

Applied Deep Learning

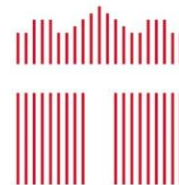


Word Representations



February 21st, 2022

<http://adl.miulab.tw>



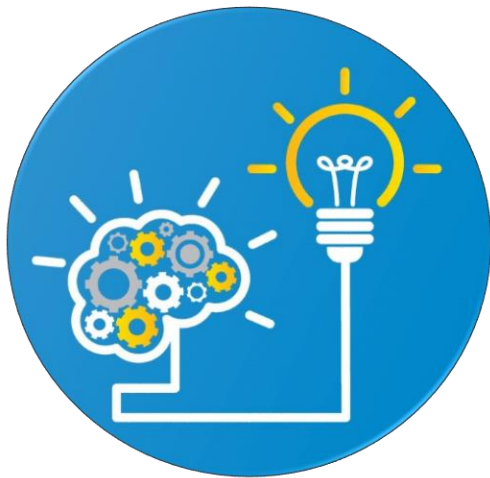
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Meaning Representations

- Definition of “Meaning”
 - the idea that is represented by a word, phrase, etc.
 - the idea that a person wants to express by using words, signs, etc.
 - the idea that is expressed in a work of writing, art, etc.

Meaning Representations in Computers

Knowledge-Based Representation

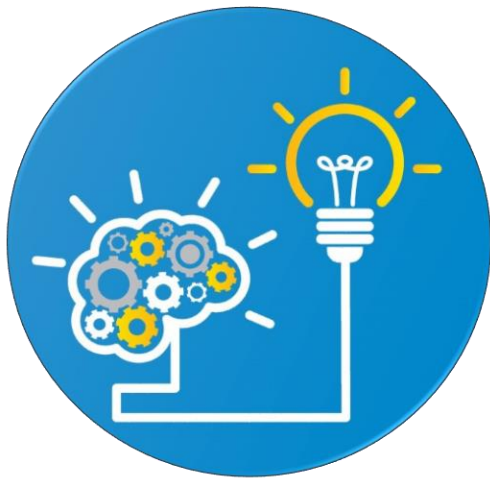


Corpus-Based Representation



Meaning Representations in Computers

Knowledge-Based Representation



Corpus-Based Representation

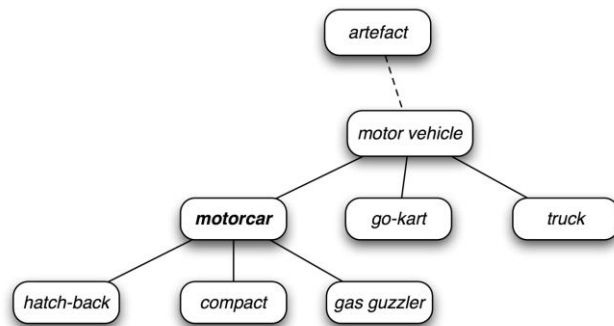


Knowledge-Based Representation

Hypernyms (is-a) relationships of WordNet

```
from nltk.corpus import wordnet as wn
panda = wn.synset('panda.n.01')
hyper = lambda s: s.hypernyms()
list(panda.closure(hyper))
```

```
[Synset('procyonid.n.01'),
Synset('carnivore.n.01'),
Synset('placental.n.01'),
Synset('mammal.n.01'),
Synset('vertebrate.n.01'),
Synset('chordate.n.01'),
Synset('animal.n.01'),
Synset('organism.n.01'),
Synset('living_thing.n.01'),
Synset('whole.n.02'),
Synset('object.n.01'),
Synset('physical_entity.n.01'),
Synset('entity.n.01')]
```

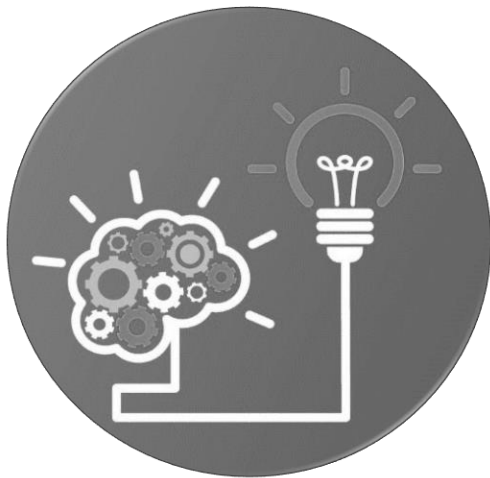


Issues:

- newly-invented words
- subjective
- annotation effort
- difficult to compute word similarity

Meaning Representations in Computers

Knowledge-Based Representation



Corpus-Based Representation



7 — Corpus-Based Representation

- Atomic symbols: **one-hot** representation

car $[0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ \dots \ 0]$



car

Issues: difficult to compute the similarity (i.e. comparing “car” and “motorcycle”)

$[0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ \dots\ 0]$ **AND** $[0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ \dots\ 0] = 0$

car motorcycle

Idea: words with similar meanings often have similar neighbors

Corpus-Based Representation

- Neighbor-based representation
 - Co-occurrence matrix constructed via neighbors
 - Neighbor definition: full document v.s. windows

full document

word-document co-occurrence matrix gives general topics

→ “Latent Semantic Analysis”

windows

context window for each word

→ capture syntactic (e.g. POS) and semantic information

Window-Based Co-occurrence Matrix

Example

- Window length=1
- Left or right context
- Corpus:

I love AI.
I love deep learning.
I enjoy learning.

similarity > 0

Counts	I	love	enjoy	AI	deep	learning
I	0	2	1	0	0	0
love	2	0	0	1	1	0
enjoy	1	0	0	0	0	1
AI	0	1	0	0	0	0
deep	0	1	0	0	0	1
learning	0	0	1	0	1	0

Issues:

- matrix size increases with vocabulary
- high dimensional
- sparsity → poor robustness

Idea: low dimensional word vector

Low-Dimensional Dense Word Vector

- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X

Diagram illustrating the Singular Value Decomposition (SVD) of a co-occurrence matrix X and its approximation \hat{X} .

The top row shows the decomposition of matrix X (dimensions $n \times m$):

$$X = U S V^T$$

where:

- U is an $n \times r$ matrix with columns U_1, U_2, U_3, \dots .
- S is an $r \times r$ diagonal matrix with singular values $S_1, S_2, S_3, \dots, S_r$ and zeros elsewhere.
- V^T is an $r \times m$ matrix with rows V_1, V_2, V_3, \dots .

The bottom row shows the decomposition of the approximated matrix \hat{X} (dimensions $n \times m$):

$$\hat{X} = \hat{U} \hat{S} \hat{V}^T$$

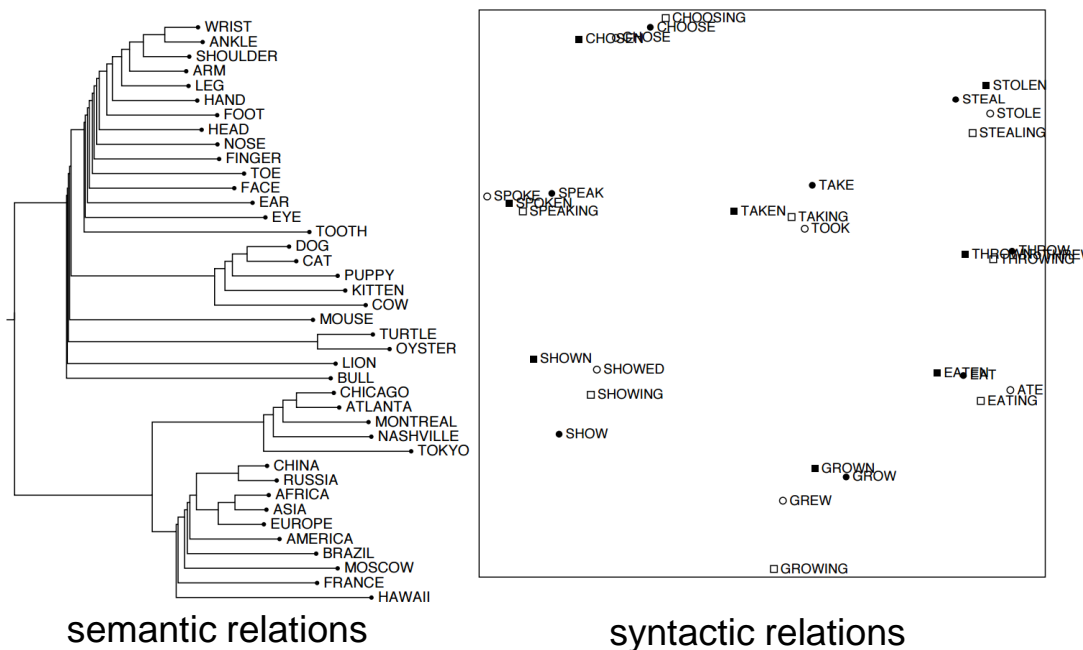
where:

- \hat{U} is an $n \times k$ matrix with columns $\hat{U}_1, \hat{U}_2, \hat{U}_3, \dots$.
- \hat{S} is a $k \times k$ diagonal matrix with singular values $\hat{S}_1, \hat{S}_2, \hat{S}_3, \dots, \hat{S}_k$ and zeros elsewhere.
- \hat{V}^T is a $k \times m$ matrix with rows $\hat{V}_1, \hat{V}_2, \hat{V}_3, \dots$.

A red arrow labeled "approximate" points from \hat{X} up to X , indicating that \hat{X} is an approximation of X .

Low-Dimensional Dense Word Vector

- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X



Issues:

- computationally expensive:
 $O(mn^2)$ when $n < m$ for $n \times m$ matrix
- difficult to add new words

Idea: directly learn low-dimensional word vectors

Low-Dimensional Dense Word Vector

- Method 2: directly learn low-dimensional word vectors
 - Learning representations by back-propagation. (Rumelhart et al., 1986)
 - A neural probabilistic language model (Bengio et al., 2003)
 - NLP (almost) from Scratch (Collobert & Weston, 2008)
 - Recent and most popular models: word2vec (Mikolov et al. 2013) and Glove (Pennington et al., 2014)
 - As known as “Word Embeddings”

Summary

- Knowledge-based representation
- Corpus-based representation
 - ✓ Atomic symbol
 - ✓ Neighbors
 - High-dimensional sparse word vector
 - Low-dimensional dense word vector
 - Method 1 – dimension reduction
 - Method 2 – direct learning