

# **Software Verification & Validation**

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Handout 8

# Acknowledgement

- Some slides in this lecture are adapted from
  - **Paul Ammann and Jeff Offutt's** slides for their textbook **“Introduction to Software Testing”**
  - **Prof. Lori A. Clarke's** slides for her course **“CS521-621 : Advanced Software Engineering: Analysis and Evaluation”** at University of Massachusetts Amherst

# Error Seeding

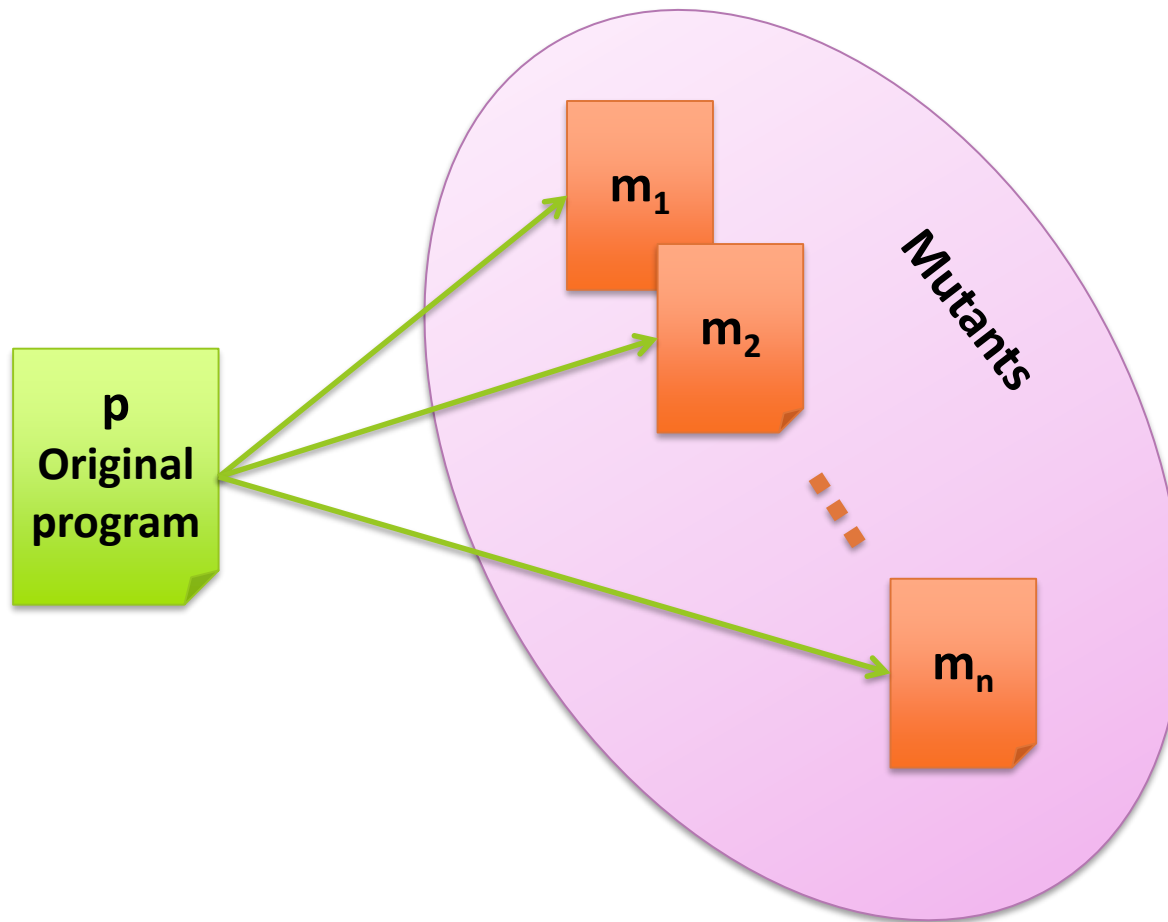
- Intentionally insert faults into a system. Why?
  1. Evaluate the effectiveness of a test set.
    - Suppose  $S$  faults have been seeded.
    - After executing a test set  $T$ ,  $S^*$  out of  $S$  seeded faults are caught by the test.
    - Assuming that seeded faults and actual faults are equally likely to be caught by test  $T$ , then the effectiveness of  $T$  is  $S^*/S$ .
  2. Estimate the number of actual faults.
    - Suppose  $S$  faults have been seeded.
    - After executing a test set  $T$ ,
      - $S^*$  out of  $S$  seeded faults have been caught by the test.
      - $N^*$  actual faults have been caught by the test.
    - Assuming that seeded faults and actual faults are equally likely to be caught by test  $T$ , we may conclude (with a certain confidence) that the number of actual faults is
$$N = (N^*/S^*) \times S$$
  3. Motivate developers/testers
    - Know there is something to find
    - Not looking for their own faults, so more motivated

# Mutation Testing

- Mutation testing is a systematic method of error seeding
  - originally proposed by Budd, Lipton, DeMillo, and Sayward in the mid 1970s
- Approach: considers all simple faults that could occur
  - introduces single faults one at a time to create “mutants” of original program
  - apply test set to each mutant program
  - “test adequacy” is measured by % “mutants killed”

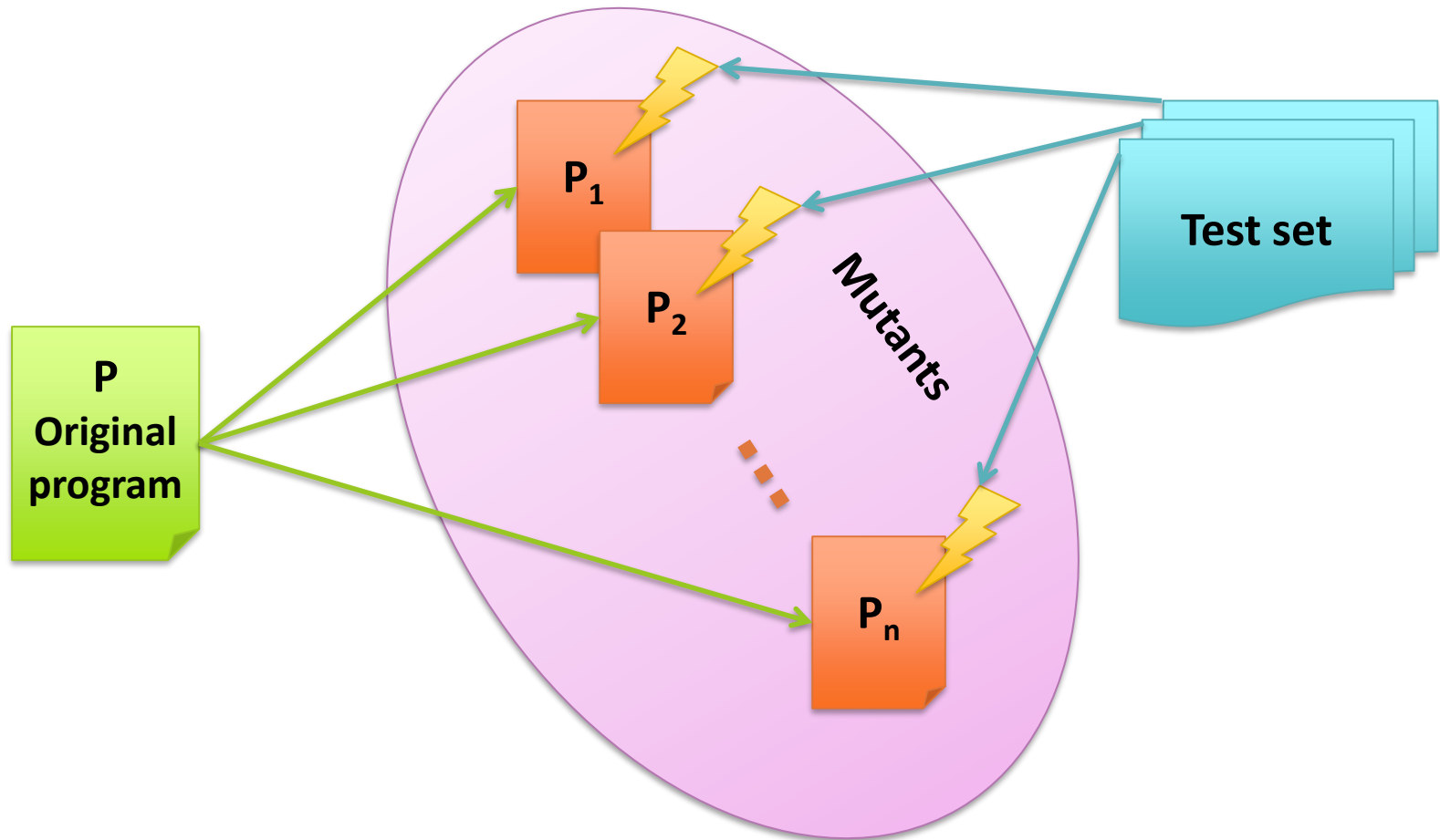
# Mutation Testing

- Mutate original program by inserting a simple fault



# Mutation Testing

- Design a test set to kill each mutant



# Mutation Testing

- Operators modify a program under test to create mutant programs
- Mutant programs must compile correctly
- Mutants are not tests, but used to find or evaluate tests
- Once mutants are defined, tests must be found to cause mutants to fail when executed
- This is called “killing mutants”

# Killing Mutants

Given a mutant  $m \in M$  for a program  $P$  and a test  $t$ ,  $t$  is said to kill  $m$  if and only if the output of  $t$  on  $P$  is different from the output of  $t$  on  $m$ .

- If mutation operators are designed well, the resulting tests will be very powerful
- Different operators must be defined for different programming languages and goals
- Testers can keep adding tests until all mutants have been killed
  - Dead mutant : A test case has killed it
  - Trivial mutant : Almost every test can kill it
  - Equivalent mutant : No test can kill it (equivalent to original program)



# Mutating programs

## Original Method

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < A)
    {
        minVal = B;
    }
    return (minVal);
}
```

**6 mutants**

**Each represents a  
separate program**

## With Embedded Mutants

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    Δ 1 minVal = B;
    if (B < A)
    Δ 2 if (B > A)
    Δ 3 if (B < minVal)
    {
        minVal = B;
    Δ 4 Bomb ();
    Δ 5 minVal = A;
    Δ 6 minVal = failOnZero (B);
    }
    return (minVal);
}
```

*Replace one variable  
with another*

*Changes operator*

*Immediate runtime  
failure ... if reached*

*Immediate runtime  
failure if B==0 else  
does nothing*

# Syntax-Based Coverage Criteria

Mutation Coverage (MC) : For each  $m \in M$ , there is a test case that kills  $m$ .

- Mutant 1 in the Min( ) example is:

```
minVal = A;  
Δ 1 minVal = B;  
  if (B < A) minVal = B;  
  return minVal
```

- Find a test case that kills Mutant 1.
- Find a test case that does not kill Mutant 1.

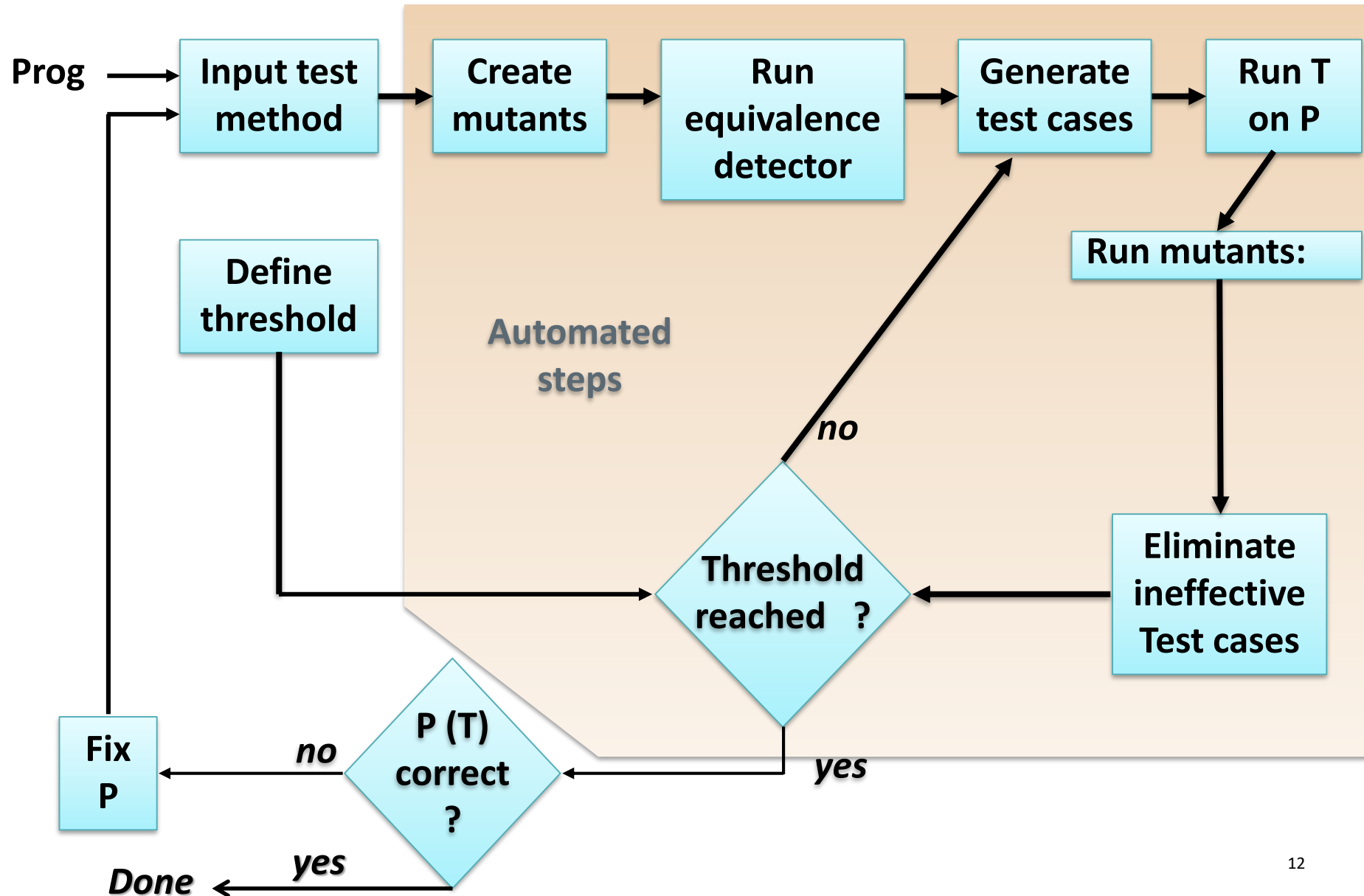
# Equivalent Mutation Example

- Mutant 3 in the Min() example is equivalent:

```
minVal = A;  
if (B < A)  
Δ 3  if (B < minVal)
```

- The infection condition is “ $(B < A) \neq (B < \text{minVal})$ ”
- However, the previous statement was “ $\text{minVal} = A$ ”
  - Substituting, we get: “ $(B < A) \neq (B < A)$ ”
- Thus no input can kill this mutant

# Testing Programs with Mutation



# Why Mutation Works

## Fundamental Premise of Mutation Testing

If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault

- This is not an absolute !
- The mutants guide the tester to a very effective set of tests
- A very challenging problem :
  - Find a fault and a set of mutation-adequate tests that do not find the fault
- Of course, this depends on the mutation operators ...

# Designing Mutation Operators

- At the method level, mutation operators for different programming languages are similar
- Mutation operators do one of two things:
  - Mimic typical programmer mistakes ( incorrect variable name )
  - Encourage common test heuristics ( cause expressions to be 0 )
- Researchers design lots of operators, then experimentally select the most useful.
- The following are some example of mutation operators for Java.

# Mutation Operators for Java

## 1. *ABS* — *Absolute Value Insertion*:

Each arithmetic expression (and subexpression) is modified by the functions *abs()*, *negAbs()*, and *failOnZero()*.

## 2. *AOR* — *Arithmetic Operator Replacement*:

Each occurrence of one of the arithmetic operators  $+$ ,  $-$ ,  $*$ ,  $/$ , and  $\%$  is replaced by each of the other operators. In addition, each is replaced by the special mutation operators *leftOp*, and *rightOp*.

## 3. *ROR* — *Relational Operator Replacement*:

Each occurrence of one of the relational operators ( $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $=$ ,  $\neq$ ) is replaced by each of the other operators and by *falseOp* and *trueOp*.

# Mutation Operators for Java (2)

## 4. *COR* — *Conditional Operator Replacement*:

Each occurrence of one of the logical operators (and - &&, or - || , and with no conditional evaluation - &, or with no conditional evaluation - |, not equivalent - ^) is replaced by each of the other operators; in addition, each is replaced by falseOp, trueOp, leftOp, and rightOp.

## 5. *SOR* — *Shift Operator Replacement*:

Each occurrence of one of the shift operators <<, >>, and >>> is replaced by each of the other operators. In addition, each is replaced by the special mutation operator leftOp.

## 6. *LOR* — *Logical Operator Replacement*:

Each occurrence of one of the logical operators (bitwise and - &, bitwise or - |, exclusive or - ^) is replaced by each of the other operators; in addition, each is replaced by leftOp and rightOp.



# Mutation Operators for Java (3)

## 7. *ASR — Assignment Operator Replacement:*

Each occurrence of one of the assignment operators (`+=`, `-=`, `*=`, `/=`, `%=`, `&=`, `|=`, `^=`, `<<=`, `>>=`, `>>>=`) is replaced by each of the other operators.

## 8. *UOI — Unary Operator Insertion:*

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is inserted in front of each expression of the correct type.

## 9. *UOD — Unary Operator Deletion:*

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is deleted.

# Mutation Operators for Java (4)

## *10. SVR — Scalar Variable Replacement:*

Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

## *11. BSR — Bomb Statement Replacement:*

Each statement is replaced by a special Bomb() function.