman +r (RH) => ZIIYn-yo-RXn-++ Yoll Pn ->min H= S (anbn7) Pn = 11 4n-40- ( Xn - 40) 112 Pn 2min find R mass to (RH) SVD(H)= UDVT => 311 8n-40- R(Xn-X0) 112 Pn ->min UTU=I x pac 2 = min ) my w .. R Xo = argmin ZII yn-yo- R (xn-xo) || Pn R. Xo VV = I D = diag (di) R=VUT H=UDVT 重(xo\_R)=2[(4n-40)-R(xn-x0)][(4n-40)-R(xn-x0)]Pn +r(RH)=+r(VUTUDVT) = +r (VDVT) = +r (V D= D= V7) set + Z (xn-x0) (xn-x0) Pn no R = +r (AAT) -22(yn-50) TR(Xn-X0)Pn on (RH)=+r(AAT) +r (AAT) = +r (R'AAT) Schwarz inequality 25(x-x) =-23(x-x) Px+22RT(y-y)Px +r(RH)=+r(AAT)Z+r(R'AAT) ·· 0=-25(xn-x)Pn+25RT(yn-yo)Pn +-(R'RH) any other rotation EXPN-ZXPN=0 .. choice R=VU? optimal to Optimal value for is the weighted mean of populs maxise the trace R'R is also another 50(3) let R'R=R" R = argmin - 23 (yn-ya) 7 R (xn-xo) pn tr(R"H) will alongs < tr (RH) = arg mas 23 (yn-yo) TR (xx-x) Pn if R=VUT i.e. if RH can be written as AAT let bn = yn-yo

+r (RH) will be max.

ICP (SVD) (contid)

更(xo, R)= Z(yn-yo) (yn-yo)Pn

3 2(Xn->6) Pn = 0

an = Xn-Xo

> Xo= ZxnPn

O w.r. + X0

@ W.r. 7 R

Set 22(xx,R) = 0

