## Insertion Sort Example

$$A = 12,9,3,7,14,11$$

$$i = 0, 1, 2, 3, 4, 5$$

for i = 1 to i = 5:

set the key to A[i] (A[1]= 9). Hold the key to create an empty space.

$$A = 12, ,3,7,14,11$$

working with items at indices i-1 -> 0,

while the key is less than each item, move each up by 1 and then put the key in the empty space.

$$A = 9, 12, 3, 7, 14, 11$$
 increment i (now is  $i=2$ )

set the key to A[i] (A[2]= 3). Hold the key to create an empty space.

$$A = 9,12, ,7,14,11$$

working with items at indices i-1 -> 0,

while the key is less than each item, move each up by 1 and then put the key in the empty space.

$$A = 3,9,12,7,14,11$$
 increment i (now is i=3)

set the key to A[i] ( A[3]=7 ). Hold the key to create an empty space.

$$A = 3,9,12, ,14,11$$

working with items at indices i-1 -> 0,

while the key is less than each item, move each up by 1 and then put the key in the empty space.

$$A = 3,7,9,12,14,11$$

increment i (now is i=4)

set the key to A[i] (A[4]= 14). Hold the key to create an empty space.

$$A = 3,9,7,12, ,11$$

working with items at indices i-1 -> 0,

while the key is less than each item, move each up by 1 and then put the key in the empty space.

$$A = 3,7,9,12,14,11$$

increment i (now is i=5)

set the key to A[i] ( A[5]=11 ). Hold the key to create an empty space.

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$$A = 3,9,7,12,14,$$

working with items at indices i-1 -> 0,

while the key is less than each item, move each up by 1 and then put the key in the empty space.

$$A = 3.7.9.11.12.14$$

## Selection Sort Example

$$A = 12,9,3,7,14,11$$

for i = 0 to i = 4:

i=0

find the smallest item by checking all items between i=0 and i=5 (inclusive) and swap the smallest item with the item at at i=0

$$A = 12,9,3,7,14,11$$

$$A = 3,9,12,7,14,11$$

increment i (now is i=1)

find the smallest item by checking all items between i=1 and i=5 (inclusive) and swap the smallest item with the item at at i=1

$$A = 3,9,12,7,14,11$$

$$A = 3,7,12,9,14,11$$

increment i (now is i=2)

find the smallest item by checking all items between i=2 and i=5 (inclusive) and swap the smallest item with the item at at i=2

$$A = 3,7,12,9,14,11$$

$$A = 3,7,9,12,14,11$$

increment i (now is i=3)

find the smallest item by checking all items between i=3 and i=5 (inclusive) and swap the smallest item with the item at at i=3

$$A = 3,7,9,12,14,11$$

$$A = 3,7,9,11,14,12$$

increment i (now is i=4)

find the smallest item by checking all items between i=4 and i=5 (inclusive) and swap the smallest item with the item at at i=4

$$A = 3,7,9,11,14,12$$

$$A = 3,7,9,11,12,14$$

increment i (now is i=5)

the second last item is now sorted and this means that the last item is also sorted. So the sort is complete

## Bubble Sort Example

$$A = 12,9,3,7,14,11$$

$$i = 0, 1, 2, 3, 4, 5$$

for i = 0 to i = 4:

if A[i+1] is less that A[i] swap the two items

$$\overset{i=0}{A} = 12,9,3,7,14,11$$

$$\mathring{A}^{=1} = 9, \underline{12,3}, 7, 14, 11$$

$$\overset{i=2}{A} = 9,3,12,7,14,11$$

$$\overset{i=3}{A} = 9,3,7,12,14,11$$

$$\overset{i=4}{A} = 9,3,7,12,14,11$$

$$A = 9,3,7,12,11,14$$

end of first pass (the last item is certainly in the right place)

for i = 0 to i = 3:

if A[i+1] is less that A[i] swap the two items

$$\overset{i=0}{A} = 9,3,7,12,11,14$$

$$\mathring{A}^{i=1} = 3,9,7,12,11,14$$

$$\overset{i=2}{A} = 3,7,9,12,11,14$$

$$\overset{i=3}{A} = 3,7,9,12,11,14$$

$$A = 3.7.9.11.12.14$$

end of the second pass (the last and second last items are certainly in the right place).

We can note that the array is in fact sorted but the algorithm will need another pass to "know" that it has been sorted.

for i = 0 to i = 2:

if A[i+1] is less that A[i] swap the two items

$$\overset{i=0}{A} = 3,7,9,11,12,14$$

$$A^{i=1} = 3,7,9,11,12,14$$

$$\overset{i=2}{A} = 3,7,9,11,12,14$$

$$A = 3,7,9,11,12,14$$

end of the third pass.

No swaps have occurred so the array must be sorted

## Concept of QuickSort Example

$$A = 12,9,3,7,14,11$$

$$i = 0, 1, 2, 3, 4, 5$$

choose the last item of the array as the "pivot".

arrange the list so that all items to the left of the pivot are less than (or =) the pivot and all items to the right of the pivot are greater than the pivot.

partition the array into sub-divisions above and below the pivot

for each sub-division, choose the last item as the "pivot". arrange each sub-divided array so that all items to the left of the pivot are less than (or =) the pivot and all items to the right of the pivot are greater than the pivot.

$$12,9,3,7,14,\underline{11}$$

$$9,3,7,\underline{11},14,12$$

$$\downarrow \qquad \qquad \downarrow$$

$$9,3,\underline{7} \qquad 14,\underline{12}$$

$$3,\underline{7},9 \qquad \underline{12},14$$

$$A = 3,7,9,11,12,14$$

the process is continued unless the subdivision is size = 1