

Exercise 3

```
for (int i = 0; i < 4; ++i) {
    for (int j = 1; j < 4; ++j) {
        a[i + 2][j - 1] = b * a[i][j] + 4;
    }
}
```

(2, 0) -> i = 0 und j = 2 und i = 2 und j = 1

Some true dependencies here:

$a[i + 2][j - 1] = b * a[i][j] + 4;$

from lecture

The **dependence direction vector** $D(\vec{i}, \vec{j})$ is a vector of length n such that

$$D(\vec{i}, \vec{j})_k = \begin{cases} "<" & \text{if } (d(\vec{i}, \vec{j}))_k > 0 \\ "=" & \text{if } (d(\vec{i}, \vec{j}))_k = 0 \\ ">" & \text{if } (d(\vec{i}, \vec{j}))_k < 0 \end{cases}$$

▶ With $d(\vec{i}, \vec{j})_k = j_k - i_k$

Dep	Source	Type	Sink	Dist Vec	Dir Vec	Loop carried	Loop ind.	Dependence carried by loop
Dep1	$a[i+2][j-1]$	True dependency	$a[i][j]$	(2,-1)	(<, >)	x		i, j -loop

$A[i+2][j-1]$ which are actually being read later on: i in interval $[0,4]$ and j in interval $[1,4]$

	$j=1$	2	3	4
$i = 0$	$A[2][0]$	$A[2][1]$	$A[2][2]$	$A[2][3]$
1	$A[3][0]$	$A[3][1]$	$A[3][2]$	$A[3][3]$
2	$A[4][0]$	$A[4][1]$	$A[4][2]$	$A[4][3]$
3	$A[5][0]$	$A[5][1]$	$A[5][2]$	$A[5][3]$
4	$A[6][0]$	$A[6][1]$	$A[6][2]$	$A[6][3]$

The **green** statements

are not dependent and can be parallelized, the **red** ones can't.