

12 Animation Frame

12.1 A bit of a code review - preparation

You do not need to have exactly this.

```
1 // init file with canvas set up
2 // colours
3 // functions
4 //...
5 canvas = document.querySelector('#myCanvas');
6 let ctx = canvas.getContext('2d');
7 // define width and height
8 let width = 1000;
9 let height = 600;
10 // define scale of 1. This may be changed later to improve resolution
11 let scale = 2;
12 // set the canvas width and height
13 canvas.width = width*scale;
14 canvas.height = height*scale;
15 // scale the canvas
16 ctx.scale(scale, scale);
17 // get the canvas element
18 // style it here so it will be consistent
19 let my_c = document.getElementById('myCanvas');
20 my_c.style.backgroundColor = "rgb(100,100,100)";
21 my_c.style.width = width+"px";
22 my_c.style.height = height+"px";
23 my_c.style.border = "6px solid rgba(200,200,200,0.5)";
24 my_c.style.display = "block";
25 my_c.style.margin = "auto";
26 document.body.style.backgroundColor = "rgb(190,190,190)";
27
28
29 // two dimensional array of colours
30 const col= [
31     [ // opaque
32         // black (0)           grey (1)           white (2)
33         "rgba(0,0,0,1)" , "rgba(150,150,150,1)", "rgba(255,255,255,1)" ,
34         // pink (3)           purple (4)           deep blue (5)
35         "rgb(243,92,155,1)", "rgb(153,19,206,1)", "rgb(16,16,162,1)",
36         // pale blue (6)           yellow (7)           bright yellow (7)
37         "rgba(135,211,243,1)", "rgba(246,244,193,1)", "rgba(250,250,0,1)"
38     ],
39     [ // semi-transparent
```

```

40 // black (0)                grey (1)                white (2)
41     "rgba(0,0,0,0.5)" , "rgba(150,150,150,0.5)", "rgba(255,255,255,0.5)" ,
42 // pink (3)                purple (4)                deep blue (5)
43     "rgb(243,92,155,0.5)", "rgb(153,19,206,0.5)", "rgb(16,16,162,0.5)",
44 // pale blue (6)                yellow (7)                bright yellow (7)
45     "rgba(135,211,243,0.5)", "rgba(246,244,193,0.5)", "rgba(250,250,0,0.5)"
46 ]
47 ]

```

Listing 13: init

It is good to have a grid object and a textbox object.

Let's also start doc typing.

```

1 /**
2  * Grid - draws a square grid of given interval width
3  * across the whole canvas
4  * @param {number} w width of canvas
5  * @param {number} h height of canvas
6  * @param {number} intervalWidth distance each grid unit
7  * @param {string} strokeColour stroke colour
8  * @param {number} strokeWidth width of outline
9  */
10 class Grid{
11     constructor(w,h,intervalWidth, strokeColour, strokeWidth){
12         this.w = w;
13         this.h = h;
14         this.intervalWidth=intervalWidth;
15         this.strokeColour = strokeColour;
16         this.strokeWidth = strokeWidth;
17     }
18     update(){
19         this.draw()
20     }
21     draw(){
22         // these loops also draw the grid outside (as is useful when analysing
translations
23         // and rotations (so your can ignore the negatives and use 0 instead
24         // a loop for the vertical lines
25         for(let i = -this.w ; i <= this.w ; i+= this.intervalWidth){
26             this.drawLine(i,-this.h, i,this.h, this.strokeColour, this.
strokeWidth);
27         }
28         // a loop for the horizontals
29         for(let j = -this.h ; j <= this.h ; j+= this.intervalWidth){
30             this.drawLine(-this.w,j, this.w,j, this.strokeColour, this.
strokeWidth);
31         }

```

```

32     }
33     drawLine(x_1,y_1, x_2, y_2, strokeColour,strokeWidth){
34         ctx.beginPath();
35         ctx.moveTo(x_1,y_1);
36         ctx.lineTo(x_2,y_2);
37         ctx.lineCap = "round";
38         ctx.strokeStyle = strokeColour;
39         ctx.lineWidth = strokeWidth;
40         ctx.stroke()
41     }
42 }
43
44 /**
45  * A little textbox (text on coloured rectangle)
46  * @param {number} x top corner of bounding box
47  * @param {number} y top corner of bounding box
48  * @param {number} w width
49  * @param {string} txt text
50  * @param {string} fill fill colour
51  * @param {string} txtColour colour of text
52  */
53 class TextBox{
54     constructor(x,y,width, fillColour, txtColour) {
55         this.x = x;
56         this.y = y;
57         this.w = width;
58         // fixed height
59         this.h = 50;
60         // text managed through update
61         this.txt = "Placeholder";
62         console.log(this.txt)
63         this.fillColour = fillColour;
64         this.txtColour = txtColour;
65     }
66     // the text can be changed using the update function
67     update(txt ="Placeholder"){
68         this.txt = txt
69         this.draw()
70     }
71     draw(){
72         ctx.beginPath();
73         ctx.rect(this.x,this.y,this.w,this.h);
74         ctx.fillStyle= this.fillColour;
75         ctx.fill();
76         ctx.font = "20px monospace";
77         ctx.textAlign = "center";
78         ctx.textBaseline = "middle";

```

```

79     ctx.fillStyle = this.txtColour;
80     ctx.fillText(this.txt, this.x+this.w/2, this.y+this.h/2);
81 }
82 }

```

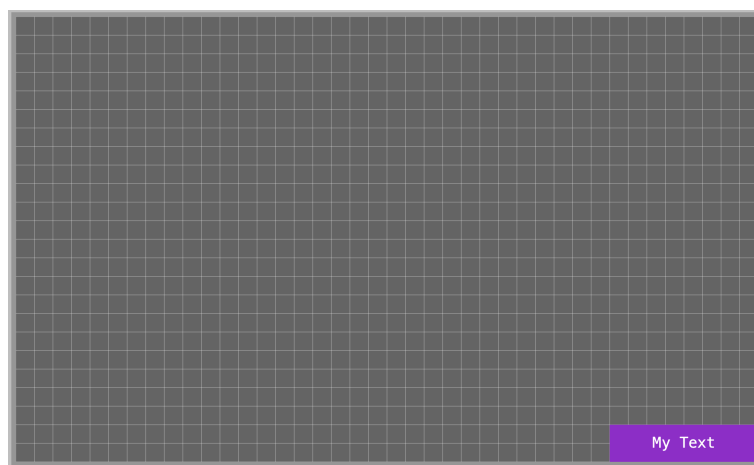
Listing 14: objects

```

1 <!DOCTYPE html>
2 <html lang="en">
3 <head>
4   <meta charset="UTF-8">
5   <meta name="viewport" content="width=device-width, initial-scale=1.0">
6   <meta http-equiv="X-UA-Compatible" content="ie=edge">
7   <title>Objects Start</title>
8 </head>
9 <body>
10 <canvas id='myCanvas'></canvas>
11 <script type="text/javascript" src="init.js"> </script>
12 <script type="text/javascript" src="objects.js"> </script>
13 <script>
14   let G = new Grid(width, height, 25, col[0][2], 0.3)
15   let T = new TextBox(800,550,200, col[0][4], col[0][2])
16   G.update();
17   // note that the text is set through the update function call
18   T.update("My Text");
19
20 </script>
21 </body>
22 </html>

```

Listing 15: index (note text being set using update function call)



12.2 Introduce the animation frame

We can create a function, `animate`.

At the end of, and in, the function we have the `'window.requestAnimationFrame()'`, in the parameter you put the `'animate'` function.

This means that, at the browser's discretion the function will be called over and over again. This should happen somewhere between 50 - 60 times persecond.

We don't give `animate` any parameter, but a parameter is sent (let's call it `'t'`) and can be used.

In this case it is the number of milliseconds since the animation began.

Inside the `animate` function , the first thing we do is erase the canvas and then redraw what we want after that.

This will give us 'frame-by-frame' animation.

```
1 <script>
2   let G = new Grid(width, height, 25, col[0][2], 0.3)
3   let T = new TextBox(800,550,200, col[0][4], col[0][2])
4   // create an animation function
5   function animate(t){
6       ctx.clearRect(0,0, width, height);
7       G.update();
8       let timer = Math.round(t)
9       T.update(timer);
10      // the call below is a request to the browser
11      // the function is called again (about 50 times a second)
12      window.requestAnimationFrame(animate)
13  }
14  // start off call to get it going
15  animate()
16 </script>
```

Listing 16: index



13 Animation

13.1 Linear Interpolation

Consider the graph below.

The graph runs of a interval of T and moves between a maximum height of H and a minimum of 0.

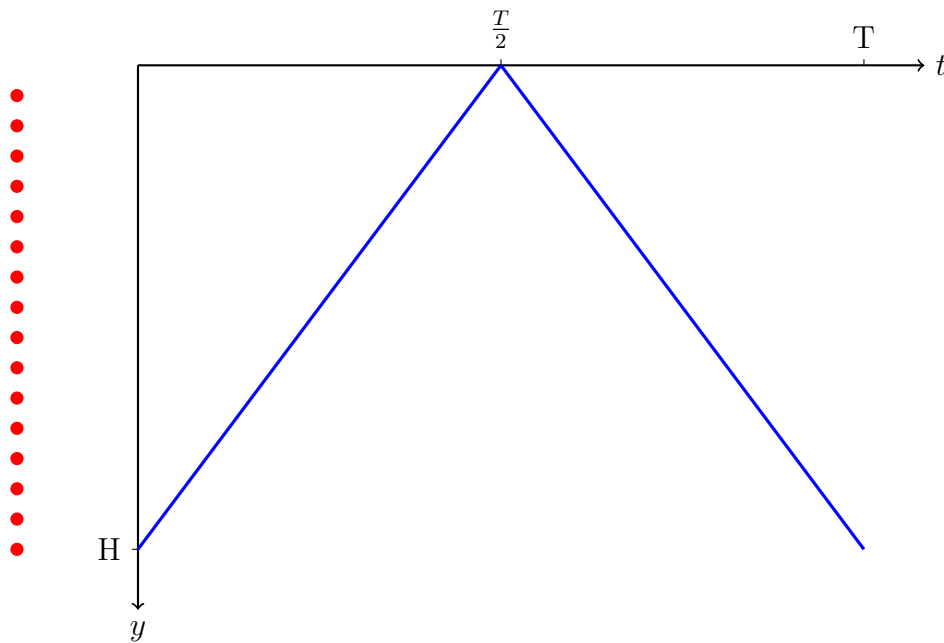
We could use this to represent a, very simple, motion of a ball going up and down.

If we keep repeating the interval, the ball would go up and down indefinitely.

The lower case t represents the ‘time ticks’ and is like the x value.

The equations for this piecewise graph are given below and you should be able to work these out for yourself.

The graph has been drawn upside down, so it is like the canvas co-ordinate system



$$\begin{cases} y = \frac{-2Ht}{T} + H & , \quad 0 < t \leq \frac{T}{2} \\ y = \frac{2Ht}{T} - H & , \quad \frac{T}{2} < x \leq T \end{cases}$$

We have an animation frame that runs at somewhere between 40 and 60 time ticks per second.

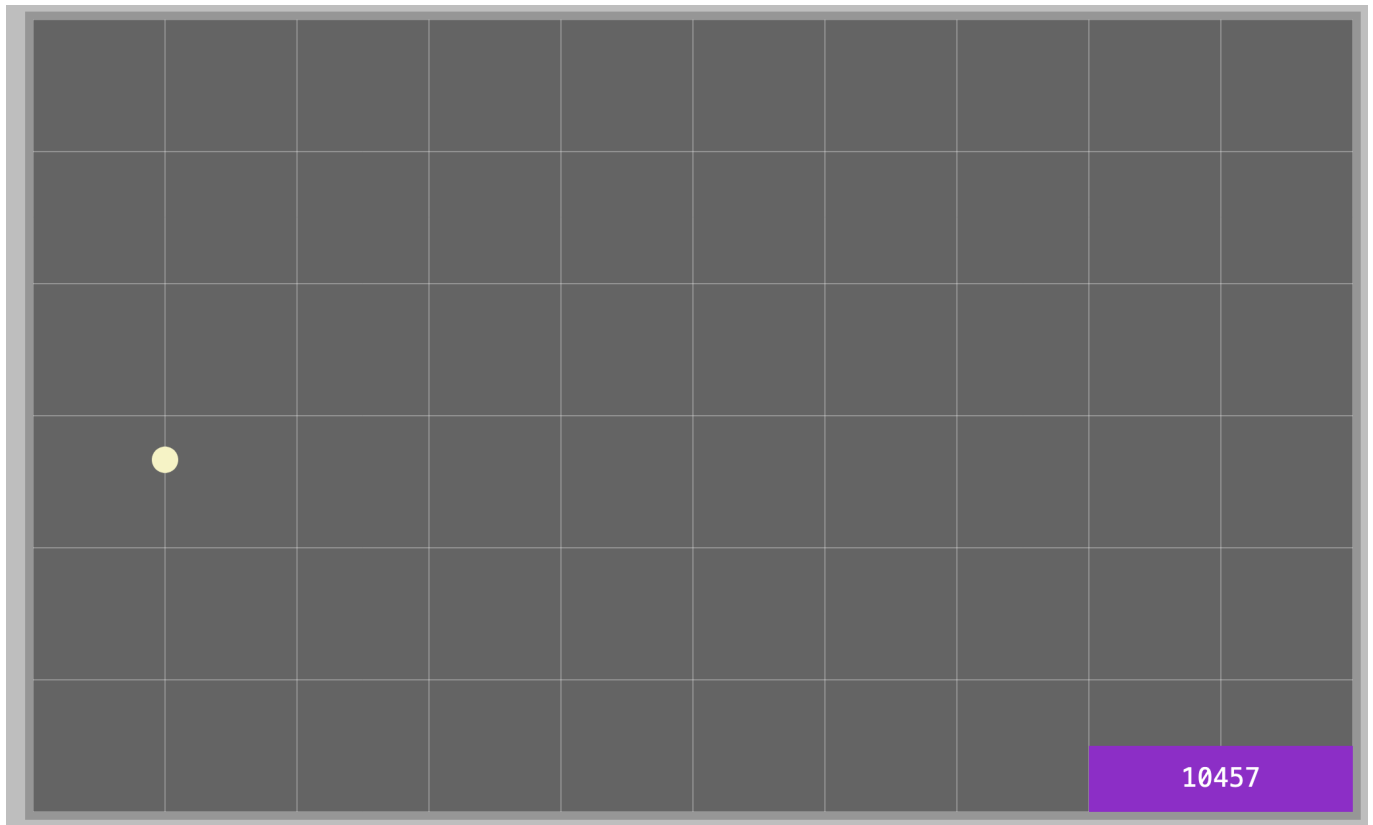
So we should be able to implement the functions given about and update the t value, for every tick of the animation frame.

Moving Ball Object

```
1 /**
2  * Ball that moves up down
3  * @param {number} x_b base x position
4  * @param {number} y_b base y position
5  * @param {number} radius radius
6  * @param {string} fillColour fill colour
7  * @param {number} T total Tick interval (50 ticks = about 1 second)
8  * @param {number} H total Height covered by up/down motion
9  */
10 class MovingBall{
11     constructor(x_b,y_b,r, fillcolour, T, H){
12         this.x_b = x_b;
13         this.y_b = y_b;
14         this.r = r;
15         this.fillColour = fillcolour;
16         // animation variables
17         this.t = 0;
18         this.T = T;
19         this.H = H;
20     }
21     update(){
22         // add one to the value of little t each time update is called
23         this.t +=1
24         this.draw()
25     }
26     draw(){
27         // get y value from the piecewise function
28         let y = this.linearinterpolate(this.t, this.T, this.H)
29         this.drawCircle(this.x_b,y+this.y_b, this.r)
30     }
31
32     linearinterpolate(t,T,H){
33         // takes parameter t , T, H
34         // we could hard code in this.T etc but is more flexible to have
35         parameters
36         // make sure t is between 0 and T
37         t = t%T; // modulus operator
38         // set y variable and use to get value from equations
39         let y;
40         if(t<T/2){
41             y = (-2*H*t)/(T) + H
42         }else{
43             y = (2*H*t)/(T) - H
44         }
45         return y
46     }
47 }
```

```
45     }  
46     drawCircle(x,y,r){  
47         ctx.beginPath()  
48         ctx.arc(x, y, r, 0, 2*Math.PI)  
49         ctx.fillStyle = this.fillColour  
50         ctx.fill();  
51     }
```

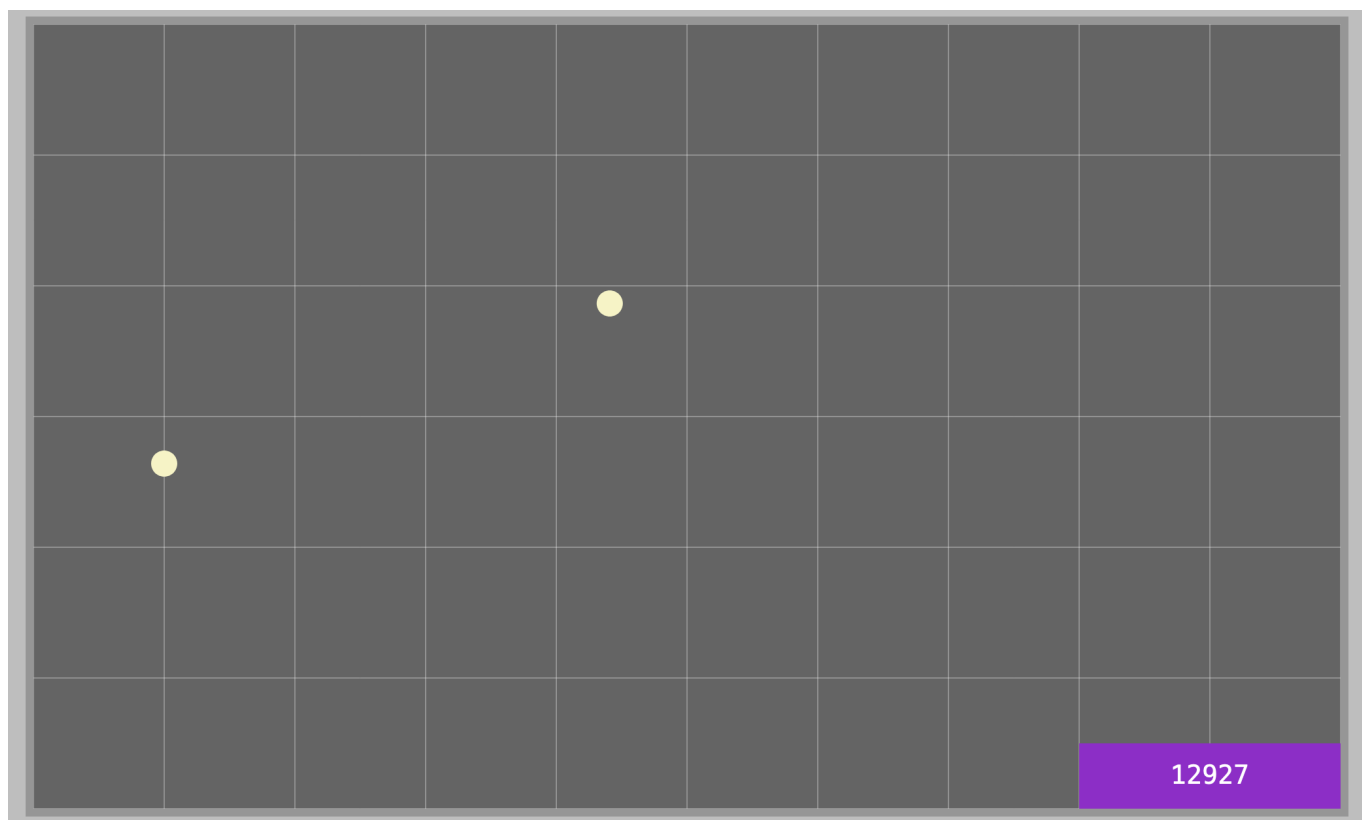
Listing 17: Moving Ball



We can introduce left right motion.

```
1  */
2  class MovingBallBoth{
3      constructor(x_b,y_b,r, fillcolour, T, H, xIS){
4          this.x_b = x_b;
5          this.y_b = y_b;
6          this.r = r;
7          this.fillColour = fillcolour;
8          // animation variables
9          // set a random starting point (while be helpful when we have lots of
moving balls)
10         this.t = T*Math.random();
11         this.T = T;
12         this.H = H;
13         // introduce an interval shift for the x interval
14         // this will make the ball behave more naturalistically
15         this.xIntervalShift = xIS
16     }
17     update(){
18         // add one to the value of little t each time update is called
19         this.t +=1
20         this.draw()
21     }
22     draw(){
23         // get y value from the piecewise function
24         let y = this.linearinterpolate(this.t, this.T, this.H)
25         // the interval is multiplied by the x interval shift
26         let x = this.linearinterpolate(this.t, this.T*this.xIntervalShift, this.H
27     )
        this.drawCircle(x+this.x_b,y+this.y_b, this.r)
```

Listing 18: Part of Bothways Moving Ball



Introduce a whole group (or field) of moving balls.

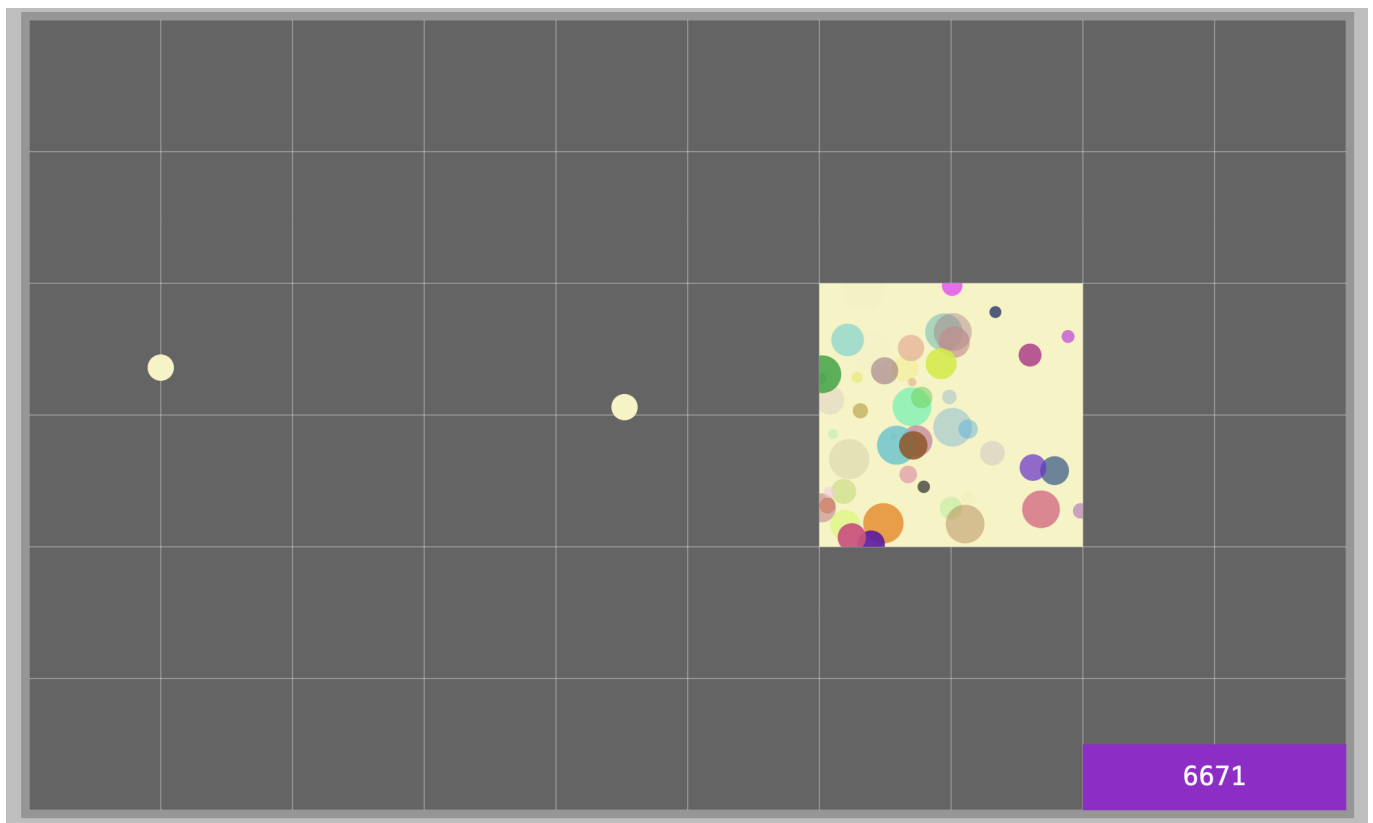
```
1 /**
2  * Block of moving balls
3  * @param {number} x_b base x position
4  * @param {number} y_b base y position
5  * @param {number} radius radius
6  * @param {string} fillColour fill colour
7  * @param {number} T total Tick interval (50 ticks = about 1 second)
8  * @param {number} H total Height covered by up/down motion
9  */
10 class BallGroup{
11     constructor(x_b,y_b,r, fillColour, T, H){
12         this.x_b = x_b
13         this.y_b = y_b
14         this.H = H
15         this.fillColour = fillColour
16         // create a list that is going to hold a whole set of ball objects
17         this.BSet = []
18         //run a loop (in this case x50)
19         for(let i=0; i<50; i++){
20             // randomly set the amount of x interval shift
21             let xIS = 1+5*Math.random()
22             // randomly adjust the interval
23             let randT = T + 2*T*Math.random()
24             // create random red, green, blue
25             let red = 255*Math.random();
26             let green = 255*Math.random();
27             let blue = 255*Math.random();
28             // create random transparency
29             let alpha = Math.random();
30             // concatenate to make a rgb string
31             let randColour = "rgba("+ red + ","+ green + ","+ blue + ","+ alpha
32             +")"
33             // randomly adjust the radius size
34             let radius = r*7*Math.random()+r
35             // create a moving ball using these values
36             let temp = new MovingBallBoth(x_b,y_b,radius, randColour, randT, H,
37             xIS)
38             // push it into the BSet list
39             this.BSet.push(temp)
40         }
41     }
42     update(){
43         // this is an extra bit
44         // save the canvas
```

```

43     ctx.save()
44     // draw and fill a background rectangle
45     this.drawRect(this.x_b, this.y_b, this.H, this.H)
46     // the clip method will "clip out" anything outside the rectangle
47     ctx.clip()
48     // run a loop through the BSet
49     for(let i=0; i<this.BSet.length ; i++){
50         // call update on each moving ball
51         this.BSet[i].update()
52     }
53     // restore the context (this removes the clip)
54     ctx.restore()

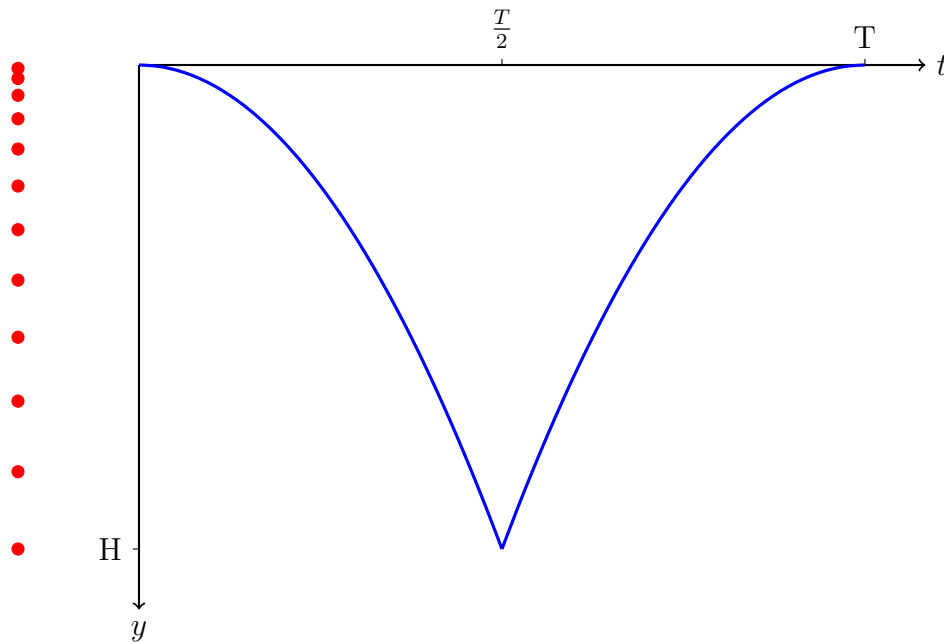
```

Listing 19: Field of moving balls



13.2 Quadratic Interpolation

We can follow the same idea using parabolas:



$$\begin{cases} y = \frac{4Ht^2}{T^2} & , \quad 0 < t \leq \frac{T}{2} \\ y = \frac{4H(t-T)^2}{T^2} & , \quad \frac{T}{2} < t \leq T \end{cases}$$

In this case, we would have the up down motion as quadratic, and the the left right as linear.

Below is the code for a Quadratic Ball Class.

Notice how short it is. What's going on here?

```

1 class QuadraticBall extends MovingBallBoth{
2     draw(){
3         // get y value from the piecewise function
4         let y = this.quadraticInterpolate(this.t, this.T, this.H)
5         // the interval is multiplied by the x interval shift
6         let x = this.linearinterpolate(this.t + this.T*this.xIntervalShift/2, this
7         .T*this.xIntervalShift, this.H)
8         this.drawCircle(x+this.x_b,y+this.y_b, this.r)
9     }
10    quadraticInterpolate(t,T,H){
11        // takes parameter t , T, H
12        // we could hard code in this.T etc but is more flexibile to have
13        parameters
14        // make sure t is between 0 and T
15        t = t%T; // modulus operator
16        // set y variable and use to get value from equations

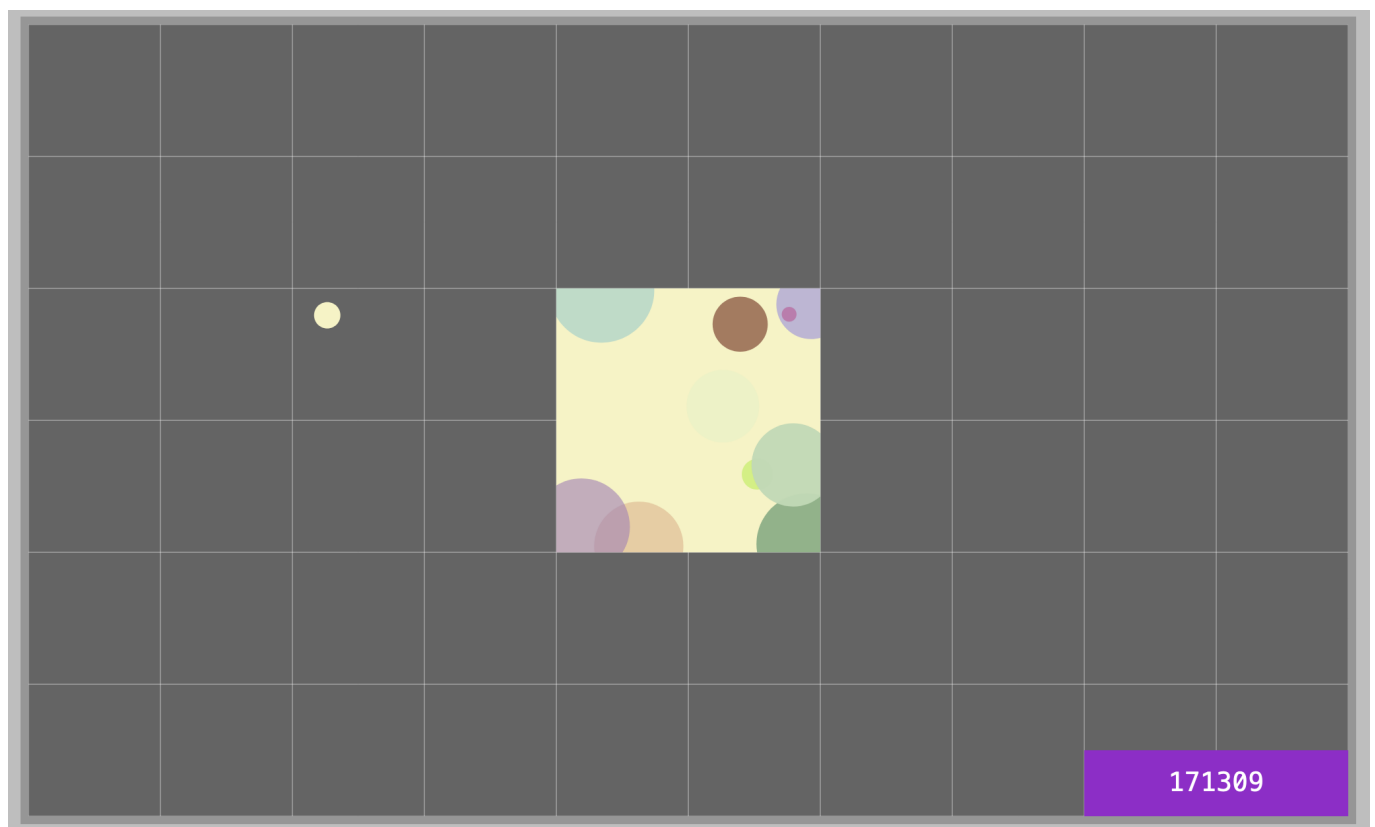
```

```

15     let y;
16     if(t<T/2){
17         y = ( 4*H*Math.pow(t,2) )/( Math.pow(T,2) )
18     }else{
19         y = ( 4*H*Math.pow(t-T,2) )/( Math.pow(T,2) )
20     }
21     return y
22 }
23 }

```

Listing 20: Quadratic Ball Class



A small rewrite has been done on the QuadraticBallGroup Class.

This will mean it can be extended in the next section.

```

1     let radius = r*10*Math.random()+r
2     // create a moving ball using these values
3     let temp = this.getObject(x_b,y_b,radius, randColour, randT, H, xIS)
4     // push it into the BSet list
5     this.BSet.push(temp)
6 }
7
8 getObject(x_b,y_b,radius, randColour, randT, H, xIS){
9     return new QuadraticBall(x_b,y_b,radius, randColour, randT, H, xIS)
10 }

```

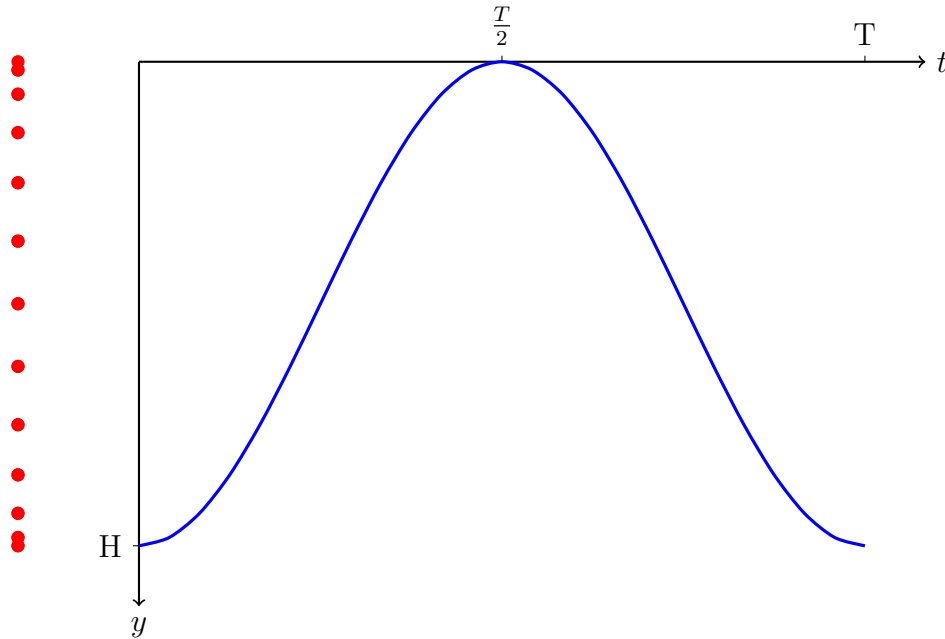
11

```
update() {
```

Listing 21: Quadratic Ball Class

13.3 Trigonometric Interpolation

We can follow the same idea using parabolas:



$$y = \frac{H}{2} \cos\left(\frac{2\pi}{T}t\right) + \frac{H}{2}$$

Complete code for both the TrigBall class and TrigBallGroup class (both are inheriting from the class referred to in the extension).

```

1  /**
2   * Ball that moves trigonometrically
3   * @param {number} x_b base x position
4   * @param {number} y_b base y position
5   * @param {number} radius radius
6   * @param {string} fillColour fill colour
7   * @param {number} T total Tick interval (50 ticks = about 1 second)
8   * @param {number} H total Height covered by up/down motion
9   * @param {number} xIS x interval shift (to make a different interval for left
10   *   right movement
11  */
12  class TrigBall extends MovingBallBoth{
13      draw(){
14          // get y value from the piecewise function
15          let y = this.trigInterpolate(this.t, this.T, this.H)
16          // the interval is multiplied by the x interval shift
17          // see what happens with this commented out code
18          //let x = this.trigInterpolate(this.t + this.T/4, this.T, this.H)
19          let x = this.linearinterpolate(this.t + this.T*this.xIntervalShift/2, this
20          .T*this.xIntervalShift, this.H)

```



```

19         this.drawCircle(x+this.x_b,y+this.y_b, this.r)
20     }
21     trigInterpolate(t,T,H){
22         let y = (H/2) * Math.cos( (2*Math.PI/T) *t) + H/2
23         return y
24     }
25 }
26 /**
27  *Group of trigonometrically moving balls
28  * @param {number} x_b base x position
29  * @param {number} y_b base y position
30  * @param {number} radius radius
31  * @param {string} fillColour fill colour
32  * @param {number} T total Tick interval (50 ticks = about 1 second)
33  * @param {number} H total Height covered by up/down motion
34  */
35 class TrigBallGroup extends QuadraticBallGroup{
36     getObject(x_b,y_b,radius, randColour, randT, H, xIS){
37         return new TrigBall(x_b,y_b,radius, randColour, randT, H, xIS)
38     }
39 }

```

Listing 22: Quadratic Ball Class

