

Key points about alpha-beta pruning:

Initially, $\text{Alpha} = -\infty$, $\text{Beta} = +\infty$

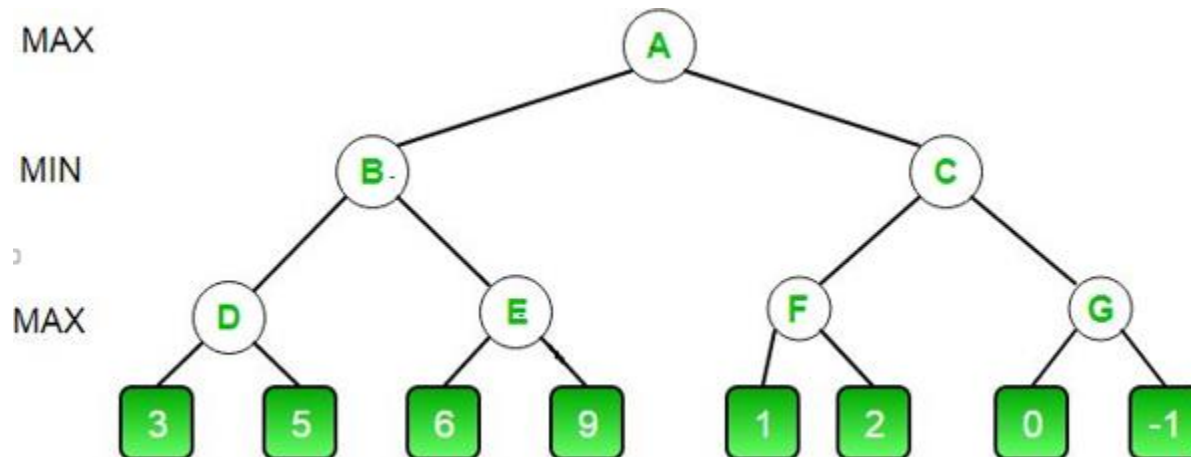
$\text{Alpha} = \max(\text{current_alpha_value}, \text{value_from_child})$

$\text{Beta} = \min(\text{current_beta_value}, \text{value_from_child})$

**$\text{Node_value} = \text{maximum value among children if it's the turn of Max}$
 $= \text{minimum value among children if it's turn of Min}$**

- ☞ The Max player will only update the value of alpha.
- ☞ The Min player will only update the value of beta.
- ☞ While backtracking the tree, the node values will be passed to upper nodes instead of values of alpha and beta.
- ☞ Only alpha and beta values are passed to the child nodes.

Example: Determine the nodes to be pruned from following game tree using Alpha-beta pruning procedure.



➔Solution: The procedure can be depicted as in following table.

Alpha Beta Pruning Example

Step No.	Node	Player	Value of α	Value of β	$\alpha \geq \beta$	Pruning	Node Value	Remarks and Description
1	A	Max	$-\infty$	$+\infty$	False	No	Not Fixed	$\alpha = -\infty$ and $\beta = +\infty$ are passed to a child node, B
2	B	Min	$-\infty$	$+\infty$	False	No	Not Fixed	$\alpha = -\infty$ and $\beta = +\infty$ are passed to a child node, D
3	D	Max	$\max(-\infty, 3) = 3$	$+\infty$	False	No	5	α is updated and backtracking to B. Here, node value 5 is backtracked (passed to B).
			$\max(3, 5) = 5$	$+\infty$	False	No		
4	B	Min	$-\infty$	$= \min(+\infty, 5) = 5$	False	No	Not Fixed	β is updated and Traversing next child of B i.e. E. Here, $\alpha = -\infty$ and $\beta = 5$ are passed to a child node, E
5	E	Max	$\max(-\infty, 6) = 6$	5	True	Yes	6	α is updated, Here $\alpha \geq \beta$ ($6 \geq 5$) so right child of E is pruned. The node value of E is set to 6 and Backtracked to B.
6	B	Min	$-\infty$	5	False	No	5	Node value is set to 5 (minimum of node values of child D and E) and Backtracking to A.
7	A	Max	$\max(-\infty, 5) = 5$	$+\infty$	False	No	Not Fixed	$\alpha = 5$ and $\beta = +\infty$ are passed to a child node, C
8	C	Min	5	$+\infty$	False	No	Not Fixed	$\alpha = 5$ and $\beta = +\infty$ are passed to a child node, F
9	F	Max	$\max(5, 1) = 5$	$+\infty$	False	No	2	α is updated, node value of F is set to 2 and Backtracking to C
			$\max(5, 2) = 5$	$+\infty$	False	No		

Alpha Beta Pruning Example

10	C	Min	5	$\min(+\infty, 2) = 2$	True	Yes	2	β is updated, Here $\alpha \geq \beta$ ($5 \geq 2$) so right child of C i.e. G is pruned. The node value of C is set to 2 which is passed to A.
11	A	Max	$\max(5, 2) = 5$	$+\infty$	False	No	5	At A, best value of A is $= \max(5, 2) = 5$

Hence, Right child of Node E and Right Child of Node C i.e .Node G are pruned from given game tree.