# Interest Rates and Credit Rationing in U.S. Mortgage Lending\*

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#### Abstract

Recent work on imperfect competition in lending markets focuses on the interest rate margin, despite the importance of credit rationing in lending. I estimate a structural model of bank competition in interest rates and credit rationing using U.S. mortgage data. I use the estimated model to show how banks optimally trade-off interest rates and credit rationing, and illustrate its policy relevance by examining the magnitude and the form of banks' pass through – to clients – of a cut in funding costs. I find that banks pass through their lower funding cost by not only cutting interest rates but also relaxing credit rationing. There is substantial heterogeneity in the pass through in both margins and this is mainly explained by heterogeneity in two different types of banks' costs: funding cost of originating mortgages and cost of processing applications. Lastly, I quantify the importance of adverse selection and moral hazard in how banks pass through lower funding costs through credit rationing. I find that moral hazard is the more important friction in the U.S. mortgage market, where shutting down moral hazard almost completely erases the pass through in the credit rationing margin.

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# 1 Introduction

Credit rationing is a universal feature of lending markets: lenders have the right to reject potential borrowers they deem too risky.<sup>1</sup> In mortgage lending, credit rationing is important to policy makers because of the strong interest in home ownership, and how mortgage lending can affect financial stability and economic activity.

Different factors affect credit rationing or the extent to which loan applications get rejected. Credit rationing entails that demand for loans is greater than supply. Given excess demand from borrowers at a given interest rate, various frictions such as adverse selection and moral hazard prevent lenders from profitably raising interest rates to clear the market because doing so would raise the riskiness of the borrowers and thereby lower profitability (Stiglitz and Weiss, 1981). In addition, lenders lowering credit rationing to fight for market share is widely attributed as a contributor to the 2008 financial crisis (see Financial Crisis Inquiry Report 2011). Despite the fundamental importance of the relationship between interest rates and credit rationing in understanding credit markets, empirical work on the relationship between the two margins is somewhat limited.

In this paper, I estimate a structural model of imperfect competition in mortgage lending using U.S. mortgage data and use the estimated model to understand how banks trade-off interest rates and credit rationing. In particular, to demonstrate the importance of understanding this trade-off for policy questions, I use the estimated model to study the pass through of a cut in banks' funding costs and show that banks adjust substantially in both the interest rate and credit rationing margins.

I define credit rationing as rejected mortgage applications. Previous papers have measured credit rationing as rejected loan applications, including Agarwal et al. (2017), Cuesta and Sepúlveda (2019), and Jappelli (1990). I use the proportion of mortgage applications accepted as a measure of credit rationing, where a higher proportion accepted means lower credit rationing. I document several stylized facts to motivate my analysis. I begin by showing that there is substantial variation in credit rationing across markets in the U.S. This variation has two dimensions: variation across markets for a given bank, and variation across banks for a given market. I show that there are systematic differences across banks, both in the levels of interest rates and credit rationing they set as well as the relationship between the two margins across markets for a given bank. I also show that while the average mortgage interest rate closely mirrors the movements of the 10 Year Treasury Rate, there is substantial heterogeneity around the mean, and that there is also substantial

<sup>&</sup>lt;sup>1</sup>There are some limits such as laws against racial discriminzation (e.g. red-lining laws).

heterogeneity in the data in how interest rates and credit rationing changes from year-to-year across markets.

Motivated by this evidence, I develop and estimate a structural model of bank competition in mortgage lending using bank-market-year data. Households choose among competing banks to apply for a mortgage given the offered interest rates and their expected acceptance probability. Characteristics such as ease of access to bank branches in the market differentiate mortgages. Banks compete by simultaneously choosing the optimal interest rates and credit rationing – measured by acceptance probabilities – to offer households.

My modeling contribution is to develop a general framework where banks take into account multiple factors when choosing the optimal acceptance probability. Following the recent literature, the fundamental reason why mortgage applications get rejected in my model is that idiosyncratic cost shocks make some mortgage applications too costly for banks to accept.<sup>2</sup> However, I allow important factors to affect the degree of credit rationing. First, adverse selection and moral hazard in mortgage defaults provide frictions that affect how banks trade-off interest rates with credit rationing. Second, banks take into account how lowering credit rationing by offering higher acceptance probabilities can attract households that, ceteris paribus, prefer to apply to banks with higher acceptance probabilities. Banks balance this incentive to offer higher acceptance probabilities to attract households with the fact that accepting too high a proportion of applications may lower the profitability of accepted mortgages due to adverse selection. As far as I am aware of, my paper is the first to capture this lowering credit rationing to capture market share mechanism in structural models of lending markets. I implement this mechanism using insights from the industrial organization literature (Hotz and Miller, 1993; Aguirregabiria and Magesan, 2013).

Another important innovation of the model is the existence of two types of bank costs: funding cost of originating mortgages and cost of processing applications. The former is only incurred for originated mortgages and reflects the costs associated with funding a mortgage whereas the latter is incurred for all received applications.<sup>3</sup> I show that banks cannot lower interest rates or raise acceptance probabilities too much lest they attract more than the optimal amount of applications and incur large processing costs. Interestingly, changes to

 $<sup>^2</sup>$ See Cuesta and Sepúlveda (2019). In addition, Allen et al. (2019) use idiosyncratic cost shocks to rationalize the heterogeneity in interest rates in the Canadian mortgage market.

<sup>&</sup>lt;sup>3</sup>Fuster et al. (2017) show evidence of "capacity constraints" in processing mortgage applications where an increase in the volume of mortgage applications in a given month leads to a significant increase in the margin between the funding cost and the mortgage interest rate. This is interpreted as banks passing through higher costs of processing mortgages to borrowers at peak times of mortgage demand.

funding costs have different implications on how banks trade-off interest rates and credit rationing versus changes to processing costs. Namely, a decrease in either cost leads to lower interest rates, but for a decrease in funding costs banks raise acceptance probabilities whereas for a decrease in processing costs banks lower acceptance probabilities. The intuition is that for a decrease in funding costs the profit margins on originated mortgages increase, but for a decrease in processing costs the profit margins decrease so banks accept a lower proportion of applications. In addition, counterfactuals show the importance of both types of costs for explaining the heterogeneity in pass through.

I estimate the model using U.S. data on mortgage applications and outcomes, interest rates, and defaults at the bank-market-year level for 2009 to 2014. The key identification challenge is in the estimation of mortgage demand and the parameters capturing households' preferences over interest rates and acceptance probabilities. Correlation between interest rates, acceptance probabilities, and unobservable bank quality over markets imply that standard OLS estimation would misattribute the effect of unobserved bank quality on demand as the causal effects of interest rates and acceptance probabilities respectively, thereby biasing my estimates.

My approach to deal with this endogeneity problem is to use instruments justified by the exclusion restriction that some bank cost shifter variables affect funding costs of originating mortgages but do not enter the demand equation. Therefore these cost shifters affect interest rates and acceptance probabilities only through their effects on bank funding costs and are not correlated with unobserved bank quality over markets. The cost shifters I use are variables that measure interest expense and the proportion of longer maturity assets on a bank's balance sheet. I argue that an increase in either variable increases the funding cost, the former by increasing the interest rate at which banks must borrow to fund mortgages, and the latter by increasing liquidity mismatch between short-maturity liabilities and long-maturity assets.<sup>4</sup>

I also estimate two types of bank costs: funding and processing costs. These costs are allowed to vary across banks, markets, and years. The identification idea is that mortgage applications and originated mortgages appear separately in the bank profit function. Data on originated mortgages and mortgage applications in conjunction with two first order conditions of optimality – one for interest rates and the other for acceptance probabilities – separately identify the two different types of costs.

Demand estimates show that households favor banks with lower interest rates and higher

<sup>&</sup>lt;sup>4</sup>See Berger and Bouwman, 2009; Brunnermeier et al., 2013; and Bai et al., 2009.

acceptance probabilities, but that households are much more sensitive to interest rates. Due to the low sensitivity of borrowers to acceptance probabilities, I find that in the aftermath of the financial crisis banks in effect did not relax credit rationing to compete for market share. There is also evidence of adverse selection and moral hazard in defaults. An increase in interest rates has a causal effect on increasing default risk, and an increase in acceptance probabilities also increases the riskiness of the pool of accepted mortgages. I also estimate funding and processing costs and find that they vary significantly across banks, markets, and years. Funding costs increase with higher bank interest expense and share of longer maturity loans on balance sheet. Processing costs increase year over year, which reflect findings in Fuster et al. (2017) that in the years after the 2008 financial crisis the cost of processing mortgage applications increased due to increased legal and regulatory burden.

I use the estimated model for three sets of counterfactuals. First, I exogenously vary funding and processing costs in order to illustrate how these two types of costs affect banks' optimal trade-off in interest rates and acceptance probabilities. I find that a decrease in funding costs lead to a decrease in interest rates and an increase in acceptance probabilities, whereas a decrease in processing costs lead to a decrease in both interest rates and acceptance probabilities. This result is important because the former cost cut unambiguously increases consumer welfare whereas the latter has ambiguous implications. To my knowledge, my paper is the first to show how changes in different types of bank costs have potentially different welfare implications.

Second, I run a series of counterfactuals studying how banks pass through lower funding costs through interest rates and acceptance probabilities, and how this pass through varies across banks and markets. The model predicts that for a 10% decrease in the cost of funding a mortgage, interest rates fall by 10.4% and acceptance probabilities increase by 7.1% on average. I show that in a model where only the interest rate is endogenous it over-predicts the interest rate pass through and the increase in consumer surplus and under-predicts the gain to banks. In addition, there is significant heterogeneity across banks and markets in the pass through in both margins. I show that markets where banks have more market power have lower predicted pass through in interest rates and acceptance probabilities, but that the heterogeneity in the levels of funding and processing costs play the biggest role in explaining the heterogeneity in pass through. Overall, my model predicts that credit rationing will respond substantially to a decrease in funding costs, and that there will be substantial heterogeneity in the pass through in both interest rates and credit rationing across banks and markets.

Third, I quantify the importance of adverse selection and moral hazard in how banks pass through lower funding costs with higher acceptance probabilities. I first look at changes in equilibrium outcomes when I shut down adverse selection and moral hazard respectively. In both cases interest rates and acceptance probabilities increase compared to the observed data, but the increase in both margins is larger when I shut down moral hazard than when I shut down adverse selection. Then, I calculate the counterfactual pass through in interest rates and acceptance probabilities for the cases where there is no adverse selection and no moral hazard respectively. I find that with no adverse selection, the percentage change in acceptance probabilities decreases from 7.073% to 3.789%, whereas with no moral hazard the percentage change in in acceptance probabilities decreases to 0.443%. These results show that moral hazard is the more important friction in U.S. mortgage lending.

Overall, these results yield insight into a fundamental aspect of credit markets: how lenders use the interest rate and credit rationing margins to maximize profits. I show the important policy implications that these insights have on the pass through of lower funding costs by banks to households, and in particular the effects that processing costs, adverse selection, and moral hazard have on the pass through in interest rates and credit rationing.

This paper contributes to three main strands of literature. First, I contribute to the recent literature of structural models of competition in lending markets. These papers focus on the competition in interest rates between lenders in different lending markets such as mortgages (Aguirregabiria et al., 2019; Allen et al., 2019; Benetton, 2019; Tsai, 2019), corporate loans (Crawford et al., 2018; Ioannidou et al., 2019), and personal loans (Cuesta and Sepúlveda, 2019). My paper contributes to this literature by making both interest rates and credit rationing endogenous, and studying how factors such as adverse selection, moral hazard, competition, and funding and processing costs affect credit rationing.

However, my paper is not the first to endogeneize credit rationing. Cuesta and Sepúlveda (2019) also study the trade-off between interest rates and credit rationing to study the effect of interest rate caps on personal loans in Chile. My paper differs from their study for at least two reasons. First, my model of credit rationing differs from theirs in that my model allows the possibility of banks lowering credit rationing to fight for market share, whereas they assume that banks always accept profitable loan applications and reject unprofitable ones. In addition, I can identify two different types of bank costs in funding and processing costs which play key roles in the trade-off between interest rates and credit rationing and have different policy implications. Second, my model incorporates both adverse selection and moral hazard whereas their model only captures adverse selection. Third, my paper

studies the effect of a different policy change – a decrease in funding costs – on the U.S. mortgage market.

Another paper that endogeneizes credit rationing is Agarwal et al. (2017), who study the U.S. mortgage market and document that contrary to the standard search model framework, borrowers that search more obtain more expensive mortgages. They also study the trade-off between interest rates and credit rationing in U.S. mortgage lending, but they estimate a search model to explain why borrowers with similar characteristics differ in search behavior and the interest rates they obtain, whereas I estimate a model of imperfect competition in mortgage lending and focus on the heterogeneity in interest rates and credit rationing across banks and markets. In addition, similar to Cuesta and Sepúlveda (2019) their model does not allow banks to lower credit rationing to fight for market share, can only identify funding costs, and only incorporates adverse selection.

Second, this paper contributes to the literature of empirical studies on credit rationing. Classic references include Cox and Jappelli (1990) and Jappelli (1990). More recent papers include Agarwal et al. (2017), Ambrose et al. (2016), Canales and Nanda (2012), Carbo-Valverde et al. (2012), Cenni et al. (2015), Cowling (2010), Cheng and Degryse (2010), Kirschenmann (2016), and Kremp and Sevestre (2013). Most of these papers are reduced form studies looking at factors that affect credit rationing for consumers and businesses. I estimate a structural model and use counterfactuals to show not only how credit rationing responds to a policy change, but also how banks trade-off interest rates and credit rationing in the process as well as how processing costs, adverse selection, and moral hazard affect this trade-off.

Third, this paper contributes to the literature on the transmission of monetary policy by financial intermediaries. Previous papers have studied how market power (Scharfstein and Sunderam, 2017) and mortgage contract design (Di Maggio et al., 2017) affect pass through of lower interest rates to mortgage borrowers in the U.S. There are also papers studying interest rate pass through in other settings (Benetton and Fantino, 2019; De Graeve et al., 2007). Finally, some papers show how monetary policy affects loan quantity and lender risk-taking (Agarwal et al., 2018; Drechsler et al., 2017; Jiménez et al., 2014). In this paper, I study how changes in bank funding costs are passed on through changes in mortgage interest rates and credit rationing. I contribute to this literature by showing how credit rationing is an important margin in the pass through of lower funding costs by banks to households, and that the heterogeneity in the pass through in interest rates and credit rationing is driven by heterogeneity in bank funding and processing costs. In addition, I show that without moral

hazard the pass through in the credit rationing margin is trivial.

The rest of the paper is organized as the following. Section 2 describes data sources and descriptive evidence. Section 3 explains the model of demand and supply of mortgages. Section 4 describes identification and estimation. Section 5 presents estimation results. Section 6 discusses counterfactuals. Section 7 concludes.

# 2 Data and Descriptive Evidence

#### 2.1 Data Sources

The Home Mortgage Disclosure Act (HMDA) data contains application-level information on mortgage applications and outcomes as well as some information about the applicants such as income, race, and sex as well as where the property is located down to the census tract.<sup>5</sup> All banks that have received a mortgage application in a Metropolitan Statistical Area (MSA) and have assets greater than \$10 million or originate more than 100 loans in a year are required to report all mortgage applications and their outcomes, and it is estimated that upwards to 90% of all mortgage applications in the U.S. are observed in HMDA data. As is well known, HMDA lacks some key information such as the term and interest rate of the loan, and the credit score of the borrower.<sup>6</sup>

Fannie Mae and Freddie Mac, two government sponsored enterprises (GSE) that purchase the bulk of mortgages from banks in the U.S., provide loan-level data on 30-year fixed rate mortgages<sup>7</sup> including the interest rate of the loan and borrower credit score. I observe the location of the mortgage to first three digits of the zip code. However, GSE data only discloses the identity of the lending institution for the top few lenders in terms of overall volume due to privacy concerns. Data is available from 2000 onwards, and monthly default status of each loan is available up to present day.

Summary of Deposits (SOD) data includes information on all bank branches of all banks

<sup>&</sup>lt;sup>5</sup>Data is available from 1990 onwards.

<sup>&</sup>lt;sup>6</sup>Even with the increasing availability of detailed micro-level data on credit markets such as credit registry data, it is rare for a dataset to have information on credit rationing such as rejected applications. An exception is Agarwal et al. (2017), who use data from one of the two government sponsored enterprises to obtain a sample of 5.36 million mortgage application from 2001 to 2013 with data on outcomes and detailed information on applicant characteristics. However, this is a small proportion of the overall mortgage lending activity that goes on in the U.S. Cuesta and Sepúlveda (2019) is another exception where they have information on applications for personal loans in Chile.

<sup>&</sup>lt;sup>7</sup>Freddie Mac data also contains 10 and 20-year fixed rate mortgages.

in the U.S. down to the zipcode and how much deposits are in each branch each year. Deposit data is available from 1994 onwards. I use the SOD data to calculate the share of bank branches each bank has in a year-MSA. In addition, I obtain bank cost shifters from the Uniform Bank Performance Report (UBPR) data, which contains measures of bank performance derived from Call Reports data. I also obtain conforming loan limits from FHFA. Finally, I use the American Community Survey (ACS) data to count the number of households in each MSA per year. I use this information to calculate market size, with a market defined as an MSA.

In order to merge application information from HMDA data with information about loan characteristics from GSE data, I aggregate loan-level data from HMDA and GSE data to bank-MSA-year unit of observation. For both HMDA and GSE data I identify to which bank the mortgage application or originated mortgage was for. Once the proportions and averages of mortgage and borrower characteristics are calculated at the bank-MSA-year unit of observation for HMDA and GSE data, HMDA and GSE variables are merged. SOD bank branch network data is aggregated and merged at year-MSA-bank level.

Because GSE data only discloses the identity of the bank for top sellers in terms of volume whereas HMDA data discloses the identity of the bank for every mortgage application, I focus my analysis on the top 5 banks in terms of volume in both HMDA and GSE data for much of my sample: Bank of America, Citigroup, JP Morgan Chase, and Wells Fargo, and US Bank. These top 5 banks lend mortgages extensively across the U.S. and are therefore ideal for studying their response to variation in demand and moral hazard across the country. Non-bank lenders such as Quicken Loans are not included because bank cost shifter variables from UBPR data are only available for banks. The model will be estimated using data from the top 5 banks only.

Because I only have data on interest rates from GSE data, I drop applications from HMDA data that are not GSE-eligible. Merging conforming loan limits from FHFA to HMDA data, I drop all applications whose loan size is above the conforming loan limit before I aggregate loans at the bank-MSA-year level. After aggregating and merging HMDA and GSE data, I drop bank-MSA-year observations where all or none of the mortgage applications were originated. I also drop all bank-MSA-year observations where the bank received less than

<sup>&</sup>lt;sup>8</sup>Starting in 2009 the GSEs instituted minimum FICO scores for GSE-securitization eligibility. Unfortunately HMDA does not report credit scores so I assume that all mortgage applications below the loan conforming limit are GSE-eligible.

<sup>&</sup>lt;sup>9</sup>I assume that interest rates from GSE data are broadly representative of the interest rates that HMDA applications in my regression sample had.

100 applications, and then I keep observations from MSA-years where at least 4 of the top 5 banks have observations in that MSA-year.<sup>10</sup> The regression sample runs from 2009 to 2014<sup>11</sup>, includes 281 MSAs, and has 6,052 bank-MSA-year observations.

Table 1 shows summary statistics of the key variables of interest. The average interest rate is 0.0431 and the average acceptance probability is 0.4357. The table shows considerable variation in acceptance probabilities, ranging from 0.0144 to 0.9064. The proportion of mortgages that defaulted, defined as 1 month or more delinquent in payment within two years of origination<sup>12</sup>, is on average 0.0346, with one outlier in Idaho Falls, ID in 2012 where half the mortgages defaulted for Citigroup. FICO scores averages are high at 761.5258 and reflects the fact that these are coming from originated mortgages. Market share, defined as the number of applications to a bank-MSA-year over the total number of households in the MSA-year, is small with an average market share of 0.0067. The share of bank branches a bank has a MSA-year is on average 0.0515. There are numerous MSA-years where a bank originates mortgages in the MSA-year but has a zero bank branch share.

# 2.2 Descriptive Evidence

I use the proportion of mortgage applications accepted or "acceptance probabilities" as my measure of credit rationing, where a lower acceptance probability means higher credit rationing. Acceptance probabilities are calculated at the bank-MSA-year level. Panel (a) of figure 1 shows wide variation in both average interest rates and acceptance probabilities across MSAs for the top 5 banks. There also some systematic differences between the banks. For example, US Bank seems to have higher acceptance probabilities while Citigroup seems to accept a lower proportion of applications and have lower average interest rates. This variation in interest rates and acceptance probabilities across the U.S. and across banks are key features of the data that this paper tries to explain, and the structural model helps to decompose this variation across demand and supply factors. Panel (b) of figure 1 shows that

<sup>&</sup>lt;sup>10</sup>This is done to ensure that there are enough observations per MSA-year fixed effect which will be included in all regression specifications.

<sup>&</sup>lt;sup>11</sup>Due to concern about preponderance of subprime loans in the HMDA data before the recent financial crisis in the U.S., I only use data from 2009 onwards to keep the sample more representative of prime-eligible applications.

<sup>&</sup>lt;sup>12</sup>The literature typically defines default as 2 or 3-month delinquency on loan payments. I define defaults as 1-month or more delinquent in order to avoid zeros in defaults since in my estimation all observations with defaults equal to 0 or 1 will be dropped. The proportion of mortgages 1-month or more delinquent is highly correlated with the proportion of mortgages 2-month or more delinquent. I discuss this issue further in the estimation section.

Table 1: Summary Statistics

	count	mean	std	min	50%	max
Mkt. Shr.	6052.0	0.0067	0.0067	0.0002	0.0046	0.1131
Interest Rate	6052.0	0.0431	0.0049	0.0262	0.0437	0.0540
Acc. Prob.	6052.0	0.4357	0.1628	0.0144	0.4399	0.9064
Branch Shr.	6052.0	0.0515	0.0602	0.0000	0.0278	0.4130
Defaults	6052.0	0.0346	0.0278	0.0000	0.0303	0.5000
FICO	6052.0	761.5258	11.0080	665.0000	762.8578	817.0000
LTV	6052.0	69.9372	4.9598	26.0000	70.2441	94.0000
DTI	6052.0	31.3539	2.1686	11.0000	31.3356	40.1434

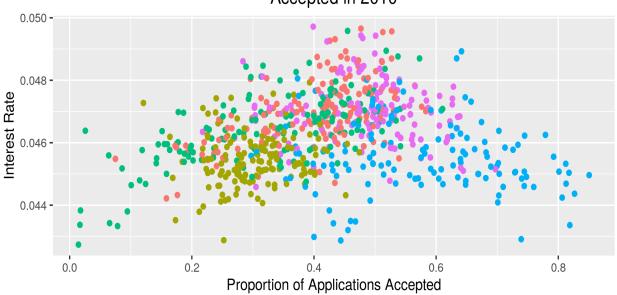
*Notes:* Table shows summary statistics for key variables of interest. Variables at bank-MSA-year unit of observation.

the relationship between interest rates and proportion of applications accepted differ across banks. JP Morgan, Bank of America, and Citigroup has a positive correlation between interest rates and proportion of applications accepted whereas US Bank and Wells Fargo has a negative relationship. How banks trade-off interest rates with credit rationing and what explains the differences across banks will be studied through the lens of a structural model.

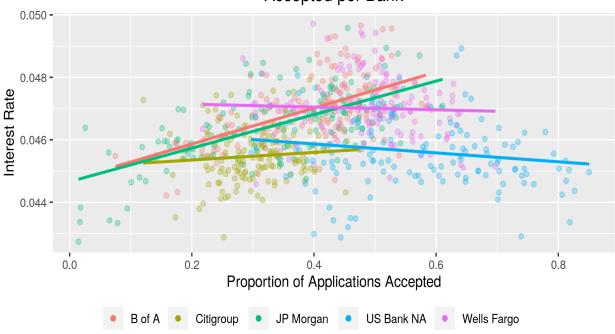
Panel (a) of figure 2 shows the distribution of bank-MSA-year average interest rates per year as well as the year-average interest rate and the 10-year Treasury rate which is a benchmark rate for 30-year fixed rate mortgages. Despite the correlation coefficient of the year-average mortgage interest rate and the Treasury rate being 0.925, there is considerable heterogeneity in the bank-MSA-year average interest rates per year. There is also considerable heterogeneity in the yearly changes in interest rates and proportion of applications accepted for a given bank-MSA-year. This can be seen from panel (b) of figure 2, which plots the percentage change in bank-MSA-year average interest rates and proportion of applications accepted from 2010 to 2011. The plot shows wide heterogeneity both for a given bank and across banks. Numerous factors could explain this heterogeneity in the interest rate and credit rationing margins, such as differences in market power and cost differences across banks and MSAs. I use my structural model to explain the heterogeneity in pass through across banks and MSA-years.

Figure 1: Bank-MSA-Year Level Variation in Interest Rates and Credit Rationing

# (a) Bank-MSA Average Interest Rates and Proportion of Applications Accepted in 2010



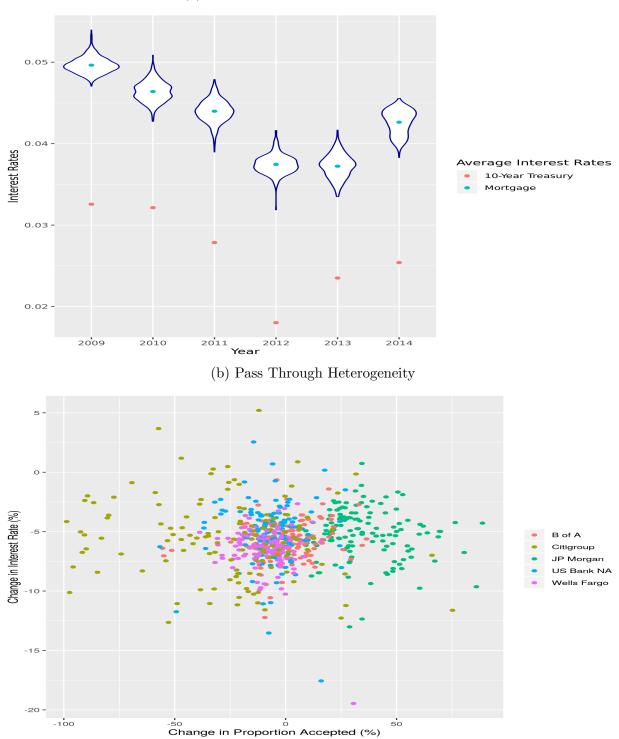
# (b) Relationship between Interest Rates and Proportion of Applications Accepted per Bank



Notes: Figure shows bank-MSA-year level variation in interest rates and credit rationing. Panel (a) plots bank-MSA average interest rates and proportion of applications accepted for the top 5 banks in the U.S. with different colored dots indicating different banks. In panel (b), for each bank the relationship between interest rates and proportion of applications accepted is shown with a linear line of fit.

Figure 2: Descriptive Evidence on Pass Through

#### (a) Interest Rate Heterogeneity per Year



Notes: Panel (a) shows the distribution mortgage interest rates per year as well as the average mortgage interest rate and 10-year Treasury rate. Panel (b) plots the percentage change in bank-MSA-year average interest rates and proportion of mortgage applications accepted from 2010 to 2011.

# 3 A Model of the Mortgage Market with Credit Rationing

I develop a model of the U.S. mortgage market where banks compete for mortgage applications through interest rates and probabilities of accepting mortgage application ("acceptance probabilities"). First, I describe households' mortgage application decision. Second, I describe households' mortgage default decision and how I incorporate adverse selection and moral hazard into the model. Third, I describe banks' optimal choice of interest rates and acceptance probabilities. Fourth, I describe the equilibrium of the model.

# 3.1 Demand for Mortgages by Households

The model is a one-shot game where in each market banks compete for mortgage applications and households make application decisions. For a given household each bank b in the market offers interest rate  $i_b$ . Through rational expectations households can calculate the acceptance probability  $a_b$  for each bank. The utility of applying for a mortgage to bank b is:

$$u_b = \alpha_i \cdot i_b + \alpha_a \cdot a_b + X_b \cdot \alpha_X + \xi_b + \varepsilon_b \tag{1}$$

Households have linear preferences over interest rates and acceptance probabilities.  $^{14}$ 

 $X_b$  is a vector of exogenous observable characteristics that affect the utility of applying to bank b, and one of the key variables is the share of bank branches that bank b has in the market. This captures how households are more willing to apply to a bank that has a higher share of bank branches because it increases the convenience of applying for a mortgage to a bank that is easy to access its bank branches, and may also capture how it is also more valuable to purchase other banking services with a more accessible bank. A higher share of bank branches increases the market power of a bank.  $^{15}$   $\xi_b$  represents unobserved quality of

<sup>&</sup>lt;sup>13</sup>In the estimation of the model the definition of a market is an MSA. However, the definition of the market could be more narrowly defined as a combination of geographic location and a particular group of households according to common characteristics that are observable and common knowledge to all the banks, such as a group of high or low credit score households.

<sup>&</sup>lt;sup>14</sup>Household utility could increase in acceptance probability if there are search or application costs. See Cuesta and Sepúlveda (2019) for a more explicit incorporation of application costs in a model where households apply for consumer loans.

<sup>&</sup>lt;sup>15</sup>The share of bank branches could also be a proxy for the proportion of households that have a bank as their home bank. Allen et al. (2019) shows how banks have market power over consumers that have their main banking services with them due to brand loyalty.

the bank, and  $\varepsilon_b$  is an idiosyncratic error term. The household utility of not applying to any bank is normalized to  $u_0 = \varepsilon_0$ . As is common in the literature, I assume that a household's choice of which property to buy with the mortgage is fixed and does not vary across which bank they apply to.

The conditional choice probability of a household choosing to apply to bank b is:

$$q_b = Pr\left(u_b > u_{b'}, \,\forall b' \neq b\right) \tag{2}$$

# 3.2 Mortgage Default

There are two key frictions that household default behavior could impose on how banks trade-off interest rates and credit rationing. One is moral hazard in defaults where a rise in interest rates has a causal effect in increasing default probability. The other friction is adverse selection, where a household's unobserved willingness to apply for a mortgage is correlated with its unobserved default risk. My model allows for both frictions in the following way. For households that obtain a mortgage, the probability of default is:

$$d_b = Pr\left(\delta_i i_b + \delta_a a_b + V_b \cdot \delta_V + \eta_b + \nu_b > 0\right)$$
(3)

 $d_b$  is the probability of default. I allow moral hazard in default by including interest rates  $i_b$  in the default probability. Moral hazard exists if  $\delta_i > 0$ , which means that higher interest rates increases the probability of default. I also capture adverse selection by including  $a_b$  in the default probability, where adverse selection exists if  $\delta_a > 0$ . The intuition is as follows: increasing the acceptance probability means lowering the risk threshold for accepting a mortgage application, and this increases the average risk of the pool of accepted mortgages. As a result, larger  $a_b$  implies larger probability of default.  $V_b$  is a vector of exogenous characteristics that affect household probability of default, including average credit or FICO scores, loan-to-value (LTV) and debt-to-income (DTI) ratios, and bank and year-MSA fixed effects.  $\eta_b$  summarizes unobserved factors that affect default probability and is observed by banks before they offer interest rates.  $\nu_b$  is an idiosyncratic error term.

# 3.3 Supply of Mortgages by Banks

Banks compete for mortgage applications by simultaneously choosing interest rates and acceptance probabilities. I describe the main factors that affect the trade-off between interest rates and acceptance probabilities.

#### 3.3.1 Ex-Ante Mortgage Profit

For each household in the market, I assume that bank b observes ex-ante mortgage profitability  $\pi_b$ :

$$\pi_b = PV_b(i_b, d_b) - mc_b \tag{4}$$

 $\pi_b$  is the ex-ante profitability of the mortgage observed by bank b before they receive an application. An originated mortgage with interest rate  $i_b$  and default probability  $d_b$  has a present value of  $PV_b(.)^{16}$ , and for each originated mortgage bank b incurs a funding cost  $mc_b$ . With moral hazard, there is a trade-off in raising interest rates for profitability of the mortgage since on the one hand raising rates has the direct effect of raising payments from the mortgage, but on the other hand may decrease the present value by increasing default probability through moral hazard:

$$\frac{dPV_b}{di_b} = \underbrace{\frac{\partial PV_b}{\partial i_b}}_{\text{Increases payments}} + \underbrace{\frac{\partial PV_b}{\partial d_b} \cdot \frac{\partial d_b}{\partial i_b}}_{\text{Moral hazard}}$$
(5)

Adverse selection implies that  $\pi_b$  decreases in  $a_b$ :

$$\frac{dPV_d}{da_b} = \frac{\partial PV_b}{\partial d_b} \cdot \frac{\partial d_b}{\partial a_b} < 0 \tag{6}$$

#### 3.3.2 Expected Profit of Mortgage Applications

I assume that once a bank receives a mortgage application, it observes an idiosyncratic cost shock that affects the actual profit of originating the mortgage and chooses to accept or reject the application. A key assumption is that banks cannot adjust their interest rate offers after observing these idiosyncratic cost shocks.<sup>17</sup> The ex-post profits are:

 $<sup>^{16}</sup>$ I assume that  $PV_b(.)$  is known by the econometrician and is a simple accounting expression.

 $<sup>^{17}</sup>$ Agarwal et al. (2017) assumes a similar structure where banks first post interest rates and then screen borrowers.

$$\begin{cases} \pi_b - e_b & \text{, if } y_b = 1\\ 0 & \text{, if } y_b = 0 \end{cases}$$
 (7)

Where,  $y_b$  is an indicator for accepted applications, and  $e_b$  is an idiosyncratic cost shock which are idiosyncratic per bank-household. The ex-ante profit of rejecting a mortgage application is normalized to 0. These cost shocks – only observed after an application comes in – represent random variation in funding, regulatory, and administrative costs.<sup>18</sup>

I assume that banks accept and reject mortgage applications according to a decision rule which they commit to at the beginning of the year and that households can observe. Let the decision rule be of the following form:<sup>19</sup>

$$y_b = 1 \Leftrightarrow \rho_b(\pi_b) - e_b > 0 \tag{8}$$

Where  $\rho_b : \pi_b \to \mathbb{R}$ .  $\rho_b(.)$  implies a probability of acceptance  $a(\rho_b) \equiv Pr\left(\rho_b(\pi_b) > e_b\right)$ . The expected profit of receiving a mortgage application is:

$$E\pi_b = a(\rho_b) \cdot \left(\pi_b + \mathbb{E}[e_b|\rho_b(\pi_b) > e_b]\right)$$
(9)

It could be natural to consider that a bank will accept a mortgage application if and only if it is ex-post profitable  $(y_b = 1 \Leftrightarrow \pi_b - e_b > 0)$ . Indeed, this will maximize the expected profit of receiving an application. However, this simple decision rule does not take into account that the acceptance decision not only affects the expected profit of a mortgage application  $(E\pi_b)$ , but has an externality effect on total expected profits for a bank. Accepting additional applications increases the acceptance probability, which attracts more applications since households, ceteris paribus, prefer to apply to banks with higher acceptance probabilities.<sup>20</sup> This implies that a bank could increase its total expected profits

<sup>&</sup>lt;sup>18</sup>Idiosyncratic cost shocks have been used to rationalize screening and interest rate variation in previous papers including Agarwal et al. (2017); Allen et al. (2019); and Cuesta and Sepúlveda (2019)

<sup>&</sup>lt;sup>19</sup>I derive the optimal decision rule in Appendix A.

<sup>&</sup>lt;sup>20</sup>To illustrate, define  $\tilde{\rho}_b \equiv 1$ ,  $\forall \pi_b$  which implies that the bank accepts applications iff  $\pi_b - e_b > 0$ . Define another decision rule as  $\rho_b' \equiv \pi_b + p$  where p > 0 and the bank accepts applications iff  $\pi_b + p - e_b > 0$ . This decision rule  $\rho_b'$  represents bank b accepting all mortgage applications that would have been accepted under  $\tilde{\rho}_b$  as well as accepting additional applications rejected under  $\tilde{\rho}_b$ , namely applications with cost shock  $\pi_b + p > e_b > \pi_b$ . It is easy to see that  $a(\rho_b') \equiv Pr(\pi_b + p - e_b > 0) > a(\tilde{\rho}_b) \equiv Pr(\pi_b - e_b > 0)$ .

by accepting more than just the ex-post profitable applications in order to attract more applications at the expense of reducing the expected profit per application.<sup>21</sup> Therefore, I do not assume that banks always accept ex-post profitable and reject ex-post unprofitable mortgage applications but instead allow banks to choose decision rules that will take into account this externality effect.

I use the fact that  $\mathbb{E}[e_b|\rho_b(\pi_b) > e_b]$  is only a function of the probability that  $\rho_b(\pi_b) > e_b$  or  $a(\rho_b)^{22}$  to represent  $E\pi_b$  as a function of the acceptance probabilities  $a_b \equiv a(\rho_b)$  instead of as a function of the decision rule  $\rho_b$ :

$$E\pi_b = a_b \cdot \left(\pi_b + \sigma \cdot g(a_b)\right) \tag{10}$$

Where  $\sigma \cdot g(a) \equiv \mathbb{E}[e_b | \rho_b(\pi_b) > e_b]$  and  $\sigma$  is the variance of  $e_b$ . From here on I will describe the bank problem as choosing interest rate  $i_b$  and acceptance probability  $a_b$ .

#### 3.3.3 Total Expected Profits

Assuming constant returns to scale (thereby ignoring loan amount), the total expected profits of bank b is:

$$\Pi_b(i, a; \mathbf{i}_{-b}, \mathbf{a}_{-b}) \equiv \underbrace{q_b(i, a; \mathbf{i}_{-b}, \mathbf{a}_{-b})}_{\text{Probability of application}} \times \underbrace{a \cdot \left(\pi_b + \sigma \cdot g(a)\right)}_{\text{Exp. profit from application}} - \underbrace{C_b(q_b)}_{\text{Processing costs}}$$
(11)

Where,  $q_b$  is the probability of a mortgage application to bank b,  $a \cdot (\pi_b + g(a))$  is the expected profit of receiving an application, and  $C_b(.)$  is the cost of processing a mortgage application regardless of whether it is accepted or rejected.  $\mathbf{i}_{-b}$  and  $\mathbf{a}_{-b}$  are vectors of other banks' interest rates and acceptance probabilities respectively. The probability of the household applying to bank b depends not only on bank b's offered interest rate and acceptance probability, but the interest rates and acceptance probabilities of all other banks that offered the household a mortgage. Note that this competition for applications from households is the only source of strategic interaction between banks in my model.  $a \cdot (\pi_b + \sigma \cdot g(a))$  is the expected profit conditional on receiving an application, and  $C_b(q_b)$  is the cost of processing every received mortgage application, regardless of whether the application

<sup>&</sup>lt;sup>21</sup>This trade-off will be made explicit in the following sub-section.

<sup>&</sup>lt;sup>22</sup>Shown in Hotz and Miller (1993) and others.

is eventually accepted or rejected. I assume that  $C_b(.)$  is increasing in  $q_b$ , implying that processing costs increase with the volume of mortgage applications.

The first order condition for  $i_b$  is:

$$FOC_{i} \equiv \underbrace{\frac{\partial q_{b}}{\partial i_{b}}}_{\text{Competing for applicants}} \cdot a_{b} \cdot \left(\pi_{b} + \sigma \cdot g(a_{b})\right)$$

$$+ q_{b} \cdot a_{b} \cdot \left(\underbrace{\frac{\partial PV_{b}}{\partial i_{b}}}_{\text{Increases payments}} + \underbrace{\frac{\partial PV_{b}}{\partial d_{b}} \cdot \frac{\partial d_{b}}{\partial i_{b}}}_{\text{Moral hazard}}\right) - \underbrace{\frac{\partial C_{b}}{\partial q_{b}} \cdot \frac{\partial q_{b}}{\partial i_{b}}}_{\text{Processing costs}} = 0$$

$$(12)$$

The first order condition for  $a_b$  is:

$$FOC_{a} \equiv \underbrace{\frac{\partial q_{b}}{\partial a_{b}}}_{\text{Competing for applicants}} \cdot a_{b} \cdot \left(\pi_{b} + \sigma \cdot g(a_{b})\right)$$

$$+ q_{b} \cdot \left(a \cdot \underbrace{\frac{\partial PV_{b}}{\partial d_{b}} \cdot \frac{\partial d_{b}}{\partial a_{b}}}_{\text{Adverse selection}} + \pi_{b} + \sigma \cdot \underbrace{G'(a)}_{\text{Cost shocks}}\right) - \underbrace{\frac{\partial C_{b}}{\partial q_{b}} \cdot \frac{\partial q_{b}}{\partial a_{b}}}_{\text{Processing costs}} = 0$$

$$(13)$$

Where,  $FOC_i$  and  $FOC_a$  denote first order conditions with respect to interest rate i and acceptance probability a respectively, and  $G(a) \equiv a \cdot g(a)$  and G'(a) denote the partial derivative w.r.t. a. The two first order conditions reveal the tension between attracting applications and maximizing the profitability of mortgages in the optimal choice of i and a. For example, in  $FOC_i$  it can be seen that on the one hand banks need to balance the trade-off in raising interest rates between higher payments and moral hazard, but on the other hand banks must also lower interest rates in order to attract households. Similarly for  $FOC_a$ , there is tension between the need to attract applications by increasing a with the need to maximize the expected profitability of applications by reducing adverse selection and optimizing expected cost shocks. The incentive to attract applications, and how the probability of a household applying to bank b is affected by competition from other banks, is the mechanism through which banks may become more willing to originate mortgages as competition increases. Finally, in both margins banks need to keep in mind processing costs. Decreasing a increases a, which increases processing costs. Therefore, banks cannot lower a or raise a too much lest they incur too much processing costs.

Therefore, there are four main reasons why there is credit rationing in my model. First, moral hazard may prevent profitable increases in the interest rate for a given level of default

risk, thereby limiting the number of interest rate-acceptance probability pairs that banks are indifferent between. Second, adverse selection implies that it may be profitable to reject applications to decrease the default risk of accepted applications. Third, ex-post idiosyncratic cost shocks imply that banks may not want to commit to accepting all applications to avoid really costly shocks. Fourth, processing costs may incentivize banks to accept a lower proportion of applications to avoid attracting too many applicants.

# 3.4 Equilibrium

For a given market, vectors of interest rates  $\mathbf{i}$  and acceptance probabilities  $\mathbf{a}$  form an equilibrium if each bank b maximizes total expected profits given other banks' interest rates  $\mathbf{i}_{-b}$  and acceptance probabilities  $\mathbf{a}_{-b}$ :

$$(i_b, a_b) = \arg\max_{(i,a)} \Pi_b(i, a; \mathbf{i}_{-b}, \mathbf{a}_{-b})$$

$$\tag{14}$$

Because the total expected profits of a bank is not strictly concave or quasi-concave, only the existence of a mixed strategies equilibrium via Theorem of the Maximum and Kakutani fixed point theorem can be proven. For estimation I assume that the observed data is a result of equilibrium in pure strategies and for counterfactuals I check that equilibrium in pure strategies exist.

# 4 Estimation

This section describes identification and estimation of the demand, default, and supply parameters of the model. I use GSE and HMDA data merged at the bank-year-MSA level.

#### 4.1 Demand

I assume that idiosyncratic errors  $\varepsilon$  in demand in equation (2) are distributed Extreme Value Type I (EVI), resulting in the following equation for the probability of an application to bank b in year-MSA t:

$$q_{b,t} = \frac{exp\left(\alpha_i \cdot i_{b,t} + \alpha_a \cdot a_{b,t} + X_{b,t} \cdot \alpha_X + \xi_{b,t}\right)}{1 + \sum_{b'} exp\left(\alpha_i \cdot i_{b',t} + \alpha_a \cdot a_{b',t} + X_{b',t} \cdot \alpha_X + \xi_{b',t}\right)}$$
(15)

I estimate a logit demand model where the estimation equation is the following:

$$ln(q_{b,t}/q_{0,t}) = \alpha_i \cdot i_{b,t} + \alpha_a \cdot a_{b,t} + X_{b,t} \cdot \alpha_X + \xi_{b,t}$$

$$\tag{16}$$

Where for bank b and year-MSA t,  $q_{b,t}$  is the market share of applications,  $i_{b,t}$  is the average interest rate,  $a_{b,t}$  is the acceptance probability (proportion of applications accepted),  $X_{b,t}$  is a vector of exogenous characteristics which include bank branch share and bank and year-MSA fixed effects, and  $\xi_{b,t}$  are unobservables that affect households' willingness to apply to bank b in year-MSA t.  $q_{0,t}$  is the share of the outside option of not applying for a mortgage. I assume that all households in a market are identical net of the idiosyncratic errors and that they face the same interest rate and acceptance probability from a given bank. The endogeneity problem with OLS estimation of the above estimating equation is that  $i_{b,t}$  and  $a_{b,t}$  will be correlated with unobservables  $\xi_{b,t}$ .  $\xi_{b,t}$  captures the unobservable quality of a bank in a year-MSA that affects household utility. For example, if Wells Fargo branches have superior customer service than other competitors in the year-MSA and therefore can charge higher interest rates, not accounting for this correlation between  $i_{b,t}$  and  $\xi_{b,t}$  will lead to a positive bias in the estimate of  $\alpha_i$ . Similarly, a bank with superior unobservable quality may not need to accept as high a proportion of applications in order to attract mortgage applicants and so there may be a negative correlation between  $a_{b,t}$  and  $\xi_{b,t}$  which leads to a negative bias in the estimate of  $\alpha_a$ .

I address the endogeneity problem in the estimation of equation (16 by combining a rich set of bank and year-MSA fixed effects with instrumental variables estimation using cost shifter instruments. The rationale for the instruments is that the cost shifters are excluded from the demand equation since they do not directly affect demand and only indirectly affect demand through their effect on  $i_{b,t}$  and  $a_{b,t}$ . This is because the cost shifters affect the funding cost of originating mortgages, and so variation in the cost shifters will lead to variation in funding costs which affect banks' choice of  $i_{b,t}$  and  $a_{b,t}$ . I use the cost shifter variables Interest Expense and Noncurrent Loans from UBPR data as instruments for  $i_{b,t}$  and  $a_{b,t}$  assuming that these bank cost shifters affect bank profits but are excluded from the demand equation.<sup>23</sup> The effect of Interest Expense on the funding cost of banks is obvious, where higher interest expense leads to a higher cost of funds and higher funding cost of originating mortgages. Therefore, in general a higher interest expense should lead to higher

<sup>&</sup>lt;sup>23</sup>Interest Expense (UBPRE002): interest expense as a percentage of average assets. Noncurrent Loans (UBPR7414): ratio of noncurrent loans and leases to gross loans and leases.

interest rates and lower acceptance probabilities since it is lowering the profit from any given mortgage. The intuition behind Noncurrent Loans is that a higher share of longer maturity loans in a bank's balance sheet raises the risk of maturity mismatch since banks in general hold longer maturity assets and have shorter maturity liabilities, and that this is costly for banks.<sup>24</sup> Therefore, a higher share of noncurrent loans increases the costliness of adding additional longer maturity loans to its balance sheet and this will increase the funding cost of originating mortgages.<sup>25</sup> These cost shifter variables vary at the bank-year level.

#### 4.2 Defaults

I assume that the idiosyncratic error term  $\nu$  in equation (3) is distributed EVI. The equation for the probability of default is:

$$d_{b,t} = \frac{exp\left(\delta_i \cdot i_{b,t} + \delta_a \cdot a_{b,t} + V_{b,t} \cdot \delta_V + \eta_{b,t}\right)}{1 + exp\left(\delta_i \cdot i_{b,t} + \delta_a \cdot a_{b,t} + V_{b,t} \cdot \delta_V + \eta_{b,t}\right)}$$
(17)

The estimation equation for the logit default model is the following:

$$ln(d_{b,t}) - ln(1 - d_{b,t}) = \delta_i \cdot i_{b,t} + \delta_a \cdot a_{b,t} + V_{b,t} \cdot \delta_V + \eta_{b,t}$$
(18)

Where,  $d_{b,t}$  is the proportion of mortgages that defaulted,  $i_{b,t}$  and  $a_{b,t}$  are interest rates and acceptance probabilities respectively,  $V_{b,t}$  are exogenous variables including the average FICO scores, LTV and DTI ratios, and bank and year-MSA fixed effects, and  $\eta_{b,t}$  are unobservables affecting default probability across banks and year-MSAs. The key parameters of interest are  $\delta_i$  and  $\delta_a$ , which represents the moral hazard and adverse selection respectively. If  $\delta_i > 0$ , then a higher interest rate would increase the default probability of the household due to moral hazard, and if  $\delta_a > 0$ , then a higher acceptance probability leads to a higher default probability due to adverse selection. The endogeneity problem in estimating  $\delta_i$  and  $\delta_a$  is that banks observe  $\eta_{b,t}$  before setting  $i_{b,t}$  and  $a_{b,t}$  but it is unobserved by the econometrician. I use bank branch share and the bank cost shifters discussed above as instruments for  $i_{b,t}$  and

<sup>&</sup>lt;sup>24</sup>Refer to Bai et al. (2018), Berger and Bouwman (2009), and Brunnermeier et al. (2013) for more detailed discussions on maturity or "liquidity mismatch".

<sup>&</sup>lt;sup>25</sup>Most originated mortgages are securitized but bigger banks tend to receive in return mortgage-backed securities that represent a claim on the interest payments of long maturity mortgages.

 $a_{b,t}$  in instrumental variables in addition to the same rich set of bank and year-MSA fixed effects also included demand estimation, where the bank branch share and bank cost shifters are excluded from the default equation but affect  $i_{b,t}$  and  $a_{b,t}$  by affecting demand and bank funding costs respectively.

One problem with estimating equation (18) is that there are 1,608 observations out of 6,052 that will drop out of the regression sample because they have  $d_{b,t} = 0$ . This may introduce sample selection bias because the observations that drop out will have less default risk than the observations that remain. In order to include all 6,052 observations I follow Gandhi et al. (2013) use a Laplace transformation of the variable  $d_{b,t}$  and estimate:

$$ln(d_{b,t} + \tau) - ln(1 - d_{b,t} - \tau) = \delta_i \cdot i_{b,t} + \delta_a \cdot a_{b,t} + V_{b,t} \cdot \delta_V + \eta_{b,t}$$
(19)

Where,  $\tau = 0.001$ . This will prevent  $d_{b,t} = 0$  observations from dropping out of my regression sample.

# 4.3 Supply

The key objects of interest in the supply model are the ex-ante profitability of mortgages  $\pi_{b,t}$  and processing costs  $C_{b,t}(q_{b,t})$ .  $\pi_{b,t} = PV_{b,t}(i_{b,t}, d_{b,t}) - mc_{b,t}$  is the present value of a mortgage with interest rate  $i_{b,t}$  and default probability  $d_{b,t}$  minus the funding cost  $mc_{b,t}$ . I make the following parametric assumptions for these objects:

$$PV_{b,t} = i_{b,t} \cdot (1 - d_{b,t})$$

$$- mc_{b,t} = W_{b,t} \cdot \beta_W + \omega_{b,t}$$

$$C_{b,t}(q_{b,t}) = c_{b,t} \cdot q_{b,t}$$
(20)

I assume that the present value of a mortgage with interest rate  $i_{b,t}$  and default probability  $d_{b,t}$  is approximated by  $i_{b,t} \cdot (1 - d_{b,t})$ . The funding cost of originating a mortgage is  $-mc_{b,t} = W_{b,t} \cdot \beta_W + \omega_{b,t}$  where  $W_{b,t}$  includes the two cost shifter variables and bank and year-MSA fixed effects.  $\omega_{b,t}$  is the unobserved component of the funding cost that varies across banks and markets. Processing costs are linear in application probability  $q_{b,t}$  and are allowed to vary across banks and year-MSAs, reflecting heterogeneity in efficiencies across banks, and regulatory burden across different jurisdictions and across time.

<sup>&</sup>lt;sup>26</sup>Allen et al., 2019; Benetton, 2019 utilize similar approximations.

I assume that the idiosyncratic cost shocks e in equation (7) follows EVI, which jointly with the assumptions of logit demand and defaults imply the following first order conditions for the bank problem:

$$FOC_{b,t}^{i} \equiv \alpha_{i} \cdot (1 - q_{b,t}) \times \left[ a_{b,t} \cdot \left( \pi_{b,t} + \sigma \cdot g(a_{b,t}) \right) - c_{b,t} \right] + a_{b,t} \cdot (1 - d_{b,t}) \cdot (1 - \delta_{i} \cdot d_{b,t} \cdot i_{b,t}) = 0$$

$$FOC_{b,t}^{a} \equiv \alpha_{a} \cdot (1 - q_{b,t}) \times \left[ a_{b,t} \cdot \left( \pi_{b,t} + \sigma \cdot g(a_{b,t}) \right) - c_{b,t} \right] - \delta_{a} \cdot a_{b,t} \cdot i_{b,t} \cdot d_{b,t} \cdot (1 - d_{b,t}) + \pi_{b,t} + \sigma \cdot G'(a_{b,t}) = 0$$

$$(21)$$

Where  $g(a) \equiv \frac{\gamma - ln(1-a)}{a} + ln(1-a) - ln(a)$ ,  $\gamma$  is the Euler-Mascheroni constant,  $G(a) \equiv a \cdot g(a)$ , and G'(a) = ln(1-a) - ln(a). Given demand  $(\alpha)$  and default  $(\delta)$  estimates, I have three unknowns in  $\pi_{b,t}^{27}$ ,  $c_{b,t}$ , and  $\sigma$  in the two first order conditions. Note that  $FOC_{b,t}^i$  and  $FOC_{b,t}^a$  together identify  $\pi_{b,t} + \sigma \cdot G'(a_{b,t})$  since  $\alpha_i \cdot FOC_{b,t}^i - \alpha_a \cdot FOC_{b,t}^a = 0$  yields the following expression:

$$\kappa_p \equiv \delta_a \cdot a_{b,t} \cdot i_{b,t} \cdot d_{b,t} \cdot (1 - d_{b,t}) - \frac{\alpha_a \cdot a_{b,t} \cdot (1 - d_{b,t}) \cdot (1 - \delta_i \cdot d_{b,t} \cdot i_{b,t})}{\alpha_i} = \pi_{b,t} - \sigma \cdot G'(a_{b,t})$$
(22)

All objects on the left-hand side of equation (22) are either observed or parameters estimated from demand and default models. Substituting in the expression for  $\pi_{b,t}$  and rearranging leads to the following estimation equation for  $\sigma$ :

$$\kappa_p - i_{b,t} \cdot (1 - d_{b,t}) = \sigma \cdot G'(a_{b,t}) + W_{b,t} \cdot \beta_W + \omega_{b,t}$$
(23)

There is an endogeneity problem where  $G'(a_{b,t})$  is correlated with unobserved  $\omega_{b,t}$ . Supposing I have a valid instrument for  $G'(a_{b,t})$  that is uncorrelated with  $\omega_{b,t}$ , I could estimate  $\sigma$  as the coefficient of  $G'(a_{b,t})$  using linear instrumental variables regression. Then, once  $\sigma$  and  $\beta_W$  are estimated I could substitute them in to one of the first order conditions to obtain estimates of  $c_{b,t}$ .

Instead, I estimate the supply model in the following way. Given a value for  $\sigma$ , say  $\hat{\sigma}$ , I can use the two first order conditions to solve for  $\hat{\pi}_{b,t}(\hat{\sigma})$  and  $\hat{c}_{b,t}(\hat{\sigma})$  for every bankmarket pair, where the notation represents the dependence of the estimates of mortgage

<sup>&</sup>lt;sup>27</sup>Note that what is really unknown is the funding cost  $-mc_{b,t} = \pi_{b,t} - i_{b,t} \cdot (1 - d_{b,t})$ .

profit and processing cost on  $\hat{\sigma}$ .<sup>28</sup> Then, with  $\hat{\pi}_{b,t}(\hat{\sigma})$  I can obtain estimates  $-\hat{m}c_{b,t} = \hat{\pi}_{b,t}(\hat{\sigma}) - i_{b,t} \cdot (1 - d_{b,t})$ . Given  $-\hat{m}c_{b,t}$ , I estimate  $\beta_W$  from the following equation by OLS:

$$-\hat{m}c_{b,t}(\hat{\sigma}) = W_{b,t} \cdot \beta_W + \omega_{b,t} \tag{24}$$

The identifying assumption is that bank cost shifters  $W_{b,t}$  are exogenous and uncorrelated with  $\omega_{b,t}$ , and they include the Interest Expense and Noncurrent Loans variables as well as bank and year-MSA fixed effects. Finally, to pin down the value of  $\hat{\sigma}$ , I do a grid search over the values of  $\hat{\sigma}$  such that in a counterfactual where I lower the funding cost of originating mortgages, the average pass through in interest rates is 100%. Therefore, my estimation approach is based on the moment restrictions: i) cost shifters  $W_{b,t}$  are exogenous, i.e.,  $\mathbb{E}[W_{b,t} \cdot \omega_{b,t}] = 0$ , ii) the average pass through in interest rates of a decrease in funding costs is 100%. To save computational time, I only use observations from 2010 for calculating the pass through counterfactuals.

The second moment restriction is motivated by the fact that the average interest rate closely tracks the 10 Year Treasury Rate, and other papers have shown that the average interest rate pass through is 100%. For example, Agarwal et al. (2017) shows that banks on average pass through all of the lower costs through interest rates. The focus of the paper is not on the average interest rate pass through but in comparing the magnitude of the pass through in credit rationing to the interest rate pass through, as well as the heterogeneity of pass through in interest rates and acceptance probabilities across banks and markets.

# 5 Results

This section discusses the results of demand, defaults, and supply estimation.

#### 5.1 Demand

Table 2 shows the estimation results of equation (16). The first two columns show OLS and 2SLS estimates of the demand parameters respectively. The first column shows that for OLS estimates, the coefficient on interest rates  $(\hat{\alpha}_i)$  is not statistically significant from 0 and the coefficient on acceptance probabilities ("Acc. Prob.",  $\hat{\alpha}_a$ ) is negative instead of the expected positive sign. 2SLS estimates show markedly different results, with  $\hat{\alpha}_i$  becoming

<sup>&</sup>lt;sup>28</sup>The exact expressions are derived in Appendix B.

significantly more negative and statistically significant from 0, and  $\hat{\alpha}_a$  becoming positive. This is a typical pattern in demand estimation, where the OLS estimates of the coefficient on price can be positive or attenuated and estimation with valid instruments make the price coefficient more negative. This is due to the fact that firms that have products with better unobservable quality can charge higher prices, thereby causing correlation between price and unobservables that significantly bias the price coefficient in OLS estimation. A similar logic follows here, where it seems that banks with better unobservable quality  $\xi_{b,t}$  can charge higher interest rates and have lower probabilities of acceptance but still draw applications. Ignoring this correlation between  $\xi_{b,t}$ ,  $i_{b,t}$  and  $a_{b,t}$  seems to cause significant bias in the demand estimates. For 2SLS estimates, the average own-demand elasticity of interest rate and acceptance probability are 6.637 and -0.3 respectively. 2SLS estimates yield significantly higher interest rate elasticity than OLS estimates, while demand is relatively inelastic with respect to the acceptance probabilities.

#### 5.2 Defaults

Table 3 shows the estimation results for equation (18). The first column shows OLS estimates and the second column shows 2SLS estimates. The key result of interest is that the 2SLS estimates show evidence of moral hazard as the estimated  $\delta_i$  parameter is positive and statistically significant from 0. The  $\delta_i$  estimate increases sharply from the OLS to the 2SLS estimate. This implies that moral hazard is a friction that imposes a trade-off when banks think of raising interest rates to compensate for higher default risk. On the one hand raising rates will raise payments, but on the other hand it will increase the default risk. Average FICO scores have a negative coefficient as expected, implying that a higher FICO scores lead to less default risk. One thing to note is that the number of observations drop from 6,052 in demand estimation to 4,444 in defaults estimation due to some bank-MSA-year observations having zero defaults, and this may lead to some bias in the estimates. Finally, the direction of movement in  $\hat{\delta}_i$  estimates going from OLS to 2SLS is as expected. Banks are likely to not raise interest rates where default probability is unobservably higher, and so not accounting for this source of endogeneity is likely to underestimate the  $\hat{\delta}_i$  parameter, which is exactly what table 3 shows.

Table 2: Estimates of Demand Parameters

	OLS	2SLS	Interest Rate	Acc. Prob.
Interest Rate	-11.48	-155.1*		
	(6.263)	(69.58)		
Acc. Prob.	-0.712***	$0.697^{*}$		
	(0.0629)	(0.289)		
Branch Shr.	6.488***	6.012***	0.000668*	0.414***
	(0.144)	(0.221)	(0.000327)	(0.0312)
Noncur. Loans			0.000248***	-0.0420***
			(0.0000284)	(0.00272)
Interest Expense			0.00216***	0.0451
			(0.000333)	(0.0319)
Constant	-4.981***	0.663	0.0413***	0.666***
	(0.274)	(3.115)	(0.000279)	(0.0266)
Bank FE	X	X	X	X
MSA-Year FE	X	X	X	X
N	6052	6052	6052	6052
Interest Rate El.	0.580	6.637		
Acc. Prob. El.	0.114	-0.30		

Notes: Standard errors in parentheses. Unit of observation is bank-MSA-year. The first two columns show OLS and 2SLS estimates respectively, and the third and fourth columns show the first stage regressions of the 2SLS regression. The coefficients on Interest Rate and Acc. Prob. (acceptance probabilities) are as expected with household utility decreasing in interest rates and increasing in acceptance probabilities. Branch Shr. – a bank's share of total bank branches in the market – also increase household utility in applying to the bank. \* p < 0.05, \*\* p < 0.01, \*\*\* p < 0.001.

Table 3: Evidence of Adverse Selection and Moral Hazard in Defaults

OI C	OCT C	Internal Dat	Λ D . 1
		interest Kate	Acc. Prob.
(15.43)	(133.1)		
-1.117***	1.435***		
(0.145)	(0.421)		
-0.00722***	-0.000740	-0.0000328***	-0.00172***
(0.00219)	(0.00506)	(0.00000201)	(0.000201)
0.0313***	0.0372**	0.0000850***	-0.00527***
(0.00573)	(0.0126)	(0.00000531)	(0.000531)
0.0545***	0.0641***	0.0000395***	-0.00806***
(0.0108)	(0.0120)	(0.0000101)	(0.00101)
		0.000188***	-0.0395***
		(0.0000268)	(0.00269)
		0.00139***	0.140***
		(0.000319)	(0.0319)
		0.00141***	0.367***
		(0.000308)	(0.0308)
-0.270	-11.60	0.0598***	2.555***
(2.020)	(8.650)	(0.00169)	(0.169)
X	X	X	X
X	X	X	X
6052	6052	6052	6052
1.080	-3.45		
0.180	-0.62		
	(0.145) -0.00722*** (0.00219) 0.0313*** (0.00573) 0.0545*** (0.0108)  -0.270 (2.020)  x  x  6052 1.080	-22.13 80.60 (15.43) (133.1)  -1.117*** 1.435*** (0.145) (0.421)  -0.00722*** -0.000740 (0.00219) (0.00506)  0.0313*** 0.0372** (0.00573) (0.0126)  0.0545*** 0.0641*** (0.0108) (0.0120)  -0.270 -11.60 (2.020) (8.650)  x x x x x 4 x 56052 6052 1.080 -3.45	-22.13 80.60 (15.43) (133.1)  -1.117*** 1.435*** (0.145) (0.421)  -0.00722*** -0.000740 -0.0000328*** (0.00219) (0.00506) (0.00000201)  0.0313*** 0.0372** 0.0000850*** (0.00573) (0.0126) (0.00000531)  0.0545*** 0.0641*** 0.0000395*** (0.0108) (0.0120) (0.0000101)  0.000188*** (0.0000268)  0.00139*** (0.0000319)  0.00141*** (0.0000308)  -0.270 -11.60 0.0598*** (0.000308)  x x x x x x x x x x x x x x x x x x x

Notes: Standard errors in parentheses. Unit of observation is bank-MSA-year. The first two columns show OLS and 2SLS estimates respectively, and the third and fourth columns show the first stage regressions of the 2SLS regression. Positive coefficients on Interest Rate and Acc. Prob. (acceptance probability) represent moral hazard and adverse selection respectively. \* p < 0.05, \*\* p < 0.01, \*\*\* p < 0.001.

# 5.3 Supply

Figure 3 plots the distributions of processing costs  $(c_{b,t})$  and funding costs  $(mc_{b,t})$  per bank. It shows substantial heterogeneity in  $c_{b,t}$  and  $mc_{b,t}$  estimates within and across banks. Table 4 shows estimates of the parameters for the bank cost shifters. Both cost shifters are statistically significant from zero and as expected, higher Interest Expense and Noncurrent Loans increase funding cost.

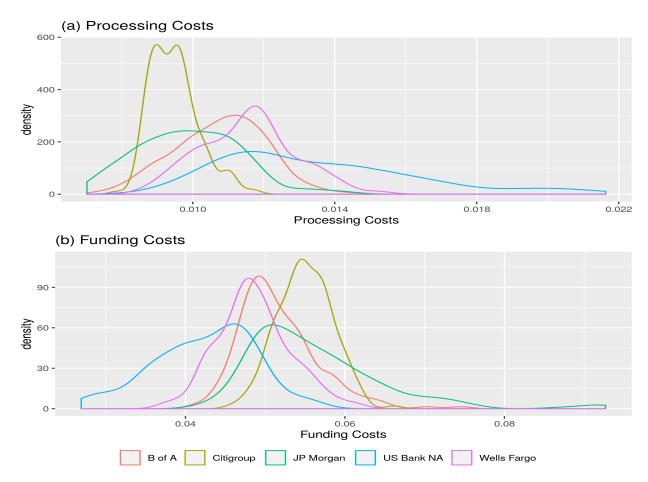


Figure 3: Heterogeneity in Processing and Funding Costs in 2010

Notes: Panel (a) and (b) show the distributions of processing costs  $(c_{b,t})$  and funding costs  $(mc_{b,t})$  per bank respectively. It illustrates the heterogeneity in processing and funding costs across banks and also across markets for any given bank.

Table 4: Funding Costs Increase in Bank Cost Shifters

	-mc
Noncur. Loans	-0.00314***
	(0.000145)
_	
Interest Expense	-0.00223
	(0.00170)
Constant	-0.0253***
	(0.00143)
Bank FE	X
MSA-Year FE	X
N	6052

Notes: Standard errors in parentheses. Unit of observation is bank-MSA-year. The dependent variable is the negative of the funding cost  $-mc_{b,t} = \pi_{b,t} - i_{b,t} \cdot (1 - d_{b,t})$ . The bank cost shifters from UBPR data are the ratio of noncurrent loans and leases to gross loans and leases (UBPR7414) and interest expense as a percent of average assets (UBPRE002). \* p < 0.05, \*\* p < 0.01, \*\*\* p < 0.001.

# 6 Counterfactuals

In this section I discuss two counterfactuals. First, I illustrate different implications that processing and funding costs have on how banks trade-off interest rates and acceptance probabilities. Second, I study how banks pass through lower funding costs through interest rates and acceptance probabilities and how factors such as market power and processing costs affect the heterogeneity in pass through. Third, I study the role that adverse selection and moral hazard play on pass through in the credit rationing margin.

To address the strong possibility of the existence of multiple equilibria in my model, for all counterfactuals I always set the starting values of interest rates and acceptance probabilities equal to the observed values in the data. This is done to prevent equilibria-switching to drive my counterfactual results where changing the starting values of a counterfactual simulation could lead to a different equilibrium purely due to multiple equilibria, rather than due to any changes in the primitives of the model. <sup>29</sup>

 $<sup>^{29}\</sup>mathrm{More}$  details on how I simulate counterfactuals can be found in Appendix C.

# 6.1 Funding and Processing Costs

The first set of counterfactuals illustrates the different implications that funding and processing costs have on how banks trade-off interest rates and credit rationing. I pick a representative market in 2010 (Youngstown-Warren-Boardman OH-PA MSA)<sup>30</sup> and first exogenously shut down all heterogeneity across banks and calculate a new equilibrium as the baseline. Then, I compare how new equilibrium interest rates and acceptance probabilities move in response to adding back heterogeneity across banks in processing costs versus adding back heterogeneity in funding costs.

Figure 4 shows the results of the counterfactuals described above. In both panel (a) and (b) arrows indicate the movement from the baseline where there is no heterogeneity in any dimension across banks to the new equilibrium after bank heterogeneity is re-introduced. This is implemented by assigning all banks the average values of all exogenous variables. Panel (a) shows the movements in interest rates and acceptance probabilities when I add back processing cost heterogeneity to the baseline. In the baseline all banks charge 0.0527 interest rate and offer 0.323 acceptance probability. When processing cost heterogeneity is re-introduced, banks that experience an increase in processing costs compared to the baseline (Wells Fargo, JP Morgan) increase interest rates and acceptance probabilities. In contrast, banks that experience a decrease in processing costs compared to the baseline (Citigroup, US Bank NA) decrease interest rates and acceptance probabilities. Bank of America does not materially change its interest rates and acceptance probabilities because its actual processing cost is close the the value from the baseline.

Similarly, panel (b) shows the movements in interest rates and acceptance probabilities when I re-introduced funding cost heterogeneity across banks. It shows that for banks that see their funding cost increase from the baseline (Citigroup, US Bank NA), they increase interest rates and decrease acceptance probabilities. If banks see a decrease in the funding cost (Wells Fargo, US Bank NA, Bank of America), then they lower rates and increase acceptance probabilities. From this figure it can be seen that banks trade-off interest rates and acceptance probabilities differently for changes to different types of costs. This means that the welfare implications of a reduction in processing costs can be qualitatively different than a reduction in funding costs. When funding costs decrease, households unambiguously benefit because interest rates become lower and acceptance probability becomes higher. However, reductions in processing costs has ambiguous implications for households since

<sup>&</sup>lt;sup>30</sup>I pick the MSA-year with demand, defaults and funding cost fixed effects close to their respective averages in 2010.

households benefit from lower interest rates but are harmed by lower probabilities of acceptance.

The intuition for this result is as follows. My estimates imply that acceptance probabilities are determined by the profit margin a bank makes on originated mortgages (as opposed to competition between banks for market share of applications), with a bigger profit margin implying higher acceptance probabilities. When funding costs decrease, banks lower interest rates to attract more applications at the expense of the now higher margin. But this will still result in higher profit margins than before the funding cost decrease due to downward sloping demand, and higher profit margins mean banks will increase acceptance probabilities. Therefore, interest rates decrease and acceptance probabilities increase with a funding cost decrease. On the other hand, a processing cost decrease will also lead banks to decrease interest rates in order to attract more applications because now the cost incurred per application has decreased. However, since funding costs have not changed but banks lowered interest rates, the profit margin will be smaller than before the processing cost decrease which means banks will lower acceptance probabilities. This explains why funding and processing costs have different implications on how banks trade-off interest rates and credit rationing.

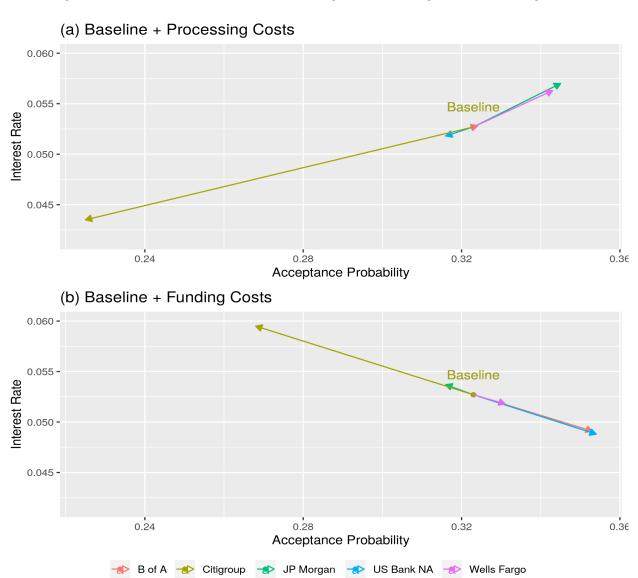
# 6.2 Funding Cost Pass Through

The second set of counterfactuals study how banks pass through lower funding costs through interest rates and acceptance probabilities in order to simulate the effects of an expansionary monetary policy. For all observations in 2010, I lower funding costs by 10% and then look at equilibrium outcomes, in particular:<sup>31</sup> a) the magnitude of the pass through in acceptance probabilities, and b) the heterogeneity in pass through in interest rates and acceptance probabilities. In addition to calculating the equilibrium for each market where banks can endogenously adjust in interest rates and acceptance probabilities, I also run two parallel sets of counterfactuals where funding costs decrease by 10% and banks can: only adjust in interest rates holding acceptance probabilities fixed, and only adjust in acceptance probabilities holding interest rates fixed. The purpose of these parallel counterfactuals is to compare and contrast implications on welfare for a model where both interest rates and credit rationing are endogenous versus models that only allow for endogenous changes in one margin.

Figure 5 shows an illustration of pass through for a single market (same market explored

 $<sup>^{31}</sup>$ I estimate the variance of the idiosyncratic cost  $\sigma$  with the moment condition that interest rates decrease by 10% on average for a 10% decrease in funding costs using 2010 observations.

Figure 4: Interest Rates, Credit Rationing, and Funding and Processing Costs



Notes: Figure shows movements in equilibrium interest rates and acceptance probabilities as I add back heterogeneity across banks in processing and funding costs to a baseline where there is no heterogeneity across banks in any dimension. Panel (a) shows the results of adding back bank heterogeneity in processing costs to the baseline. Similarly, panel (b) shows the results from adding bank funding cost heterogeneity to the baseline.

in section 6.1). In panel (a), each colored arrow represents the equilibrium pass through where in the solid arrow banks can adjust through both interest rates and acceptance probabilities, in the dashed arrow banks can only adjust through interest rates holding acceptance probabilities fixed, and in the dotted arrow banks can only adjust in acceptance probabilities holding interest rates fixed. Panel (b) shows the same results for Bank of America only. Panel (b) shows that only allowing adjustments in interest rates over-predicts the interest rate pass through by 4 basis points. Holding the credit rationing margin fixed has ambiguous implications for household welfare predictions. On the one hand, it over-predicts the interest rate pass through which implies an over-prediction of the gains to households from the change in interest rates, but on the other hand it does not take into account the welfare gain for households in the increased acceptance probabilities.

Table 5 shows the average percentage change in equilbrium outcomes for the three parallel pass through counterfactuals. The first column shows average percentage change in equilibrium outcomes where banks can adjust in both interest rates and acceptance probabilities. The second and third columns show results for the case where banks can only adjust in interest rates and acceptance probabilities respectively. Comparing the first two columns, the table shows that only allowing banks to adjust in interest rates over-predicts the interest rate pass through and, the gains to households, and the decrease in defaults due to the moral hazard in defaults w.r.t. interest rates. It also under-predicts the gains to banks. In terms of magnitudes, the over-prediction in the pass through is more important for under-predicting the average percentage gain to banks (approximately a percentage point) than gains to households (less than a percentage point). Comparing the first and third columns, only allowing banks to adjust in acceptance probabilities over-predicts the increase in acceptance probabilities, under-predicts to gains to households, and – most interestingly – significantly over-predicts the gains to banks. This seems to suggest that there is a prisoner's dilemma type of effect when funding costs decrease and banks can compete in interest rates as all banks would like to keep the interest rate fixed in response to lower funding costs, but each bank's best-response to other banks holding rates fixed is to undercut them, leading to a Pareto-inferior equilibrium where interest rates are lower in the new equilibrium. Finally, in the third column defaults increase due to adverse selection effects where bank increasing the proportion of mortgage applications leads to a riskier pool of accepted mortgages and defaults increase.<sup>32</sup>

<sup>&</sup>lt;sup>32</sup>It is important to note that in my model consumer surplus does not include the cost of defaults to households and therefore gives an incomplete view of changes in household welfare. This is a common limitation in structural models of competition in credit markets.

Table 5: Average Percentage Change in Equilibrium Outcomes with Pass Through

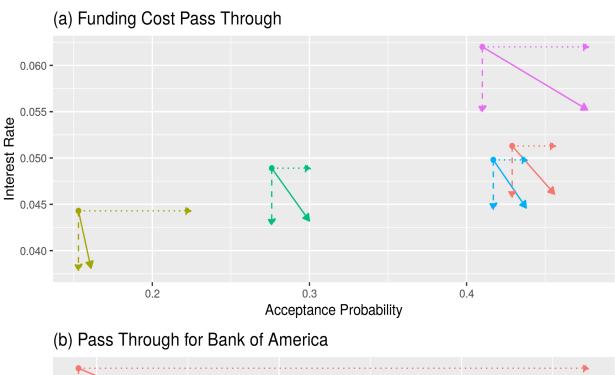
	i and $a$ (%)	i only (%)	a  only  (%)
Interest Rates	-10.407	-11.328	0.000
Acc. Prob.	7.073	0.000	25.559
Consumer Surplus	3.608	3.963	0.269
Profits	2.461	1.467	16.508
Defaults	-28.864	-33.563	13.129
Applications	108.774	118.923	6.097
Mortgages	124.011	118.923	33.455

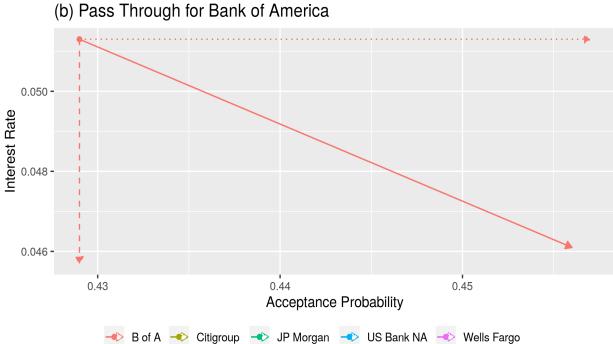
Notes: Table shows average percentage change in interest rates, acceptance probabilities, consumer surplus, profits, defaults, applications, and mortgages for counterfactuals where I decrease funding costs by 10% for all banks. The first column shows results for the case where banks can adjust through both interest rates and acceptance probabilities to reach the new equilibrium. The second and third columns show results for the cases where banks are only allowed to adjust in interest rates (holding acceptance probabilities fixed) and acceptance probabilities (holding interest rates fixed) respectively.

Panel (a) of figure 6 shows the pass through in interest rates and acceptance probabilities for all observations in 2010 where each colored arrow represents the movement from observed data to the new pass through equilibrium for a bank-market observation. The figure shows that there seems to be heterogeneity in the pass through of interest rates and acceptance probabilities. Panel (b) shows the average pass through in interest rates and acceptance probabilities per bank. There is clear heterogeneity across banks with US Bank NA showing the smallest pass through in both interest rates and acceptance probabilities and JP Morgan Chase showing some of the biggest pass through in both margins. On average Bank of America benefits the most in the pass through counterfactual.

Figure 7 looks more closely at the heterogeneity in pass through in 2010. Panels (a) and (b) show how processing costs and bank branch share (as a measure of bank market power) affect interest rate and acceptance probability pass throughs respectively. Each dot is a bank-MSA in 2010, and bright green dots indicate the largest pass throughs (largest decreases in interest rates and largest increases in acceptance probabilities). Panel (a) shows that interest rate pass through is larger in bank-MSA where banks have less market power and have lower processing costs. Things are more ambiguous for acceptance probability pass through in panel (b), although in general the brightest green dots are where there is lower

Figure 5: Funding Cost Pass Through in a Given Market

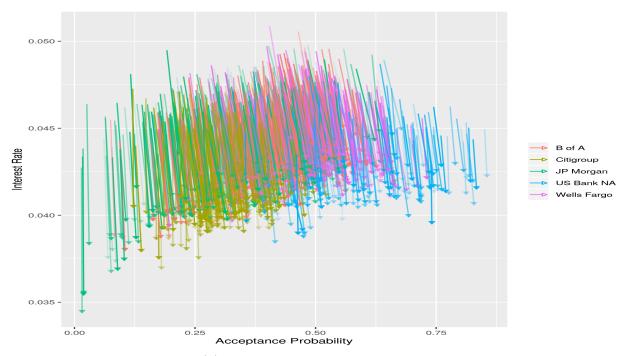




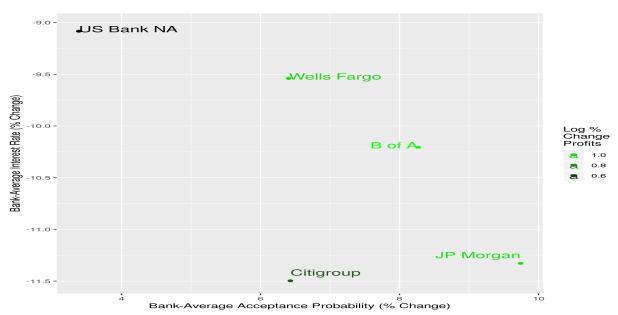
Notes: Figure shows the pass through in interest rates and acceptance probabilities for a 10% cut in funding cost. The solid line shows the case where banks can adjust to the new equilibrium through both interest rates and acceptance probabilities, the dashed line shows the case where banks can only adjust through interest rates, and the dotted line shows the case where banks can only adjust through acceptance probabilities. Panel (a) shows pass through for a single market and panel (b) shows pass through for a single bank.

Figure 6: Pass Through in Interest Rates and Acceptance Probabilities in 2010

#### (a) Pass Through in All Bank-Markets



### (b) Average Pass Through per Bank



Notes: Panel (a) shows the pass through in interest rates and acceptance probabilities for a 10% cut in funding cost for all bank-MSA observations in 2010. Panel (b) shows average pass through per bank in 2010 with the color representing the log of the average percentage change in profits.

processing costs. Panels (c) and (d) plot the gain to households and banks respectively on processing costs and bank branch share. There is heterogeneity in how much households and banks gain across MSAs and the pattern is not straightforward. Tables 6 and 7 compares how exogenous characteristics differ across quartiles of interest rate and acceptance probability pass through respectively. Table 6 shows that in bank-MSAs where there is higher pass through, the bank branch share is higher and processing costs are lower whereas the funding costs are higher. Average FICO, LTV, and DTI does not seem to vary across different quartiles of percentage pass through in interest rates. Mirroring results from table 6, table 7 shows that bank branch share and processing costs are lower in bank-MSAs with higher pass through, and funding costs are higher.

Table 6: Averages of Demand, Defaults, and Supply Variables for Quartiles of Interest Rate Pass Through

% Change in $i$ (-) Variables	(6.142, 9.404]	(9.404, 10.216]	(10.216, 11.271]	(11.271, 19.521]
Bank Branch Share	0.081753	0.076805	0.033329	0.007377
Processing Cost	0.012207	0.010203	0.009044	0.007905
Funding Cost	0.038348	0.043332	0.046673	0.052651
FICO	764.832644	764.595769	762.573313	763.322327
LTV	68.415884	68.246536	66.870548	66.181095
DTI	31.256928	31.586690	31.148484	30.823536

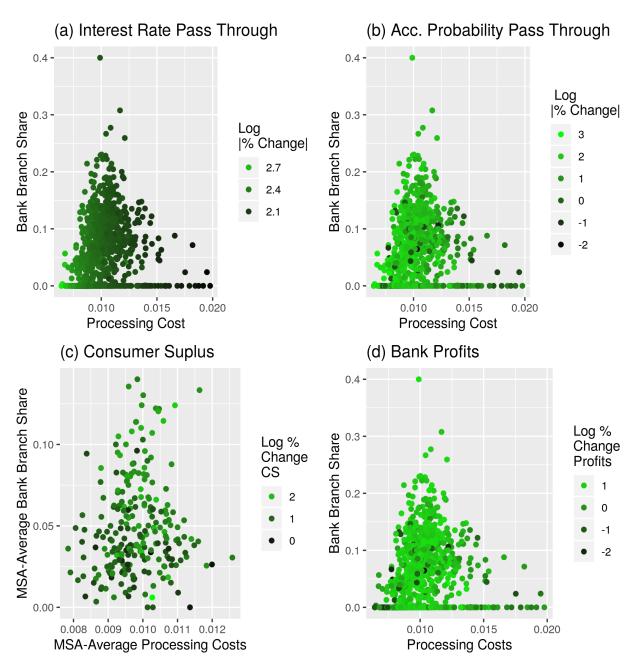
*Notes:* Table shows averages of bank branch share, processing costs, funding costs, and average FICO, DTI, and LTV for each quartile of (negative) percentage pass through in interest rates.

### 6.3 Adverse Selection, Moral Hazard, and Pass Through

The final set of counterfactuals explore how adverse selection and moral hazard affect funding cost pass through. Because adverse selection and moral hazard are key frictions that can appear in any credit market, it is important to understand how they affect the pass through of expansionary monetary policy. Note that all my results discussed below only include observations from 2010.

I first examine the effects of adverse selection and moral hazard on mortgage lending. Table 8 shows the average percentage change in going from the observed data to equilibrium

Figure 7: Pass Through, Consumer Surplus, and Bank Profits in 2010



Notes: Panels (a) and (b) plot pass through in the interest rates and acceptance probabilities respectively on processing costs and bank branch share, where each dot represents a bank-MSA and bright green color indicates larger pass through in terms of the absolute value of the percentage change. Panel (c) plots the percentage change in consumer surplus on processing costs and bank branch share where each dot is an MSA. Panel (d) plots the percentage change in bank profits where each dot is a bank-MSA.

Table 7: Averages of Demand, Defaults, and Supply Variables for Quartiles of Acceptance Probability Pass Through

% Change in $a$ Variables	(0.117, 4.677]	(4.677, 6.925]	(6.925, 9.314]	(9.314, 21.114]
Bank Branch Share	0.051887	0.065872	0.059254	0.022304
Processing Cost	0.010954	0.010103	0.009682	0.008622
Funding Cost	0.041742	0.043854	0.045361	0.050044
FICO	766.643856	765.091407	763.245272	760.347764
LTV	67.181043	67.007546	67.504334	68.018938
DTI	30.744499	31.257379	31.404827	31.408668

*Notes:* Table shows averages of bank branch share, processing costs, funding costs, and average FICO, DTI, and LTV for each quartile of percentage pass through in acceptance probabilities.

outcomes where adverse selection and/or moral hazard is shut down exogenously. My model predicts that interest rates and acceptance probabilities will increase in all of the scenarios above. For example, the first column shows that interest rates would increase on average by 1.082% (5 basis points) and acceptance probabilities would increase by 12.202% (4.8 percentage points). If I shut down moral hazard, the percentage change from observed to new interest rates would be 1.729% (8 basis points) and for acceptance probabilities it would be 22.626% (8.1 percentage points). Shutting down both adverse selection and moral hazard yields results very similar to the case where I only shut down moral hazard.

Two things should be noted. First, the directions in which interest rates and acceptance probabilities move as I remove adverse selection and moral hazard effects from the model are as expected. These frictions prevent banks limit banks' ability to charge higher rates for higher default risk, so removing these frictions leads to higher interest rates charged by banks, and higher acceptance probabilities due to the larger profit margins. Second, moral hazard is quantitatively the more important friction. Shutting down moral hazard from the model leads to larger increases in interest rates and acceptance probabilities than when I shut down adverse selection.

Now I move on to calculating the pass through of decreased funding costs as I shut down adverse selection and moral hazard respectively. Table 9 shows the results of these counterfactuals. Each column specifies what part of the model was shut down. For each of these columns, I calculate the pass through of lower funding costs in the following way.

First, I calculate the new equilibrium outcomes after shutting down one of the frictions mentioned above. Then, I calculate the new equilibrium under the same model conditions with funding costs decreased by 10%. Then I calculate the average percentage change in equilibrium outcomes from the former to the latter equilibria.

Table 9 reports the average percentage change in equilibrium outcomes going from before the funding cost decrease to after. I explore the same three scenarios reported in table 8: no adverse selection, no moral hazard, and no adverse selection nor moral hazard. In all three scenarios, the interest rate pass through is very similar to the counterfactual pass through for observed data reported in table 5 of -10.407%. What is interesting is that the pass through in acceptance probabilities is lower in all scenarios than as predicted for the full model with adverse selection and moral hazard. With no adverse selection, pass through in acceptance probabilities is 3.789% on average, whereas for the full model pass through in acceptance probabilities is predicted to be 7.073% on average. When I shut down moral hazard acceptance probability pass through is even lowered to 0.443%. These results imply that banks only pass through funding cost decreases in the credit rationing margin if there are frictions such as adverse selection or moral hazard in mortgage lending.

The intuition for the above result is that according to my estimates, acceptance probabilities are almost entirely driven by the profit margins on originated mortgages, and that the profit margins become larger after the funding cost decrease when there is adverse selection or moral hazard. I explain the intuition for the case where there is no moral hazard in more detail. Following a funding cost decrease, the marginal benefit of a bank reducing its interest rate comes from the increased market share that it will attract, at the expense of reducing profit margins and incurring higher processing costs from attracting more applications. When there is moral hazard, the expense of lowering profit margins by lowering interest rates is somewhat mitigated by households becoming less likely to default as interest rates decrease. This means that for any decrease in interest rates, the profit margins are larger in the case where there is moral hazard than where there is no moral hazard. In all the above scenarios banks find it optimal to reduce interest rates by approximately 10% for a 10% decrease in funding costs, so profit margins will be bigger where there is moral hazard than where there is no moral hazard. When there is moral hazard, banks find it optimal to decrease interest rates by approximately 10% and enjoy the large profit margins on originated mortgages by increasing the acceptance probability, rather than decreasing interest rates by less than 10% and keeping similar profit margins. Therefore banks increase the acceptance probability more for the case where there is moral hazard than when there is no moral hazard. These results imply that the extent of adverse selection and moral hazard in a credit market is important for policy makers in predicting the effects of expansionary monetary policy on pass through in the credit rationing margin.

Table 8: The Effects of Adverse Selection and Moral Hazard

	No AS (%)	No MH (%)	No MH/AS (%)
Interest Rates	1.082	1.729	1.745
Acc. Prob.	12.202	22.626	23.063
Consumer Surplus	-0.154	-0.210	-0.210
Profits	3.498	7.791	7.890
Defaults	-39.442	-97.221	-98.573
Applications	-4.192	-6.279	-6.283
Mortgages	7.473	14.689	15.084

Notes: Table shows the average percentage change in equilibrium outcomes when comparing the new equilibrium outcomes where I shut down key frictions in the model to the observed data. First, second, and third columns report the average percentage change in equilibrium outcomes from the observed data to counterfactuals where I shut down adverse selection, moral hazard, and both adverse selection and moral hazard respectively.

Table 9: Adverse Selection, Moral Hazard, and Funding Cost Pass Through

	Full Model (%)	No AS (%)	No MH (%)	No MH/AS (%)
Interest Rates	-10.407	-10.426	-10.493	-10.490
Acc. Prob.	7.073	3.789	0.443	0.416
Consumer Surplus	3.608	3.466	3.403	3.402
Profits	2.461	1.711	0.267	0.263
Defaults	-28.864	-31.952	0.281	0.000
Applications	108.774	109.374	109.982	109.949
Mortgages	124.011	117.741	110.937	110.845

Notes: Table shows the average percentage change in equilibrium outcomes after funding cost is decreased by 10%. The first column shows the results from the full model (same as the results in the first column of table 5). Second, third, and fourth columns show funding cost pass through where there is no adverse selection, no moral hazard, and neither adverse selection nor moral hazard respectively.

### 7 Conclusion

In this paper I study how banks optimally trade-off interest rates and credit rationing in U.S. mortgage lending, where credit rationing is defined as the probability of accepting a mortgage application. I develop a novel model of imperfect competition in mortgage lending with adverse selection and moral hazard where the model allows me to identify the cost of processing mortgage applications in addition to the cost of funding mortgages. These costs play an important role in explaining the relationship between interest rates and credit rationing, and the changes in these two types of costs have potentially different welfare implications. I estimate the model using U.S. data on mortgage applications, interest rates, and defaults aggregated at the bank-MSA-year level.

I use the estimated model to run a counterfactual where funding costs decrease in order to understand how banks trade-off interest rates and credit rationing, and to show how this trade-off has important policy implications. First, I show that credit rationing is an important margin in the pass through of changes in funding costs. For a 10% decrease in funding costs, the average percentage change in interest rates and acceptance probabilities are -10.407% and 7.073% respectively. Second, there is substantial heterogeneity in the pass through of changes in funding costs in both interest rates and acceptance probabilities, which implies that some markets will receive significantly more benefit from say, expansionary monetary policy, than others. Processing costs play an important role in the heterogeneity in pass through since banks gain less from cutting interest rates to attract more applications where the cost of processing applications is higher. Third, I quantify the role that adverse selection and moral hazard has on pass through in the credit rationing margin. I find that moral hazard is the more important friction for U.S. mortgage lending: with no moral hazard, the average percentage change in acceptance probabilities almost goes to zero. This implies that frictions such as adverse selection and moral hazard play a key role in how banks tradeoff interest rates and acceptance probabilities, and how this trade-off is of central importance for policy questions.

My paper can be extended in several different directions. More work can be done on explaining the variation in funding and processing costs across banks and markets. One potential key dimension is the extent to which a bank securitizes its mortgages to the GSEs and how this affects funding costs. Greater familiarity and access to the GSEs as a source of funds for originating mortgages could provide a competitive advantage for banks. Processing costs increase in years after the financial crisis, which is consistent with the increasing regulatory burden as Dodd-Frank Act comes into effect and the Consumer

Financial Protection Bureau is established during this period. However, more can be done to understand the cross-sectional variation in processing costs, for example whether differences in regulations across markets such as recourse versus non-recourse are important. Finally, my model could be extended to micro-data that contains information on interest rates and credit rationing at the individual borrower level, although at the time of writing such data is not readily available.

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# **Appendix**

# A Optimal Decision Rule $\rho_b$

Here I derive the optimal decision rule  $\rho_{b,t}$  with all the parametric assumptions of the model. First, with idiosyncratic cost shocks  $e_{b,t}$  distributed EVI, from Hotz and Miller (1993) we know that the observed acceptance probabilities  $a_{b,t}$  satisfy:

$$\rho_{b,t}(\pi_{b,t}) + \sigma G'(a_{b,t}) = 0 \tag{25}$$

Where,  $G'(a_{b,t}) \equiv ln(1 - a_{b,t}) - ln(a_{b,t})$ . From equation (21), the first order condition w.r.t.  $a_{b,t}$  can be written as:

$$FOC_{b,t}^{a} \equiv \pi_{b,t} \times \left[ \alpha_{a} \cdot (1 - q_{b,t}) \cdot a_{b,t} + 1 \right] + \alpha_{a} \cdot (1 - q_{b,t}) \cdot \left[ a_{b,t} \cdot \sigma \cdot g(a_{b,t}) - c_{b,t} \right] - \delta_{a} \cdot a_{b,t} \cdot i_{b,t} \cdot d_{b,t} \cdot (1 - d_{b,t}) + \sigma \cdot G'(a_{b,t}) = 0$$
(26)

Therefore, in order for equations (25) and (26) to be consistent, it must be that:

$$\rho_{b,t}(\pi_{b,t}) = \rho_{b,t}^{1} \cdot \pi_{b,t} + \rho_{b,t}^{2} 
\rho_{b,t}^{1} \equiv \alpha_{a} \cdot (1 - q_{b,t}) \cdot a_{b,t} + 1 
\rho_{b,t}^{2} \equiv \alpha_{a} \cdot (1 - q_{b,t}) \cdot [a_{b,t} \cdot \sigma \cdot g(a_{b,t}) - c_{b,t}] - \delta_{a} \cdot a_{b,t} \cdot i_{b,t} \cdot d_{b,t} \cdot (1 - d_{b,t})$$
(27)

Notice that if  $\alpha_a = \delta_a = 0$ , then  $\rho_{b,t}^1 = 1$  and  $\rho_{b,t}^2 = 0$ , i.e., with households that do not have any preference over acceptance probabilities and no adverse selection, banks accept mortgage applications if and only if it is ex-post profitable  $(\rho_{b,t} = 1, \forall \pi_{b,t} \Rightarrow y_b = 1 \Leftrightarrow \pi_{b,t} - e_{b,t} > 0)$ .

## B Estimating Funding and Processing Costs

The first order conditions of optimality from equation (21) can be re-arranged to solve for  $\pi_{b,t}$  and  $c_{b,t}$  under the assumption that  $\sigma$  is known. First, rearrange  $FOC_{b,t}^i$  from equation (21) and define:

$$\kappa_{b,t}^{i} \equiv a_{b,t} \cdot \sigma \cdot G(a_{b,t}) + \frac{a_{b,t} \cdot (1 - d_{b,t}) \cdot (1 - \delta_{i} \cdot d_{b,t} \cdot i_{b,t})}{\alpha_{i} \cdot (1 - q_{b,t})} = c_{b,t} - a_{b,t} \cdot \pi_{b,t}$$
(28)

Also rearrange  $FOC_{b,t}^a$  from equation (21) and define:

$$\kappa_{b,t}^{a} \equiv a_{b,t} \cdot \sigma \cdot G(a_{b,t}) + \sigma \frac{G'(a_{b,t})}{\alpha_{a} \cdot (1 - q_{b,t})} - \frac{\delta_{a} \cdot a_{b,t} \cdot i_{b,t} \cdot d_{b,t} \cdot (1 - d_{b,t})}{\alpha_{a} \cdot (1 - q_{b,t})} = c_{b,t} - \frac{\alpha_{a} \cdot (1 - q_{b,t}) \cdot a + 1}{\alpha_{a} \cdot (1 - q_{b,t})} \cdot \pi_{b,t}$$
(29)

Note that all objects on in  $\kappa_{b,t}^i$  and  $\kappa_{b,t}^a$  are known (with  $\sigma$  assumed to be known). Taking the difference between  $\kappa_{b,t}^i$  and  $\kappa_{b,t}^a$  and rearranging yields  $\pi_{b,t}$ :

$$\alpha_a \cdot (1 - q_{b,t}) \cdot (\kappa_{b,t}^i - \kappa_{b,t}^a) = \pi_{b,t} \tag{30}$$

Next, substituting in and rearranging  $\pi_{b,t}$  into  $\kappa_{b,t}^a$  and rearranging yields:

$$\kappa_{b,t}^{a} + \left[\alpha_{a} \cdot (1 - q_{b,t}) \cdot a_{b,t} + 1\right] \cdot \left(\kappa_{b,t}^{i} - \kappa_{b,t}^{a}\right) = c_{b,t}$$
(31)

Thus, conditional on knowing the value of  $\sigma$  the two first order conditions of optimality from equation (21) identify  $\pi_{b,t}$  and  $c_{b,t}$ .

## C Details on the Simulation of Counterfactuals

The algorithm for calculating a counterfactual equilibrium for a given market consists of an inner loop that finds the optimal interest rate and acceptance probability for each bank given the interest rates and acceptance probabilities of rival banks, and an outer loop that checks whether a proposed vector of interest rates and acceptance probabilities are in equilibrium.

Let  $r \in \{0, 1, 2, ...\}$  represent an iteration of the outer loop. For a starting vector of interest rates  $\mathbf{i}^r$  and acceptance probabilities  $\mathbf{a}^r$ , the inner loop finds the optimal interest rate  $i_b^{r,*}$  and acceptance probabilities  $(\mathbf{a}_{-\mathbf{b}}^r)$  of rival banks. Then, with the resulting vectors of optimal interest rates  $\mathbf{i}^{r,*}$  and  $\mathbf{a}^{r,*}$  from the inner loop, the outer loop checks whether these are in equilibrium according to equation (14). If  $\mathbf{i}^{r,*}$  and  $\mathbf{a}^{r,*}$  is not in equilibrium, then I set  $\mathbf{i}^{r+1} = \mathbf{i}^{r,*}$  and  $\mathbf{a}^{r+1} = \mathbf{a}^{r,*}$  and feed these vectors into the inner loop again. This algorithm continues until an equilibrium is

found, meaning the maximum of the difference between  $\mathbf{i}^r$  and  $\mathbf{i}^{r,*}$ , and  $\mathbf{a}^r$  and  $\mathbf{a}^{r,*}$  is smaller than 0.00001. To address the fact that multiple equilibria is a strong possibility and that I do not want my results to be driven by equilibria switching across counterfactuals, the starting values  $\mathbf{i}^0$  and  $\mathbf{a}^0$  are always set to the observed interest rates and acceptance probabilities in the data.

The inner loop finds the optimal interest rate and acceptance probability for a bank given the interest rates and acceptance probabilities of rival banks. I use a hybrid algorithm where I first evaluate the bank profit function on a grid of interest rates and acceptance probabilities<sup>33</sup>, and then for each of the 20 highest grid points in terms of profits I run a constrained optimization algorithm (implemented with Python SciPy Optimize package). I found that this hybrid algorithm yielded the best combination of speed and robustness. Counterfactual equilibria for different markets were calculated in parallel using MPI for Python in the SciNet high performance computing cluster.

 $<sup>^{33}</sup>$ The grid for interest rates are [0.02, 0.07] with step values of 0.0001 and the grid for acceptance probabilities are [0.001, 0.999] with step values of 0.0001.