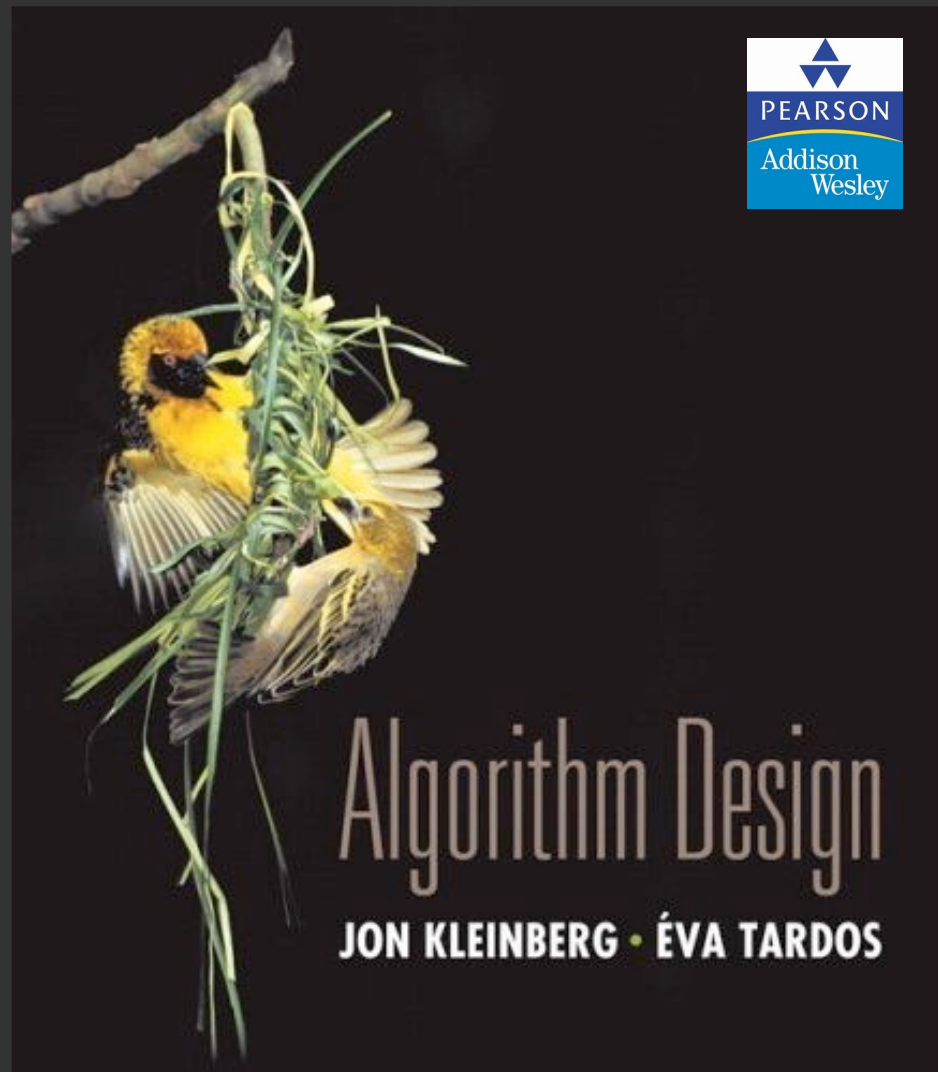


## 4. GREEDY ALGORITHMS II

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► *red-rule blue-rule demo*



Lecture slides by Kevin Wayne

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<http://www.cs.princeton.edu/~wayne/kleinberg-tardos>

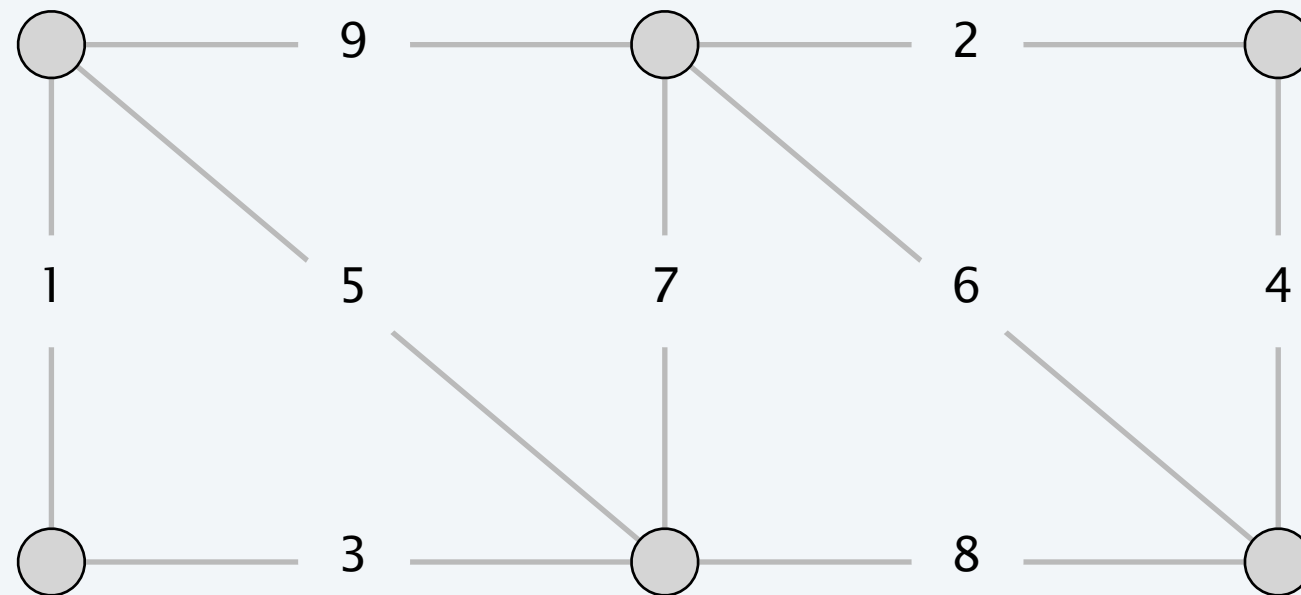
# Red-rule blue-rule demo

---

**Red rule.** Let  $C$  be a cycle with no red edges. Select an uncolored edge of  $C$  of max weight and color it red.

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

the input graph

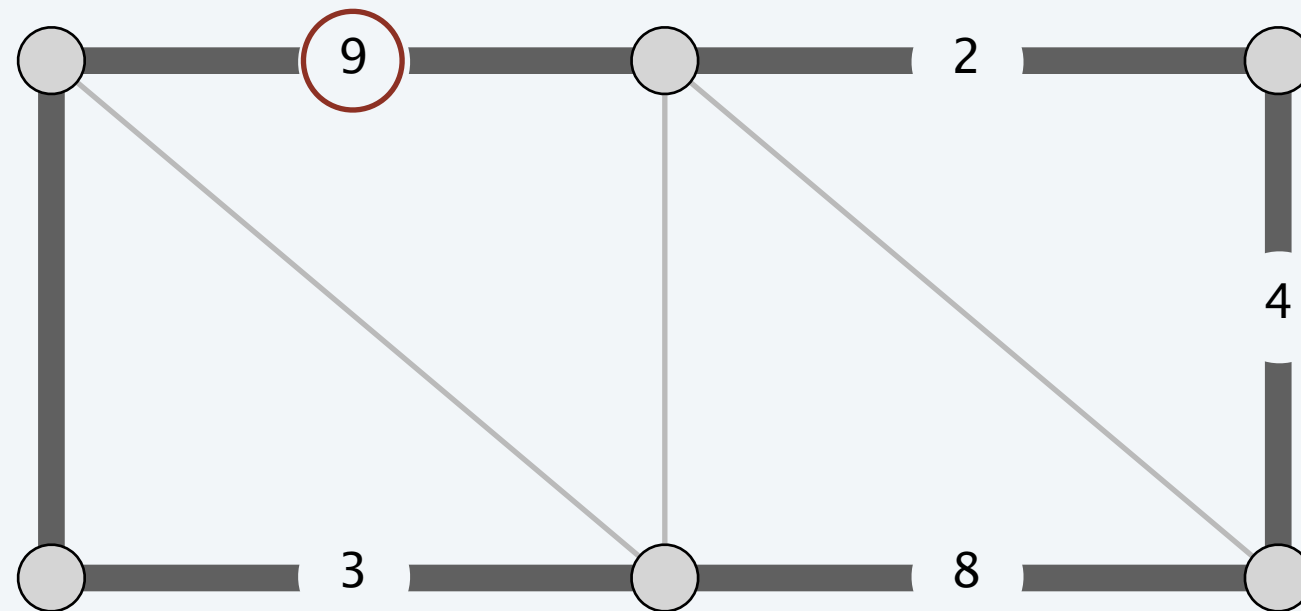


## Red-rule blue-rule demo

---

**Red rule.** Let  $C$  be a cycle with no red edges. Select an uncolored edge of  $C$  of max weight and color it red.

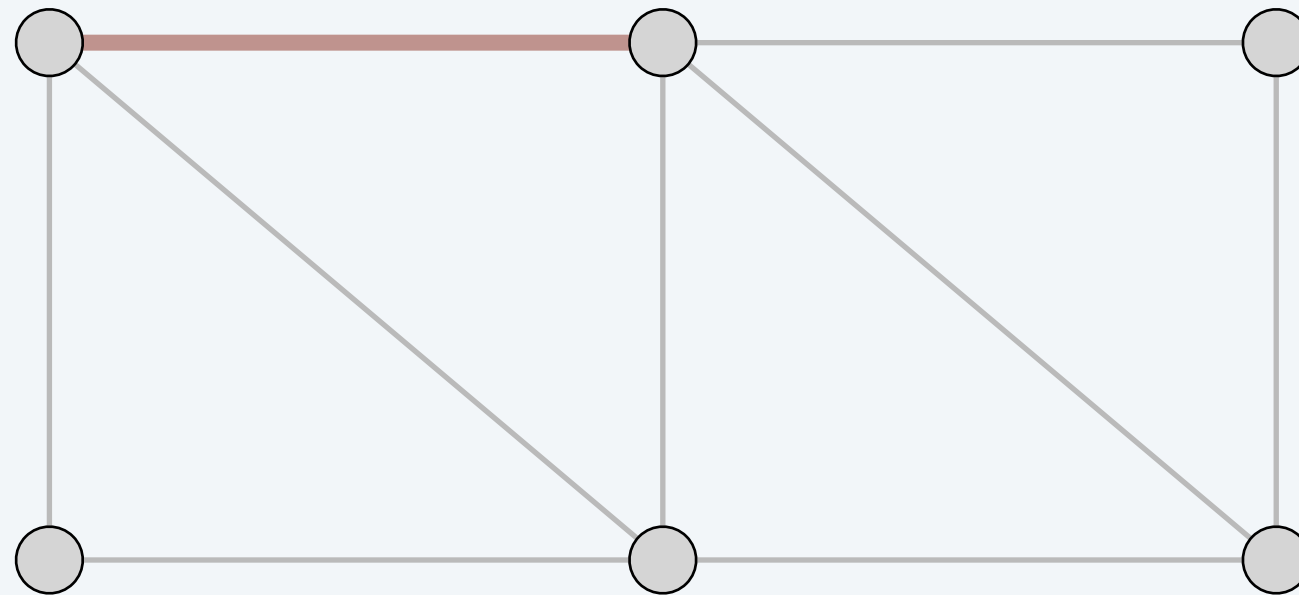
apply the red rule to the cycle



# Red-rule blue-rule demo

---

current set of red and blue edges

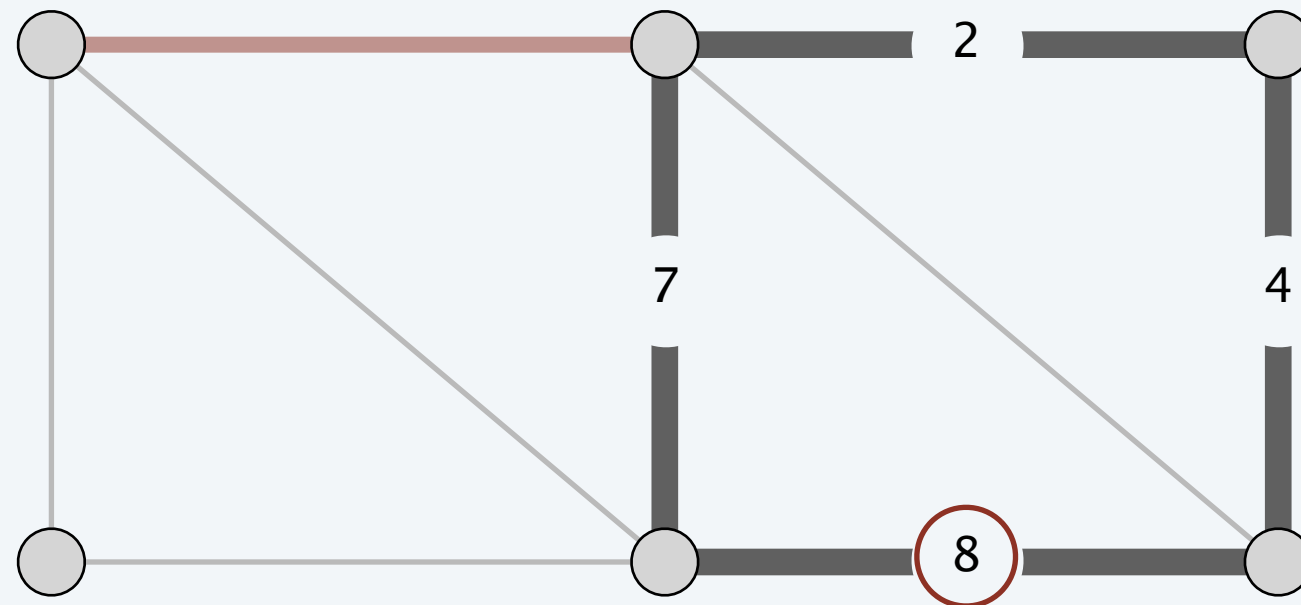


## Red-rule blue-rule demo

---

**Red rule.** Let  $C$  be a cycle with no red edges. Select an uncolored edge of  $C$  of max weight and color it red.

apply the red rule to the cycle

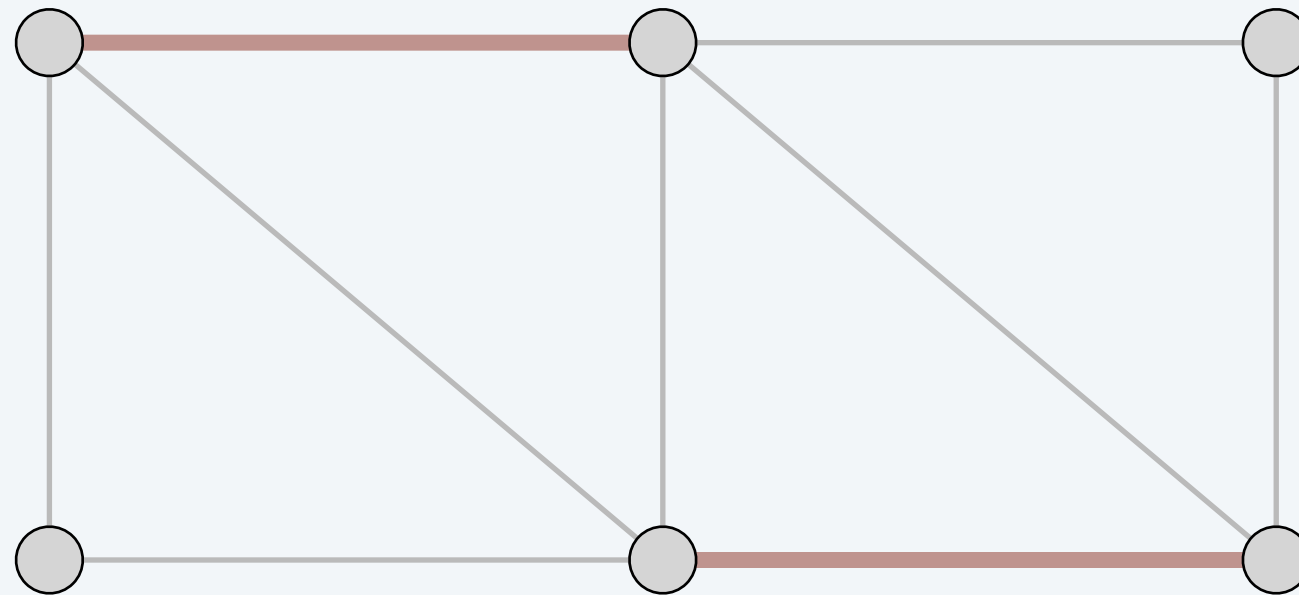


## Red-rule blue-rule demo

---

**Red rule.** Let  $C$  be a cycle with no red edges. Select an uncolored edge of  $C$  of max weight and color it red.

current set of red and blue edges

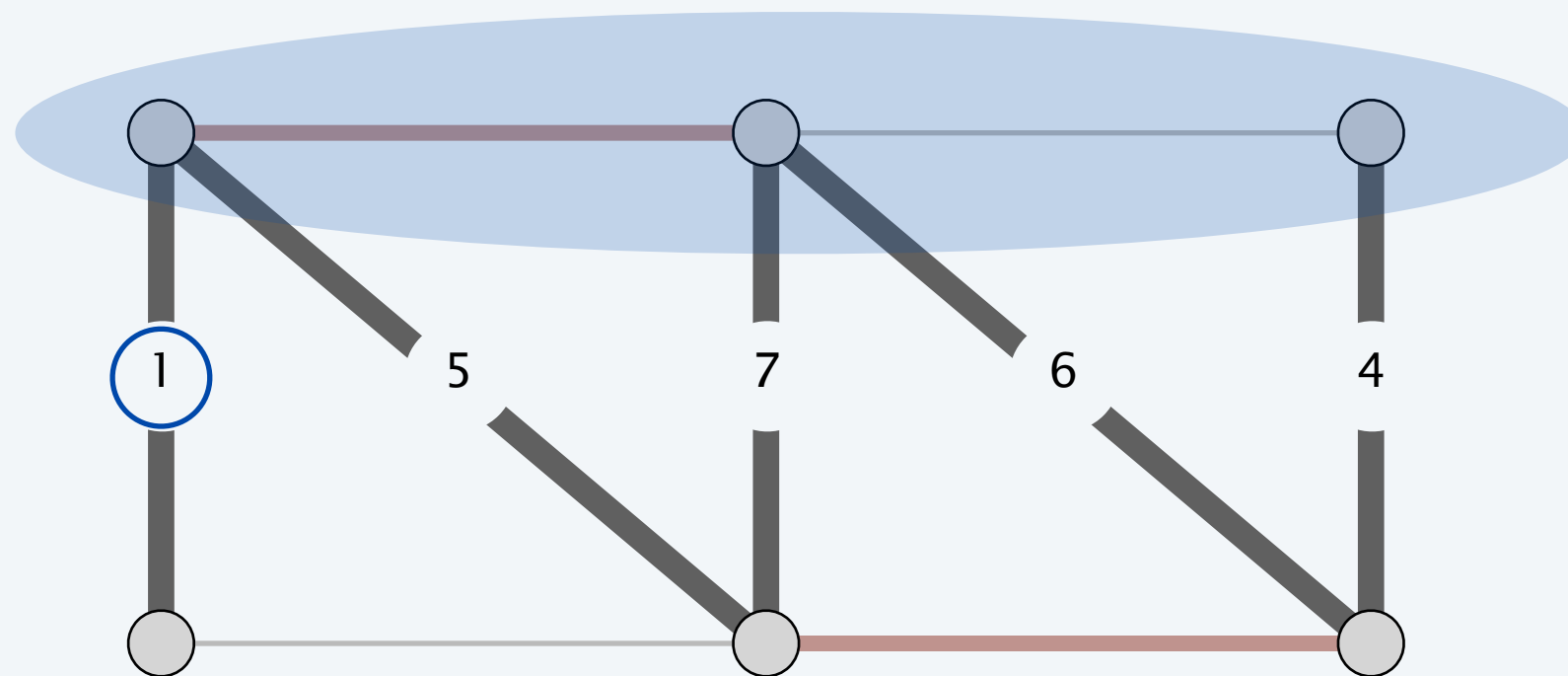


## Red-rule blue-rule demo

---

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

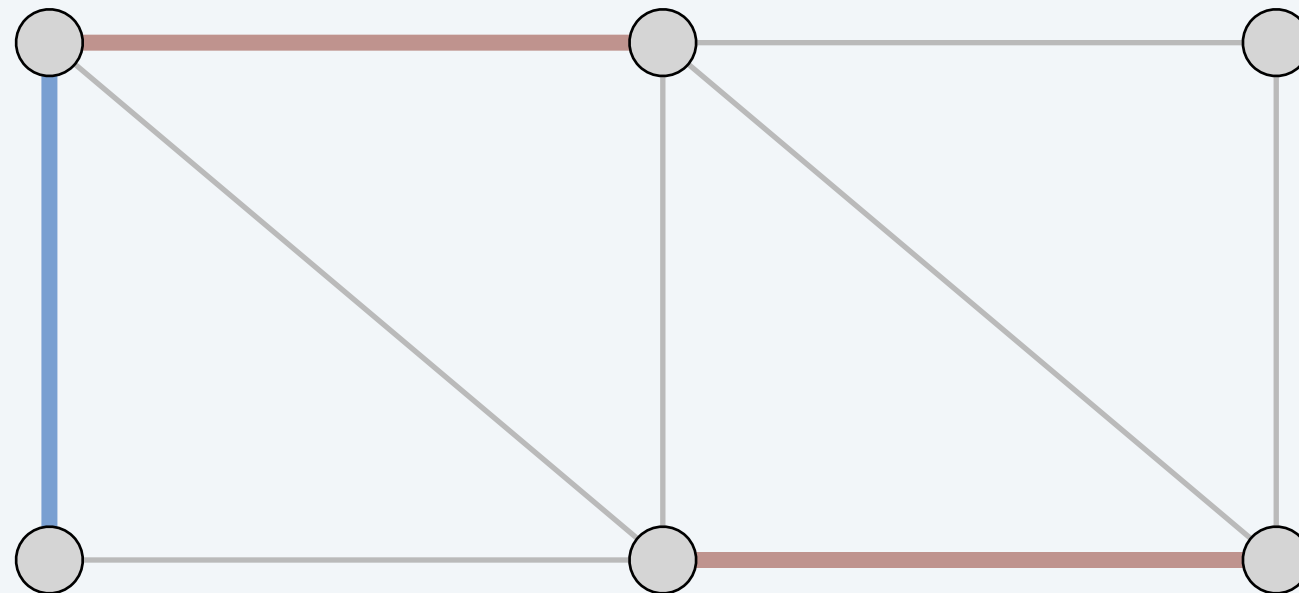
apply the blue rule to the cutset



# Red-rule blue-rule demo

---

current set of red and blue edges



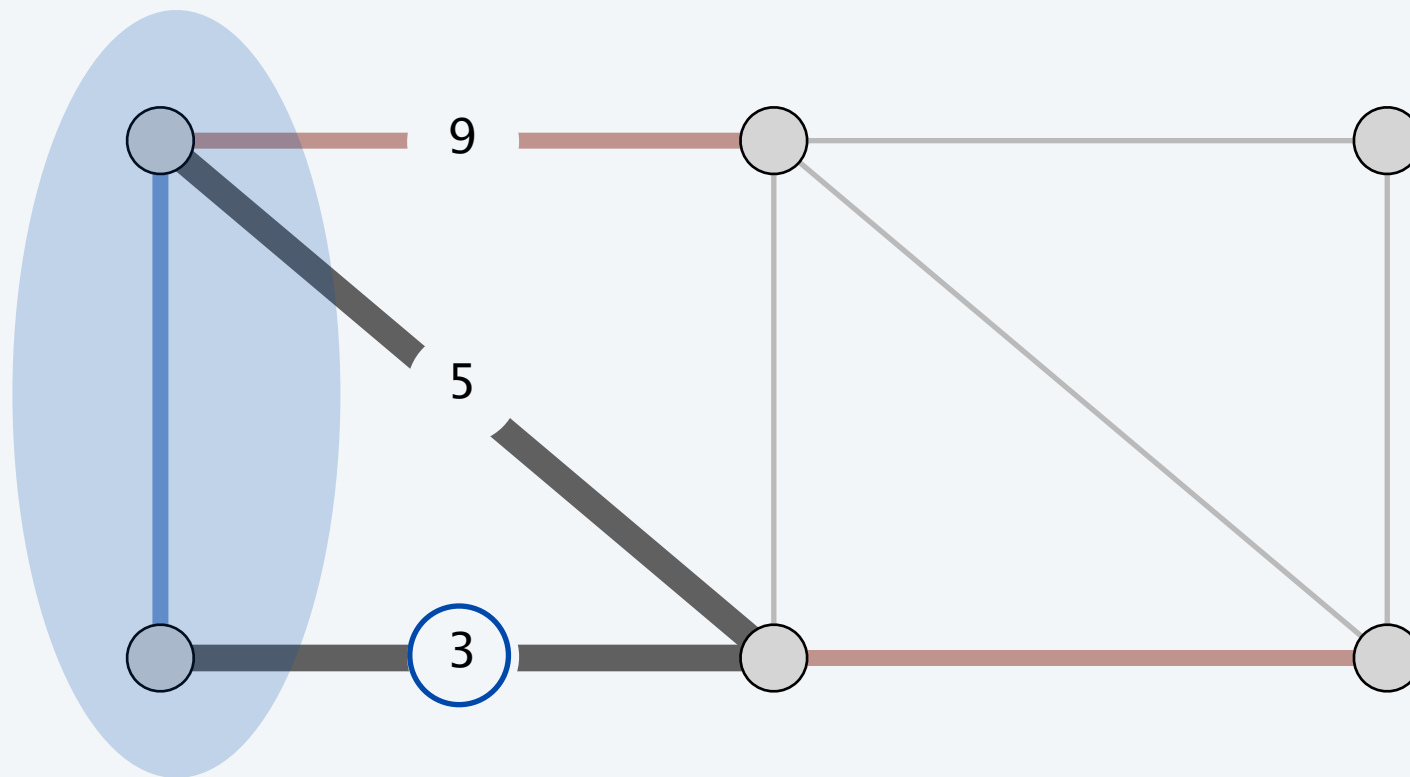


## Red-rule blue-rule demo

---

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

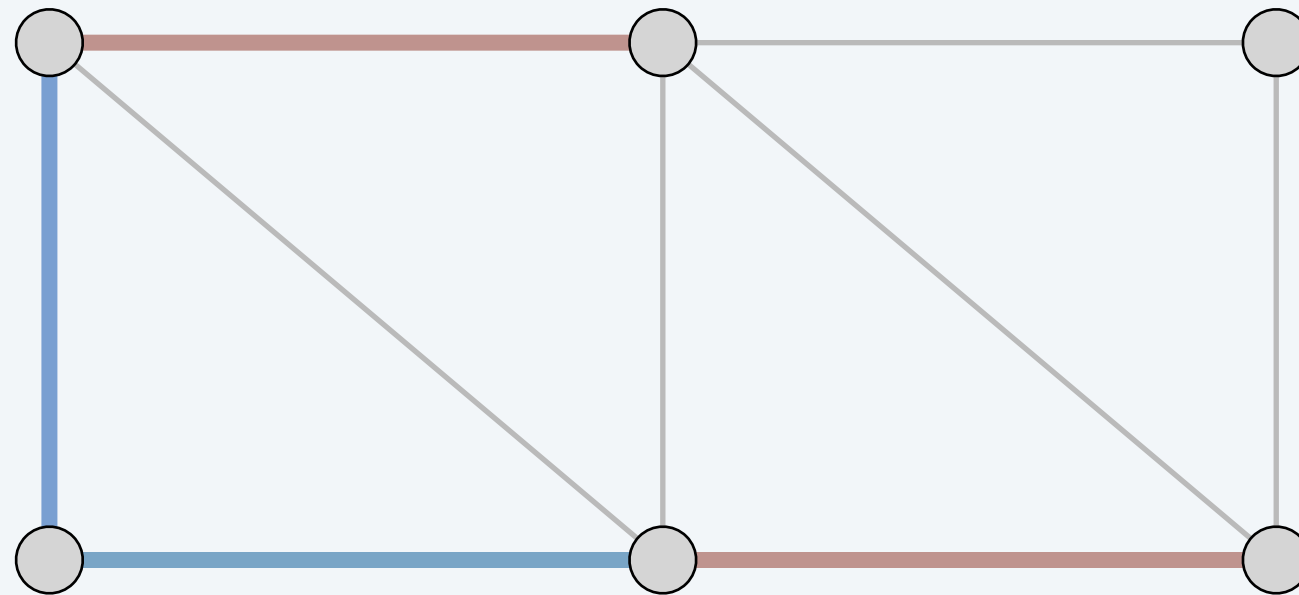
apply the blue rule to the cutset



# Red-rule blue-rule demo

---

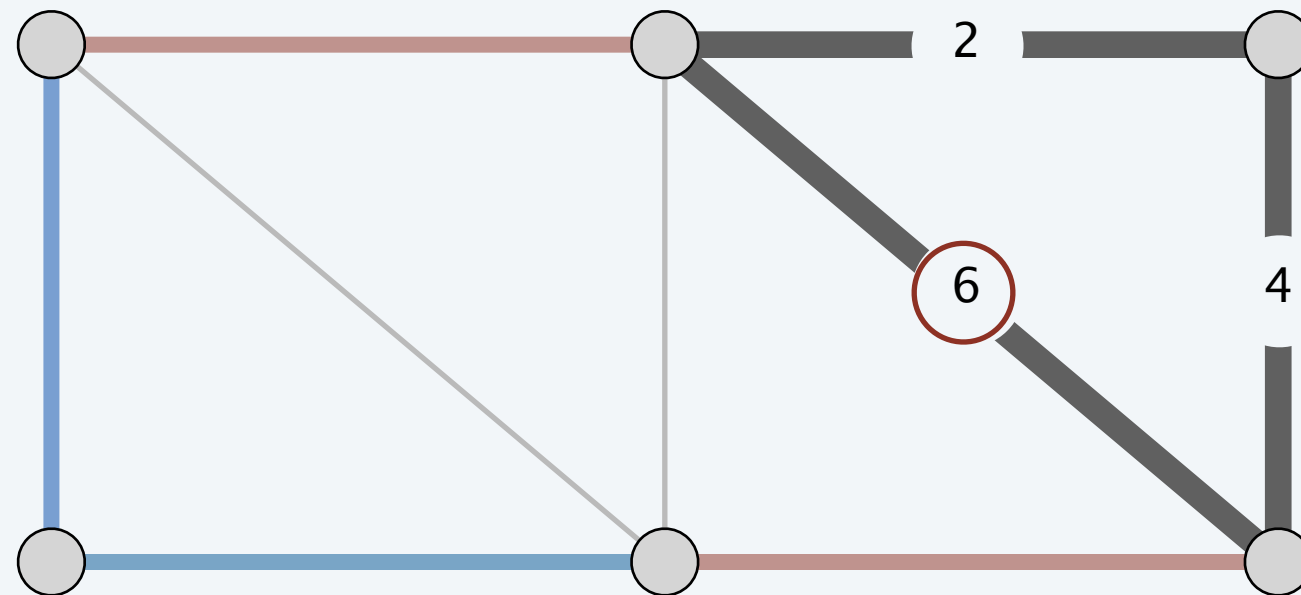
current set of red and blue edges



# Red-rule blue-rule demo

---

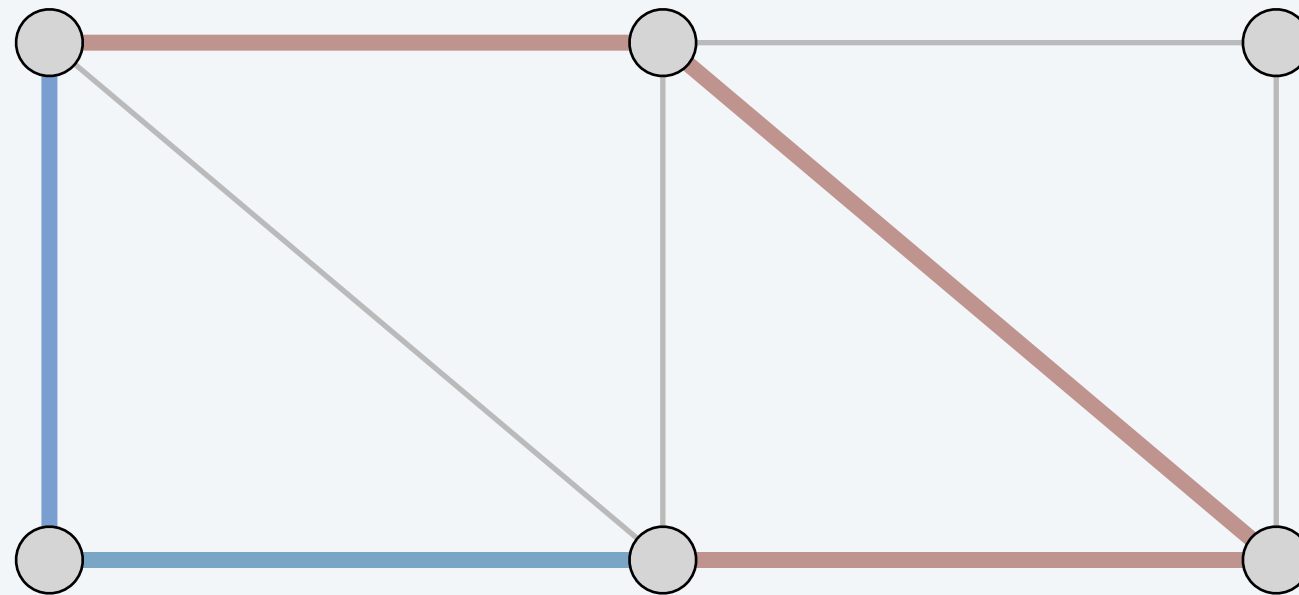
apply the red rule to the cycle



# Red-rule blue-rule demo

---

current set of red and blue edges

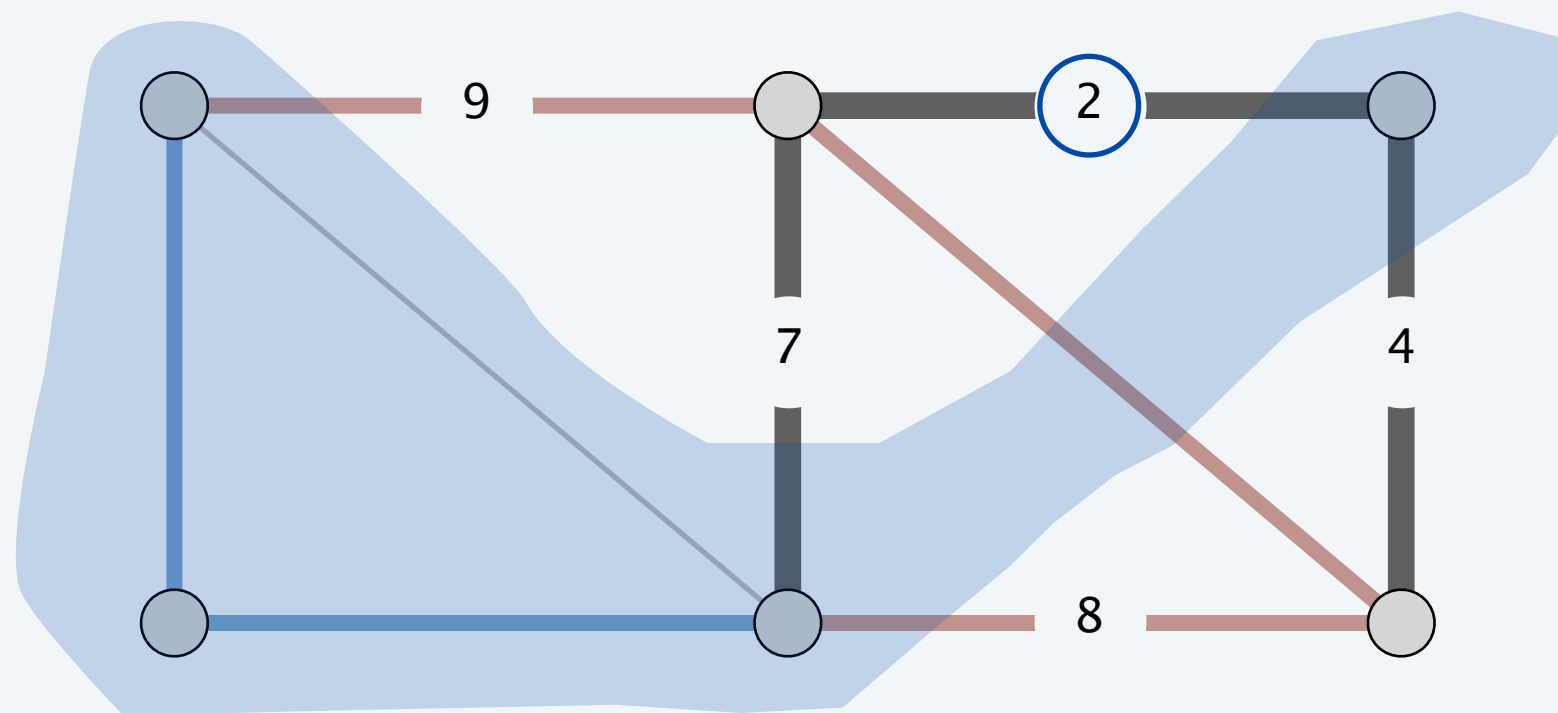


# Red-rule blue-rule demo

---

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

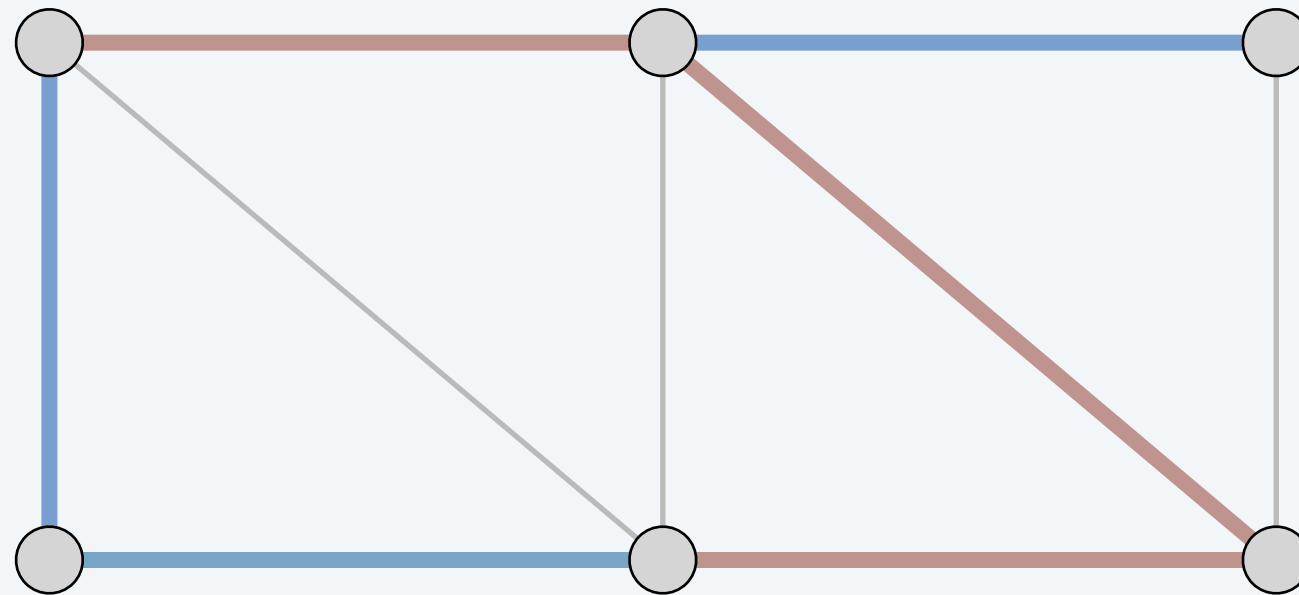
apply the blue rule to the cutset



# Red-rule blue-rule demo

---

current set of red and blue edges

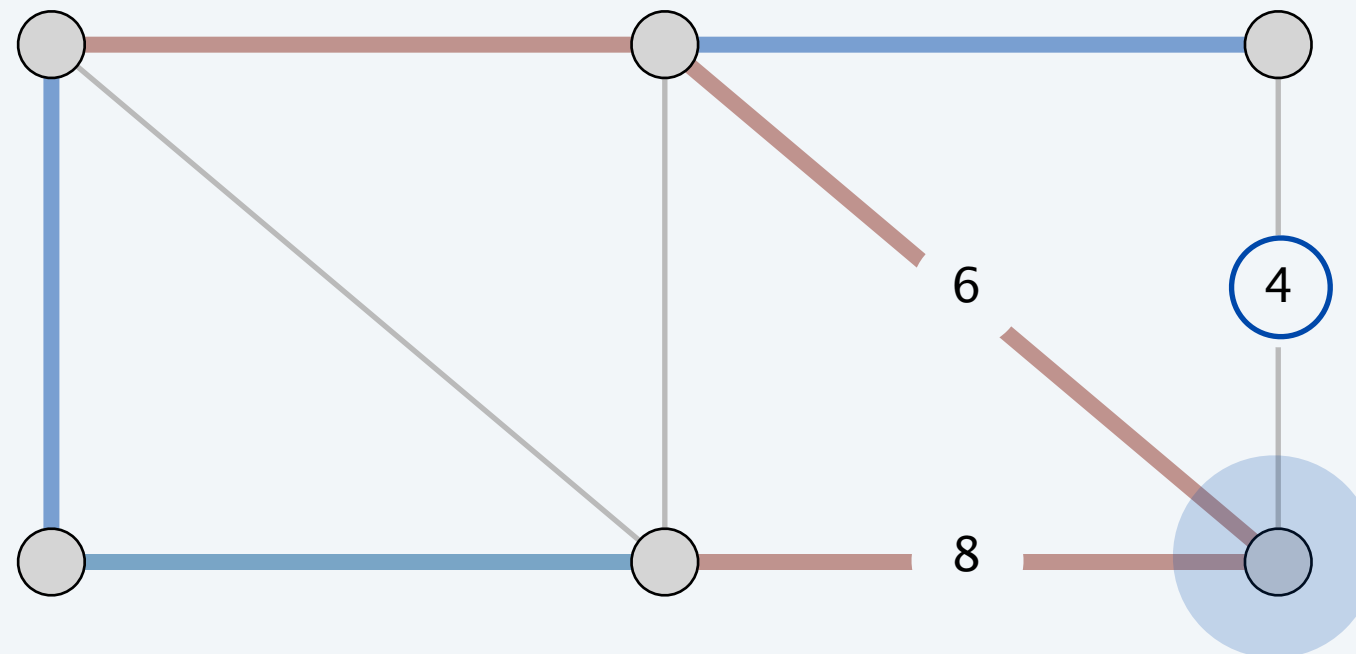


# Red-rule blue-rule demo

---

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

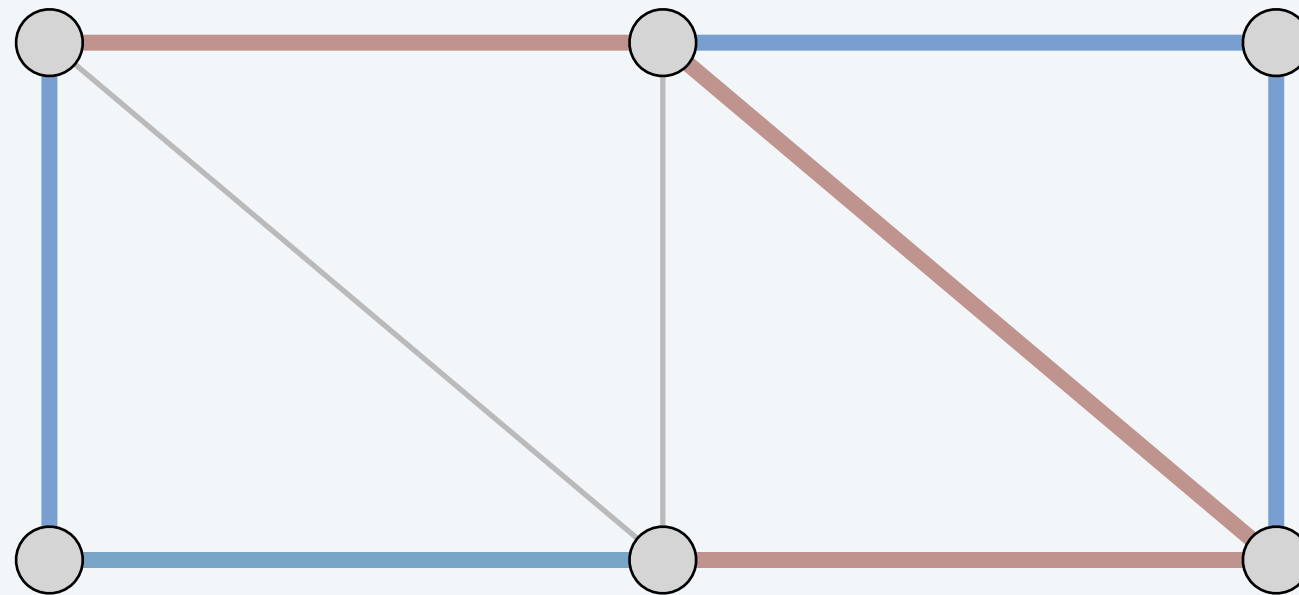
apply the blue rule to the cutset



# Red-rule blue-rule demo

---

current set of red and blue edges



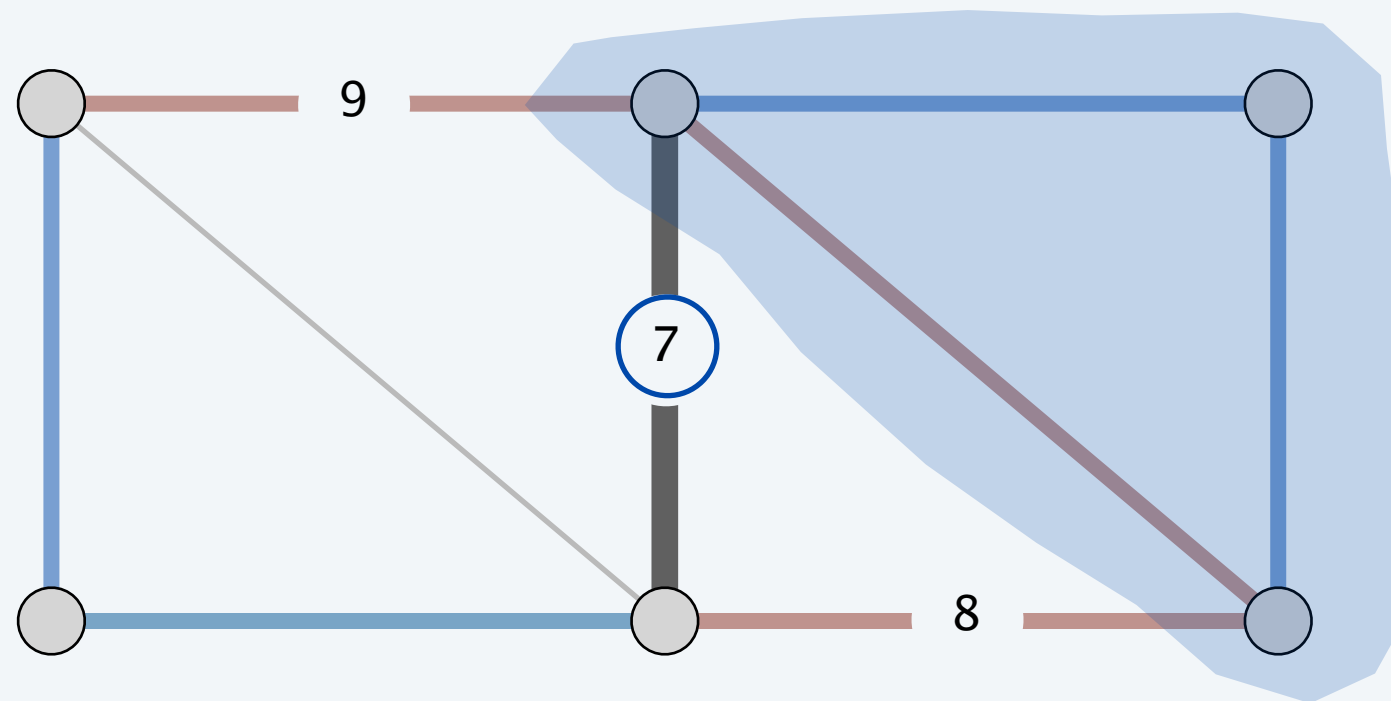


## Red-rule blue-rule demo

---

**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

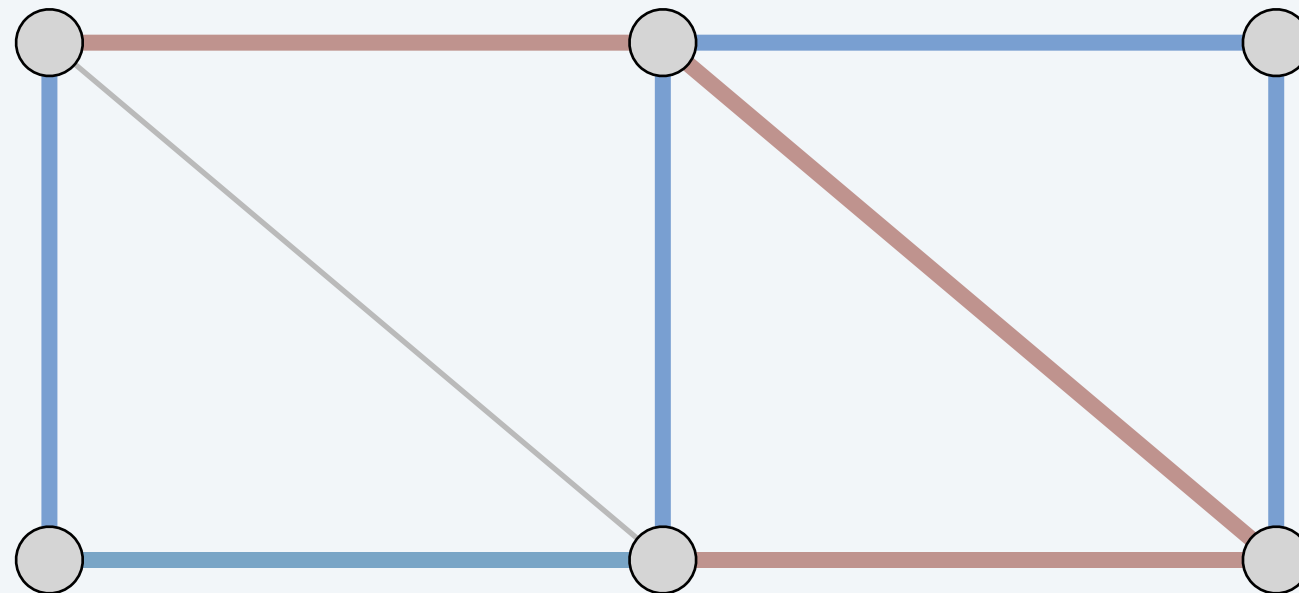
apply the blue rule to the cutset



# Red-rule blue-rule demo

---

current set of red and blue edges

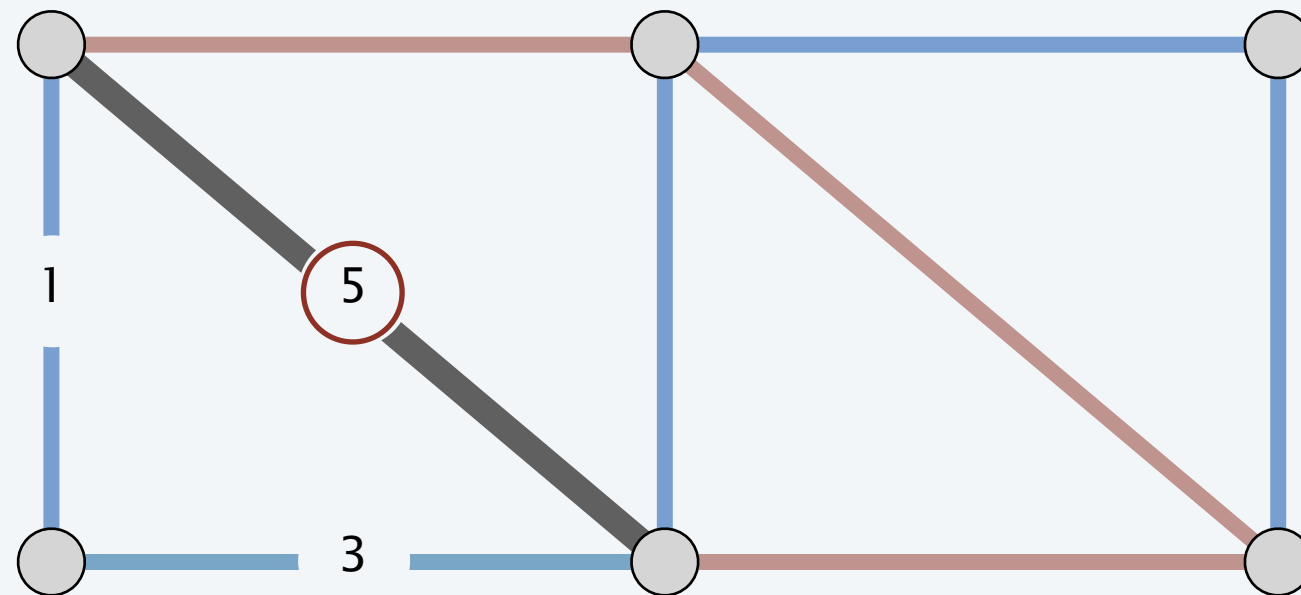


## Red-rule blue-rule demo

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**Blue rule.** Let  $D$  be a cutset with no blue edges. Select an uncolored edge in  $D$  of min weight and color it blue.

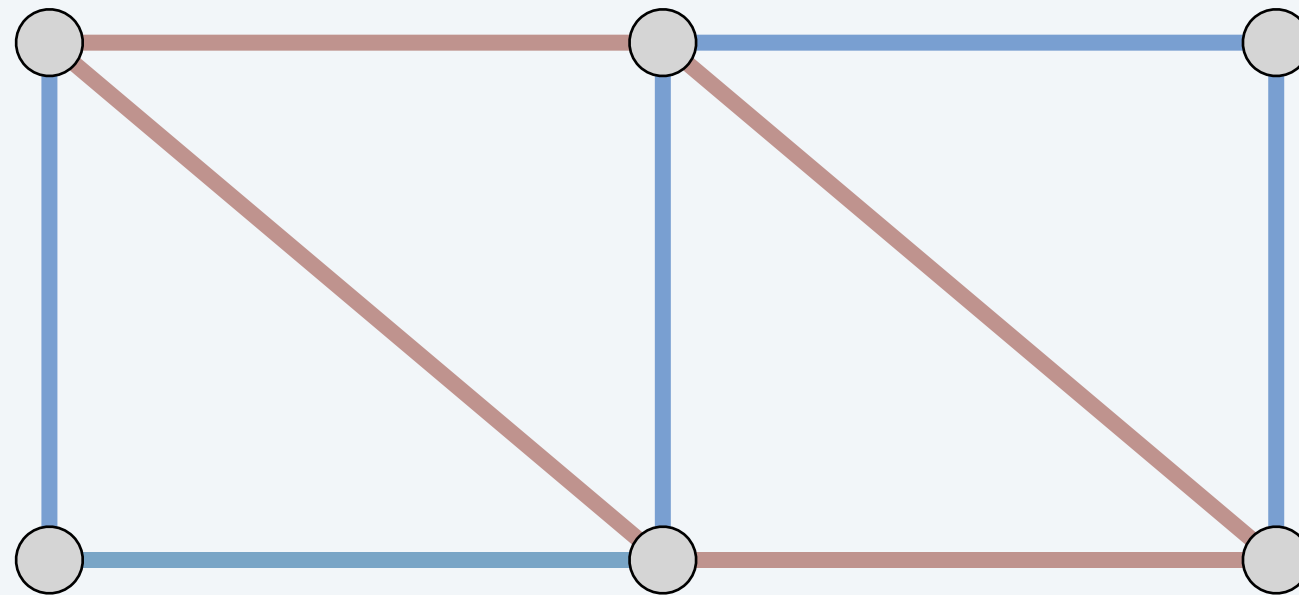
apply the red rule to the cycle



# Red-rule blue-rule demo

---

current set of red and blue edges



# Red-rule blue-rule demo

---

**Greedy algorithm.** Upon termination, the blue edges form a MST.

a minimum spanning tree

