



Predicting Dynamic Embedding Trajectory in Temporal Interaction Networks



Srijan Kumar

Stanford University

Georgia Institute of Technology

Xikun Zhang

UIUC

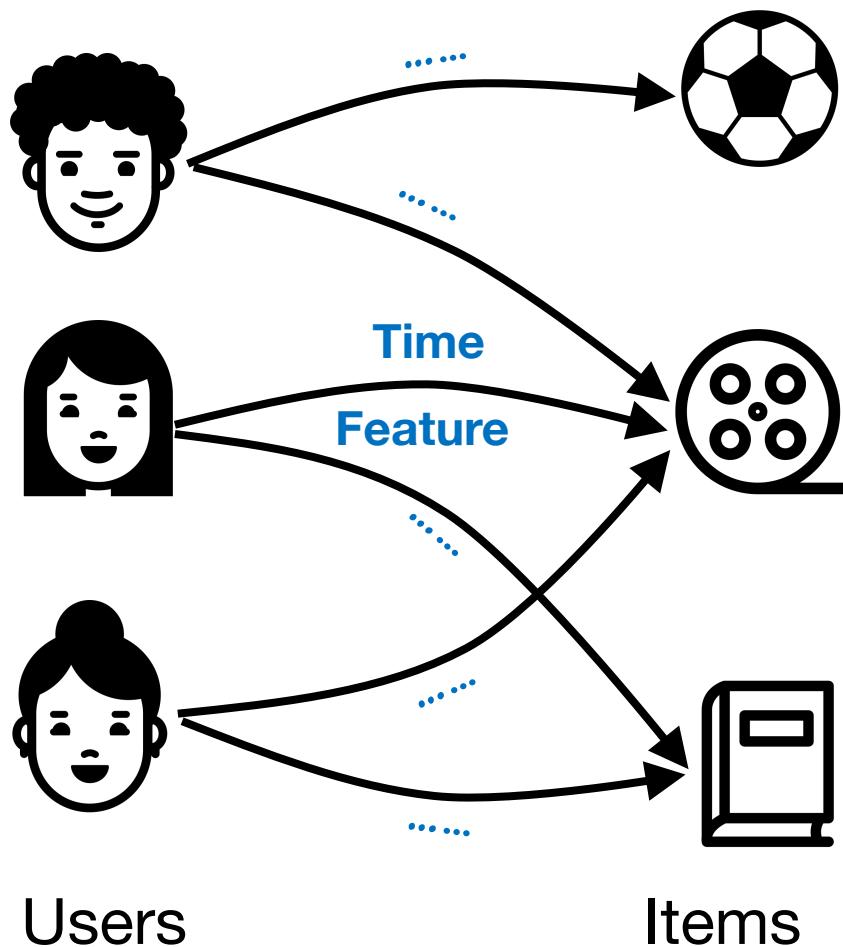
Jure Leskovec

Stanford University

Code and Data: <https://snap.stanford.edu/jodie>

Temporal Interaction Networks

Flexible way to represent time-evolving relations



Represented as a sequence of interactions, sorted by time:

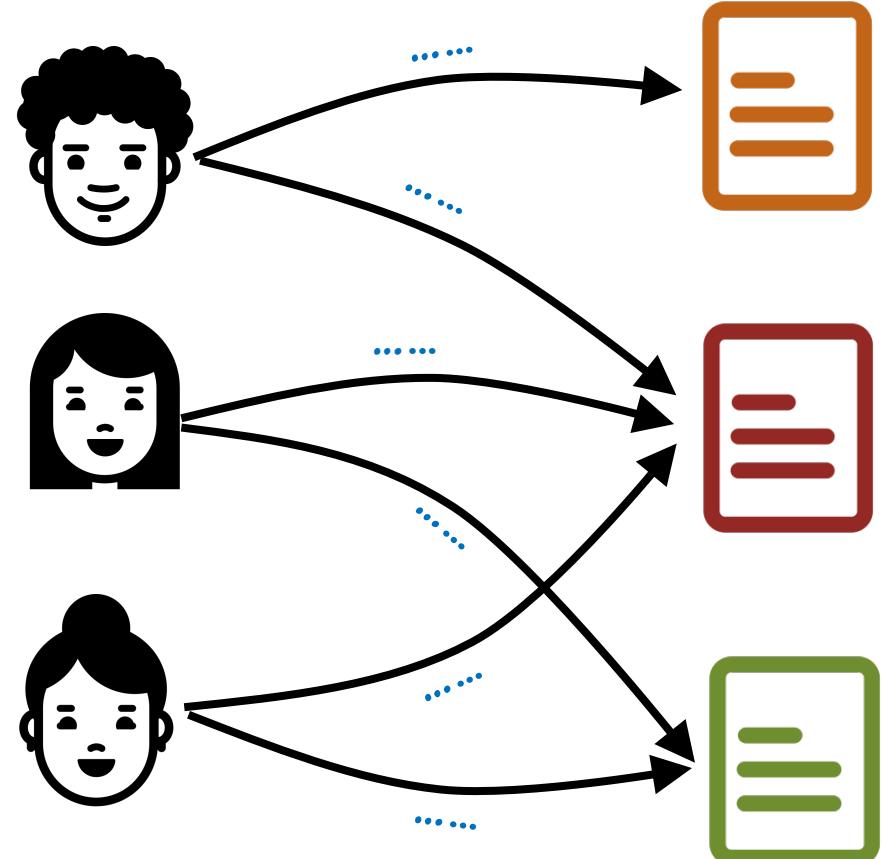
$$S_r = (u_r, i_r, t_r, f_r)$$

↑
interaction user item time features

Temporal Interaction Networks



Application domains



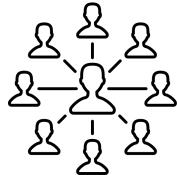
Accounts

Posts

Temporal Interaction Networks



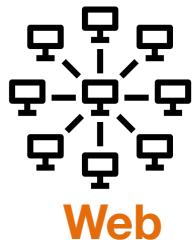
E-commerce



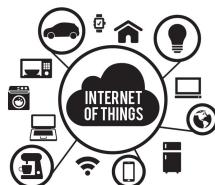
Social media



Education



Web

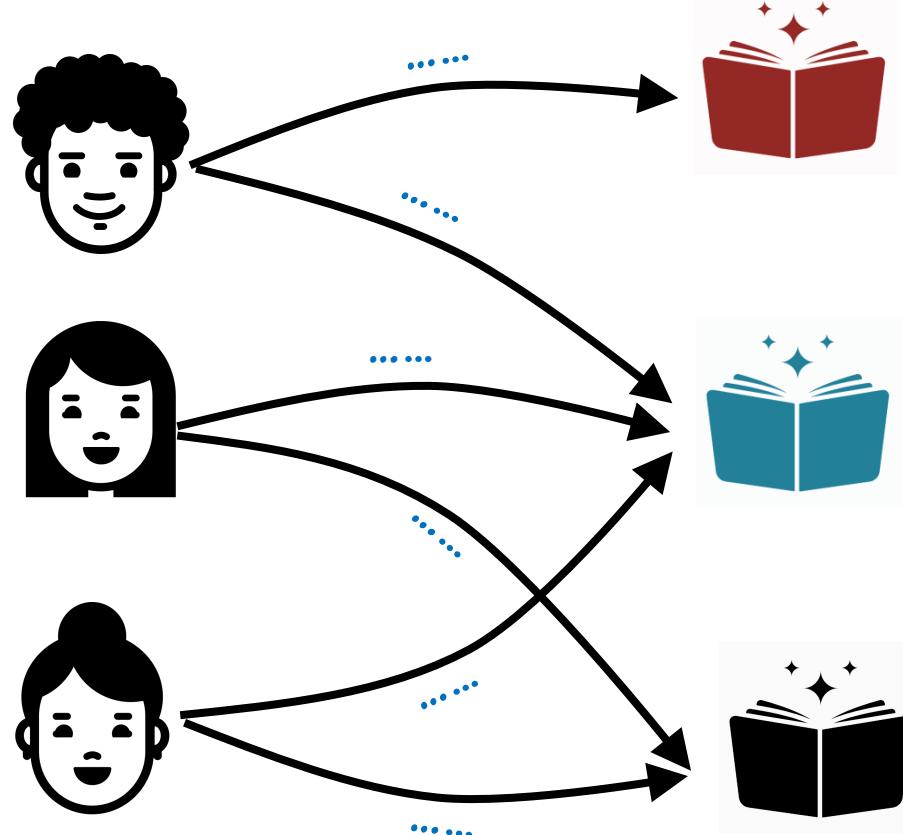


IoT



Finance

Application domains



Students

Courses

Problem Setup

Given a temporal interaction network

$$S_r = (u_r, i_r, t_r, f_r)$$

↑ ↑ ↑ ↑
interaction user item time features

where $u_r \in \mathcal{U}, i_r \in \mathcal{I}, t_r \in \mathbb{R}^+, 0 < t_1 \leq \dots \leq T, f_r \in \mathbb{R}^d$

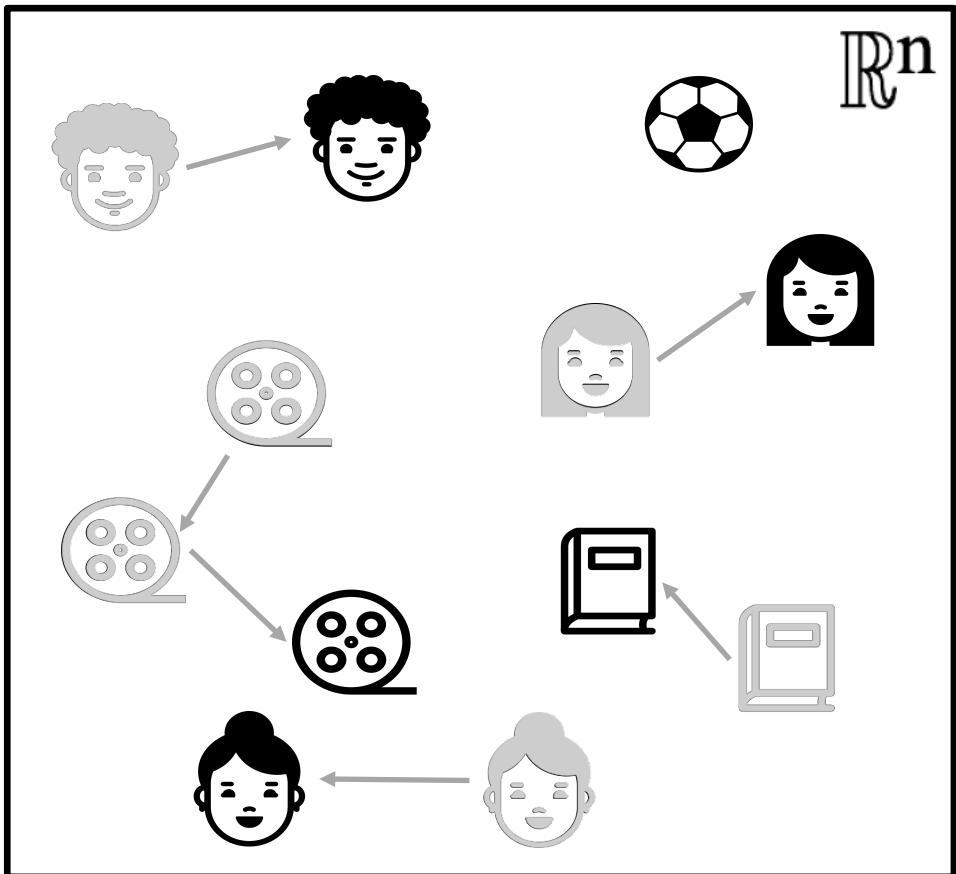
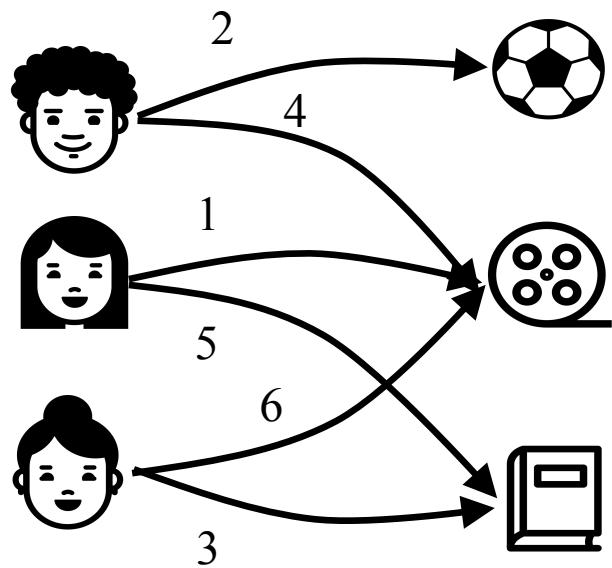
generate an embedding trajectory of every user

$$\mathbf{u}(t) \in \mathbb{R}^n \quad \forall u \in \mathcal{U}, \forall t \in [0, T]$$

and an embedding trajectory of every item

$$\mathbf{i}(t) \in \mathbb{R}^n \quad \forall i \in \mathcal{I}, \forall t \in [0, T]$$

Goal: Generate Dynamic Trajectory



Input: Temporal
interaction network

Output: Dynamic trajectory
in embedding space

Challenges

Challenges in modeling:

- **C1:** How to learn inter-dependent user and item embeddings?
- **C2:** How to generate embedding for every point in time?

Challenges in scalability:

- **C3:** How to scalably train models on temporal networks?

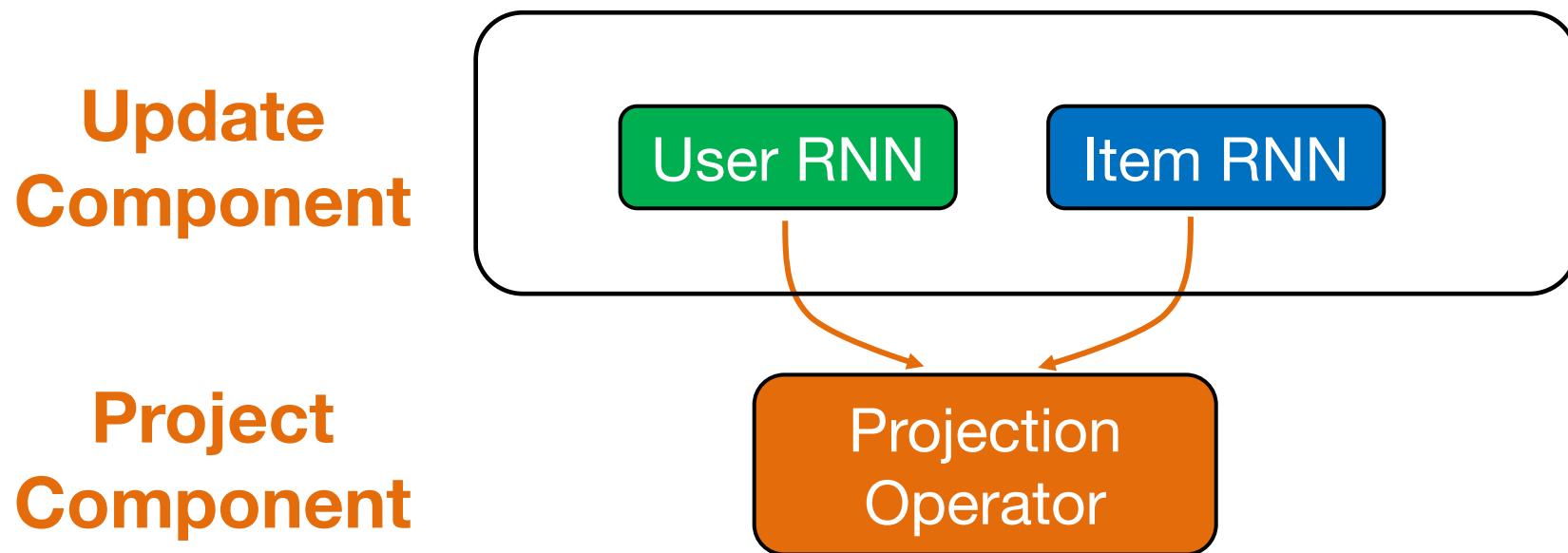
Existing Methods

	C1 Co-influence	C2 Embed any time	C3 Train in batches
Deep recommender systems			✓
Dynamic co-evolution	✓		
Temporal network embedding	✓		✓
Our model: JODIE	✓	✓	✓

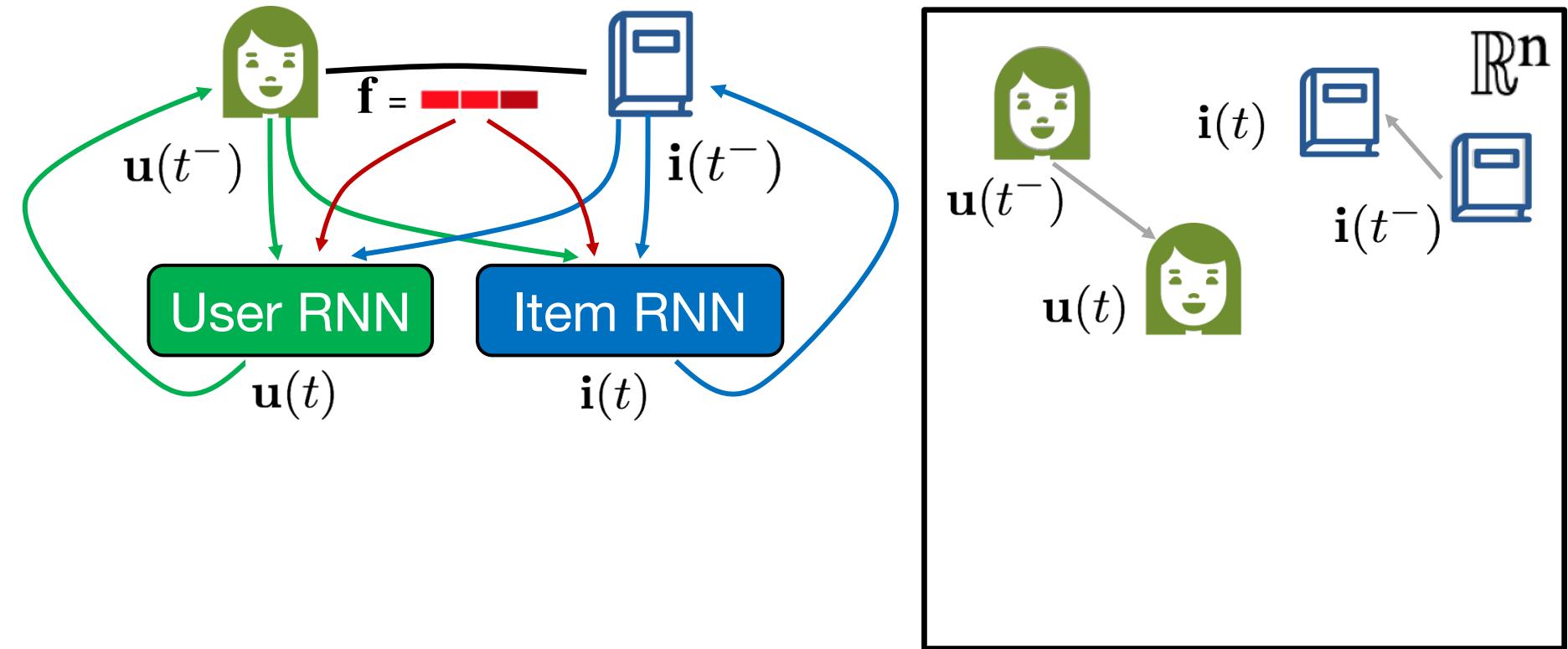
Our Model: JODIE

JODIE: Joint Dynamic Interaction Embedding

- Mutually-recursive recurrent neural network framework



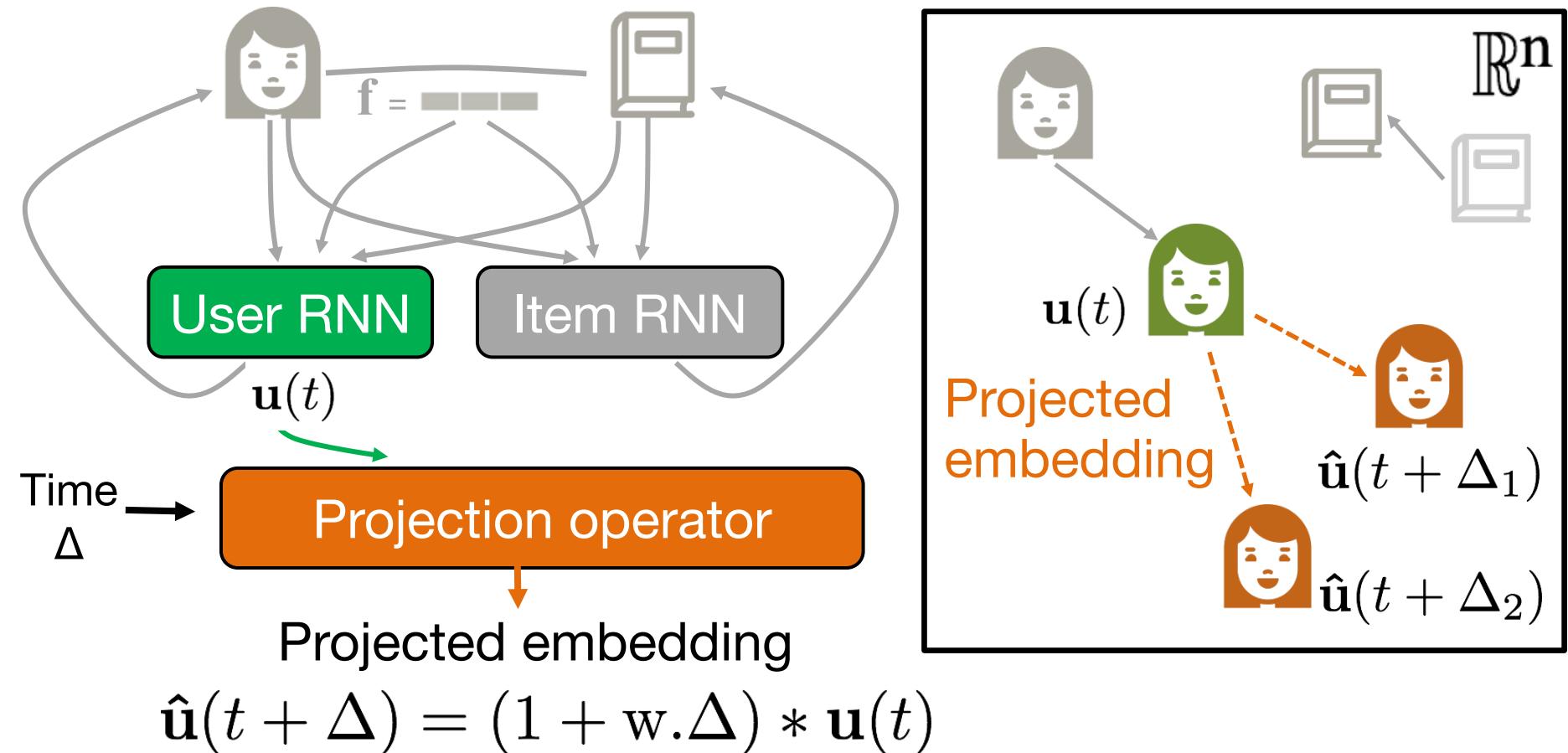
JODIE: Update Component



$$\begin{aligned} \mathbf{u}(t) &= \sigma(W_1 \mathbf{u}(t^-) + W_2 \mathbf{i}(t^-) + W_3 \mathbf{f}) \\ \mathbf{i}(t) &= \sigma(W_4 \mathbf{i}(t^-) + W_5 \mathbf{u}(t^-) + W_6 \mathbf{f}) \end{aligned} \quad \left. \begin{array}{l} \text{Weight matrices } W \\ \text{are trainable} \end{array} \right\}$$

- All users share the User-RNN parameters. Similar for items.

JODIE: Project Component



How can we predict the next item?

- Rank items using distance in the embedding space

Summary: JODIE Formulation

**Update
embeddings:**

$$\mathbf{u}(t) = \sigma(W_1 \mathbf{u}(t^-) + W_2 \mathbf{i}(t^-) + W_3 \mathbf{f})$$

$$\mathbf{i}(t) = \sigma(W_4 \mathbf{i}(t^-) + W_5 \mathbf{u}(t^-) + W_6 \mathbf{f})$$

**Project user
embedding:**

$$\hat{\mathbf{u}}(t + \Delta) = (1 + w \cdot \Delta) * \mathbf{u}(t)$$

**Predict
next item:**

$$\tilde{\mathbf{j}} = W_7 \hat{\mathbf{u}}(t + \Delta) + B$$

$$\text{Loss: } \sum_{S_r: (u, i, t, f)} \|\tilde{\mathbf{j}}(t) - \mathbf{i}(t^-)\|_2 + \lambda_U \|\mathbf{u}(t) - \mathbf{u}(t^-)\|_2$$

$$+ \lambda_I \|\mathbf{i}(t) - \mathbf{i}(t^-)\|_2$$

**Predicted next item is
close to the real item
embedding**

**Smoothness in evolving
embeddings**

Challenges in Dynamic Trajectories

Challenges in learning:

- **C1:** How to learn inter-dependent user and item embeddings? **Solution: Update component**
- **C2:** How to generate embedding for every point in time? **Solution: Project component**

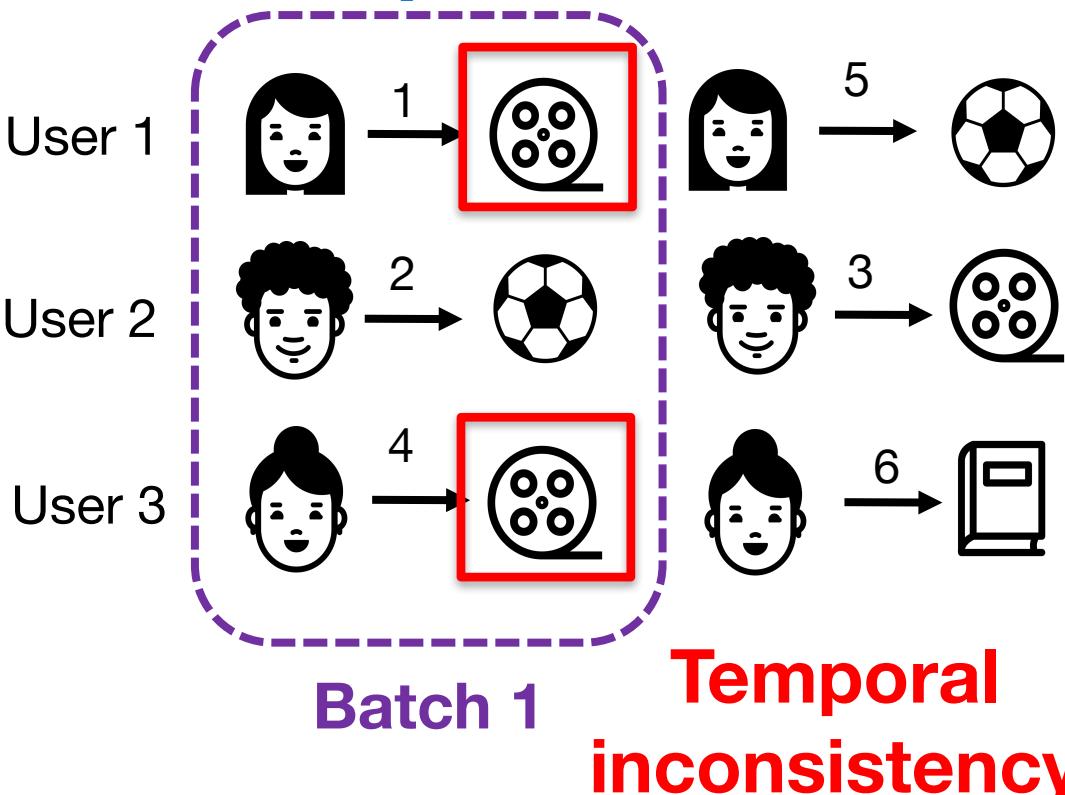
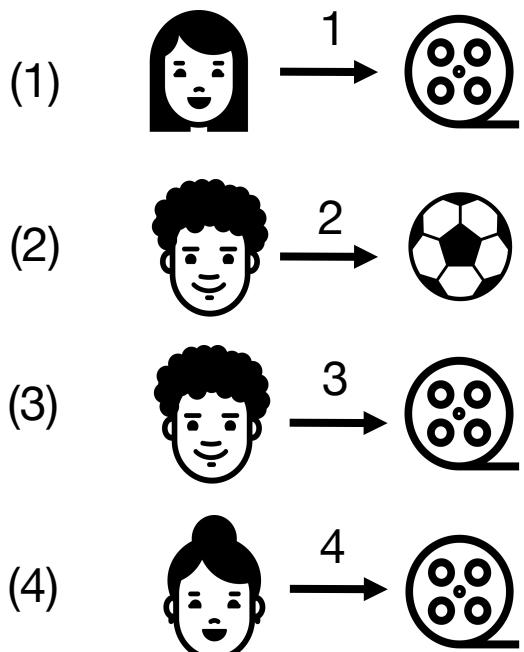
Challenges in scalability:

- **C3:** How to scalably train models on temporal networks?



Standard Training Processes: N/A

Training must maintain temporal order



Sequential processing:
not scalable

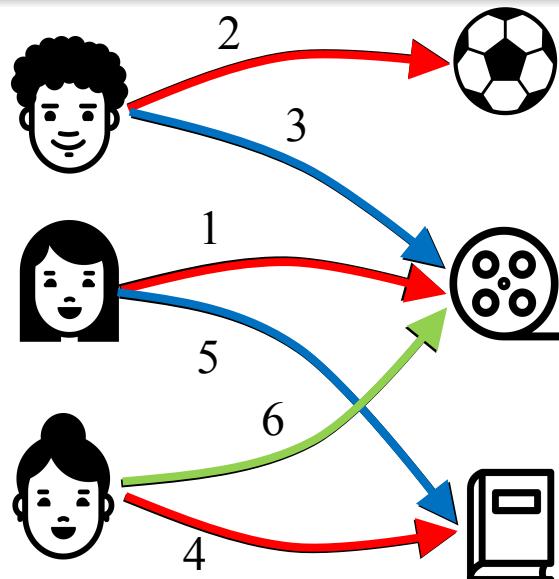
Split by user (or item):
not allowed

T-batch: Batching for Scalability

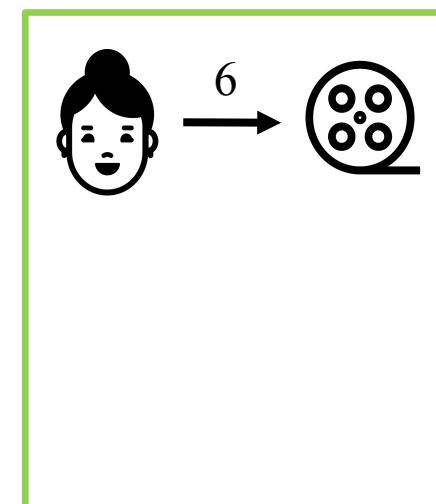
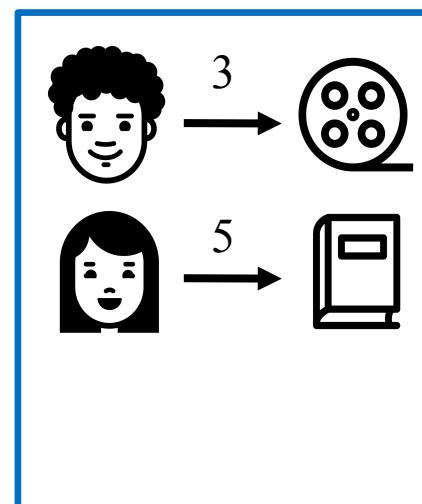
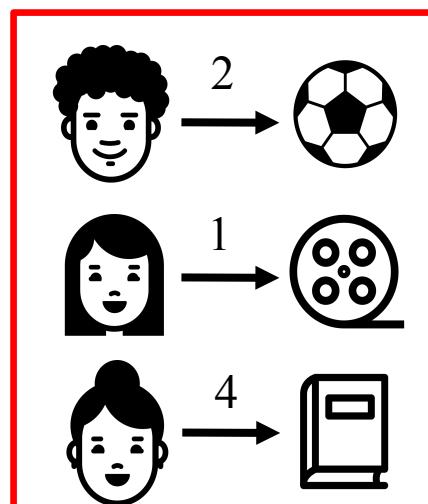
T-batch: Temporal data batching algorithm

- Main idea: create each batch as an independent edge set
- Create a sequence of batches
 - Interactions in each batch are processed in parallel
 - Process the batches in sequence to maintain temporal ordering

T-batch: Batching for Scalability



Iteratively
select the
maximal
independent
edge set.



Batch 1

Batch 2

Batch 3

Challenges in Dynamic Trajectories

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Challenges in scalability:

- **C3:** How to scalably train models on temporal networks? **Solution: T-batch Algorithm**

Experiments: Prediction Tasks

- **Temporal Link Prediction:**
 - Which item $i \in I$ will user u interact with at time t ?
- **Temporal Node Classification:**
 - Does a user u become anomalous after an interaction?
- **Settings:**
 - **Temporal Splits:** 80%, 10%, 10%
 - **Metrics:** Mean reciprocal rank, Recall@10, AUROC

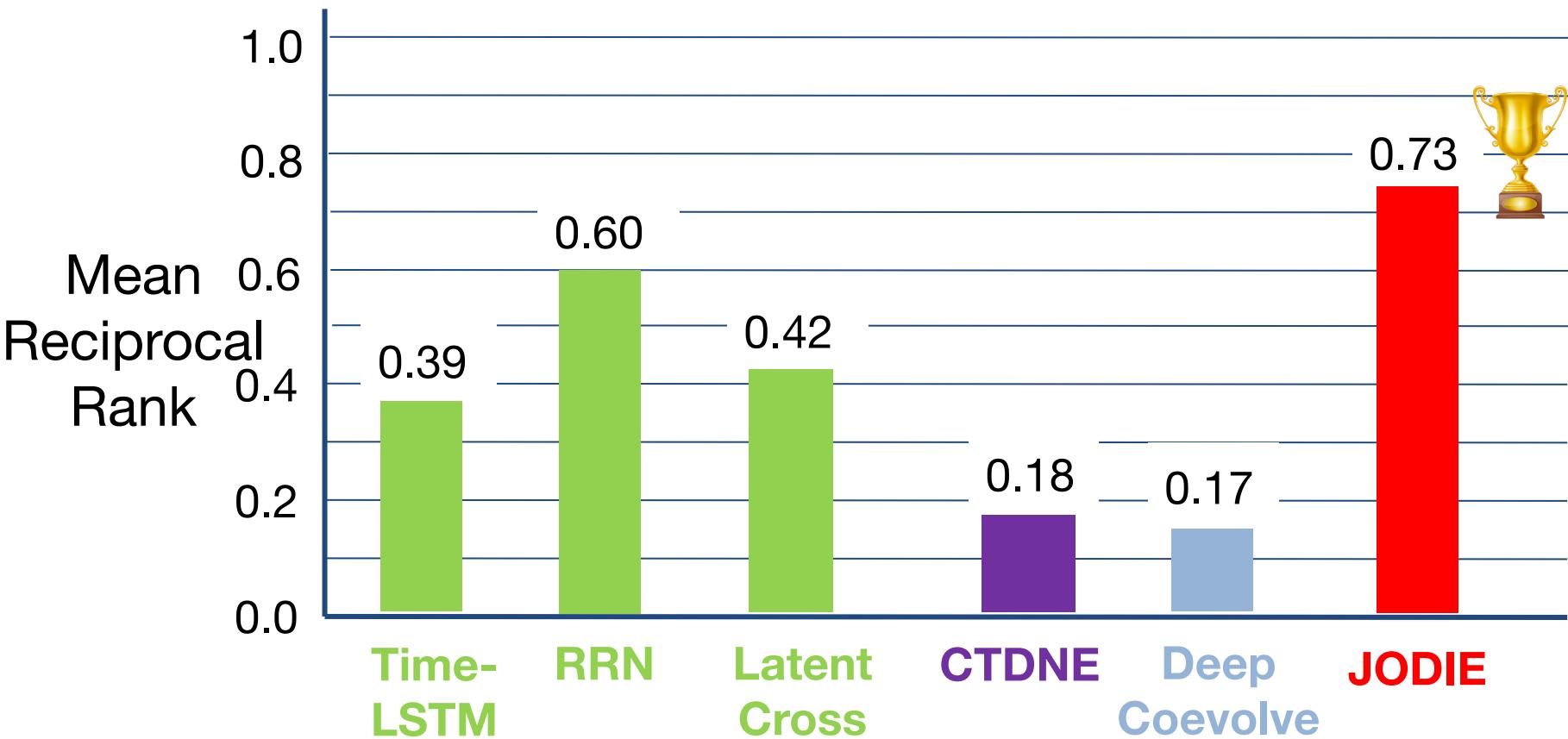
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Datasets

Dataset	Users	Items	Interactions	Temporal Anomalies	
Reddit	10,000	984	672,447	366	NEW!
Wikipedia	8,227	1,000	157,474	217	NEW!
LastFM	980	1,000	1,293,103	-	
MOOC	7,047	97	411,749	4,066	

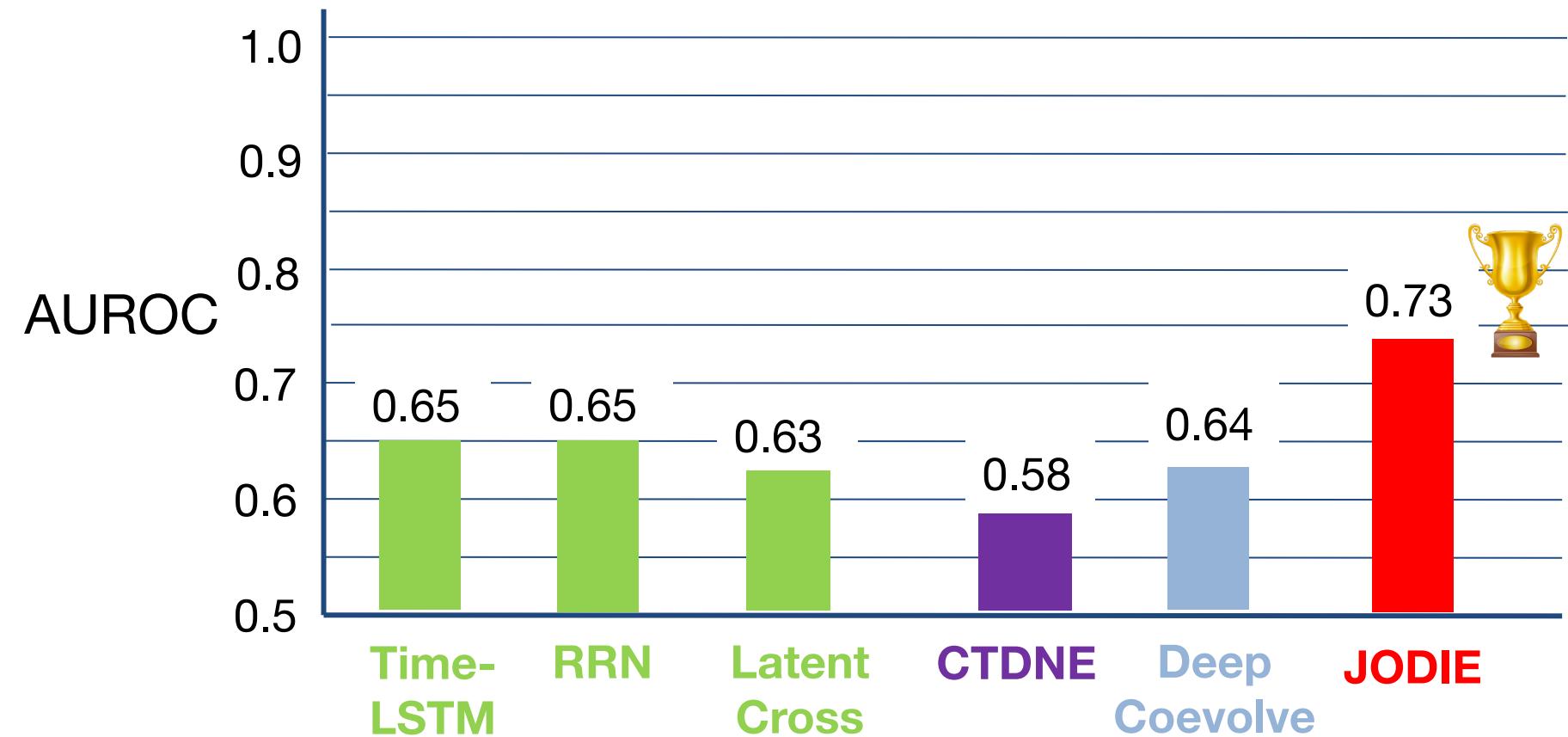
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Experiment 1: Link Prediction



JODIE outperforms baselines by > 20%

Experiment 2: Node Classification



JODIE outperforms all baselines by >12%

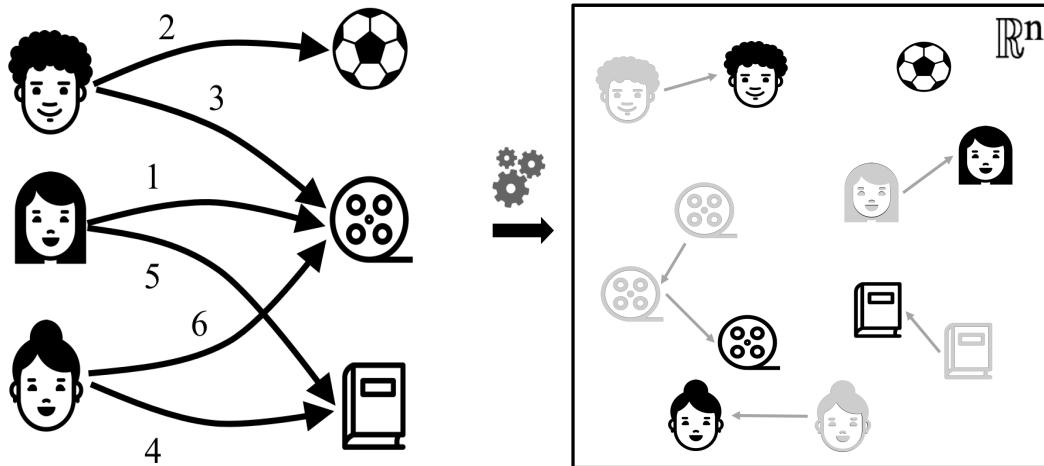
Experiment 3: T-batch Speed-up



T-batch leads to 8.5x speed-up in training

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**JODIE generates and
projects embedding
trajectories**

- **JODIE: a mutually-recursive RNN** framework
- **T-batch:** 8.5x training speed-up
- **Efficient** in temporal link prediction and node classification
- **Extendible** to > 2 entity types

Code and Data: <https://snap.stanford.edu/jodie>

Open Positions @ Georgia Tech

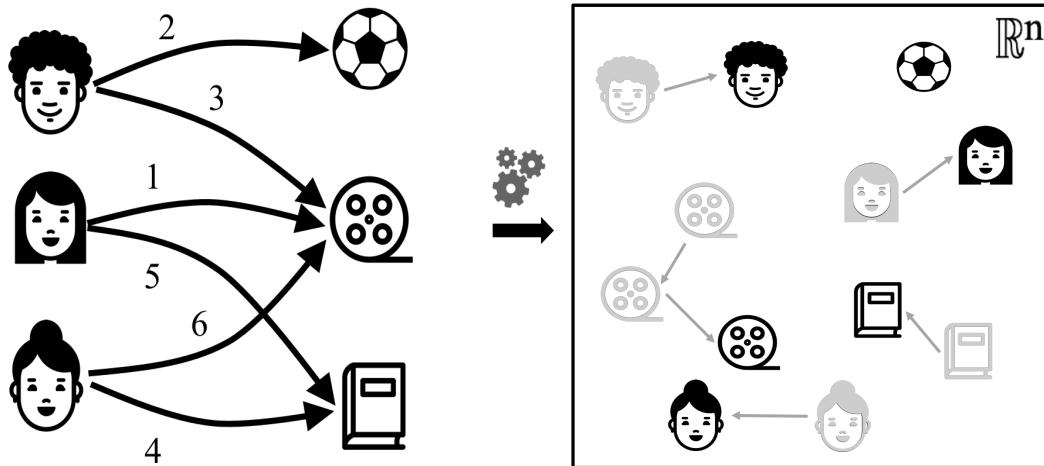
- **Hiring multiple Ph.D. students**
- **Research areas:**
 - Machine Learning for Networks
 - Safety, Integrity, and Anti-Abuse
 - Computational Social Science
- **Collaborations**



Contact: srijan@cs.stanford.edu

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