```
<u> LQR</u>
        X=Ax+Bu
        13 = Cx + Du
          K.
 O in Linear system
     in Liverity of the Tikk Set K
    5.4.
                    A-BK is
    *= Ax+Bh
   * * Ax-8K
      = (A-BK) x
  @ LQR, me optimize K
SLOR formulation
  J= J (= Rx+ u Ru) dt
    => u=-K ×
    => ×=A>+Bu
 aso, Rso
A Ricerri equation
  minimize J= $ (x&x+wiRu)olt
  S.t. X=Ax+Bu
  >> [x,P] = lgz (A,B,Q,R)
sult
 1. Brute-funce
 2. Lewing Algorithms
(Gradiens descent)
 3. Analysic approach
    · Introduce Pept
      J= x3p x - x p x + J (x 2 x + u R v)dt
      PJO MIPX+ SEEWAND+XAMMENTER
                   ([x'Px] = 0-x0P'x
                   #(xTPx) = xTPx+xTPx
                 = (Ax+Bu) PX+x"P(Ax+Bu)
95=x7x+5[[ax+3]7x+x72(2x+3)+x32x+274]4
  = x Px + [] x (ATP+PAMR) x+w 8+ + x P8++ 687]
uTRU+X'PBU+UTBTPX

(N+R"6TPX)TR(U+R"6TPX)-XT(PBR"8TP)X
  I to exercise
         XTEATP+ PA+Q-PB&"BTPJX
         MR"B"PX)TR(NTR"BTPX)
         Det an "u" st. the S is minimized
  > u=-A"B"PX
                  -- K=R-B-P
     4= -K X
  ATPIPATA - PBRTBTP = 0
   (Algebraic Riccomi Openia - ARE)
     - Simil P that sales ARE
      - Use P to get K
           (subtane)
Attacking Trajecounies
   ×-> ×0
 At e= x-xd
     V= W-WI
     dixing fix)+ pixxu
     * = f(x, m)
=> e=x-x
     =f(x)+g(x)u-\{f(xx)+g(xx)\cdot\phi(x)
     = f(e1x4)-f(x4)
```

* glerky (must pixoud = Flev. Xettlumin) $\Rightarrow linearize arount e = 0$ $v = K_{\ell} = k(x - x_{\ell})$

=> u= K(x-xx)+ud

```
*(t)=f(x(t), u(t)) | y(c[ow)

*(t) & X

u(t) & (X
minimize for x(1) [ax(1) + w(1) [Ruce) dz
        X(T)=AX(T)+BAIT)
X(T) & X

ATTELON
         x(t) = x = 

x(t) = f(x(t), w(t)) 

Yteletal
```

ATLIDR of OCP

minimize for d(xct), u(t)) of t

×(*) * ×

openeral OCP

≤.1. ×(0)=×5

6.th x(t)= x0

x17) & K

minimize St+N &(xet), u(t)) oft

un ell

· LOR

· MPC

A Standard Sommlerum $\ell(x, u) = \|x_u - x^2\|_Q^2 + \|u - u^n\|_R^2$ $J_{N}(x,u) = \underbrace{J_{N}(x_{n}(k), u(k))}_{l=0}$ => mininge Jr (xo, e) s.T. × n(k+1) = f(xu(k), a(k)) ×4(0)=16 nck) ell YkeEo.N-13 x LK) EX. YKEEDON] a mobile nobot as an example $\mathbf{x} = \mathbf{1} \times \mathbf{4}, \boldsymbol{\theta} \mathbf{J}^{\mathsf{T}}$ $\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \frac{3}{\Delta} \begin{bmatrix} (\dot{p}_0 + \dot{p}_0) \cos \theta \\ (\dot{p}_0 - \dot{p}_0) \sin \theta \\ (\dot{p}_0 - \dot{p}_0) \end{bmatrix}$ 20 (da- De)

a Optime Noullness Corone - $\frac{d}{dx} \times = f(x(\tau), u(\tau), \tau) d\tau$ - J(xct), uct), to, tf) $= Q(x(ti),ti) + \int_{ti}^{ti} \ell(x(ti),u(ti))dt$ - viscoloury) + was Jismy ster and) x(40) x(4)

 $= V\left(\mathbf{x}(t_0), d_0, \tau\right) + V\left(\mathbf{x}(t_0), \tau_0 \tau_0^2\right)$

Hamilto Jecob: Bellman (HJB) ogu

V(X(ta), to tg)

 $= -\frac{\partial V}{\partial t} = \sup_{k \in \mathcal{C}_k} \left(\frac{\partial V}{\partial x} \Big| \mathcal{L}_{(M^{(k)}(M^{(k)}) + 1, \mathcal{L}(M^{(k)}(M^{(k)}))} \Big| \right)$